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THE DISTRIBUTION OF ENERGY IN THE SPECTRA OF THE SUN AND STARS

BY

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Until recently, one could form an estimate of the temperatures prevailing in the sun and other stars only by a determination of the distribution of energy in their spectra and the application of the laws of the perfect radiator or absolutely black body. Although recent advances in the physics of the atom point to a new method of approach to this subject, the form of the energy curve still remains of great theoretical interest.

In the measurement of the solar constant of radiation by the method of Langley, it requires us to determine the ratio of the areas of the energy curve of the sun at the earth's surface and outside the atmosphere, and knowledge of the distribution of intensities of the solar rays is indispensable. To be sure, the values come in merely as a series of weights in forming a pair of sums, one in the numerator, the other in the denominator of the fraction which gives the ratio of the solar energy outside the atmosphere to the solar energy within it. Hence no very high degree of accuracy is needful for this purpose. This is fortunate, for so far as our experiments have gone we have never succeeded in obtaining so high a degree of accuracy as would satisfy us from the workmanlike point of view.

This comes out clearly if one compares the results of our various determinations of the form of the solar energy curve as published in Volumes III and IV of the *Annals of the Astrophysical Observatory*. The divergence in these values is considerable, and when in 1920 the experiments for the determination of the form of the sun's energy curve were repeated, a still wider discrepancy appeared, so great that although these experiments of 1920 were ready at the time of printing of Volume IV of the *Annals* we hesitated to include them until they should be checked by other independent determinations.

These proposed new determinations have been made at Mount Wilson during the summer of 1922, and form the first part of the present communication. The latter part includes the application of them to the spectra of ten of the brightest stars observed with a

special bolometric outfit by Messrs. Abbot and Aldrich at Mount Wilson in 1922. The work was done in connection with the 100-inch telescope.

We here return our thanks for the aid and encouragement furnished in the stellar work by Dr. Hale, Dr. Adams, and many of the staff of the Mount Wilson Solar Observatory.

SOLAR SPECTRUM ENERGY CURVE

A statement of the method adopted for the observations may be found in Volume II of the *Annals of the Astrophysical Observatory*, pages 24, 50-57. Briefly, it is this:

At each of a number of wave lengths in the solar spectrum it is required to determine: (1) The intensity of the spectrum observed in the bolometer; (2) the selective transmission of the spectroscope; (3) the selective reflection of the coelostat; (4) the transmission of the atmosphere. The bolograph indicates the first, and the measurements on a series of bolographs taken at different zenith distances of the sun furnish the means of computing the last. The reflection of the coelostat is determined by taking bolographs (*a*) with the ordinary pair of mirrors, (*b*) with a substitute pair of mirrors, (*c*) with a combination of both regular and substitute mirrors. The selective transmission of the spectroscope is determined by first passing the ray through an auxiliary spectroscope, selecting certain wave lengths and observing their intensity, (*d*) as transmitted by the auxiliary spectroscope, (*e*) as transmitted by both spectroscopes.

The observation (*d*) is made by setting the bolometer to occupy the position usually occupied by the slit of the usual spectroscope. In this position a number of settings of the auxiliary spectroscope are made, so as to determine the intensity of its radiation at a sufficient number of wave lengths. Then the slit of the usual spectroscope is restored to its proper position so as to permit nearly monochromatic beams of light to pass through the usual spectroscope after having been sorted out by the auxiliary one. The relative intensities of these nearly monochromatic beams are determined by taking bolographic energy curves of them. The areas included in these bolographic energy curves give the relative amounts of energy remaining in these wave lengths after having suffered absorption in the usual spectroscope. Thus the galvanometer deflections with the bolometer at the slit divided by the areas of the corresponding energy curves formed by the bolometer in its usual position, give numbers inversely pro-

portional to the transmission of the usual spectroscope, and suitable to correct its losses.

It will be noted that the procedure thus outlined takes no account of selective absorption by the bolometer for different wave lengths. If, for example, the bolometer should only absorb 50 per cent of the rays in the ultra-violet while it absorbed 95 per cent of the rays in the infra-red, the form of the energy curve would be quite erroneous. We confess that in even our present experiments the possibilities of error from this cause have not been eliminated, but as will appear we have at least shown that with several different bolometers, some camphor smoked, some painted with lamp-black, some in atmospheric pressure, and some in high vacuum, there is no certain difference beyond the experimental error, and we continue here, as heretofore, tacitly to make the assumption that the bolometer absorbs a uniform proportion of the rays throughout the region of spectrum we are concerned with, namely, from 0.3μ to 3μ . Our position is strengthened by the fact that Angström, Coblentz, and others estimate the absorption coefficient of blackened surfaces for total solar radiation as high as 97 or 98 per cent. This leaves little room for selective absorption.

Observations of 1920.—The determination of the transmission of the spectroscope was repeated in 1920 with new stellite mirrors, those used in 1917 and 1918 having gone to Chile. There is nothing new in the method employed, but the work was done with all possible care and with independent adjustments on July 16, 17, and 19, and August 18 and 19, 16 determinations in all. Ten points in the spectrum were observed in July and nine others alternating with them in August. The average probable error of the determination of relative spectroscopic transmission at these 19 points was 1.2 per cent. The results run as shown in table 1.

Combining these results with the determination of the reflecting power of the stellite-mirror coelostat made in 1918, and determinations of the form of the energy curve at the earth's surface and of atmospheric transmission accompanying made at Mount Wilson on 10 satisfactory days of 1920, of which five gave high, five low solar constants, we obtained the distribution of solar energy in the spectrum outside our atmosphere. These values will be given below.

Observations of 1922.—All the apparatus used in 1920 having been removed to Mount Harqua Hala, we used an entirely new outfit. The coelostat mirrors were silvered but the main spectroscope had new stellite ones.

In repeating the work, we were well convinced that the principal uncertainty rested on the determination of the absorption of the spectroscope. So many closely agreeing observations have been made in former years of the transmission of the atmosphere, the results of which fall in so well with the theory of Rayleigh on the molecular

TABLE I.—*Spectroscopic Transmission. Observations of 1920*

| | | | | | | | |
|-------------------------------------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| Place by counter..... | 193 18 | 194 00 | 194 45 | 195 30 | 196 15 | 196 45 | 197 20 |
| Prismatic deviation from ω_1 | 224.6' | 210.6' | 195.6' | 180.6' | 165.6' | 155.6' | 144.0' |
| Wave length μ | .355 | .370 | .391 | .412 | .441 | .463 | .492 |
| Relative transmission | 194 | 243 | 297 | 291 | 314 | 328 | 343 |
| Probable error, per cent... | 3.2 | 3.0 | 1.8 | 0.4 | 1.4 | 0.7 | 0.9 |

| | | | | | | | |
|-------------------------------------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| Place by counter..... | 198 00 | 198 35 | 199 15 | 200 12 | 200 30 | 201 10 | 201 45 |
| Prismatic deviation from ω_1 | 130.6' | 119.0' | 105.6' | 86.6' | 80.6' | 67.2' | 55.6' |
| Wave length μ | .533 | .578 | .650 | .798 | .859 | 1.040 | 1.215 |
| Relative transmission | 372 | 378 | 362 | 348 | 335 | 295 | 291 |
| Probable error, per cent... | 1.1 | 1.1 | 0.9 | 1.2 | 0.3 | 0.9 | 0.7 |

| | | | | | | |
|-------------------------------------|-----------|-----------|-----------|-----------|-----------|--|
| Place by counter | 202 00 | 203 00 | 203 30 | 205 00 | 205 50 | |
| Prismatic deviation from ω_1 | 50.6' | 30.6' | 20.6' | -9.4' | -26.0' | |
| Wave length μ | 1.297 | 1.594 | 1.733 | 2.118 | 2.310 | |
| Relative transmission | 324 | 365 | 383 | 351 | 186 | |
| Probable error, per cent... | 1.0 | 1.2 | 0.5 | 0.4 | 2.3 | |

scattering, that we could not doubt that the atmospheric transmission coefficients obtained on excellent days were abundantly accurate for the purpose here in view. At least this is true for the wave lengths greater than 0.4μ . In the ultra-violet, we are well aware that there is contamination of the spectrum by stray light from longer wave lengths, so that the atmospheric transmission coefficients determined for that region are too high, and the magnitude of this error increases

as the wave length diminishes. If that were the only effect of the stray light, it would tend to diminish the intensities of the solar energy spectrum outside the atmosphere in the region of the ultra-violet rays, but there are also two additional effects of stray light, both of which tend in the other direction.

The first of these is the building up of the bolographic energy curve at the earth's surface in the ultra-violet by these same stray radiations which, as we have just said, tend to raise the atmospheric transmission coefficients. Obviously the effect of this building up tends to make the ultra-violet too high.

The third effect of stray light is in the determination of the transmission of the spectroscop. If the reader will go over the summary of procedure for that purpose, which has just been stated, he will perceive that the auxiliary spectrum which falls at the slit of the main spectroscop will be subject to contamination by the stray light. Monochromatic beams of energy result at the usual position of the bolometer, after the passage of the light through both spectroscopes, in which the stray light will be practically eliminated. Consequently in the ultra-violet the auxiliary spectrum will be relatively too bright, owing to the influence of stray light, while in the final spectrum represented by the little energy curves, the stray light will be eliminated. Hence, the ratios of the bolometric deflections at the focus of the auxiliary spectrum divided by the bolographic areas observed in the usual spectrum will be too large in the ultra-violet, indicating a greater absorption in the spectroscop than actually exists, and this will tend to make the ultra-violet part of the solar spectrum outside the atmosphere too high. We shall recur to this question of stray light a little later, and introduce an estimate of the combined effect of these three different influences.

In considering the best means of assuring a trustworthy result, it seemed to us that great advantage would come from using several different prisms, both in the auxiliary and in the usual spectroscop, so that we could carry through the whole determination of the solar energy curve outside the atmosphere with instruments of very different dispersion characteristics. In order to get these as decisively different as possible and at the same time to use materials of high transmissibility throughout the region of the spectrum we were concerned with, it occurred to us to use prisms of rock salt in substitution for the ultra-violet crown glass prisms we usually employ. Moreover, as the work of 1920 and some previous years had been done with ultra-violet crown glass prisms in both the auxiliary and usual spectro-

TABLE 2.—*Circumstances of the Observations*

| 1922 Date | Object | Prisms | | Bolometer | Type of blackening | Spectrum places | | No. of tests | Notes |
|-----------|-------------------------------------|-------------------|------------------|----------------------|--------------------|-----------------|---|--------------|-------|
| | | 1st spectro-scope | 2d spectro-scope | | | | | | |
| Aug. 28 | Spectroscope absorption | Great flint | U. V. Crown. | New vacuum | Lamp-black paint. | First set | 1. Part of plates melted. | 2 | |
| " 29 | " | " | " | " | " | Second set | 2. " " melted. | 2 | |
| " 30 | " | " | " | Old air | Campbor smoke. | " | 3. Bolometer wiggles. | 1 | |
| " " | " | " | " | " | Lamp-black paint. | " | 4. Correction for shutter. | 1 | |
| " " | " | " | " | " | " | " | 5. Shutter changed. | 1 | |
| " " | " | " | " | " | " | " | 6. Bolometer wiggles much. | 2 | |
| " " | " | " | " | " | " | " | 7. Bolometer wiggles much. | 2 | |
| " 31 | Test of bolometers. | " | None | Old vacuum in air | " | " | 8. Bolometer of 1916. | 2 | |
| Sept. 1 | " | " | " | Old air exhausted | " | " | 9. Same as Aug. 30. | 1 | |
| " 2 | " | " | " | Old vacuum exhausted | " | " | 10. On these days many experiments alter- | 2 | |
| " 3 | " | " | " | " exhausted | " | " | nately with and | 1 | |
| " 4 | " | " | " | " in air | " | " | without air. | 1 | |
| " 5 | galvanometer scale | None | " | " | " | None | 11. Varied shut. | 1 | |
| " 6 | sectors | " | U. V. Crown. | " | " | Selected | 12. Eye observations. | 1 | |
| " 7 | bolometers | Great flint | None | " | " | Second set | 13. First spectroscope re- | 1 | |
| " 8 | " | " | " | " | " | " | silvered. | 1 | |
| " 9 | " | " | " | New vacuum repaired | " | " | 14. Strips resoldered and re-evacuated. | 1 | |
| " 10 | Spectroscope absorption | " | " | " | " | " | 15. Excellent conditions. | 2 | |
| " 11 | Solar energy spectrum distribution. | None | U. V. Crown. | " | " | First set | 16. Cloudless. | 2 | |
| " 12 | Spectroscope absorption | Great flint | " | " | " | Bolographs | 17. See final discussion. | 10 | |
| " 13 | Solar energy spectrum distribution. | None | Rock salt | " | " | Combined set. | 18. Cloudless, good sky. | 10 | |
| " 14 | Spectroscope absorption | Great flint | " | " | " | Bolographs | 19. Excellent conditions. | 1 | |
| " 15 | Test of bolometers. | Great flint | " | " | " | Combined set. | 20. Compare Sept. 2. | 1 | |
| " 16 | Spectroscope absorption | U. V. Crown. | None | Old vacuum in air | " | " | 21. Little value. | 1 | |
| " 17 | Spectroscope great wave-lengths | None | Rock salt | Old air repaired | " | " | 22. Eye observations also. | 4 | |
| " 18 | Test of sector values. | None | " | " | " | Bolographs | 23. Bolographic. | 3 | |

NOTES.—1, 2, Wash water too hot. Only half plates saved. 3, Progressive increase of bolometer disturbance led finally to resoldering of connections and reevacuating the bolometer. 4, No glass being in front of bolometer the shutter gave a deflection due to its difference of temperature from surroundings. Noted magnitude and applied corrections. 5, Shutter moved over in front of slit instead of in front of bolometer. Correction avoided. 6, 7, In painting the bolometer strip it was slightly torn. Hence bad wiggles spoiled this work. Rejected. 8, 9, 10, 20, This bolometer was connected to mercury vapor pump and used alternately with and without vacuum of less than 0.001 mm. mercury on Aug. 31, Sept. 1, 2, and 6. Readings in the auxiliary spectrum by eye observations at galvanometer compared with and without air, and with old air bolometer repaired and with new vacuum bolometer repaired. 11, Observed by eye the galvanometer deflections for increasing bolometer shut by 1, 2, 3, 4, 5, 6, 7 ohms from 1930 ohms originally. First swings were 31.3, 61.0, 122.0, 152, 181, 211 mm. No corrections seem required for inequalities of galvanometer scale. 12, A few trials of deflections at the same spectrum points with different rotating sectors. Better determinations later. 14, The new vacuum bolometer returned from Pasadena resoldered and reevacuated with liquid air trap. 15, Results of highest weight. 16, Atmospheric transmission coefficient and absorption of coelostat mirrors entirely determined. 17, Changed to rock salt prism. Good determination. 18, Same remark as 16. 19, Good determination. 21, The old bolometer No. 20, used for many years at Washington (See *Annals*, Vol. I) had been broken as per note 6. New coarse strips of only 0.7 ohms resistance were now inserted. The purity of the spectrum with these and U. V. prism in first spectroscope insufficient. 22, Used sifting train of salt for eye observations. Observed to 14 microns. 23, Excellent sector determination.

scopes, we determined to substitute in the auxiliary spectroscope a prism of ordinary flint glass which, as is well known, produces a far greater relative dispersion in the ultra-violet than the ultra-violet crown glass.

It seemed to us that when these various modifications of the experiments had been made, namely, the use of bolometers in air, bolometers in vacuum, bolometers painted with lamp-black, and bolometers smoked with camphor smoke; when we had employed several different types of prisms; and when we had independently set up the apparatus with the greatest possible care on several different occasions; then, if the results of all these modifications should agree among themselves and should agree either with the work of 1920 or with the work of the earlier years, as reported in Volumes III and IV of the *Annals of the Astrophysical Observatory*, the final result, supported by such far-reaching agreements, ought to be entitled to confidence.

We now proceed to give in table 2 in abbreviated form the data of the observations and their results.

As noted above, the measurements of the degree of uniformity of the galvanometer scale do not indicate appreciable corrections to be necessary. For though the increase of deflection for successive steps of one ohm diminishes slightly with increasing deflection, yet there should be a small change in this direction depending on the fact that a change of one ohm on a shunt of 1,937 ohms about a Wheatstone's bridge coil of 56 ohms produces less current in the galvanometer than 1 ohm change on 1,930 ohms. With allowance for this, the readings differ by less than their probable error from linear relations.

The deflections are governed by rotating sectors. As determined with automatic recording of deflections in numerous series, the deflections for sectors are as follows:

| Sector No. | 3 | 2 | 1 | 0 |
|------------------|--------|-------|-------|--------|
| Deflection | 1.000 | 3.159 | 9.161 | 26.677 |
| Deflection | 0.3748 | 1.184 | 3.434 | 10.000 |

From this we derive factors of reduction:

| | | | | |
|-----------------|--------|--------|--------|---------|
| To reduce | 3 to 0 | 2 to 0 | 1 to 0 | 0 to 0 |
| Factor | 26.68 | 8.445 | 2.913 | 1.000 |
| To reduce | 3 to 3 | 2 to 3 | 1 to 3 | 0 to 3 |
| Factor | 1.000 | 0.3166 | 0.1092 | 0.03748 |

TABLE 3.—*Ratios of Deflections of Various Bolometers as Reduced to Nearly Equal Scales*

A = old bolometer No. 20 in air, camphor-smoked.

B = old bolometer No. 20 in air, lamp-black-painted.

C = 1916 bolometer in air, lamp-black-painted, glass plate in front.

D = 1916 bolometer in vacuum, lamp-black-painted, glass plate in front.

E = 1922 bolometer in vacuum, lamp-black-painted, glass plate in front.

| Spectrum place | Wave length | A/C | B/C | D/C | D/C | D, C | D/C | D/C Mean | E/C |
|----------------|----------------|-----|-----|-----|-----|------|-----|----------|-----|
| | <i>microns</i> | | | | | | | | |
| 06:00 | 0.37 | 89 | 105 | 107 | 105 | 99 | 103 | 1.035 | 94 |
| 04:30 | 0.40 | 100 | 91 | 100 | 106 | 103 | 104 | 1.032 | 108 |
| 03:15 | 0.46 | 100 | 100 | 104 | 101 | 100 | 99 | 1.010 | 106 |
| 02:00 | 0.53 | 103 | 106 | 95 | 90* | 99 | 105 | .997 | 102 |
| 00:45 | 0.65 | 102 | 100 | 102 | 88* | 95 | 100 | .992 | 99 |
| 99:50 | 0.86 | 110 | 100 | 105 | 100 | 98 | 101 | 1.010 | 100 |
| 98:15 | 1.22 | 106 | 99 | 108 | 100 | 99 | 101 | 1.020 | 100 |
| 97:00 | 1.60 | 111 | 109 | 89* | 99 | 93 | 95 | .970 | 103 |
| 95:00 | 2.12 | 110 | 105 | 100 | 102 | 93 | 98 | .982 | 100 |

*Omit.

These figures perhaps show that the camphor-smoked bolometer No. 20 read low in the visible and ultra-violet spectrum as compared with the infra-red, but this result may have been produced by changes of sky between the two series of observations, which in this instance were not made on the same day. In all the other cases we incline to think there is nothing definite shown, and the fluctuations were due to slight differences of wave length between settings, or to changes in sky between observations, as well as to accidental errors of galvanometer readings, which latter were sometimes no doubt more than 1 per cent. The change between air pressure and evacuated condition of the 1916 bolometer seemed to us at one time real, but looking at the individual determinations we now incline to doubt it. In vacuum the 1916 bolometer was about five times as sensitive as in air. The observations in vacuum in each case were taken immediately preceding those in air, and at high sun.

Reduction of the observations of spectroscopic absorption.—As a sample of the work we give the observations and reductions for September 2, first series.

TABLE 4.—*Sample of Spectroscopic Absorption Work*

| Place by second spectro-scope | Sector-free deflections and times | | | | Sector-free areas and times | | Sector-free mean deflection | Spectroscopic absorption. Arbitrary units |
|-------------------------------|-----------------------------------|--------------------------------|--------------------|--------------------------------|--------------------------------|--------------------------------|-----------------------------|---|
| | Deflection | Time | Deflection | Time | Mean measures | Time | | |
| 06:00 | <i>cm.</i> 0.77 | 3 ^h 07 ^m | <i>cm.</i> 0.52 | 3 ^h 54 ^m | <i>cm.²</i> 1.97 | 3 ^h 29 ^m | 0.645 | 327 |
| 04:30 | 5.54 | | 4.95 | | 16.19 | | 5.25 | 325 |
| 03:15 | 15.10 | 3 ^h 09 ^m | 14.15 | 3 ^h 56 ^m | 48.5 | 3 ^h 35 ^m | 14.62 | 302 |
| 02:00 | 30.51 | | 28.89 | | 112.1 | | 29.70 | 265 |
| 00:45 | 56.58 | | 54.89 | | 204.5 | | 55.73 | 273 |
| 99:50 | 85.29 | 3 ^h 11 ^m | 86.15 | 3 ^h 59 ^m | 323.0 | 3 ^h 39 ^m | 85.72 | 266 |
| 98:15 | 91.20 | | 90.20 | | 330.5 | | 90.70 | 275 |
| 97:00 | 60.63 | | 61.16 | | 236.2 | | 60.90 | 258 |
| 95:00 | 17.61 | 3 ^h 14 ^m | 17.61 | 4 ^h 01 ^m | 51.7 | 3 ^h 46 ^m | 17.61 | 341 |

Working along in this way, and reducing all of the ratios, deflection divided by area, proportional to spectroscopic absorption, to the same scale of arbitrary units, we come at length to the following tables:

TABLE 5.—*Collected U. V. Glass Spectroscopic Absorption. First Places*

| Place by second spectro-scope | Dates of observation | | | Mean values | Per cent probable error |
|-------------------------------|----------------------|-----------|------------|-------------|-------------------------|
| | Aug. 28 | Sept. 3-I | Sept. 3-II | | |
| 05:15 | 518 | 431 | 417 | 455 | 4.2 |
| 03:45 | 495 | 480 | 484 | 486 | 0.6 |
| 02:40 | 448 | 446 | 437 | 444 | 0.4 |
| 01:25 | 403 | 427 | 432 | 421 | 1.3 |
| 99:48 | 384 | 409 | 422 | 404 | 1.6 |
| 98:30 | ... | 428 | 425 | 426 | .. |
| 98:00 | ... | 437 | 420 | 428 | .. |
| 96:30 | 416 | 405 | 398 | 406 | 0.7 |
| 94:10 | ... | 703 | 735 | 419 | .. |

Similarly for the other set of spectrum places we obtained:

TABLE 6.—*Collected U. V. Glass Spectroscopic Absorption. Second Places*

| Place by second spectro-scope | Dates of observation | | | | | | Mean values | Per cent probable error |
|-------------------------------|----------------------|-------------|--------------|-----------|-----------|------------|-------------|-------------------------|
| | August 28 | August 29-1 | August 29-11 | August 30 | Sept. 2-1 | Sept. 2-11 | | |
| 06:00 | 500 | 541 | 507 | 496 | 515 | 544 | 517 | 1.0 |
| 04:30 | 508 | 458 | 495 | 368 | 507 | 547 | 480 | 3.0 |
| 03:15 | 466 | 461 | 452 | 400 | 471 | 473 | 454 | 1.3 |
| 02:00 | 410 | 433 | 426 | 397 | 412 | 440 | 420 | 1.0 |
| 00:45 | 490 | 445 | 450 | 436 | 426 | 421 | 445 | 1.2 |
| 99:50 | 408 | 413 | 400 | 428 | 413 | 385 | 408 | 0.8 |
| 98:15 | 433 | 428 | 419 | 422 | 426 | 436 | 427 | 0.3 |
| 97:00 | ... | 377 | 370 | 481 | 402 | 398 | 406 | 2.5 |
| 95:00 | ... | 553 | 591 | 630 | 532 | 569 | 575 | 1.7 |

In the same manner we arrived at the following results for the spectroscopic absorption values in arbitrary units applicable to the case of the rock salt prism replacing the U. V. crown glass prism in the

TABLE 7.—*Collected Rock Salt Spectroscopic Absorption*

| Place by U. V. spectro-scope | Dates of observation | | | Mean values | Per cent probable error |
|------------------------------|----------------------|---------|---------|-------------|-------------------------|
| | Sept. 5 | Sept. 6 | Sept. 9 | | |
| 06:00 | 699 | 644 | 693 | 679 | 1.5 |
| 05:15 | 582 | 567 | 513 | 554 | 2.1 |
| 04:30 | 522 | 539 | 476 | 512 | 1.6 |
| 03:15 | 451 | 438 | 412 | 434 | 1.6 |
| 02:00 | 411 | 391 | 384 | 395 | 1.2 |
| 00:45 | 349 | 352 | 368 | 356 | 1.0 |
| 99:50 | 313 | 305 | 327 | 315 | 1.2 |
| 98:15 | 264 | 271 | 281 | 272 | 1.0 |
| 97:00 | 239 | 260 | 270 | 256 | 2.1 |
| 95:00 | 215 | 227 | 223 | 222 | 0.9 |
| 94:10 | 203 | 208 | ... | 210 | .. |

second spectro-scope. As we had no reason to expect absorption bands introduced by rock salt it was unnecessary to investigate so many places in the spectrum as were used for the U. V. crown glass prism which has several such bands. Eleven places were chosen including all the wave lengths of the "Second Places" above and in

addition two others from the "First Places." For clearness we give the spectrum settings which the U. V. crown glass prism would have required at these wave lengths, so as to compare with those in the preceding tables.

These determinations of spectroscopic absorption for the U. V. glass and for the rock salt spectroscopes were plotted on a large scale and smooth curves drawn to fix the best values to use for the absorption coefficients at the wave lengths where bolographic ordinates are measured. These results will appear in a later table.

Reductions of observations of coelostat absorption.—On September 5, and again on September 6, bolographs were taken to determine coelostat absorption. Thus, for instance, on September 5, after a series of four bolographs beginning at 6^h 36^m and finishing with the bolograph at 8^h 13^m taken to determine atmospheric transmission coefficients, two additional silvered mirrors were employed in connection with the bolographs as follows:

| | | | | | | |
|---------------------|--------------------------------|---------------------------------|---------------------------------|---------------------------------|---------------------------------|---------------------------------|
| Time of observation | 9 ^h 45 ^m | 10 ^h 01 ^m | 10 ^h 20 ^m | 10 ^h 39 ^m | 10 ^h 49 ^m | 11 ^h 03 ^m |
| Mirror arrangement | 4 mirrors | Usual | 4 mirrors | 2 substitutes | 2 substitutes | Usual |

These bolographs of the solar spectrum having been marked with smoothed curves as usual, were measured in ordinates at the usual places as in solar-constant determinations. The results were then combined in the following manner:

From the usual bolographs taken at 8^h 13^m, 10^h 01^m, and 11^h 03^m, it was determined what would have been the usual ordinates at the various times when four mirrors and two substitute mirrors were employed, and thus the whole body of data could be brought to a common time and air mass. Mean values of ordinates for the four mirrors and for two substitutes were determined. Let A , B , and C be directly comparable ordinates at a certain wave length with usual, substitute, and four mirrors, respectively, then the correcting factor for the combined absorptions of the usual mirrors at this wave length is B/C . If that for the substitute mirrors was desired, it would be A/C .

Proceeding thus in effect, we obtained the correcting factors for the absorption of the usual mirrors over the whole spectrum for both September 5 and September 6. The latter day's values were obtained for slightly different wave lengths as observed with the rock salt prism. But the values were readily convertible to a comparable basis, and were thus compared by plotting on a large scale. The two sets of data were in satisfactory accord throughout, but were mutually helpful in smoothing out accidental errors. This being

done, smoothed curves were drawn for each day separately and applied independently in the final computations of the energy curves of the two days. From inspection of the results it is believed that the determinations of coelostat reflection are surely correct to within 1 per cent, except as far as they may be affected systematically in the violet by stray light as already referred to above.

TABLE 8.—*The Solar Energy Curve. U. V. Glass Prism. September 5, 1922*

| Prismatic deviation from ω_1 | Wave length μ | Dispersion coefficient | Coelostat reflection | Spectroscopic coefficient | Prismatic energy curve outside atmosphere | Normal energy curve outside atmosphere |
|-------------------------------------|-------------------|------------------------|----------------------|---------------------------|---|--|
| 230' | 0.3504 | 110.4 | 0.545 | 632 | 394 | 435 |
| 220 | 0.3600 | 990 | 0.616 | 580 | 506 | 501 |
| 210 | 0.3709 | 887 | 0.667 | 530 | 615 | 546 |
| 200 | 0.3853 | 788 | 0.705 | 490 | 825 | 650 |
| 190 | 0.3974 | 692 | 0.734 | 480 | 980 | 678 |
| 180 | 0.4127 | 605 | 0.760 | 480 | 1445 | 875 |
| 170 | 0.4307 | 529 | 0.784 | 487 | 1820 | 963 |
| 160 | 0.4516 | 460 | 0.807 | 470 | 2350 | 1081 |
| 150 | 0.4753 | 397 | 0.829 | 450 | 2960 | 1175 |
| 140 | 0.5026 | 338 | 0.850 | 436 | 3390 | 1146 |
| 130 | 0.5348 | 282 | 0.870 | 420 | 3806 | 1073 |
| 120 | 0.5742 | 230 | 0.890 | 420 | 4500 | 1035 |
| 115 | 0.5980 | 206 | 0.899 | 428 | 5002 | 1030 |
| 110 | 0.6238 | 183 | 0.907 | 440 | 5650 | 1034 |
| 105 | 0.6530 | 162 | 0.915 | 444 | 6000 | 972 |
| 100 | 0.6858 | 144 | 0.923 | 435 | 6400 | 922 |
| 95 | 0.7222 | 127 | 0.930 | 420 | 6380 | 810 |
| 90 | 0.7644 | 112 | 0.936 | 410 | 6270 | 702 |
| 85 | 0.8120 | 98.8 | 0.941 | 407 | 6250 | 618 |
| 80 | 0.8634 | 86.5 | 0.945 | 410 | 6165 | 533 |
| 75 | 0.9220 | 76.8 | 0.949 | 413 | 5910 | 454 |
| 70 | 0.9861 | 71.5 | 0.953 | 418 | 5620 | 402 |
| 65 | 1.062 | 68.0 | 0.957 | 422 | 5248 | 357 |
| 60 | 1.146 | 66.0 | 0.960 | 426 | 4760 | 314 |
| 55 | 1.225 | 66.0 | 0.963 | 429 | 4400 | 290 |
| 50 | 1.302 | 66.0 | 0.966 | 428 | 3850 | 254 |
| 45 | 1.377 | 66.0 | 0.970 | 424 | 3312 | 218 |
| 40 | 1.452 | 66.0 | 0.973 | 418 | 2880 | 190 |
| 35 | 1.528 | 66.4 | 0.975 | 411 | 2460 | 163 |
| 30 | 1.603 | 67.3 | 0.977 | 406 | 2164 | 146 |
| 25 | 1.670 | 68.1 | 0.978 | 405 | 2013 | 137 |
| 20 | 1.739 | 69.6 | 0.979 | 408 | 1774 | 123 |
| 10 | 1.870 | 72.3 | 0.979 | 430 | 1390 | 100 |
| 0 | 2.000 | 76.8 | 0.980 | 495 | 1088 | 84 |
| -10 | 2.123 | 83.0 | 0.980 | 574 | 662 | 55 |
| -20 | 2.242 | 90.5 | 0.981 | 660 | 378 | 34 |

TABLE 9.—*The Solar Energy Curve. Rock Salt Prism. September 6, 1922*

| Prismatic deviation from <i>A</i> | Wave length μ | Dispersion coefficient | Coelostat reflection | Spectro-scope coefficient | Prismatic energy curve outside atmosphere | Normal energy curve outside atmosphere |
|-----------------------------------|-------------------|------------------------|----------------------|---------------------------|---|--|
| 200' | 0.3749 | 1585 | 0.676 | 630 | 199 | 313 |
| 190 | 0.3820 | 1484 | 0.699 | 592 | 193 | 286 |
| 180 | 0.3881 | 1384 | 0.717 | 562 | 231 | 321 |
| 170 | 0.3975 | 1280 | 0.735 | 543 | 335 | 429 |
| 160 | 0.4057 | 1193 | 0.751 | 526 | 420 | 500 |
| 150 | 0.4145 | 1113 | 0.766 | 508 | 447 | 496 |
| 140 | 0.4242 | 1036 | 0.781 | 492 | 461 | 477 |
| 130 | 0.4350 | 958 | 0.796 | 476 | 524 | 502 |
| 120 | 0.4463 | 886 | 0.811 | 463 | 620 | 549 |
| 110 | 0.4590 | 817 | 0.825 | 450 | 672 | 549 |
| 105 | 0.4652 | 785 | 0.831 | 443 | 676 | 530 |
| 100 | 0.4720 | 750 | 0.839 | 436 | 745 | 558 |
| 95 | 0.4790 | 714 | 0.845 | 430 | 826 | 590 |
| 90 | 0.4860 | 679 | 0.852 | 424 | 867 | 589 |
| 85 | 0.4937 | 642 | 0.858 | 419 | 880 | 565 |
| 80 | 0.5017 | 607 | 0.865 | 414 | 917 | 555 |
| 75 | 0.5105 | 571 | 0.871 | 408 | 951 | 544 |
| 70 | 0.5199 | 534 | 0.877 | 402 | 974 | 521 |
| 65 | 0.5290 | 500 | 0.882 | 396 | 1020 | 510 |
| 60 | 0.5400 | 466 | 0.888 | 392 | 1088 | 507 |
| 55 | 0.5513 | 434 | 0.893 | 388 | 1165 | 506 |
| 50 | 0.5638 | 404 | 0.898 | 384 | 1228 | 496 |
| 45 | 0.5767 | 377 | 0.902 | 379 | 1307 | 493 |
| 40 | 0.5905 | 351 | 0.907 | 374 | 1426 | 501 |
| 35 | 0.6052 | 323 | 0.910 | 368 | 1436 | 464 |
| 30 | 0.6212 | 294 | 0.914 | 362 | 1482 | 435 |
| 25 | 0.6380 | 267 | 0.917 | 355 | 1517 | 404 |
| 20 | 0.6557 | 243 | 0.920 | 348 | 1648 | 400 |
| 15 | 0.6784 | 222 | 0.923 | 341 | 1743 | 386 |
| 10 | 0.7037 | 199 | 0.927 | 334 | 1843 | 366 |
| 5 | 0.7302 | 174 | 0.930 | 326 | 1965 | 342 |
| 0 | 0.7604 | 152 | 0.933 | 318 | 2087 | 317 |
| —5 | 0.7957 | 135 | 0.935 | 307 | 2170 | 293 |
| —10 | 0.8321 | 117 | 0.937 | 298 | 2261 | 265 |
| —15 | 0.8788 | 975 | 0.939 | 290 | 2396 | 234 |
| —20 | 0.9322 | 820 | 0.941 | 282 | 2514 | 206 |
| —25 | 0.9970 | 670 | 0.943 | 272 | 2676 | 179 |
| —30 | 1.093 | 527 | 0.945 | 262 | 2831 | 149 |
| —35 | 1.202 | 402 | 0.947 | 250 | 2897 | 117 |
| —40 | 1.332 | 300 | 0.949 | 242 | 2961 | 89 |
| —45 | 1.500 | 245 | 0.951 | 232 | 2947 | 72 |
| —50 | 1.751 | 216 | 0.953 | 222 | 2821 | 61 |
| —55 | 2.070 | 208 | 0.954 | 212 | 1657 | 35 |

In further reduction we now include the mean result of 1920, the U. V. glass prism result of 1922, and the rock salt prism result of 1922, with the object of comparing these several determinations, getting from them the best general representative values, and finally comparing these with the earlier results of 1903 to 1910, and 1916 to 1918, respectively, given in Table 58 of Volume IV, *Annals Astrophysical Observatory*. In order to do this we first reduced the results of 1922 to the scale of those of 1920. In the following table we do not retain the individual wave lengths observed for rock salt, but have read off from a large scale plot the values which the rock salt work would indicate for the wave length places used in U. V. glass work.

We give in figure 1 the individual values found for the different wave lengths for the work of 1920 and the U. V. glass and rock salt prisms in 1922. As will be seen by inspection of the plot, when we consider all circumstances, particularly the wide differences in dispersion characteristics, the agreement of the rock salt work of 1922 with the U. V. glass work of 1920 is little less than remarkable over the whole extent of spectrum covered. Agreement even descends to the details in the solar bands near wave lengths 0.386, 0.425, and 0.535 micron. There are moderate divergences central at wave lengths 0.65 and 1.3 microns. The discrepancy beyond 1.7 microns is not surprising in view of the difficulty introduced by the water-vapor bands, and the approaching opacity of U. V. crown glass.

Turning to the U. V. glass work of 1922, its agreement with 1920 between wave lengths 0.5 and 1.7 microns is nearly perfect. At greater wave lengths than 1.7 it lies between the 1920 work and the rock salt work. For wave lengths less than 0.5 micron there is a pretty wide divergence, the 1922 U. V. glass work running smaller. The departure does not much exceed 10 per cent until the wave length is less than 0.40 micron.

We incline to attribute this ultra-violet discrepancy to the inferiority of the day, September 5, 1922, as indicated by the logarithmic plots of atmospheric extrapolation. These indicate that the sky was growing less transparent towards noon, for the computed coefficients of atmospheric transmission in the infra-red are all closer to unity than they ought to be. This mediocre character, and the excessively high transmission coefficients, would scarcely affect the form of the energy curve for wave lengths greater than 0.6 micron, because here the atmospheric transmission is always above 90 per cent, so that changes of it affect the form of curve only slightly. But supposing the sky

TABLE 10.—*Comparison of Normal Solar Energy Curves*

| Wave length ω_1 | U. V. glass de- viation from μ | Energy curves outside the atmosphere | | | | | | Weighted mean, 1920-22 |
|---------------------------|---|--------------------------------------|---------------|---------------|---------|---------------------------------------|---------|------------------------------|
| | | 1920 | 1922 U. V. | 1922 R. S. | 1903-10 | 1903-10 omitting quartz work | 1916-18 | |
| 0.3415 | 240' | 262 | ... | ... | 226 | ... | 263 | 262 |
| 0.3504 | 230 | 307 | 200 | ... | 272' | ... | 304 | 281 |
| 0.3600 | 220 | 330 | 230 | ... | 310 | ... | 330 | 297 |
| 0.3709 | 210 | 340 | 251 | 325 | 342 | ... | 353 | 318 |
| 0.3853 | 200 | 304 | 299 | 300 | 344 | ... | 385 | 301 |
| 0.3974 | 190 | 343 | 312 | 350 | 413 | ... | 411 | 340 |
| 0.4127 | 180 | 484 | 403 | 513 | 506 | 500 | 567 | 480 |
| 0.4307 | 170 | 482 | 443 | 495 | 535 | 506 | 518 | 479 |
| 0.4516 | 160 | 569 | 497 | 548 | 610 | 567 | 580 | 548 |
| 0.4753 | 150 | 570 | 540 | 575 | 625 | 569 | 622 | 566 |
| 0.5026 | 140 | 558 | 527 | 553 | 604 | 548 | 566 | 546 |
| 0.5348 | 130 | 515 | 493 | 509 | 578 | 515 | 530 | 506 |
| 0.5742 | 120 | 498 | 476 | 493 | 538 | 484 | 508 | 489 |
| 0.5980 | 115 | 487 | 474 | 493 | 505 | 464 | 482 | 485 |
| 0.6238 | 110 | 466 | 475 | 430 | 472 | 434 | 450 | 457 |
| 0.6530 | 105 | 446 | 447 | 400 | 424 | 400 | 423 | 431 |
| 0.6858 | 100 | 419 | 424 | 384 | 384 | 370 | 391 | 409 |
| 0.7222 | 95 | 373 | 373 | 350 | 333 | 340 | 351 | 366 |
| 0.7644 | 90 | 332 | 323 | 315 | 293 | 310 | 313 | 323 |
| 0.8120 | 85 | 287 | 284 | 279 | 256 | 275 | 278 | 283 |
| 0.8634 | 80 | 244 | 245 | 244 | 227 | 245 | 247 | 244 |
| 0.9220 | 75 | 212 | 209 | 211 | 198 | 220 | 212 | 211 |
| 0.9861 | 70 | 191 | 185 | 191 | 172 | 200 | 187 | 189 |
| 1.062 | 65 | 182 | 164 | 162 | 144 | 180 | 165 | 169 |
| 1.146 | 60 | 150 | 144 | 135 | 119 | 153 | 135 | 143 |
| 1.225 | 55 | 133 | 133 | 113 | 102 | 125 | 118 | 126 |
| 1.302 | 50 | 113 | 117 | 96 | 89 | 96 | 101 | 109 |
| 1.377 | 45 | 97 | 100 | 84 | 78 | 85 | 87 | 94 |
| 1.452 | 40 | 87 | 87 | 76 | 68 | 75 | 75 | 83 |
| 1.528 | 35 | 77 | 74 | 72 | 59 | 67 | 65 | 74 |
| 1.603 | 30 | 68 | 67 | 68 | 52 | 57 | 57 | 68 |
| 1.670 | 25 | 60 | 63 | 63 | 45 | 51 | 50 | 62 |
| 1.738 | 20 | 53 | 57 | 61 | 42 | 46 | 45 | 57 |
| 1.870 | 10 | 40 | 46 | 51 | 33 | 38 | 31 | 46 |
| 2.000 | 00 | 28 | 39 | 42 | 25 | 26 | 23 | 36 |
| 2.123 | -10 | 18 | 25 | 32 | 18 | ... | 15 | 25 |
| 2.242 | -20 | 16 | 16 | ... | 14 | ... | 12 | 16 |
| 2.348 | -30 | 20 | ... | ... | 12 | ... | 10 | 20 |

was actually growing worse, the effect on the wave lengths less than 0.6 micron would be more and more serious, as indeed the energy curves of figure 1 indicate.

The second day, September 6, is not subject to this criticism. The work of 1920 rests on many good days of observation. Accordingly we decided to give the 1920 work and the 1922 rock salt work each double weight for wave lengths less than 0.5 micron, and all three curves equal weight for greater wave lengths. With this convention we compute the weighted mean of table 10 as plotted in heavy full line in figure 1.

This new result, namely the weighted mean of the 1920 and 1922 observations, given in table 10 and in the heavy full line of figure 1, we regard as our best determination of the form of the solar energy curve outside the atmosphere.

It rests principally on our very careful work of 1920, which, however, on account of its divergence from our previously published work of 1903 to 1910 we had hesitated to publish until further tested. Now it is confirmed beautifully by the rock salt work of 1922, a determination as absolutely different as possible. The principal differences are: Silver in place of stellite at the coelostat; new stellite mirrors in the usual spectroscope; a flint glass prism of high dispersion in place of the low dispersion U. V. crown prism in the auxiliary spectroscope; a rock salt prism of excessively different dispersion in place of the U. V. crown glass prism in the usual spectroscope; a new bolometer and new galvanometer. Also the U. V. crown glass work of 1922 is in almost perfect agreement over the whole range of longer wave lengths, and where it differs in the visible and ultra-violet it differs in the opposite sense to the 1903 to 1910 work.

We place little confidence in our work of 1916 to 1918 on the form of the energy curve, for a reason already explained in Volume IV of the *Annals*. To avoid confusion we have not plotted it, although its mean result is given in table 10. The mean value of 1903 to 1910 is given there and plotted in figure 1. As it rests on a great number of observations at different stations, and as these individual determinations differ widely among themselves, as given in the *Annals*, Volume III, table 62, it is interesting to examine them separately and see if any class of the individual determinations would have tended to agree better with the new work. We are at once struck by the fact that it is the quartz prism work at Mt. Wilson and Mt. Whitney which has given most of the divergence, excepting of course the three short-wave values at the top of column 4 of the above cited

Table 62 of *Annals*, Volume III. These are very likely vitiated by stray light. The quartz prism was very imperfect, being greatly blemished by interior striae and a tinge of smokiness, and its definition was so abominable that hardly any lines could be distinguished in its solar spectrum. Very possibly the determinations with quartz ought therefore to be rejected.

If we should reject all of them, there would result the following modification of Table 62 of *Annals*, Volume III:

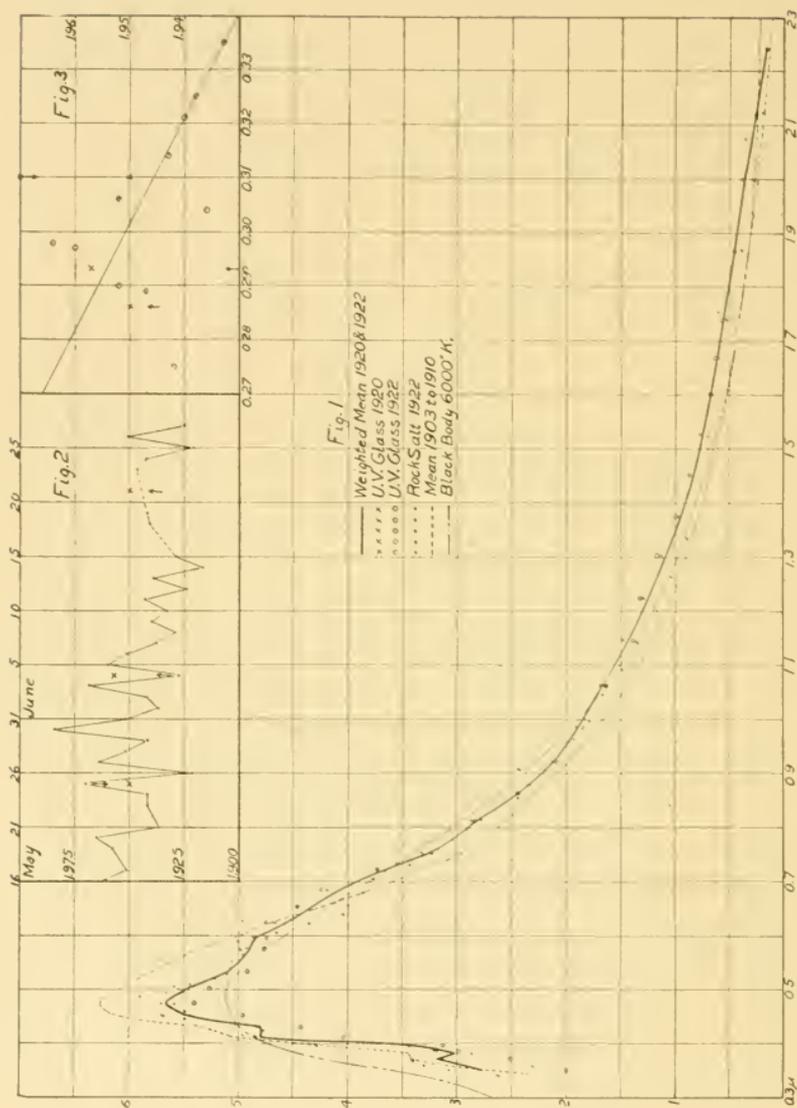
| | | | | | | | |
|--|------|------|------|------|------|-------|-------|
| Wave length | 0.42 | 0.43 | 0.45 | 0.47 | 0.50 | 0.55 | 0.60 |
| Percentage correction by determinations 1, 2, 3, 4.. | -3.7 | -4.8 | -6.1 | -8.7 | -9.3 | -10.5 | -10.1 |
| Corrected intensities..... | 506 | 506 | 566 | 570 | 550 | 503 | 453 |

| | | | | | | |
|--|------|------|------|------|------|------|
| Wave length..... | 0.70 | 0.80 | 1.00 | 1.30 | 1.60 | 2.00 |
| Percentage correction by determinations 1, 2, 3, 4.. | -1.6 | +5.4 | +2.8 | +0.9 | +6.2 | +3.2 |
| Corrected intensities..... | 358 | 280 | 171 | 90.6 | 56.5 | 25.5 |

These corrected values are given in table 10 and are much closer to the new determination, indeed they are mainly in very good agreement. We therefore are the more confirmed in our view that the new values, the weighted mean of 1920 and 1922, are good, and that the old ones called "Mean 1903 to 1910" were vitiated by the inclusion of the numerous quartz prism determinations.

In figure 1 we have given in dot and dash lines the distribution of energy in the spectrum of the perfect radiator or "black body" at 6,000° absolute centigrade. It is apparent that closer agreement exists between this and the new curve of 1920 and 1922 than exists between it and the old one of 1903 to 1910. But still the observed solar energy curve is far from being of the "black body" form. In order to match the two from 0.6 to 2.0 microns, a higher "black body" temperature than 6,000° would be required, and then the visible and ultra-violet parts of the observed curve would lie far beneath the computed one.

We have explained this kind of phenomenon by a double hypothesis. First, because we see deeper into the sun the longer the wave length, because long-wave rays are less scattered. Hence the infra-red region is supplied by a hotter, because deeper lying, layer. Secondly,



FIGS. 1, 2, AND 3.

the profusion of Fraunhofer lines in the visible, and still more in the ultra-violet solar spectrum, must cut this part down very greatly. The purity of our spectrum does not suffice to enable us to restrict our measurements to spaces between the lines, as was done by Fabry and Buisson in their beautiful studies of the ultra-violet.¹ They find even for the ultra-violet solar spectrum between wave lengths 0.394 and 0.292 micron, the corresponding "black-body" temperatures between $6,020^{\circ}$ and $5,970^{\circ}$ K. These measurements, however, relate to the center of the solar image, while ours include the rays as mixed in ordinary sunlight and coming from all parts of the sun's image. Ours is therefore a cooler source than theirs.

Fabry and Buisson draw attention to our over-estimate of the transparency of the earth's atmosphere for rays in this region, which indeed we have already admitted. As they point out, it is impossible to determine the atmospheric transmission correctly in this region without screening out stray light arising in the more intense spectrum regions.

We may remark, however, that the high altitudes of our observing stations, as they tend strongly to build up the ultra-violet compared to other parts of the spectrum, are favorable to diminishing this source of error below what might appear from a mere inspection of Fabry and Buisson's sea-level atmospheric transmission coefficients.

As we have stated at the beginning, we have tried to estimate the effects of the three kinds of errors stray light produces in our work on the form of the ultra-violet solar energy curve outside the atmosphere. Two of these tend to make our values in the ultra-violet too high, and the third acts oppositely. Assuming for the moment that the spectroscopic correction factor is right, suppose the true ordinate of the energy curve outside the atmosphere for a wave length λ in the ultra-violet should be e_t , but that in the ordinary bolographic work we determine this ordinate from observations as e_c . The discrepancy is caused by stray light coming from another part of the spectrum, which increases the intensity observed at the wave length λ , and also increases the apparent atmospheric transmission coefficient because the stray light being of longer wave length is of higher real transmission coefficient than the ray in question. Let e_s be the intensity of the stray light outside the atmosphere, and a_s , a_c , and a_t be the true atmospheric transmission coefficient for stray light, the falsified computed one, and the true one for the wave length λ .

¹ *Astrophysical Journal*, December, 1921, and *Comptes rendus t.* 175, p. 156, 1922.

Then for air masses 2 and 1, respectively, the observed intensities will be:

$$\{e_t a_t^2 + e_s a_s^2\} \text{ and } \{e_t a_t + e_s a_s\}.$$

Therefore $\frac{e_t a_t^2 + a_s a_s^2}{e_t a_t + e_s a_s} = a_c$ and $e_c a_c = e_t a_t + e_s a_s$.

Whence $\frac{e_t}{e_c} = \frac{a_c}{a_t} \left\{ \frac{a_s - a_c}{a_s - a_t} \right\}$.

Judging from the visible appearance in the eyepiece of the bolometer, when the spectroscope is set for infra-red rays, where there is properly no visible light, the stray radiation there, and presumably in the ultra-violet region as well, represents impartially the whole spectrum, for it appears in the infra-red as white light. If so, we may reasonably assign for a_s the value 0.90. Other lesser values, 0.80, 0.70, may also be used for illustrative purposes.

Take now a wave length in the ultra-violet for which a_c is 0.60. This in ordinary Mt. Wilson observing is about $\lambda = 0.35\mu$. In the following table we give values of the expression $\frac{e_t}{e_c}$ corresponding to assumed values of a_s and a_t , a_c being 0.60 in all cases.

TABLE II.—*Comparison of True and Measured Radiation Outside Atmosphere. Specimens of ratio $\frac{e_t}{e_c}$.*

| Stray light transmission | True transmission coefficient | | |
|--------------------------|-------------------------------|------|------|
| | 0.55 | 0.50 | 0.40 |
| 0.90 | 0.93 | 0.90 | 0.90 |
| 0.80 | 0.87 | 0.80 | 0.75 |
| 0.70 | 0.73 | 0.60 | 0.50 |

These illustrations indicate that for the more probable conditions the ratio of real to bolographically determined radiation outside the atmosphere, so far as this depends on daily observations, is between 0.8 and unity. It is of course easy to see why the ratio falls rapidly when the stray light is assumed to have nearly the same transmission coefficient as that observed, for it must then require a far greater dilution with the stray light to change equally the transmission coefficient of the combination.

Returning now to its influence on the spectroscopic correction factors, we have already pointed out that it tends to make this correction

factor too large, but just how much we cannot tell. However, as it works in the same sense as the combined effects just tabulated, we can finally say that the complete tendency of stray light is to cause the ultra-violet region of our spectrum energy curve to be too high. The real values would be such as to give smaller intensities in the ultra-violet than our curve indicates. In other words, the real curve would deviate still further below the "black-body" curve in the ultra-violet than figure 1 indicates.

That the error is not so large as the figures of table II indicate, or as readers of Fabry and Buisson's paper might suppose, seems apparent from computations by Fowle of the Rayleigh atmospheric transmission coefficients based on the number of molecules of air above Mt. Wilson. For comparison we give observed transmission coefficients of a good day, September 20, 1914, when we observed from sunrise until noon and also the mean of many good days of the years 1909 to 1912.¹

TABLE 12.—*Atmospheric Transmission Coefficients. Mt. Wilson*

| | | | | | | | |
|--------------------------------|-------|-------|-------|-------|-------|-------|-------|
| Wave-length in microns . . . | 0.342 | 0.350 | 0.360 | 0.371 | 0.384 | 0.397 | 0.413 |
| Computed | — | 0.617 | 0.650 | 0.684 | 0.719 | 0.751 | 0.784 |
| Observed Sept. 20, 1914. . . . | 0.615 | 0.600 | 0.618 | 0.681 | 0.681 | 0.743 | 0.764 |
| Observed mean of many days | 0.604 | 0.605 | 0.635 | 0.656 | 0.686 | 0.726 | 0.741 |

| | | | | | | |
|--------------------------------|-------|-------|-------|-------|-------|-------|
| Wave-length in microns . . . | 0.431 | 0.452 | 0.475 | 0.503 | 0.535 | 0.574 |
| Computed | 0.815 | 0.845 | 0.872 | 0.897 | 0.919 | 0.939 |
| Observed Sept. 20, 1914. . . . | 0.794 | 0.820 | 0.859 | 0.881 | 0.893 | 0.889 |
| Observed mean of many days | 0.784 | 0.812 | 0.841 | 0.865 | 0.882 | 0.887 |

Our observed transmission coefficients actually fall below the computed values for all wave lengths given in the table, which shows that even with the blue skies of excellent days on Mt. Wilson there is still some effect of haziness additional to molecular scattering. But we do not see that it is necessary to suppose that our observed values are greatly erroneous, at least for wave lengths above 0.350 micron.

¹ See *Annals Astrophysical Observatory*, Vol. IV, p. 243, and Vol. III, p. 138.

Before leaving the subject of our solar work and its relations to the ultra-violet solar observations of Fabry and Buisson, we give in the following table 13 Fabry and Buisson's determinations of atmospheric ozone for 14 days of the year 1920, and corresponding solar-constant values as determined by Smithsonian observers at Calama, Chile. In giving the solar-constant observations we add for three days corrected values. They are determined by drawing, in figure 2, a smoothed curve following the run of the numbers from day to day. In figure 3 we plot Fabry and Buisson's ozone values as abscissae, with solar-constant numbers as ordinates. The observed values are given

TABLE 13.—*Ozone and the Solar Constant*

| Date 1920 | Ozone value Fabry and Buisson | Solar constant, Calama | |
|--------------|-------------------------------------|------------------------|--------------|
| | | Observed | Smooth curve |
| | <i>cm.</i> | <i>cal.</i> | |
| May 21 | 0.304 | 1.936 | |
| 25 | 0.310 | 1.970 | 1.950 |
| 27 | 0.298 | 1.964 | |
| 28 | 0.290 | 1.952 | |
| 29 | 0.275 | 1.942 | |
| 31 | 0.306 | 1.952 | |
| June 4 | 0.293 | 1.929 | 1.957 |
| 5 | 0.297 | 1.960 | |
| 7 | 0.325 | 1.938 | |
| 9 | 0.321 | 1.940 | |
| 10 | 0.335 | 1.933 | |
| 11 | 0.314 | 1.943 | |
| 21 | 0.286 | ... | 1.950 |
| 23 | 0.289 | 1.947 | |

as circles, the corrected values as crosses. We believe readers who examine figure 2 will scarcely hesitate to think the three corrected values (the crosses) are probable ones. If that is admitted, we think the run of observations in figure 3 gives some indication that increasing values of the solar constant are associated with decreasing quantities of atmospheric ozone.

If this is so, the important infra-red ozone band¹ at a wave length of about 10.4 microns, falling exactly in the region where terrestrial radiation is otherwise most freely transmitted by the atmosphere, very likely changes greatly its absorbing power for outgoing earth rays along with changes in the solar radiation, but in the sense to

¹ See figure 41, *Annals Astrophysical Observatory*, Vol. IV, p. 285.

diminish terrestrial temperatures as solar radiation increases. This, if true, must be an important meteorological consideration. We hope soon to make an investigation of this ozone problem.

STELLAR SPECTRUM ENERGY CURVES

By invitation of Dr. Hale, given in the year 1916, we devised a spectro-bolographic outfit for obtaining spectrum energy curves of images of the brighter stars focused by the 100-inch telescope of the Mount Wilson Solar Observatory. The experiments were unavoidably postponed until the summer of 1922. We do not give here an extended account of them because we hope to repeat them with improvements in sensitiveness and accuracy. We are convinced that though we succeeded in making a vacuum galvanometer of 11 ohms resistance with which we measured 5×10^{-12} amperes, and though in combination with the vacuum bolometer we measured with it a change of temperature of 1×10^{-8} degrees Centigrade, satisfactory stellar spectrum energy observations demand at least tenfold more sensitiveness with fivefold less disturbance than we could achieve in this way. Hence, although we observed roughly the distribution of energy in the spectra of 10 of the brighter stars, including nearly all of the principal Harvard classes, we propose to employ new devices in further experiments.

Without the aid furnished by Dr. Stratton and the Bureau of Standards, Dr. Thomson and the General Electric Laboratory, at Lynn, Dr. Nichols and the Nela Research Laboratory, and especially Dr. Hale, Dr. Adams, and the staff of the Mount Wilson Solar Observatory, we could not have obtained these preliminary results.

Figure 4 gives a general view of the arrangement of apparatus successfully employed after a failure of preliminary experiments at the Newtonian focus of the great telescope, due to electrical and temperature disturbances. The rays *ab* coming from the star were reflected from *b* backwards towards the focus of the 100-inch mirror and were reflected a second time at *c* by a convex mirror whose property it was to increase the focal length from 40 to 250 feet. There was a third reflection by a plane mirror at *d*, so that the rays came at length to the so-called Coudé focus at *e*, in the southern prolongation of the equatorial axis of the telescope.

Here the rays entered the nearly constant temperature room *g*, whose roof, walls, floors, and piers are so massively built of cement as almost to remind one of Egyptian pyramids. The star rays diverged to the concave mirror *f* (at 6 meters distance beyond the

Coudé focus) which brought them a second time to focus over a meter distant at the slit *g*. Thence they diverged to the collimating mirror *h*, of 45 centimeters focus, proceeded parallel to the 18°

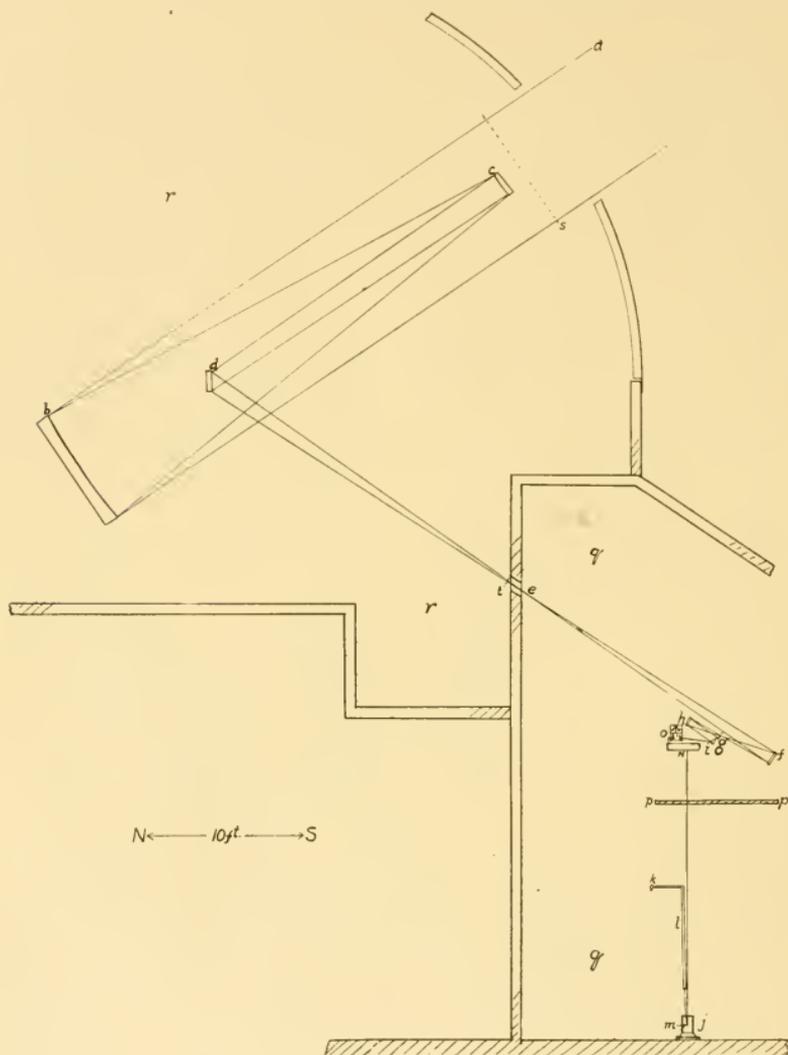


FIG. 4.

ultra-violet crown glass prism *i*, and were returned nearly over the same path by a reflecting coat of silver on the back of the prism so that they came at last to focus on the special vacuum bolometer close to the slit *g*.

Electrical connections led from the spectrobolometer situated 6 meters above the floor (but conveniently adjustable from the platform p, p) to the special magnetically shielded galvanometer j , whose tiny platinized mirror, m , reflected a beam of light from the brilliant special incandescent lamp k up to the photographic plate carrier n , where holographs of the stellar spectra were to be taken. The astronomical clock o was connected so as to move the prism and photographic plate simultaneously for this purpose.

In practise we found that owing (1) to a slow but persistent drift of the galvanometer due to temperature changes, and (2) to a continual oscillation of the galvanometer light spot over a range of from 1 to 5 millimeters, occasioned apparently by electrical oscillations induced by power and light circuits, it was inadvisable to use the photographic recorder. All of our results were obtained by eye observing upon a ground glass scale drawn with luminous paint, and resting on the platform p, p , at 5 meters from the galvanometer.

The procedure of observing was as follows: A selected star having been brought into focus at e by the night assistant at the telescope in the dome, r, r , the mirror, f , was adjusted so as to form its image centrally within the slit at g . The prism, previously set by means of a sodium flame exposed at c so that the D line fell upon the bolometer, was then rotated by turning the driving shaft which connected to the clock o through a certain number of turns sufficient to go beyond the region of spectrum where sensible heat could be observed. Then one observer (Mr. Aldrich) made successive settings of whole turns down through the star spectrum, and recorded the other observer's (Mr. Abbot's) galvanometer readings at these settings. Arrived at the other end of the spectrum region where sensible deflections were observed, a return series of settings was made at places half-way between those of the first series. Exposures in the spectrum were made by pulling a cord which lifted a shutter at t near the Coudé focus. Frequently the slit g was inspected from a distance by a telescope so as to correct if necessary the position of the star image within its jaws.

All of the observations of stellar spectra were made when the stars observed were within less than 50° of the zenith, so that the air-mass never exceeded 1.5. For the purpose of eliminating in one operation the selective losses in the atmosphere, the telescope, and the spectroscope, so far as necessary for such rough measures, it was contrived to observe near midday with the same apparatus an image of the sun whose energy spectrum is known. For this purpose a screen, s , with eight symmetrically distributed quarter-inch holes was placed

over the top of the telescope tube, and a diaphragm of $\frac{1}{8}$ -inch aperture inserted at t . These reductions of the solar intensity sufficed, with a little series resistance added in the galvanometer circuit, to permit the solar spectrum to be observed on nearly equal terms with those of the stars. The factor of reduction to bring the sun down to about the intensity of Capella proved to be as expected a little more than 26 magnitudes.

Employing these solar comparisons together with the 1920 determination of the forms of the sun's energy curve outside the atmosphere both for the prismatic and the normal spectra, we have eliminated selective effects of absorption from the stellar spectra which follow.

On various accounts we are unable to claim much accuracy for our results. They are to be regarded merely as a preliminary feeling-out of the problem. Better knowledge of the distribution of these stellar spectra has, we believe, already been obtained by Coblentz with his method of absorbing screens, also being employed by Pettit and Nicholson. But of course if the employment of a prism could be made satisfactorily, its results would be far preferable to those of absorption methods. Our experiments show us just what must be done to bring this about, and we now have great hope of succeeding in new experiments with modified instruments.

In our experiments of 1922 the principal defects are these:

1. Insufficient sensitiveness. It was impossible to measure the radiation, as weakened by increasing prismatic dispersion and increasing atmospheric and instrumental absorption, far enough towards the violet to follow with any accuracy the normal spectra of stars of types G , F , A , and B to their maxima.

2. Insufficient accuracy of wave length. With the moderate dispersion of what was practically a 36° crown glass prism, the wanderings of the star image in the wide slit of the spectroscope were sufficient to produce uncertainties of wave length amounting roughly to as much as the distance from D to B in the orange-red of the spectrum. This defect could have been reduced greatly had we been able to continue the experiments one or two more nights, and will easily be made small hereafter by better following devices.

3. Insufficient accuracy of intensity measures. Owing to bad following the image wandered sometimes partly onto the slit jaw before it was corrected. This would, of course, have been prevented had the work gone on. But more serious, because incessant, were the oscillations of the galvanometer light-spot on the scale, through amounts which, for some stars, were nearly as great as the observed maximum deflection in the spectrum. Though every deflection re-

TABLE 14.—Original Observations of Intensities in Stellar Spectra
Galeometer deflections in millimeters

| Spectrum place | | Name of star observed, its magnitude and spectrum class | | | | | | | | | | |
|--------------------|-------------|---|---------------------------------------|-------------------------------------|--|--------------------------------------|--|----------------------------|---|--------------------------------------|---|--|
| Shaft turns from D | Wave length | ϵ Orionis 1.8, B_0 (2) | β Orionis 0.3, B_8P (2) | α Lyrae 0.1, A_0 (3) | α Can. Mag. -1.6, A_0 (3) | α Aquile 0.9, F_5 (3) | α Aurige 0.2, G_0 (2) (3) | Sun -26.5, G_0 (1) | α Tauri 1.1, K_5 (2) (3) | β Pegasi Var., M_0 (2) | α Herculis Var., M_b (2) | α Orionis Var., M_0 (1) (3) |
| -3.0 | 0.477 | 0 | ... | ... | ... | ... | 0 1 | ... | .. | ... | ... | .. |
| -2.5 | 0.465 | ... | ... | ... | ... | 0 | 1 .. | 3 | .. | ... | ... | .. |
| -2.0 | 0.484 | 0 | 0 | ... | 1 | ... | 2 1.5 | ... | .. 1.5 | ... | ... | .. |
| -1.5 | 0.505 | 0 | 0 | ... | ... | 2.5 | 3 .. | 13 | 0 5 | ... | ... | .. |
| -1.0 | 0.529 | 0.5 | 1.5 | ... | 10 | ... | 3 4 | ... | .. 3 | ... | ... | .. 1 |
| -0.5 | 0.557 | 4 | 6 | 0 | 9 | 2 | 7 .. | 20 | 2 7 | ... | ... | .. |
| 0.0 | 0.589 | 4.5 | 2 | 6 | 15 | ... | 5 7 | 37 | 3 7 | ... | 0.5 | 0.5 9 |
| +0.5 | 0.628 | 5.5 | 1 | 1.5 | 13 | 6 | 4 .. | 34 | 3 10 | ... | ... | 1.5 0 |
| 1.0 | 0.674 | 1 | 5 | 4 | 11 | 5 | 7 10 | 43 | 5 13 | 0 | 5 | 3 16 |
| 1.5 | 0.729 | ... | 0 | 5 | 17 | 5 | 6 .. | 45 | 4 14 | ... | ... | 6.5 11 |
| 2.0 | 0.797 | ... | 0 | 4 | 6 | 2 | 6 14 | 45 | 9 17 | 4? | 9 | 9 18 |
| 2.5 | 0.874 | ... | ... | 6 | ... | 1.5 | 6 .. | 45 | 4 15 | ... | ... | 12.5 26 |
| 3.0 | 0.956 | ... | ... | 2.5 | 1 | ... | 5 15 | 36 | 12 15 | 5? | 7 | 9 33 |
| 3.5 | 1.088 | ... | ... | 3 | ... | ... | 1 8.5 | 41 | 7 .. | ... | ... | 6 30 |
| 4.0 | 1.204 | ... | ... | 0 | ... | ... | 1 7 | 30 | 10 13.5 | 0.5? | 7 | 3 23 |
| 4.5 | 1.320 | ... | ... | ... | ... | ... | .. 6 | 30 | 10 .. | ... | ... | 2.5 29 |
| 5.0 | 1.434 | ... | ... | ... | ... | ... | .. 2 | 18 | 10 14 | 0 | 5 | 2 16 |
| 5.5 | 1.544 | ... | ... | ... | ... | ... | | 13 | 4 .. | ... | ... | 2 20 |
| 6.0 | 1.652 | ... | ... | ... | ... | ... | | 15 | 0 3.5 | 0 | 1 | 1 28 |
| 6.5 | 1.755 | ... | ... | ... | ... | ... | | 11 | 0 .. | ... | ... | .. 11 |
| 7.0 | 1.855 | ... | ... | ... | ... | ... | | 4 | 0 0 | 0 | 0 | .. 7 |
| 7.5 | 1.954 | ... | ... | ... | ... | ... | | ... | | ... | ... | .. 5 |
| 8.0 | 2.048 | ... | ... | ... | ... | ... | | ... | | ... | ... | .. 12 |
| 8.5 | 2.141 | ... | ... | ... | ... | ... | | ... | | ... | ... | .. 0 |
| 9.0 | 2.230 | ... | ... | ... | ... | ... | | ... | | ... | ... | .. 0.5 |

(1) Observations of August 19, 1922.

(2) Observations of September 13, 1922.

(3) Observations of September 14, 1922.

corded is the mean of several trials, it cannot be hoped that these relatively large disturbances are eliminated satisfactorily. Moreover, the uncertainties of wave-length settings mentioned above aggravate the errors of intensities, because the deflections, even if true, might have related to wave lengths somewhat different from those supposed. If the experiments on each star had been repeated several times on later nights very much greater accuracy could doubtless have been had in the final means. But, after all, the sensitiveness available was not adequate ever to give satisfactory results, and it would have been a waste of time to go on with the apparatus as it was in 1922. With these remarks we give the observations. We have arranged the stars in order of the Harvard spectrum classification, although the order of observing followed approximately the order of their right ascensions.

The scale of galvanometer deflections differs on the three nights of observation and even at different hours of the same night according to the time of swing which was practicable at the time. Wherever there are two observations on one star we have reduced the smaller deflection data to the scale of the larger approximately and have given the observations of larger deflection greater weight in drawing smoothed curves. In view of what has been said of the sources of error always present, readers will not be surprised at the irregularities which the data present.

As the work is altogether rough and preliminary we shall not take space to detail what steps were necessary to reduce the direct observations for the selective losses in the atmosphere and the apparatus, merely repeating that these reductions depended on the solar-spectrum observations of 1920 taken together with those made on August 19, 1922, with the great telescope and stellar spectro-bolometric outfit.

In figure 5 we have given in smooth curves as well as we can the stellar distribution outside the atmosphere on the scale of the 36° ultra-violet crown glass prism, and in figure 6 the corresponding curves reduced to the normal or wave-length scale. In drawing the normal curves we were immediately made conscious that for the stars of types *B*, *A*, *F*, *G*, the original very small deflections in the shorter wave lengths lacked a sufficient degree of accuracy to warrant multiplying them by the very large prismatic dispersion factors. Such results would have had no meaning and would have been apt to mislead. Accordingly we cut off all of these normal curves beyond wave length 0.5 micron, and omitted four stars of types *B* and *A* for which the observed deflections at maximum ordinate in the prismatic spectrum did not exceed 5 millimeters.

Obviously in order to determine at all satisfactorily by heat methods the spectrum distribution for stars of types *B*, *A* and *F*, it will be necessary to use apparatus of a decidedly higher order of sensitiveness than ours.

On the whole the positions of maximum ordinates in the prismatic spectra shift with spectrum type much as we should have expected.

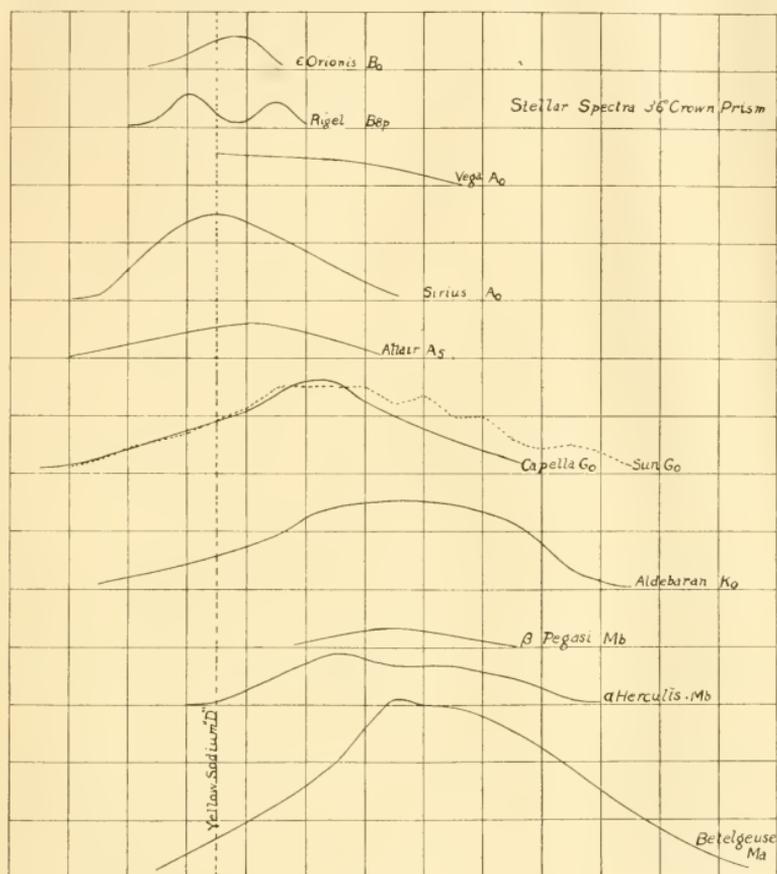


FIG. 5.

It is satisfactory that the curves for the sun and Capella agree so well. The several depressions in the infra-red of the solar curve are most likely real, as they coincide closely with great infra-red water vapor bands. The stellar curves would doubtless have shown them too if there had been enough energy so that they had been equally as accurate.

We attribute little weight to the circumstance that the maximum in the normal spectrum curve of α Herculis falls to the violet of that of α Orionis. That Aldebaran gives its maximum at shorter wave lengths than either, we think is real, but we do not feel confidence in the exact places for any one of the three. Greater accuracy is essential if real deductions as to star temperatures and their approach to "black body" conditions are to be made.

Though we have not concealed the shortcomings of these stellar observations, they cost a great deal of effort. Fatalities seemed to lurk about the work to surprise us so that we were almost ashamed to meet

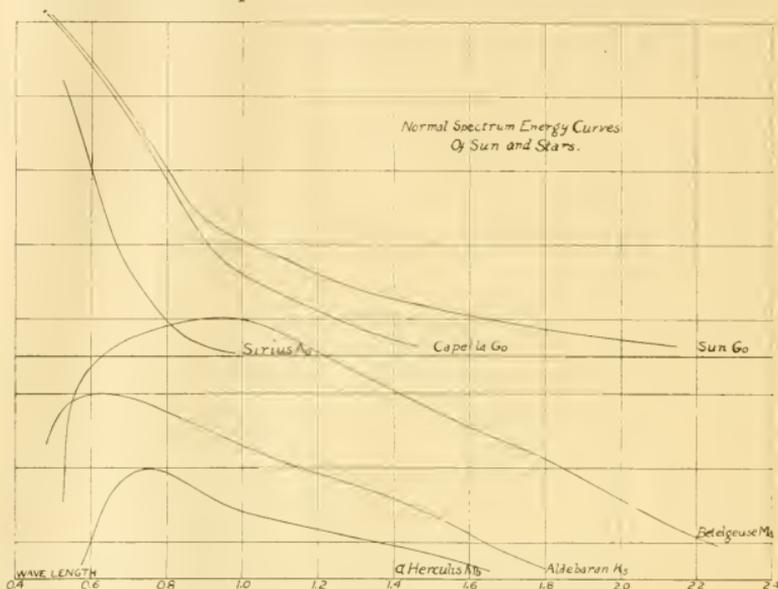


FIG. 6.

any one on Mount Wilson lest he should ask what new things had gone wrong that day. We made a list of all the serious mishaps, and they numbered nearly 30, some requiring a whole week to repair. But we feel after all that a decided step was made to have gotten from 10 to 30 millimeters deflection in the fairly extended spectra of four of the brightest stars. For it was not many years ago that Boys failed to recognize stellar heat, and Nichols observed but one or two millimeters in the total radiation of such stars. Naturally our success, such as it was, depended largely on the great size of the Mount Wilson telescope, but besides that it indicates a large gain in sensitiveness of apparatus. Furthermore, the experience gained clarifies the problem so exactly that plans for future experiments may now be laid with great certainty.