Philatelic Shade Discrimination Based on Measured Color

David L. Herendeen  
President and Senior Fellow, Institute for Analytical Philately, Inc.

James A. Allen  
Senior Fellow, Institute for Analytical Philately, Inc.

Thomas Lera  
Winton M. Blount Chair in Research, Smithsonian National Postal Museum

Prepared by the  
Institute for Analytical Philately, Inc.

Report IAP-2010-1  

November 2010

A version of this paper appeared in the  

London Philatelist, Vol. 120, No. 1384, April 2011, pp. 105-117.
Philatelic Shade Discrimination Based on Measured Color

David L. Herendeen*
President and Senior Fellow, Institute for Analytical Philately, Inc.

James A. Allen
Senior Fellow, Institute for Analytical Philately, Inc.

Thomas Lera
Winton M. Blount Chair in Research, Smithsonian National Postal Museum

Abstract. Color shades are an important aspect of philatelic study for a number of reasons. The two most important of these are the identification of specific printings and printers of stamp issues, and the discrimination of fraudulent stamps. For nearly a century, the identification of color shades has been done using two basic methods: firstly, by having reference collections of shades that can be compared to an unknown specimen; and, secondly, by training individuals with innate or intrinsic skills in color-matching to recognize the accepted shades as defined by earlier generations of such color experts.

This paper formulates a new methodology for shade identification using spectrographic measurements and color science. The methodology is then applied to a test case in order to validate its applicability.

Key words: color naming, color categories, philatelic color, shade discrimination, fuzzy set theory.

DEFINITIONS

Presented below are the definitions of a number of terms that are used throughout this paper.

Color System: also called “color-order system” is a system for arranging and describing color. At present, the most widely accepted color systems are those established by CIE (Commission Internationale de l’Eclairage) in 1931 based on visual experiments. These color systems have been modified and improved (e.g. 1960, 1976) to better reflect human visual perception of color.¹,²

Colorimetry: is the science and technology used to quantify and describe physically the human color perception, which was also established by CIE in 1931. Even though limitations are well recognized, the CIE system of colorimetry remains the only internationally agreed metric for color measurement. This definition is taken from Ohno’s excellent and recommended overview of colorimetry and the CIE color standards.³

Color Matching: is the process of determining if two colors match within a pre-determined tolerance, usually specified by some difference (i.e. distance) metric in one of the CIE color spaces.

Color Categorization: also called “color naming” or “color quantization” is the process of determining whether two colors can be visually discriminated, and then developing categories into which similar colors are placed.⁴

PHILATELIC COLOR

One of the most difficult technical issues facing advanced philatelists is the identification of stamp shades. A minor shade difference may translate into an economic value that may vary by several orders of magnitude from other stamps of different shades.

In early 1978, a study by Tyler and Peck⁵ used diffuse reflectance spectroscopy to discriminate between genuine, reprinted and forged stamps of the 1867-1868 Roman States issues. This was an application of colorimetry in which results were obtained by simple comparison of reflectance curves. The final sentence of this paper notes that:

It may be concluded that the method has considerable potential for application in the philatelic field, permitting absolute characterization of shades of color which previously could be determined only by subjective means.

In 1979 the Philatelic Foundation followed with a comprehensive effort to perform quantitative studies of color in philately.⁶ Norby (p. 116) notes, “The indiscriminate and in some instances incongruous naming of stamp colors must be resolved.” Unfortunately this situation persists now, thirty years later. This reference work presents excellent background information on: color theory; ink chemistry; paper manufacture; printing techniques; and nondestructive methods for

*Correspondence to David L. Herendeen (e-mail: DHerendeen@analyticalphilately.org)
color measurement and analysis. It also includes eleven case studies of color in specific stamps from a variety of countries. These studies only addressed colorimetry tangentially. Instead, they focused more on aspects of various x-ray emission spectroscopy techniques that allow chemical analysis of inks.

The only substantive recommendation was a proposal to adopt a very complicated set of color designations defined in the Munsell Book of Color. The findings of Kelly and Billmeyer were modified again in 1982, but the resulting complexity was far from “user friendly,” and it is doubtful if any collectors ever adopted any of the proposed conventions.9

Several subsequent studies used similar approaches,10,11 Chaplin et al. in particular gained widespread notice by using spectroscopic analysis to solve a long-standing controversy by distinguishing between genuine and forged Hawaiian Missionary stamps.

THE SCIENCE OF COLOR

Physics and Psychology

Color science encompasses two distinct areas. The first is the pure physics of light and its measurement. For simplicity, this will be called spectrometric analyses. The second is the psycho-physical manifestation of color by the human visual system, often called perception. Both of these areas have been widely studied because of their many applications including: pigments and dyes; inks; digital television; computer monitors; photography and many more. While extensive discussion of these areas is well beyond the scope of this study, specific important concepts and findings are presented as needed.

One of the most important aspects of spectrometry is the ability to measure color in an objective manner which, as noted earlier, is called colorimetry. Unfortunately, while the actual measurement of certain characteristics such as reflective or absorptive spectra is a well-defined physical phenomena, the perceptual interpretation of this electromagnetic radiation by the human eye is far from exact. The identification and comparison of colors may vary dramatically between observers, under different circumstances for the same observer, between sexes, and between the young and the elderly.

Thus, by definition, there is no exact answer to questions addressing human color perception. Instead, semi-empirical methods, often related to a specific problem domain, must be developed and used to approximate an exact meaning of “color.” In this study, the manual techniques used by a trained philatelic color expert are analyzed.

Colorimetric Analysis

As introduced above, it is generally accepted that color is a result of a psycho-physiological perception rather than an independent physical phenomenon. Specifically, it is the stimulation of the human visual system by what is called visible light. This light is simply electromagnetic radiation having wavelengths ranging from 380 nanometers (nm) to 780 nm.

While color can not be measured directly, the conditions leading to our perception of color sensations can be measured. As noted, the method for doing this was introduced in 1931 by the CIE. To measure the variables that create color sensations, the CIE established a reproducible, spectrophotometry based, device-independent color model constructed from a light source, an observer, and an object. The results of a CIE-compliant measurement and transformation are coordinates that locate the specimen in a horse-shoe-shaped color space representing human color perception. Such color spaces are called Chromaticity Diagrams, an example of such a diagram is shown later in Fig. 2. A more detailed discussion of these, and other, models is again beyond the scope of this paper (cf Refs. 1 and 2).

PHILATELIC COLOR CATEGORIZATION

The authors became involved in analytical color studies for philately in a study performed with partial funding from the Smithsonian National Postal Museum. Preliminary study had suggested that the identification of stamp shades was a problem in color matching. However, after collecting reflectance data for hundreds of samples, it became apparent that nearly every stamp (yes, even those in multiples) were different “colors” from a purely spectrographic perspective, at least in terms of chromaticity coordinates. As described in the following sections, the traditional manner in which shade determination has been made is actually through color categorization rather than matching. Therefore, the remainder of this paper formulates the theoretical basis for creating such categories.

The manual determination of shades for a family of similarly colored stamps is a straight-forward process. However, this simple observation understates the requirement that one must have an expert philatelist whose color acuity has been honed by thousands of hours of training. This requirement is supported by the extensive literature previously cited showing that the ability to distinguish and differentiate colors is extremely variable between individuals.

Generally, the color expert samples many hundreds of stamps of a given value and issue, say the U.S. 1851-1857 3c red stamp. For the vast majority of these stamps, there are many possible shades resulting from: different printings; different ink batches; different treatment of the printing plates such as cleaning and inking; different dampening of the paper; different plate pressures during the print run; and many more environmental considerations. Each sample stamp is then placed in a specific category to which a name is traditionally given. While many of the color names were first defined in the 19th century, they are still in common use today. For example, shades including orange brown, deep orange brown, copper brown, dull red, claret and others are used. The result of this categorization is still more complex. Within each of these categories, which are generally determined by chroma, or basic color, there are many
gradations, for example from light to dark.
While this primarily ad hoc procedure has been refined through the years, the question remains: can a theoretical basis for this methodology be defined?

I. MATHEMATICAL DEVELOPMENT

Hypothetical Example
Consider the manual procedure outlined in the previous section as applied to a universe, or population, of 38 samples of a specific stamp that appear to be shades of red. Assuming that the CIE 1976 $u', v'$ chromaticity coordinates for each sample are known, the plot shown in Fig. 1 may be constructed. Although not considered in this manner, some envelope of the points defines a color gamut, $G$, in this chromaticity space. The color expert has determined that the 38 points represent three perceptual colors. These fall into three subsets of the gamut, $A$, $B$ and $C$. As expected, the color categorization has partitioned the gamut into three equivalence classes such that:

$$G = A \cup B \cup C$$

$$A \cap B = \emptyset; A \cap C = \emptyset; \text{ and } B \cap C = \emptyset$$

By philatelic convention, these colors have been named Carmine-red, Red-brown and Carmine.

Further, suppose that two of these 38 points, labeled $P$ and $Q$, lie outside of the three sets. The expert feels that the colors represented by the two points is inconsistent with the other colors. This problem could arise from many circumstances, examples of which include: too small a data sample to encompass all of the possible shades; environmental changes to the color of samples which have permanently changed them; or counterfeit or forged samples printed in the wrong color. In any case, before continuing the analysis, it is necessary to resolve the problem with such points. For this hypothetical, the points will simply be ignored, i.e. eliminated.

The following steps present a methodology that is equivalent to the manual approach except all of the steps are performed by colorimetric analysis of spectrophotometry results.

Determining Chromaticity Coordinates
First, each stamp is sampled using a spectrophotometer. This device measures the resulting tristimulus values and converts them into points in the various CIE color model spaces. Without loss of generality, the CIE 1976 color space is used in this paper. Fig. 2 shows where the test samples, including the two eliminated points, lie in this full color space using the gamut defined by the color expert.

Now, in order to simplify the exposition, a mathematical idealization of this process is posed. Consider the polygon drawn in Fig. 3 to represent the color gamut covered by these samples. It has been constructed by determining the convex hull (CH) of the set of data points. The CH is the minimal convex set containing the data points. Other models are possible, and some were tested during this work. The convex hull was selected for simplicity. For any set $X$ of chromaticity points, define $H(X)$ as their convex hull.

The 36 data points, and the corresponding CH, are shown in Fig. 3. This is a very small area within the entire color space, as seen in Fig. 2. The small shaded ellipse shown in Fig. 3 is the proximate MacAdam ellipse. This is, the MacAdam ellipse closest to the algebraic center of the CH translated to that center.
In terms of the color matching process, points within a MacAdam ellipse are usually considered to represent the same perceptual color. Note that the dispersion of the hypothetical stamp shades, represented by the convex hull, is considerably larger than the MacAdam ellipse.

Next, the color expert sorted the 36 validated samples into a (modestly) finite number of color categories based on barely perceptible differences. For the hypothetical, it is assumed that this inspection results in three shades, or categories, that are denoted \( S_1, S_2, \) and \( S_3 \). Three CHs are then drawn using the chromaticity points within each of the categories:

\[
H_1 = H(S_1) \\
H_2 = H(S_2) \\
H_3 = H(S_3)
\]

Fig. 4 shows the three resulting hulls. Not surprisingly, these three hulls representing the shade categories do a good job of partitioning the set of all data points into disjoint subsets, the ideal situation.

Fuzzy Sets — A Natural Model

The analyses of the previous sections used standard set theory to describe the process of categorizing stamp shades. However, such “crisp” sets are not a realistic model for the uncertainty encountered in the perceptual color problem. An extension to set theory, called fuzzy set theory, is well-suited to describing the color category model. Fuzzy sets were so named because the usual bivalent requirement for set membership (i.e. a given element is either an element of a set, or not) is relaxed. Instead, the notion of “degrees of membership” was introduced. This allows gradations such as light and dark, or fast and slow to be represented.

This is easiest to see if the functional model of set theory is considered by defining the membership function \( \mu_A(x) \) such that:

\[
\mu_A(x) = 1 \text{ if } x \in A \\
\mu_A(x) = 0 \text{ if } x \notin A
\]

This relationship describes crisp set membership.

\[ \varphi_A(x) \in [0,1] \quad \forall x \]

Now, define a different membership function \( \varphi(x) \): This less precise statement allows membership to be measured such that for each \( x \), \( \varphi(x) \) might be 0, 1, or any real value in the closed interval \([0,1]\). While this function appears to be probabilistic, the proponents of fuzzy sets are quick to point out that it does not represent a probability, but rather a “possibility” that a given element is within a set.

Applying the Fuzzy Sets

In fact, the fuzziness of the shade categorization is self evident in both Figs. 1 and 4. There are many different “colors” in the spectrometric sense, but only three in the perceptual sense. The color expert has already applied de facto fuzzy membership functions.
When one considers the size of the CHs relative to MacAdam ellipses it is clear that different experts might well disagree on which shades fit which categories as the chromaticity moves away from the center of the individual CH.

This situation is illustrated in Fig. 5 which enlarges the data of $S_1$ of Fig. 4 along with the original data points. Since it is already conceded that some of the outlying data points could well be considered to be a different color by another expert, the CH $K$ is constructed. This is called the kernel of the set. The kernel represents the set of data that experts would agree are the same shade. In Fig. 5 the kernel, which is shown by the dashed line, has been constructed by reducing the CH by 10% of the length of the major semi-axes of the proximate MacAdam ellipse of the color gamut. The intent is that $K$ would form a greatest lower bound for the color category. Similarly, a larger CH, $F$, shown by the solid black line in Fig. 5, is constructed. At a distance of 90% of the major semi-axes of the MacAdam ellipse, $F$ represents a least upper bound on the shades that might be identified as “red carmine.”

While rational, the selection of the tolerances on the two hulls is somewhat arbitrary and may vary depending on the family of stamps being analyzed. The justification is for the total width between $K$ and $F$ to correspond to the major axis of the MacAdam ellipse, thus representing a region in which colors can be identified with less than certainty. The proportion assumed to represent the “inside” tolerance has been arbitrarily set to 10%.

The Membership Function

The membership function for the family of hulls shown in Fig. 5 may be expressed as:

\[
\begin{align*}
\text{if } (x, y) &\in K \text{ then } \varphi_F(x, y) = 1 \\
\text{if } (x, y) &\in F \text{ then } \varphi_F(x, y) \in [0,1] \\
\text{if } (x, y) &\notin (F \cup K) \text{ then } \varphi_F(x, y) = 0
\end{align*}
\]

The actual similarity function for points lying between the inner and outer hulls is defined by:

\[
\text{sim}(x, y) = 1 \left( \frac{\text{dist}_1}{\text{dist}_2} \right)^2
\]

where $\text{dist}(P, Q)$ is the Euclidean distance between any two points $P$ and $Q$ in the CIE-1976 chromaticity plane. The actual manner in which this function is applied to three typical points $A$, $B$ and $C$ is shown in Fig. 6. The CIE-1976 color difference is measured accurately by the simple Euclidean distance. The $\text{sim}$ function varies with the square of the distance ratio from 1.0 on the boundary of the inner CH to 0.0 on the boundary of the outer CH. This function had been selected to facilitate developing this methodology. Other metrics could be used such as the Gaussian distribution suggested by Regier et. al.

The Fuzzy Intersections

Fuzzy envelopes are then determined for each of the CHs shown in Fig. 4. They are all constructed in the manner described above. An idealization of the resulting hulls is shown in Fig. 7.

The figure shows the three kernels, $K_1$, $K_2$ and $K_3$, along with the outer hulls, $H_1$, $H_2$ and $H_3$. The intersections of the envelopes are simply:

\[
\begin{align*}
F_1 &= S_1 \cap S_2 \\
F_2 &= S_2 \cap S_3
\end{align*}
\]

Clearly the interesting sample points are those that lie inside the two fuzzy intersections, $F_1$ and $F_2$. There are seven such points (P1-P7) as seen in Fig. 7. By virtue of being contained in the intersections, the perceived colors for these samples become argumen-
An understanding of the color perception phenomenon virtually insures that multiple observers might well place the points into a different color category. This is analytically illustrated in Table 1. For each of the points shown in Fig. 7, the membership function is computed for the three categories. Referring to the table, all six of the samples would objectively be placed into the categories selected by the expert. Only $P_2$ has a membership function exceeding a possibility of 30%.

As seen, the model developed appears to agree with the heuristic results obtained by the human expert while having a sound basis in analytical color measurement. In the next section, the method will be validated by applying it to a case study.

**II. EXPERIMENTAL VALIDATION**

To test the validity of the theoretical model, a colorimetric analysis of actual stamps was performed. The results of the analytical testing was then compared to the results obtained by a philatelic color expert. The experimental procedures are described in the following sections.

**The Stamps Sampled**

There are many worldwide stamp issues which exhibit a wealth of color shades. For this validation, a subset of the postage due stamps issued in Slovenia (a former Yugoslavian territory) from 1919-1921 (Scott Yugoslavia 3LJ1-7 and 3LJ8-14) were used. These stamps were produced first in Vienna, Austria, and then in Ljubljana, Slovenia. The low (Vinar) values were printed in shades of red, with some brown components, and the high (Kruna) values were printed in shades of blue. The red stamps printed in Ljubljana were selected for testing. Four distinct shades of these stamps are presented in Fig. 8.

The definitive reference work on these issues indicates that there are nine identifiable shades. While some of the shades are quite distinct from one another, some are, at best, subtly different. (The author is especially intrigued by the murky brown brick red shade—someone clearly had a vivid imagination.) The stamps selected are known to have been produced by only two printings in Ljubljana. This would account for some, but not all, of the wide variety of shades. Other sources of shades may include: completely different ink batches, partial mixing of the printing ink, pressure differences during the transfer process, poor cleaning of the printing plates, and many others. Although at the outset of this study it was hoped that a sampling of all nine shades could be used, this was not possible. As a result, sufficient samples were available to consider four shades.

**The Instrumentation**

To perform this validation equipment manufactured by the English company Foster + Freeman was used. Called the Video Spectral Comparator 6000 (VSC 6000), it allowed the examination of samples in the visible and near ultraviolet regions of the spectrum carried out with incident and transmitted UV, visible and infrared illumination up to 1000nm. The device used, a photo of which is shown in Fig. 9, is located...
Sample Preparation and Measurement

All of the samples were mounted on gray card stock measuring 2.5in x 2.5in. Standard stamp mounts were used, but a large (1in diameter) hole was punched into each mount. This was done so that after mounting the exposed surface of the stamps was available to be tested without any interference from the mounts.

Each stamp was placed in the VSC6000 and enlarged using a magnification factor of 2.5 (250%). This magnification was selected so the sensor area (represented by crosshairs) was able to average the color over a small (0.03mm²) area. Then, five selected inked points were sampled for each stamp. The location of these points is shown in Fig. 10. Four points conformal to the inner elliptic design were sampled, as was the center of the stamp. An attempt was made to sample “pure” color, i.e. a region with no apparent white admixture, while remaining in a close neighborhood of the locations shown.

For each of the five points, the spectral reflectance curves were plotted to verify that the readings were yielding consistent results. During the data collection procedure, a visual inspection of each graph was made to insure that no highly inconsistent measurements were obtained. In the event that inconsistent data were recorded, one or more of the data points for the sample would be retested.

For each of the samples, a full range of colorimetry data were collected, and reviewed, including:

- chromaticity diagrams (both CIE 1931 and CIE UCS 1960)
- all tabular data including tristimulus values, CIE 1931 x,y coordinates, CIE UCS 1960 u,v coordinates and Color Space 1976 L*a*b* coordinates.
- All of the spectral reflectance curves in digital format.

Note that the CIE-1976 chromaticity coordinates u’, v’ are not reported. When needed, they were computed by an Excel spreadsheet from the measured tristimulus values.

Seventy Ljubljana stamps were tested, and the spectrographic results processed. These results are described in the following sections.

Sorting by Color Expert

Concurrently with the colorimetric analysis, the second author, a recognized philatelic color expert, sorted and categorized all of the samples by hand in a controlled environment with the samples illuminated with a 5000K daylight source as seen in Fig. 11. Samples were held at a constant angle of inclination with respect to the light source. This manual opera-
tion resulted in the identification and naming of four easily discernable shades:

- carmine
- deep brownish carmine
- brick red
- light brick red

During this procedure a number of anomalous results were encountered. Naturally, these problems had to be resolved before generating the analytical model of the test results.

Preconditioning the Expert Data

While the expert sorted and collated the shades of the test samples, a number of difficulties became apparent. These included:

- Samples that were poorly inked resulting in a certain level of “blotchiness.” This addition of underlying paper color results in the eye interpreting the stamps as a shade different (generally lighter) from that identified by the VSC 6000 (or other colorimetric equipment).
- Other samples were heavily inked resulting in visible “mounds” of ink. The roughness of the stamp surface resulting from this caused oblique light reflections during data collection.
- Damaged stamps including paper and gum creases, gum “soak-through” and other inconsistencies in printing also resulted in poor spectrographic results vis-à-vis the expert.

Chromaticity Results

As mentioned above, the VSC 6000 currently does not support CIE 1976 $u'$, $v'$ chromaticity coordinates. The measured tristimulus values $[X, Y, Z]$ were used to compute these coordinates using the standard transformations:

$$u' = \frac{4X}{X + 15Y + 3Z}$$
$$v' = \frac{9Y}{X + 15Y + 3Z}$$

After preconditioning the data, the CIE-1976 chromaticities were treated as they were in Fig. 4. The analogous figure is shown in Fig. 12. The four identified shades are also labeled in the figure, and called $A$, $B$, $C$ and $D$ to simplify reference to them.

From these data, the inner and outer convex hulls were generated using the same parameters as those used in the hypothetical example. The results are shown in Fig. 13.

While there are a number of data points that fall into the fuzzy intersections of the hulls, the results are all reasonable. Enlarged views of all four sets, $A$, $B$, $C$ and $D$, are presented in Figs. 14a-14d. These figures also highlight points from other sets that fall within their respective convex hulls and kernels.

The data for the points falling into the fuzzy regions of adjoining sets are summarized in Table 2. These results are well-behaved and indicate that the original color categories were correct.

Any points that present a disagreement between the theoretical model and the human expert may arise from several problems, the most likely of which are:

- Problems with the physical printing of the stamps described earlier in this paper.
- Experimental error in sampling stamp color.
- Data reduction error in processing chromaticity measurements.
- Classification error on the part of the expert.
This paper has described a method for measuring stamp colors using colorimetry. It then developed a model of color identification using color categories. The categories themselves were defined by a human color expert, and then fuzzy logic was applied to model the variability of human color perception.

Finally, the model was validated by applying it to the analysis of 68 stamps printed in shades of red.

ACKNOWLEDGEMENTS

This work was partially funded by a scholarship from the Smithsonian National Postal Museum and by contributions from the Institute for Analytical Philately, Inc.

Because of the multidisciplinary nature of this research, the authors requested the help of experts both in the fields of color science and philatelic research to review this work. They would like to thank the following outside readers for their valuable suggestions and encouragement. Prof. David Wyble of the Munsell Color Science Laboratory, Rochester Institute of Technology, Prof. Gurav Sharma, University of Rochester, Dr. David Beech, British Library, Robert Odenweller, International Association of Philatelic Experts, Dr. Edward Liston, and Prof. Maurice Bursey, University of North Carolina at Chapel Hill (ret.).

REFERENCES


Table 2. Allocation of color categories based on the membership function, sim.

<table>
<thead>
<tr>
<th>Sample</th>
<th>Chromaticity Coordinates</th>
<th>Expert Allocation</th>
<th>Membership Function, sim, for Convex Hull</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>x</td>
<td>y</td>
<td></td>
</tr>
<tr>
<td>P_1</td>
<td>0.3433</td>
<td>0.4993</td>
<td>H_B</td>
</tr>
<tr>
<td>P_2</td>
<td>0.3401</td>
<td>0.4980</td>
<td>H_B</td>
</tr>
<tr>
<td>P_3</td>
<td>0.3457</td>
<td>0.4998</td>
<td>H_B</td>
</tr>
<tr>
<td>P_4</td>
<td>0.3497</td>
<td>0.5007</td>
<td>H_B</td>
</tr>
<tr>
<td>P_5</td>
<td>0.3609</td>
<td>0.4950</td>
<td>H_D</td>
</tr>
<tr>
<td>P_6</td>
<td>0.3617</td>
<td>0.4958</td>
<td>H_C</td>
</tr>
<tr>
<td>P_7</td>
<td>0.3626</td>
<td>0.4960</td>
<td>H_C</td>
</tr>
</tbody>
</table>
Fig. 14a. Points in the outer hull of Group A.

Fig. 14b. Points in the outer hull of Group B.

Fig. 14c. Points in the outer hull of Group C.

Fig. 14d. Points in the outer hull of Group D.


