

Case

5-3

Shelf

Department of the Interior.

Books are issued to and returned by employés, between the hours of 11 a. m. and 2 p. m. on all days except Sundays.

The Library is open to employés, for reference, from 9 a. m. till 4 p. m.

LIBRARY RULES.

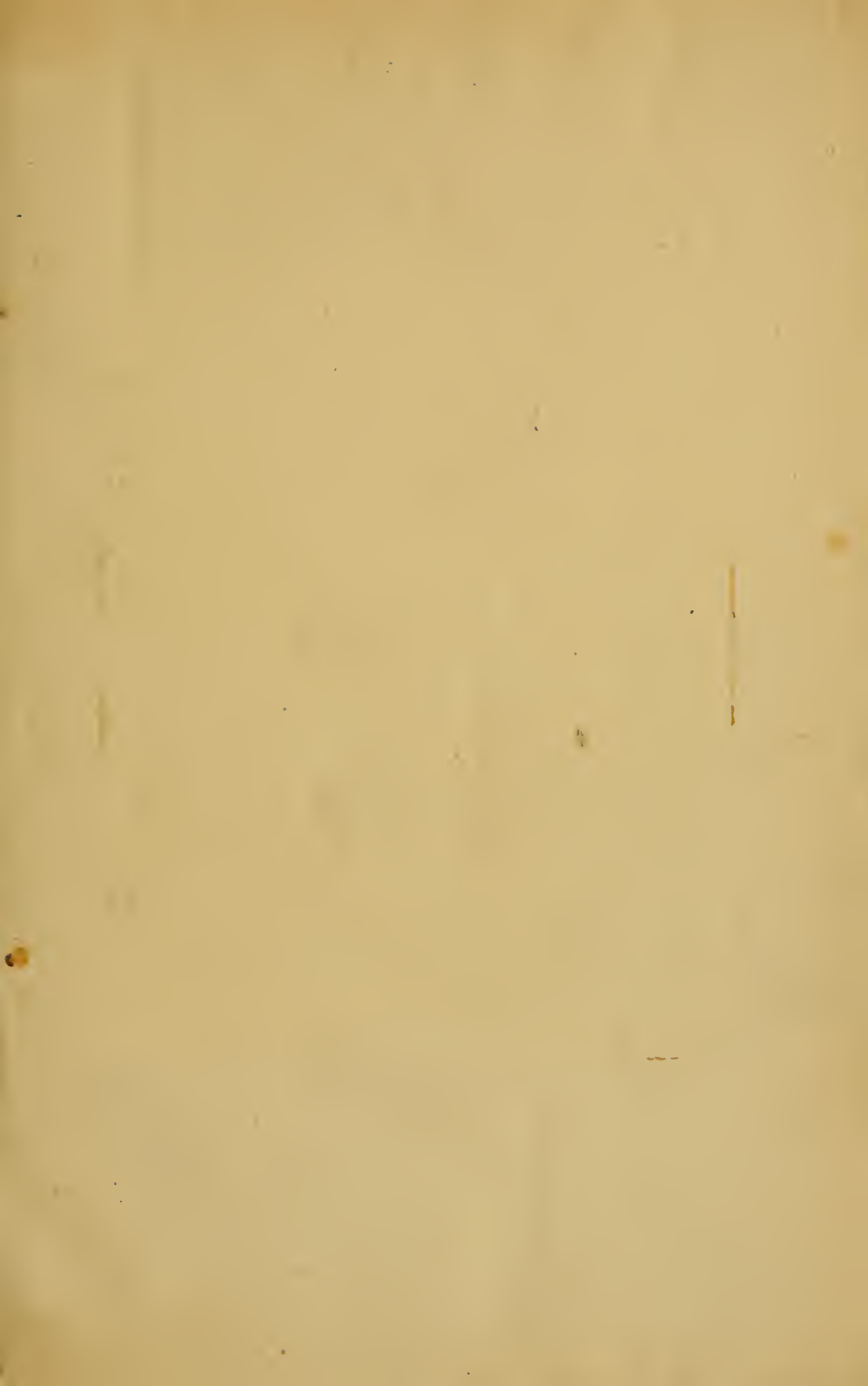
1. The employés of the Department of the Interior only are authorized to borrow books from the Library.
2. Before being allowed to draw books employés will be required to file with the Librarian a certificate of identity from the Chief Clerk of the Department, or of the Bureau or Office in which employed.
3. No book will be taken from the Library until its title and the name of the borrower shall have been registered by the Librarian.
4. Of works of single volumes only one at a time may be borrowed; of works of two or more volumes two may be taken.
5. The period of a loan of books is for two weeks, and borrowers are strictly prohibited from lending books thus drawn to other persons, whether of the Department or not.
6. Borrowers wishing to retain books for a longer period than two weeks, may at the close of the second week renew the loan for an additional two weeks.
7. The loan of a book will be renewed but once.
8. Books classed as "Works of Reference" or marked in the Catalogue with an (*), cannot be taken from the Library.
9. When a book has been injured while in the possession of a borrower, it must be replaced by a perfect copy.
10. Application for and return of books must be made in person, except in cases of sickness or absence from the city.
11. Books returned will not be reissued until they have been examined and replaced upon the shelves.
12. When a book has been retained by a borrower beyond two weeks without renewal, its price will be certified to the Disbursing Officer of the Department, and deducted from the salary of the person withholding it.
13. Writing on the leaves or covers of books, and the folding or turning down of their leaves are strictly prohibited; violation of this rule will debar employés from further privileges of the Library.
14. In selecting books from the shelves, care must be used in handling them, replacing those not drawn on the shelves from which they were taken: the number of the shelf may be ascertained from the label above.
15. Employés, on quitting the service of the Department, must return all books in their possession belonging to the Library. Final payment of their salaries will be withheld by the Disbursing Officer until he is satisfied that all books charged against them at the Library have been returned.
16. *New* books can be drawn for one week only, and not renewed.
17. Current periodicals can be drawn for three days only, and not renewed.
18. For infringements of any of the above rules the Librarian is authorized to suspend or refuse the issue of books to the culpable persons.

By order of the Secretary:

GEO. A. HOWARD,

Chief Clerk.

14520 b-1 m

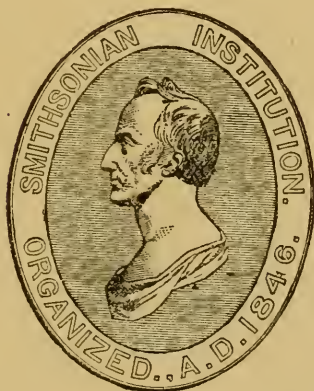




SMITHSONIAN

MISCELLANEOUS COLLECTIONS.

23
VOL. XXXIII.



"EVERY MAN IS A VALUABLE MEMBER OF SOCIETY WHO BY HIS OBSERVATIONS, RESEARCHES,
AND EXPERIMENTS PROCURES KNOWLEDGE FOR MEN."—SMITHSON.

WASHINGTON:
PUBLISHED BY THE SMITHSONIAN INSTITUTION.
1888.

PRINTED AND STEREOTYPED BY

JUDD & DETWEILER,

AT WASHINGTON, D. C.

ADVERTISEMENT.

The present series, entitled "Smithsonian Miscellaneous Collections," is intended to embrace all the publications issued directly by the Smithsonian Institution in octavo form; those in quarto constituting the "Smithsonian Contributions to Knowledge." The quarto series includes memoirs, embracing the records of extended original investigations and researches, resulting in what are believed to be new truths, and constituting positive additions to the sum of human knowledge. The octavo series is designed to contain reports on the present state of our knowledge of particular branches of science; instructions for collecting and digesting facts and materials for research; lists and synopses of species of the organic and inorganic world; museum catalogues; reports of explorations; aids to bibliographical investigations, etc., generally prepared at the express request of the Institution, and at its expense.

The assignment of a work to one or the other of the two series will sometimes depend upon whether the required illustrations can be presented more conveniently in the quarto or the octavo form.

In the Smithsonian Contributions to Knowledge, as well as in the present series, each article is separately paged and indexed, and the actual date of its publication is that given on its special title page, and not that of the volume in which it is placed. In many cases works have been published and largely distributed, years before their combination into volumes.

S. P. LANGLEY,

Secretary S. I.



TABLE OF CONTENTS.

- ARTICLE I. (543.) BULLETIN OF THE PHILOSOPHICAL SOCIETY OF WASHINGTON. Vol. VI. For the year 1883. Pp. 220.
- ARTICLE II. (592.) BULLETIN OF THE PHILOSOPHICAL SOCIETY OF WASHINGTON. Vol. VII. For the year 1884. Pp. 194.
- ARTICLE III. (636.) BULLETIN OF THE PHILOSOPHICAL SOCIETY OF WASHINGTON. Vol. VIII. For the year 1885. Pp. 115.
- ARTICLE IV. (661.) BULLETIN OF THE PHILOSOPHICAL SOCIETY OF WASHINGTON. Vol. IX. For the year 1886. Pp. 113. And Vol. X. For the year 1887. Pp. 263.
-

NOTE.

With this volume—(containing the last five volumes of the “Bulletins of the Philosophical Society of Washington”)—is terminated the reissue of these proceedings in the series of MISCELLANEOUS COLLECTIONS. It may be stated that volumes 1, 2, and 3 of these “Bulletins” formed Vol. XX of the Miscellaneous Collections. Volumes 4 and 5 were included in Vol. XXV of the Miscellaneous Collections. And, lastly, volumes 6, 7, 8, 9, and 10—together with the Memorial Proceedings in honor of Prof. Baird, and a full Index of the whole ten volumes—constitute the present Vol. XXXIII of the Miscellaneous Collections.



BULLETIN
OF THE
PHILOSOPHICAL SOCIETY
OF
WASHINGTON.

VOL. VI.

Containing the Minutes of the Society for the year 1883, and the
Minutes of the Mathematical Section from its organiza-
tion, March 29th, to the close of the year.

PUBLISHED BY THE CO-OPERATION OF THE SMITHSONIAN INSTITUTION.

WASHINGTON:
1884.

CONTENTS.

	Page.
Constitution -----	VII
Standing Rules of the Society -----	IX
Standing Rules of the General Committee -----	XII
Rules for the Publication of the Bulletin -----	XIII
Officers elected December, 1882 -----	XIV
Officers elected December, 1883 -----	XV
List of Members, corrected to December 31, 1883 -----	XVI
Annual Report of the Treasurer -----	XXII
Annual Address of the President, J. W. Powell -----	XXV
Bulletin of the General Meeting -----	I
Experiments in binary arithmetic, H. Farquhar -----	3
Refraction in a triaxial ellipsoid, (<i>Title only</i>), S. M. Burnett -----	4
Monochromatic aberration in aphakia, (<i>Title only</i>), W. Harkness --	5
The nature of matter, (<i>Title only</i>), H. H. Bates -----	5
Prevention of malarial diseases, A. F. A. King -----	5
Response of climate to variations of solar radiation, G. K. Gilbert --	10
Thermal belts of North Carolina, J. W. Chickering -----	11
Geology of the Hawaiian Islands, C. E. Dutton -----	13
Substance, matter, motion, and force, (<i>Title only</i>), M. H. Doolittle --	14
Formulas for the computation of Easter, E. B. Elliott -----	15
Florida expedition for observing transit of Venus, J. R. Eastman --	21
Determining the temperature of the air, C. Abbe -----	24
Determination of specific gravity of solids, C. E. Munroe -----	26
Geology of Hatteras, W. C. Kerr -----	28
Topographical indications of a fault, H. F. Walling -----	30
Ore deposition by replacement, S. F. Emmons -----	32
Glaciation in Alaska, W. H. Dall -----	33
The Eucalyptus on the Roman Campagna, (<i>Title only</i>), F. B. Hough	36
Hygrometric observations, H. A. Hazen -----	36
Dreams in their relation with psychology, E. Farquhar -----	37
Recent experiments on serpent venom, (<i>Title only</i>), R. Fletcher --	38
Further experiments in binary arithmetic, H. Farquhar -----	38
Medallic medical history, W. Lee -----	39

	Page.
Bulletin of the General Meeting—Continued.	
Note on the rings of Saturn, W. B. Taylor.....	41
Focal lines in astigmatism, (<i>Title only</i>), S. M. Burnett.....	45
Thermometer exposure, H. A. Hazen	46
Ichthyological results of the Albatross, (<i>Title only</i>), T. N. Gill.....	48
Fallacies concerning the deaf, A. G. Bell	48
Seismographic record from Japan, (<i>Title only</i>), E. Smith.....	87
The volcanic problem stated, C. E. Dutton.....	87
Drainage system and loess of eastern Iowa, W J McGee	93
Cambrian system in the United States and Canada, C. D. Walcott ..	98
Distribution of surplus money of the United States, J. J. Knox.....	103
An initial meridian and universal time, R. D. Cutts.....	106
Bulletin of the Mathematical Section.....	113
Rules of the Section.....	115
Members of the Section	116
Inaugural Address of the Chairman, A. Hall.....	117
A quasi general differentiation, (<i>Title only</i>), A. S. Christie.....	122
Alignment curves on any surface, C. H. Kummell.....	123
Determination of the mass of a planet, A. Hall.....	132
Infinite and infinitesimal quantities, M. H. Doolittle	133
Graphic tables for computing heights, (<i>Title only</i>), G. K. Gilbert..	136
Computation of lunar perturbations, G. W. Hill.....	136
Units of force and energy, (<i>Title only</i>), E. B. Elliott	137
Theory of errors tested by target shooting, C. H. Kummell.....	138
A special case in maxima and minima, B. Alvord.....	149
A financial problem, E. B. Elliott.....	149
A form of least-square computation, H. Farquhar	150
Note on problem discussed by Mr. Alvord, H. Farquhar	152
The rejection of doubtful observations, M. H. Doolittle.....	152
Special treatment of observation-equations, R. S. Woodward.....	156
Contact of plane curves, A. S. Christie.....	157
Committees on papers.....	161
Corrigenda to Vol. V.....	162
Index	163

BULLETIN
OF THE
PHILOSOPHICAL SOCIETY OF WASHINGTON.

CONSTITUTION, RULES,
LIST OF
OFFICERS AND MEMBERS,
AND
TREASURER'S REPORT.

CONSTITUTION

OF

THE PHILOSOPHICAL SOCIETY OF WASHINGTON.

ARTICLE I. The name of this Society shall be THE PHILOSOPHICAL SOCIETY OF WASHINGTON.

ARTICLE II. The officers of the Society shall be a President, four Vice-Presidents, a Treasurer, and two Secretaries.

ARTICLE III. There shall be a General Committee, consisting of the officers of the Society and nine other members.

ARTICLE IV. The officers of the Society and the other members of the General Committee shall be elected annually by ballot; they shall hold office until their successors are elected, and shall have power to fill vacancies.

ARTICLE V. It shall be the duty of the General Committee to make rules for the government of the Society, and to transact all its business.

ARTICLE VI. This constitution shall not be amended except by a three-fourths vote of those present at an annual meeting for the election of officers, and after notice of the proposed change shall have been given in writing at a stated meeting of the Society at least four weeks previously.

STANDING RULES

FOR THE GOVERNMENT OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON.

1. The Stated Meetings of the Society shall be held at 8 o'clock P. M. on every alternate Saturday; the place of meeting to be designated by the General Committee.

2. Notice of the time and place of meeting shall be sent to each member by one of the Secretaries.

When necessary, Special Meetings may be called by the President.

3. The Annual Meeting for the election of officers shall be the last stated meeting in the month of December.

The order of proceedings (which shall be announced by the Chair) shall be as follows:

First, the reading of the minutes of the last Annual Meeting.

Second, the presentation of the annual reports of the Secretaries, including the announcement of the names of members elected since the last annual meeting.

Third, the presentation of the annual report of the Treasurer.

Fourth, the announcement of the names of members who, having complied with Section 13 of the Standing Rules, are entitled to vote on the election of officers.

Fifth, the election of President.

Sixth, the election of four Vice-Presidents.

Seventh, the election of Treasurer.

Eighth, the election of two Secretaries.

Ninth, the election of nine members of the General Committee.

Tenth, the consideration of Amendments to the Constitution of the Society, if any such shall have been proposed in accordance with Article VI of the Constitution.

Eleventh, the reading of the rough minutes of the meeting.

4. Elections of officers are to be held as follows :

In each case nominations shall be made by means of an informal ballot, the result of which shall be announced by the Secretary ; after which the first formal ballot shall be taken.

In the ballot for Vice-Presidents, Secretaries, and Members of the General Committee, each voter shall write on one ballot as many names as there are officers to be elected, viz., four on the first ballot for Vice-Presidents, two on the first for Secretaries, and nine on the first for Members of the General Committee ; and on each subsequent ballot as many names as there are persons yet to be elected ; and those persons who receive a majority of the votes cast shall be declared elected.

If in any case the informal ballot result in giving a majority for any one, it may be declared formal by a majority vote.

5. The Stated Meetings, with the exception of the annual meeting, shall be devoted to the consideration and discussion of scientific subjects.

The Stated Meeting next preceding the Annual Meeting shall be set apart for the delivery of the President's Annual Address.

6. Sections representing special branches of science may be formed by the General Committee upon the written recommendation of twenty members of the Society.*

7. Persons interested in science, who are not residents of the District of Columbia, may be present at any meeting of the Society, except the annual meeting, upon invitation of a member.

8. Similar invitations to residents of the District of Columbia, not members of the Society, must be submitted through one of the Secretaries to the General Committee for approval.

9. Invitations to attend during three months the meetings of the Society and participate in the discussion of papers, may, by a vote of nine members of the General Committee, be issued to persons nominated by two members.

10. Communications intended for publication under the auspices

* Under this rule the Mathematical Section was organized March 29, 1883. Its rules and proceedings follow the Bulletin of the General Meeting.

of the Society shall be submitted in writing to the General Committee for approval.

11.* Any paper read before a Section may be repeated, either entire or by abstract, before a general meeting of the Society, if such repetition is recommended by the General Committee of the Society.

12. New members may be proposed in writing by three members of the Society for election by the General Committee; but no person shall be admitted to the privileges of membership unless he signifies his acceptance thereof in writing within two months after notification of his election.

13. Each member shall pay annually to the Treasurer the sum of five dollars, and no member whose dues are unpaid shall vote at the annual meeting for the election of officers, or be entitled to a copy of the Bulletin.

In the absence of the Treasurer, the Secretary is authorized to receive the dues of members.

The names of those two years in arrears shall be dropped from the list of members.

Notice of resignation of membership shall be given in writing to the General Committee through the President or one of the Secretaries.

14. The fiscal year shall terminate with the Annual Meeting.

15. † Members who are absent from the District of Columbia for more than twelve months may be excused from payment of the annual assessments. They can, however, resume their membership by giving notice to the President of their wish to do so.

16. Any member not in arrears may, by the payment of one hundred dollars at any one time, become a life member, and be relieved from all further annual dues and other assessments.

All moneys received in payment of life membership shall be invested as portions of a permanent fund, which shall be directed solely to the furtherance of such special scientific work as may be ordered by the General Committee.

* Adopted, May 19, 1883.

† Amended, Nov. 10, 1883.

STANDING RULES
OF THE
GENERAL COMMITTEE OF THE PHILOSOPHICAL
SOCIETY OF WASHINGTON.

1. The President, Vice-Presidents, and Secretaries of the Society shall hold like offices in the General Committee.

2. The President shall have power to call special meetings of the Committee, and to appoint Sub-Committees.

3. The Sub-Committees shall prepare business for the General Committee, and perform such other duties as may be entrusted to them.

4. There shall be two Standing Sub-Committees; one on Communications for the Stated Meetings of the Society, and another on Publications.

5. The General Committee shall meet at half-past seven o'clock on the evening of each Stated Meeting, and by adjournment at other times.

6. For all purposes except for the amendment of the Standing Rules of the Committee or of the Society, and the election of members, six members of the Committee shall constitute a quorum.

7. The names of proposed new members recommended in conformity with Section 11 of the Standing Rules of the Society, may be presented at any meeting of the General Committee, but shall lie over for at least four weeks before final action, and the concurrence of twelve members of the Committee shall be necessary to election.

The Secretary of the General Committee shall keep a chronological register of the elections and acceptances of members.

8. These Standing Rules, and those for the government of the Society, shall be modified only with the consent of a majority of the members of the General Committee.

RULES
FOR THE
PUBLICATION OF THE BULLETIN
OF THE
PHILOSOPHICAL SOCIETY OF WASHINGTON.

1. The President's annual address shall be published in full.
2. The annual reports of the Secretaries and of the Treasurer shall be published in full.
3. When directed by the General Committee, any communication may be published in full.
4. Abstracts of papers and remarks on the same will be published, when presented to the Secretary by the author in writing within two weeks of the evening of their delivery, and approved by the Committee on Publications. Brief abstracts prepared by one of the Secretaries and approved by the Committee on Publications may also be published.

5.* If the author of any paper read before a Section of the Society desires its publication, either in full or by abstract, it shall be referred to a committee to be appointed as the Section may determine.

The report of this committee shall be forwarded to the Publication Committee by the Secretary of the Section, together with any action of the section taken thereon.

6. Communications which have been published elsewhere, so as to be generally accessible, will appear in the Bulletin by title only, but with a reference to the place of publication, if made known in season to the Committee on Publications.

* Adopted May 19, 1883.

OFFICERS
OF THE
PHILOSOPHICAL SOCIETY OF WASHINGTON,

ELECTED DECEMBER 16, 1882.

President----- J. W. POWELL.
Vice-Presidents----- J. C. WELLING, J. E. HILGARD,
C. H. CRANE, J. S. BILLINGS.
Treasurer ----- CLEVELAND ABBE.
Secretaries----- G. K. GILBERT, HENRY FARQUHAR.

MEMBERS AT LARGE OF THE GENERAL COMMITTEE.

W. H. DALL, C. E. DUTTON,
J. R. EASTMAN, E. B. ELLIOTT,
R. FLETCHER, WM. HARKNESS,
D. L. HUNTINGTON, GARRICK MALLERY,*
C. A. SCHOTT.

STANDING COMMITTEES.

On Communications :

J. S. BILLINGS, *Chairman*, G. K. GILBERT, HENRY FARQUHAR.

On Publications :

G. K. GILBERT, *Chairman*, HENRY FARQUHAR, CLEVELAND ABBE,
S. F. BAIRD.†

* Mr. Mallery was elected Vice-President October 13 to fill the vacancy occasioned by the death of Mr. Crane. Mr. C. V. Riley was at the same time added to the General Committee to fill its number.

† As Secretary of the Smithsonian Institution.

LIST OF MEMBERS

OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON.

Corrected to December 31, 1883.

The names of founders are printed in SMALL CAPITALS.

(d) indicates *deceased*.

(a) indicates *absent* from the District of Columbia and excused from payment of dues until announcing his return.

(r) indicates *resigned*.

NAME.	P. O. ADDRESS AND RESIDENCE.	DATE OF ADMISSION.
Abbe, Cleveland.....	Army Signal Office. 2017 I St. N. W...	1871, Oct. 29
Abert, Sylvanus Thayer.....	Engineer's Office, War Department. 1724 Penn. Ave. N. W.	1875, Jan. 30
Adams, Henry.....	1607 H St.....	1881, Feb. 5
Aldis, Asa Owen.....	1518 H St. N. W.....	1873, Mar. 1
Allen, James.....	Army Signal Office. 1707 G St. N. W..	1882, Feb. 25
Alvord, Benjamin.....	1207 Q St. N. W.....	1872, Mar. 23
ANTISELL, THOMAS.....	Patent Office. 1311 Q St. N. W.....	1871, Mar. 13
Avery, Robert Stanton.....	Coast and Geodetic Survey Office. 320 A St. S. E.	1879, Oct. 11
Babcock, Orville Elias.....	2024 G St. N. W.....	1871, June 9
Bailey, Theodorus (d).....		1873, Mar. 1
BAIRD, SPENCER FULLERTON.....	Smithsonian Institution. 1445 Mass. Ave. N. W.	1871, Mar. 13
Baker, Frank.....	326 C St. N. W.....	1881, May 14
Baker, Marcus.....	347 Hill St., Los Angeles, Cal.....	1876, Mar. 11
Bancroft, George.....	1623 H St. N. W.....	1875, Jan. 16
BARNES, JOSEPH K. (d).....		1871, Mar. 13
Bates, Henry Hobart.....	Patent Office. The Portland.....	1871, Nov. 4
Beardslee, Lester Anthony (a).....	Navy Department.....	1875, Feb. 27
Bell, Alexander Graham.....	Scott Circle, 1500 R. I. Ave.....	1879, Mar. 29
Bell, Chichester Alexander.....	1221 Conn. Ave. N. W.....	1881, Oct. 8
BENÉT, STEPHEN VINCENT.....	Ordnance Office, War Department. 1717 I St. N. W	1871, Mar. 13
Bessels, Emil.....	Smithsonian Institution. 1444 N St. N. W.	1875, Jan. 16
BILLINGS, JOHN SHAW.....	Surg. Gen'l's Office, U. S. A. 3026 N St. N. W.	1871, Mar. 13
Birney, William.....	456 Louisiana Ave. 1901 Harewood Ave., Le Droit Park.	1879, Mar. 29
Birnie, Rogers (a).....	Cold Spring, Putnam Co., N. Y.....	1876, Mar. 11
Bodfish, Sumner Homer.....	Geological Survey. 605 F St. N. W.....	1883, Mar. 24
Browne, John Mills.....	Medical Director, U.S. N. The Port- land.	1883, Nov. 24
Burchard, Horatio Chapin.....	Director of the Mint. Riggs House..	1879, May 10
Burgess, Edward Sanford.....	High School. 1214 K St. N. W.....	1883, Mar. 24
Burnett, Swan Moses.....	1215 I St. N. W.....	1879, Mar. 29

LIST OF MEMBERS.

XVII

NAME.	P. O. ADDRESS AND RESIDENCE.	DATE OF ADMISSION.
Busey, Samuel Clagett.....	1525 I St. N. W.....	1874, Jan. 17
CAPRON, HORACE.....	The Portland.....	1871, Mar. 13
Case, Augustus Ludlow (a).....	Navy Department. Bristol, R. I.....	1872, Nov. 16
CASEY, THOMAS LINCOLN.....	Lieut. Col., Corps of Engineers. 1419 K St. N. W.....	1871, Mar. 13
Caziarc, Louis Vasmer.....	Army Signal Office. 1415 G St. N. W.....	1882, Feb. 25
CHASE, SALMON PORTLAND (d).....	1871, Mar. 13
Chamberlin, Thomas Crowder.....	Geological Survey.....	1883, Mar. 24
Chickering, John White, Jr.....	Deaf Mute College, Kendall Green.....	1874, Apr. 11
Christie, Alexander Smyth.....	Coast and Geodetic Survey Office. 513 6th St. N. W.....	1880, Dec. 4
Clapp, William Henry (a).....	1416 Corcoran St.....	1882, Feb. 25
Clark, Edward.....	Architect's Office, Capitol. 417 4th St. N. W.....	1877, Feb. 24
Clark, Ezra Westcote.....	Revenue Marine Bureau, Treasury Department. Woodley Road.....	1882, Mar. 25
Clarke, Frank Wigglesworth.....	Geological Survey. 1425 Q St. N. W.....	1874, Apr. 11
COFFIN, JOHN HUNTINGTON CEANE.....	1901 I St. N. W.....	1871, Mar. 13
Collins, Frederick (d).....	1879, Oct. 21
Comstock, John Henry (a).....	Cornell University, Ithaca, N. Y.....	1880, Feb. 14
Coues, Elliott.....	Smithsonian Inst. 1726 N. St. N. W.....	1874, Jan. 17
CRAIG, BENJAMIN FANEUL (d).....	1871, Mar. 13
Craig, Robert.....	Army Signal Office. 1008 I St. N. W.....	1873, Jan. 4
Craig, Thomas (a).....	Johns Hopkins Univ., Baltimore, Md.....	1879, Nov. 22
CRANE, CHARLES HENRY (d).....	1871, Mar. 13
Curtis, Josiah (d).....	1874, Mar. 28
Cutts, Richard Dominicus (d).....	1871, Apr. 29
DALL, WILLIAM HEALEY.....	P. O. Box 406. 1119 12th St. N. W.....	1871, Mar. 13
Davis, Charles Henry (d).....	1874, Jan. 17
Davis, Charles Henry.....	Navy Department. 1705 Rhode Island Ave. N. W.....	1880, June 19
Dean, Richard Crain (a).....	Navy Yard, New York.....	1872, Apr. 23
De Cindry, William Augustin.....	Commissary General's Office. 924 19th St. N. W.....	1881, Apr. 30
De Land, Theodore Louis.....	Treasury Dept. 126 7th St. N. E.....	1880, Dec. 18
Dewey, George (r).....	1879, Feb. 15
Doolittle, Myrick Hascall.....	Coast and Geodetic Survey Office. 1925 I St. N. W.....	1876, Feb. 12
Dorr, Fredric William (d).....	1874, Jan. 17
Dudwoods, Henry Harrison Chase.....	Army Signal Office. 1803 G St. N. W.....	1873, Dec. 20
Dutton, Clarence Edward.....	Geological Survey. 23 Lafayette Square.....	1872, Jan. 27
DYER, ALEXANDER B. (d).....	1871, Mar. 13
Eastman, John Robie.....	Naval Observatory. 930 18th St. N. W.....	1871, May 27
EATON, AMOS BEEBE (d).....	1871, Mar. 13
Eaton, John.....	Bureau of Education, Interior Dept. 712 East Capitol St.....	1874, May 8
Eldredge, Stewart (a).....	1871, June 9
ELLIOT, GEORGE HENRY (r).....	1871, Mar. 13
ELLIOTT, EZEKIEL BROWN.....	Office of Government Actuary, Treas- ury Department. 1210 G St. N. W.....	1871, Mar. 13
Emmons, Samuel Franklin.....	Geological Survey. 915 16th St. N. W.....	1883, Apr. 7
Endlich, Frederic Miller (a).....	Smithsonian Institution.....	1873, Mar. 1
Ewing, Charles (a).....	1874, Jan. 17
Ewing, Hugh (a).....	Lancaster, Ohio.....	1874, Jan. 17
Farquhar, Edward.....	Patent Office Library. 1915 H St. N. W.....	1876, Feb. 12
Farquhar, Henry.....	Coast and Geodetic Survey Office. Brooks Station, D. C.....	1881, May 14
Ferrel, William.....	Army Signal Office. 471 C St. N. W.....	1872, Nov. 16
Fletcher, Robert.....	Surgeon Genl's Office, U. S. A. 1326 L St. N. W.....	1873, Apr. 10
Flint, Albert Stowell.....	Naval Observatory. 1209 Rhode Island Ave. N. W.....	1882, Mar. 25
Flint, James Milton.....	Smithsonian Inst. Riggs House.....	1881, Mar. 19
FOOTE, ELISHA (d).....	1871, Mar. 13
Foster, John Gray (d).....	1873, Jan. 18
French, Henry Flagg (r).....	1882, Mar. 25
Fristoe, Edward T.....	1434 N St. N. W.....	1873, Mar. 29

XVIII PHILOSOPHICAL SOCIETY OF WASHINGTON.

NAME.	P. O. ADDRESS AND RESIDENCE.	DATE OF ADMISSION.
Gale, Leonard Dunnell (<i>d</i>).....		1874, Jan. 17
Gallaudet, Edward Miner.....	Deaf Mute College, Kendall Green....	1875, Feb. 27
Gannett, Henry.....	Geological Survey. 1881 Harewood Ave., Le Droit Park.	1874, Apr. 11
Gardiner, James Terry (<i>a</i>).....	State Library, Albany, N. W.....	1874, Jan. 17
Garnett, Alexander Young P. (<i>r</i>).....	Navy Department. 2019 Hillyer Place N. W.	1878, Mar. 16
Gihon, Albert Leary.....	Navy Department. 2019 Hillyer Place N. W.	1880, Dec. 18
Gilbert, Grove Karl.....	Geological Survey. 1424 Corcoran St.	1873, June 7
GILL, THEODORE NICHOLAS.....	Smithsonian Inst. 321-323 4/5 St. N. W.	1871, Mar. 13
Godding, William Whitney.....	Government Asylum for the Insane...	1879, Mar. 29
Goode, George Brown.....	National Museum. 1620 Mass. Ave. N. W.	1874, Jan. 31
Goodfellow, Edward.....	Coast and Geodetic Survey Office. 1330 19th St. N. W.	1875, Dec. 18
Goodfellow, Henry (<i>r</i>).....		1871, Nov. 4
Gore, James Howard.....	Columbian College. 1305 Q St. N. W.	1880, Mar. 14
Graves, Edward Oziel (<i>a</i>).....		1874, Apr. 11
Graves, Walter Hayden (<i>a</i>).....	Denver, Colorado.....	1878, May 25
Greely, Adolphus Washington (<i>a</i>)....		1880, June 19
Green, Bernard Richardson.....	1738 N St. N. W.....	1879, Feb. 15
Green, Francis Mathews (<i>a</i>).....	Navy Department.....	1875, Nov. 9
GREENE, BENJAMIN FRANKLIN (<i>a</i>).....	West Lebanon, N. H.....	1871, Mar. 13
Greene, Francis Vinton.....	District Commissioners' Office. 1915 G St. N. W.	1875, Apr. 10
Gunnell, Francis M.....	Medical Director, U. S. N. 600 20th St. N. W.	1879, Feb. 1
Hains, Peter Conover (<i>a</i>).....	1824 Jefferson Place.....	1879, Feb. 15
HALL, ASAPH.....	Naval Observatory. 2715 N. St. N. W.	1871, Mar. 13
Hanscom, Isaiah (<i>d</i>).....		1873, Dec. 20
HARNNESS, WILLIAM.....	Naval Observatory. 1415 G St. N. W.	1871, Mar. 13
Hassler, Ferdinand Augustus (<i>a</i>)....	Tustin City, Los Angeles Co., Cal.....	1880, May 8
HAYDEN, FERDINAND VANDEVEER (<i>a</i>)..	Geological Survey. 1803 Arch St., Philadelphia, Penn.	1871, Mar. 13
Hazen, Henry Allen.....	Army Signal Office. 1416 Corcoran St.	1882, Mar. 25
Hazen, William Babcock.....	Army Signal Office. 1601 K St. N. W.	1881, Feb. 5
HENRY, JOSEPH (<i>d</i>).....		1871, Mar. 13
Henshaw, Henry Wetherbee.....	Bureau of Ethnology. P. O. Box 585.	1874, Apr. 11
HILGARD, JULIUS ERASMUS.....	Coast and Geodetic Survey Office. 1709 Rhode Island Ave. N. W.	1871, Mar. 13
Hill, George William.....	Nautical Almanac Office. 314 Ind. Ave. N. W.	1879, Feb. 1
Holden, Edward Singleton (<i>a</i>).....	Madison, Wisconsin.....	1873, June 21
Holmes, William Henry.....	Geological Survey. 1100 O St. N. W...	1879, Mar. 29
Hough, Franklin Benjamin (<i>a</i>).....	Agricultural Department. Lowville, N. Y.	1879, Mar. 29
Howell, Edwin Eugene (<i>a</i>).....	Rochester, N. Y.....	1874, Jan. 31
HUMPHREYS, ANDREW ATKINSON (<i>d</i>)....		1871, Mar. 13
Jackson, Henry Arundel Lambe (<i>a</i>)	War Department.....	1875, Jan. 30
James, Owen (<i>a</i>).....	Hyde Park, Penn.....	1880, Jan. 3
Jeffers, William Nicolson (<i>r</i>).....		1877, Feb. 24
JENKINS, THORNTON ALEXANDER.....	2115 Penn. Ave. N. W.....	1871, Mar. 13
Johnson, Arnold Burges.....	Light House Board, Treasury Dept. 501 Maple Ave., Le Droit Park	1878, Jan. 19
Johnson, Joseph Taber.....	926 17th St. N. W.....	1879, Mar. 29
Johnston, William Waring.....	1603 K St. N. W.....	1873, Jan. 21
Kampf, Ferdinand (<i>d</i>).....		1875, Dec. 18
Keith, Renel (<i>a</i>).....		1871, Oct. 29
Kerr, Washington Carruthers.....	Raleigh, N. C.....	1883, Apr. 7
Kidder, Jerome Henry.....	Smithsonian Institution. 1816 N St. N. W.	1880, May 8
Kilbourne, Charles Evans.....	Army Signal Office. Lexington House.	1880, June 19
King, Albert Freeman Africanus....	726 13th St. N. W.....	1875, Jan. 16
King, Clarence (<i>r</i>).....		1879, May 10
Knox, John Jay.....	Treasury Dept. 1127 10th St. N. W....	1874, May 8
Kummell, Charles Hugo.....	Coast and Geodetic Survey Office. 608 Q St. N. W.	1882, Mar. 25
LANE, JONATHAN HOMER (<i>d</i>).....		1871, Mar. 13
Lawver, Winfield Peter.....	Mint Bureau, Treasury Department. 1912 I St. N. W.	1881, Feb. 19

LIST OF MEMBERS.

XIX

NAME.	P. O. ADDRESS AND RESIDENCE.	DATE OF ADMISSION.
Lee, William	211 Penn. Ave. N. W.	1874, Jan. 17
Lefavour, Edward Brown.....	Coast and Geodetic Survey Office. 117 C St. S. E.	1882, Dec. 16
Lincoln, Nathan Smith.....	1514 H St. N. W.	1871, May 27
Lockwood, Henry H. (r).....	1871, Oct. 29
Loomis, Eben Jenks.....	Nautical Almanac Office. 1413 Col- lege Hill Terrace N. W.	1880, Feb. 14
Lull, Edward Phelps.....	Navy Department.....	1875, Dec. 4
Lyford, Stephen Carr (r).....	1873, Jan. 18
MacCauley, Henry Clay (a).....	Helena, Montana.....	1880, Jan. 3
McGee, W. J.....	Geological Survey. 512 13th St. N. W. 1306 F St. N. W. 614 E St. N. W.....	1883, Nov. 10 1879, Feb. 15
McGuire, Frederick Bauders	1872, Jan. 27
Mack, Oscar A. (d).....	1876, Feb. 26
McMurtrie, William (a).....	Champaign, Ill	1875, Jan. 30
Mallery, Garrick	Bureau of Ethnology. P. O. Box 585. 1323 N St. N. W.
Marvin, Joseph Badger (a).....	1878, May 25
Marvine, Archibald Robertson (d).....	1874, Jan. 31
Mason, Otis Tufton.....	Columbian College. 1305 Q St. N. W.....	1875, Jan. 30
MEEK, FIELDING BRADFORD (d).....	1871, Mar. 13
Meigs, Montgomery (a).....	War Department. Rock Island, Ill.....	1877, Mar. 24
MEIGS, MONTGOMERY CUNNINGHAM.....	1239 Vermont Ave. N. W.....	1871, Mar. 13
Milner, James William (d).....	1874, Jan. 31
Morgan, Ethelbert Carroll.....	918 E St. N. W.....	1883, Oct. 13
Morris, Martin Ferdinand (a).....	1877, Feb. 24
Mussey, Reuben Delavan.....	P. O. Box 618. 508 5th St. N. W.....	1881, Dec. 3
MYER, ALBERT J. (d).....	1871, Mar. 13
Myers, William (a).....	War Department.....	1871, June 23
NEWCOMB, SIMON.....	Navy Department. Stoddard Street.....	1871, Mar. 13
Nichols, Charles Henry (a).....	1872, May 4
NICHOLSON, WALTER LAMB.....	1322 I St. N. W.....	1871, Mar. 13
Nordhoff, Charles.....	Alpine, Bergen Co., N. J.....	1879, May 10
Osborne, John Walter.....	212 Delaware Ave. N. E.....	1878, Dec. 7
OTIS, GEORGE ALEXANDER (d).....	1871, Mar. 13
PARKE, JOHN GRUBB.....	Engineer Bureau, War Department. 16 Lafayette Square.....	1871, Mar. 13
PARKER, PETER.....	2 Lafayette Square.....	1871, Mar. 13
PARRY, Charles Christopher (a).....	Burlington, Iowa.....	1871, May 13
Paterson, Carlile Pollock (d).....	1871, Nov. 17
Paul, Henry Martyr.....	Naval Observatory. 917 R St. N. W.....	1877, May 19
Peale, Albert Charles.....	Geological Survey. 1210 Mass. Ave. N. W.	1874, Apr. 11
PEALE, TITIAN RAMSAY (a).....	Philadelphia, Penn.....	1871, Mar. 13
PEIRCE, BENJAMIN (d).....	1871, Mar. 13
Peirce, Charles Sanders (a).....	Coast and Geodetic Survey Office. Baltimore, Md.	1873, Mar. 1
Pilling, James Constantine.....	Geological Survey. 918 M St. N. W.....	1881, Feb. 19
Poe, Orlando Metcalfe.....	34 Congress St. West, Detroit, Mich.....	1873, Oct. 4
Pope, Benjamin Franklin.....	Surgeon General's Office, U. S. A. 2029 P St. N. W.	1882, Dec. 16
Porter, David Dixon (r).....	1874, Apr. 11
Powell, John Wesley.....	Geological Survey. 910 M St. N. W.....	1874, Jan. 17
Prentiss, Daniel Webster.....	1224 9th St. N. W.....	1880, Jan. 3
Pritchett, Henry Smith (a).....	Washington University, St. Louis, Mo.....	1879, Mar. 29
Rathbone, Henry Reed (a).....	1874, Jan. 17
Rathbun, Richard.....	Smithsonian Institution. 1622 Mass. Ave. N. W.	1882, Oct. 7
Renshawe, John Henry.....	Geological Survey. 1221 O St. N. W.....	1883, Feb. 24
Richey, Stephen Olin.....	1426 N. Y. Ave. N. W.....	1882, Oct. 7
Ridgway, Robert (a).....	Smithsonian Inst. 1214 Va. Av. N. W.....	1874, Jan. 31
Riley, Charles Valentine.....	Agricultural Dept. 1700 13th St. N. W.....	1878, Nov. 9
Riley, John Campbell (d).....	1877, May 19
Ritter, William Francis McKnight.....	Nautical Almanac Office. 16 Grant Place.....	1879, Oct. 21
Rodgers, Christopher Raymond Perry (a).....	1723 I St. N. W.....	1872, Mar. 9
Rodgers, John (d).....	1872, Nov. 16
Rogers, Joseph Addison (a).....	Naval Observatory.....	1872, Mar. 9
Russell, Israel Cook.....	Geological Survey. 1424 Corcoran St.....	1882, Mar. 25

NAME.	P. O. ADDRESS AND RESIDENCE.	DATE OF ADMISSION.
Russell, Thomas.....	Army Signal Office. 904 M St. N. W...	1883, Feb. 10
Salmon, Daniel Elmer.....	Agricultural Dept. 1121 I St. N. W.....	1883, Nov. 24
Sampson, William Thomas.....	Naval Observatory	1883, Mar. 24
SANDS, BENJAMIN FRANKLIN (d).....	342 D St. (La. Ave.) N. W. 1315 M St.	1871, Mar. 13
Saville, James Hamilton.....	N. W.	1871, Apr. 29
SCHAEFFER, GEORGE CHRISTIAN (d).....	Coast and Geodetic Survey Office.	1871, Mar. 13
SCOTT, CHARLES ANTHONY.....	212 1st St. S. E.	1871, Mar. 13
Searle, Henry Robinson (d).....	1877, Dec. 21
Seymour, George Dudley (r)	1881, Dec. 3
Shellabarger, Samuel.....	Room 23 Corcoran Building. 812 17th	1875, Apr. 10
.....	St. N. W.	
Sherman, John	1319 K St. N. W.....	1874, Jan. 17
SHERMAN, WILLIAM TECUMSEH (r)	1871, Mar. 13
Shufeldt, Robert Wilson.....	Surgeon Gen'l's Office, U. S. A. 1619	1881, Nov. 5
.....	K St. N. W.	
Sieard, Montgomery (a)	Ordnance Bureau, Navy Department.	1877, Feb. 24
Sigsbee, Charles Dwight.....	Hydrographic Office, Navy Depart-	1879, Mar. 1
.....	ment. 3319 U St. N. W.	
Skinner, John Oscar.....	1739 F St. N. W.....	1883, Mar. 24
Smiley, Charles Wesley.....	U. S. Fish Commission, 1443 Mass.	1882, Oct. 7
.....	Ave. 1207 11th St. N. W.	
Smith, David (a).....	Navy Department.....	1876, Dec. 2
Smith, Edwin.....	Coast and Geodetic Survey Office	1880, Oct. 23
Spofford, Ainsworth Rand.....	Library of Congress. 1621 Mass. Ave.	1872, Jan. 27
.....	N. W.	
Stearns, John (a)	1874, Mar. 23
Stone, Ormond (a).....	Leander McCormick Observatory,	1874, Mar. 23
.....	University of Virginia.	
Taylor, Frederick William.....	Smithsonian Institution.....	1881, Feb. 19
TAYLOR, WILLIAM BOWER.....	Smithsonian Inst. 306 C St. N. W.....	1871, Mar. 13
Thompson, Almon Harris.....	Geological Survey.....	1875, Apr. 10
Tilden, William Calvin (a).....	Army Medical Museum	1871, Apr. 29
Todd, David Peck (a).....	Amherst, Mass.....	1878, Nov. 23
Toner, Joseph Meredith.....	615 Louisiana Ave.....	1873, June 7
True, Frederick William.....	National Museum.....	1882, Oct. 7
Twining, William J. (d).....	1878, Nov. 23
Upton, Jacob Kendrick (r)	1878, Feb. 2
Upton, William Wirt.....	2d Comptroller's Office, Treasury	1882, Mar. 25
.....	Dept. 810 12th St. N. W.	
Upton, Winslow (a).....	Army Signal Office. 1441 Chapin St.	1880, Dec. 4
.....	N. W.	
Vasey, George (r)	1875, June 5
Walcott, Charles Doolittle.....	Geological Survey. 1116 N. Y. Ave.	1883, Oct. 13
.....	N. W.	
Waldo, Frank	Army Signal Office. 1427 Chapin St.	1881, Dec. 3
.....	N. W.	
Walker, Francis Amasa (a).....	Mass. Inst. of Technology, Boston,	1872, Jan. 27
.....	Mass.	
Walling, Henry Francis.....	Geological Survey.....	1883, Feb. 24
Ward, Lester Frank.....	Geological Survey. 1464 E. I. Ave.	1876, Nov. 18
.....	N. W.	
Webster, Albert Lowry.....	Johns Hopkins University, Balti-	1882, Mar. 25
.....	more, Md.	
Welling, James Clarke.....	1302 Connecticut Ave.....	1872, Nov. 16
Wheeler, George M. (a).....	Engineer Bureau, War Department..	1873, June 7
WHEELER, JUNIUS B. (a).....	West Point, New York	1871, Mar. 13
White, Charles Abiathar.....	Geological Survey. LeDroit Park.....	1876, Dec. 16
White, Zebulon Lewis (a).....	Providence, Rhode Island.....	1880, June 19
Williams, Albert, Jr.....	Geological Survey. 23 Lafayette	1883, Feb. 24
.....	Square.	
Wilson, Allen D. (a)	Newport, R. I.....	1874, Apr. 11
Wilson, James Ormond.....	Franklin School Building. 1439 Mass.	1873, Mar. 1
.....	Ave. N. W.	
Winlock, William Crawford.....	Naval Observatory. 733 20th St. N.W...	1880, Dec. 4
Wolcott, Christopher Columbus (r).....	1876, Feb. 27
Wood, Joseph (a).....	Asst. Engineer B. & P. R. R.....	1875, Jan. 16
Wood, William Maxwell (a).....	Navy Department	1871, Dec. 2

NAME.	P. O. ADDRESS AND RESIDENCE.	DATE OF ADMISSION.
WOODWARD, JOSEPH JANVIER.....	Army Med. Museum. 620 F St. N.W.	1871, Mar. 13
Woodward, Robert Simpson.....	Naval Observatory. 1125 17th St. N.W.	1883, Nov. 24
Woodworth, John Maynard (<i>d</i>).....	1874, Jan. 31
Yarnall, Mordecai (<i>d</i>).....	1871, Apr. 29
Yarrow, Harry Crécy.....	814 17th St. N. W.....	1874, Jan. 31
Zumbrock, Anton.....	Coast and Geodetic Survey Office. 455 C St. N. W.	1875, Jan. 30

Number of <i>founders</i>	44
“ members <i>deceased</i>	36
“ “ <i>absent</i>	55
“ “ <i>resigned</i>	16
“ “ <i>active</i>	149
Total number enrolled.....	258

ANNUAL REPORT OF THE TREASURER.

WASHINGTON CITY, *December 31, 1883.**To the Philosophical Society of Washington :*

I have the honor to present herewith my annual statement as Treasurer for the year ending December 31st, and to express my regret that owing to absence from the city I was not able to present this report at the proper time on the occasion of the recent annual meeting, December 22d.

By the kindness of Messrs. Riggs & Co. the Society has been enabled to invest in another \$1,000 United States 4 per cent. bond, but in this case a few weeks in advance of the regular winter accumulation of its revenue. The balance shown by Riggs' books against the Society is, therefore, with their assent, and in fact at their suggestion, and will probably be met during January.

The total invested fund of the Society is, therefore, \$2,500, of which \$1,000 is at 4½ per cent. and \$1,500 at 4 per cent.

The further assets of the Society consist of unpaid annual dues to the amount of \$185 for 1883 and \$90 for 1882. The total active membership remains at about one hundred and fifty, and the probable income for the next year may be estimated at \$900, nearly all of which will be needed to pay current expenses and the bills for printing Volume VI.

Early in the year one hundred and fifty-five copies of Volume IV and two hundred and eighty-five of Volume V were distributed to the active members and to about fifty domestic and eighty-five foreign recipients.

The list of recipients is a slightly amended copy of that printed in Volume IV of the Bulletin of the Society. Occasional copies of the earlier volumes have been distributed to those whose sets had accidentally become imperfect, or were otherwise entitled to them.

As custodian of the library and property, I have the honor to report that the Society occasionally receives scientific publications by way of exchange with similar organizations. The accession catalogue of the library now includes a hundred and two numbers or titles, being an increase of thirty-one during the year.

By order of the General Council, the Treasurer was in 1881 instructed to initiate the keeping of a record book containing a sketch of the life and services of the individual members of the Society; this record volume is now prepared, and a notice will be sent to each member asking for the necessary data.

Very respectfully,

CLEVELAND ABBE,
Treasurer.

EXPENDITURES.				RECEIPTS.			
Date.	Vou'r.	Check.	To whom paid.	Amount.	From what source.	Amount.	Total.
1883.							
March 1	1	74	Judd & Detweiler, printers	\$60 00	Credit by receipts as follows:		
April 21	2	75	Judd & Detweiler, printers	35 50	Balance carried over from Dec. 28, 1882		\$521 07
April 21	3	75	Judd & Detweiler, printers	117 08	Annual dues received:		
April 26	4	76	Cleveland Abbe, Treasurer	46 70	and deposited December 23, 1882	\$135 00	
June 20	5	77	Judd & Detweiler, printers	11 50	and deposited February 1, 1883	25 00	
Nov. 26	6	78	G. K. Gilbert, Secretary	5 05	and deposited February 6, 1883	125 00	
Dec. 5	7	79	Riggs & Co., \$1,000 U. S. 4 per cent.	1,223 75	and deposited February 14, 1883	50 00	
					and deposited March 17, 1883	100 00	
					and deposited May 1, 1883	70 00	
					and deposited November 15, 1883	95 00	
					and deposited November 27, 1883	105 00	
					and deposited December 10, 1883	65 00	
					and deposited December 28, 1883	70 00	
					Interest on invested funds, viz:	\$840 00	
					One \$1,000 U. S. bond, at 4½ per cent.	45 00	
					One \$500 U. S. bond, at 4 per cent.	20 00	
					Total receipts		995 00
					Receipts from all sources		1,426 07
					Over-draft on Riggs & Co.		73 51
			Total	\$1,499 58	Total		\$1,499 58

BULLETIN

OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON.

.

ANNUAL ADDRESS OF THE PRESIDENT.

ANNUAL ADDRESS OF THE PRESIDENT,

J. W. POWELL,

Delivered December 8, 1883.

THE THREE METHODS OF EVOLUTION.

In the early history of research attention was chiefly given to phenomena of co-existence. In late years the phenomena of sequence have received the larger share of attention. The investigation of the phenomena of sequence has led to the invention of a number of hypotheses. In the past history of scientific research three of these have each led to a long series of important discoveries. These are the nebular hypothesis, the atomic hypothesis, and the hypothesis of the development of life. The nebular theory is an hypothesis of astronomic evolution; the atomic theory has gradually assumed the shape of an hypothesis of chemical evolution; and the development theory has been elaborated and re-stated as the hypothesis of biologic evolution. The time has come when in all fruitful research evolution in some form is postulated by each investigator in his own field. Yet many scientific men, though admitting the doctrines of evolution in their own special fields, oftentimes reject them elsewhere; and there is some disagreement even among the greatest thinkers as to the extent to which the hypotheses of evolution can be carried, but all postulate evolution in some form and to some degree.

An attempt will be made in this address to point out what is believed to be the fact—that there are three grand classes of phenomena, constituting three kingdoms of matter and representing three stages of evolution; or, stated in another way, that there has been an evolution of the methods of evolution, so that the methods discovered in the first stage have been superseded by those discovered in the second, and these superseded by the methods of the third stage. It is proposed to indicate and, as clearly as possible within the limits of an address, to define, in terms of matter and motion, the three kingdoms of matter and the three methods of evolution. As precedent to the general statement it will be well, therefore, briefly to consider the kinematic hypothesis.

THE KINEMATIC HYPOTHESIS.

That motion is persistent is the kinematic hypothesis. In the early history of research many modes or varieties of motion were directly observed. To account for these motions they were said to be caused by *forces*, and Force was sometimes defined as that which produces motion. Something, therefore, was conceived to exist—not matter, not motion—an existence that would produce motion. Then arose the question, What is Force—this antecedent of Motion? The researches inaugurated from this standpoint led again and again to the discovery that the antecedent of motion is some other motion, and one after another of the so-called “forces” were thus resolved into motions, until at last only gravity and affinity, and perhaps magnetism, remain as unexplained antecedents of motion. But gravity, affinity, and magnetism are included under one term, “*attraction*,” by those who hold that there is yet a *force*—something other than motion which produces motion. Attraction, then, is left. Sometimes these same philosophers speak of “attraction and repulsion.” If, then, all forces the actions of which are thoroughly known are resolved into antecedent motions, it is indeed an inductive hypothesis worthy of consideration that the antecedents of the phenomena of attraction and repulsion may also be regarded as modes of motion.

But this hypothesis is reached by another method. It is known that motions may be transmuted from one kind or mode into another. Affinity can be transmuted into motion, and motion into affinity. If we wish to obtain the mode of motion called electricity, we may derive it from mechanical motion through friction, or we may derive it through affinity in the voltaic cell. If we combine a gramme of hydrogen with oxygen, 34,000 units of heat—a mode of motion—are developed. If a gramme of hydrogen be combined with iodine, 3,600 units of heat—a mode of motion—are absorbed. But why introduce single illustrations? A large part of all the powers used by man in the industries of the world are derived from affinity. Affinity, therefore, is the equivalent of motion. By a similar process it is shown that gravity can be transmuted into motion and motion into gravity, and the trasmutation of magnetism into motion and of motion into magnetism is well known.

It is thus seen that while motion may be derived from the so-called forces, gravity, affinity, and magnetism, these so-called force

may also be derived from motion. In all other cases where a mode of motion is transmuted, it is but changed into another mode. It is therefore an inductive hypothesis that gravity, affinity, and magnetism are also modes of motion.

This hypothesis is reached by yet another inductive process. There is a vast multiplicity of properties which bodies present to the mind through touch, taste, smell, hearing, and sight—properties at first explained as occult. During the progress of scientific research, one after another of these properties has been resolved into motion, until at last two remain unexplained—rigidity and elasticity. By those who hold with most tenacity to older explanations of such phenomena, these two remaining properties are attributed to attraction and repulsion; but those who have fallen into the current of modern thought believe that they can be explained as the results of the composed motion of the constituent parts of the bodies which exhibit them, together with molecular impact. That some such explanation will eventually be fully established is highly probable as an inductive hypothesis.

When these various methods of induction are combined they lead to an hypothesis of the highest character, and we may reasonably expect that all forces will ultimately be resolved into motions. The term *force* will still be of value in science, to be used in each case as denoting the antecedent motion.

Intimately related to the kinematic hypothesis is the hypothesis of an ether, which has also been reached by a variety of inductive methods, *i. e.* from converging lines of research. In fact, the kinematic hypothesis and the ethereal hypothesis are identical, the first being stated in terms of motion, the second in terms of matter.

Intimately related to the ethereal hypothesis is the nebular hypothesis, also reached through a series of converging lines of induction.

Every fact that lends probability to one lends probability to all. Thus each strengthens the other. It must be understood that however probable they may be, they are yet hypotheses, and for their complete demonstration the mode of action must be specifically pointed out in each case.

The ethereal hypothesis furnishes the original homogeneous matter in motion from which the various aggregates have been segregated. The nebular hypothesis takes up this matter while it is yet in a

molecular condition and derives from it the more compounded aggregates and their motions, in obedience to the law of the persistence of motion, which is the kinematic hypothesis. Thus there are bodies of men engaged in researches relating to molecular physics, other bodies of men in researches relating to molecular physics and astronomy, and others in molecular physics and chemistry, all of whose researches converge in the kinematic hypothesis. It is therefore reached by a consilience of many inductive methods.

In the statement thus made concerning the kinematic theory there is no attempt to assemble the data on which it rests. Such task could not be performed in an address, as volumes would be needed for their presentation. An attempt has been made simply to characterize the processes of inductive reasoning by which the hypothesis is reached.

If the kinematic hypothesis should be demonstrated, it would be a veritable explanation. The dynamic hypothesis is no explanation. To exhibit this fact it must be briefly analyzed.

Philosophy is the science of opinion, and the philosopher has for the subject-matter of his science the origin and nature of opinions, and he discovers that they may be broadly grouped in three classes—mythic, metaphysic, and scientific. Mythic opinion arises from the attempt to explain the simple in terms of the compound—that is, to explain biotic and physical phenomena by their crude analogies to human activities. Early man, discovering that his own activities arose from design and will, supposed that there was design and will in all function and motion. Through this method of explanation have arisen the mythologies of the world.

But in the early civilization of the Aryan race a multitude of mythic systems were thrown together and studied by the same body of men, originally for the purpose of deriving therefrom the common truth. The resulting comparison and investigation led to the conclusion that they were all false, and in lieu thereof a new system of explanation was invented. These earlier philosophers of the cities of the Mediterranean, while engaged in the comparison of mythologies, were also engaged in the comparison of languages, and they discovered many profoundly interesting facts of linguistic structure, and the intimate relations between language and thought by which the form of thought itself is moulded. These great facts appearing at the same time that mythic philosophy was dis-

solving into idle tales, led to the origin of a new philosophic method. The men of that day supposed that the truth is in the word, and that a verbal explanation could be constructed; that the philosophy of the universe could be based on language; and to them verbal statement was explanation, final and absolute, and being was but ideal.

But metaphysic philosophy was displaced by the increase of knowledge—the development of scientific philosophy. In this system the phenomena of co-existence and sequence are objectively discerned and classified.

This bare statement of the three methods can be made more lucid by an illustration. Unsupported bodies above the earth fall, and such phenomena are seen so often as to challenge every man's attention. Early man, whose mind was controlled by mythic opinions, subjectively knew that if he wished to move a body he must push or pull it, and to him there was no other method of originating motion.

Some years ago I was with a small body of Wintun Indians on Pitt River, the chief tributary of the Sacramento, engaged in the study of mythology. I had gone among the rocks for the purpose of awakening echoes, that I might elicit from my dusky philosophers an explanation thereof. Unexpectedly I fell upon an explanation of gravity. We had climbed a high crag, and I sat at the summit of the cliff with my feet overhanging the brink. An Indian near me, who could speak but imperfect English, seemed solicitous for my safety, and said: "You better get out; hollow pull you down." I had previously been intent on watching the operations of his mind for the purpose above mentioned, and this expression seemed to me strange; and it started a line of investigation which I eagerly pursued. I soon discovered that he interpreted the fall of bodies by purely subjective analogies. He who stands on a rock but slightly elevated above the earth feels no fear, but if standing a thousand feet above the base of the cliff, he attempts to look over, fear curdles his blood, and he seems to be *pulled over*. As he climbs a lofty pine, at every increase of altitude there is an increase of fear, and he seems to be pulled down by a stronger force. When he rests upon the solid earth he feels no "pull," but when elevated above it he interprets his subjective feelings as an objective pull. Vacuity is personified and believed to be an actor.

In the early winter of 1882 I was with a party of Indians in the

Grand Cañon of the Colorado. Some of the young men were amusing themselves by trying to throw stones across a lateral gorge. No one could accomplish the feat, though they could throw stones even farther, as they believed, along the level land. Chuar, the chief, explained this to me by informing me that the cañon *pulled the stones down*. The apparent proximity of the opposite wall was believed to be actual, and vacuity was personified and believed to exert a force.

Metaphysic explanations of gravity are found. By that method an absolute up and down is predicated, and bodies have a tendency to fall down. This is an explanation in words, the words expressing no meaning but believed to be themselves thoughts. It is perhaps the earliest form of the metaphysic explanation of gravity. But with the progress of knowledge the absolute disappears, and positions are found to be but relative; there is no absolute up and down; and other facts with regard to gravity are discovered. And finally the metaphysician says bodies *attract*. Now the term *fall*, as used by the early metaphysicians, was the name of a motion observed, and it was held to be a complete explanation as long as up and down was supposed to be absolute, not relative; and the explanation was abandoned as insufficient when the ideas of absolute up and down were abandoned. But the word *attraction* does not involve this error. It is simply a name for the phenomenon, without the manifestly fallacious implication of "up and down." And it is a good name for the specific phenomenon to which it is applied. But it must not connote any other idea; in so far as it does, it is vitiated. Yet the metaphysician will suppose that by using the term "attraction" he explains gravity. The scientific philosopher uses the term purely as the name of the phenomenon, and does not suppose that thereby the phenomenon is explained; and having named it, he still seeks for its explanation—that is, he still seeks to resolve that which is manifestly a complex phenomenon, exhibited in the relations of positions of bodies, into its most simple elements. Whenever this is done he will say that attraction, or gravity—they being synonyms for the same phenomenon—is explained.

The kinematist uses "attraction" as a synonym for "gravitation." The dynamist uses "attraction" as a verbal explanation of Gravitation. The mythic philosopher uses the term to connote the still further idea that bodies exert a "pull" on one another; and this

latter concept is no less mythic than that of the Indian who believes that the vacuity between them exerts the pull.

It is fortunate for science that every discovery and every inductive hypothesis is rigidly criticised, as this leads to the careful examination of the verity of facts discerned and of the legitimacy of hypotheses derived therefrom. Against the kinematic theory of force much good rhetoric has been hurled, which may be somewhat imitated in the following manner :

Here is a quotation from Bagehot, with an interpolation of my own : "This easy hypothesis of special creation [occult force] has been tried so often, and has broken down so very often, that in no case probably do any great number of careful inquirers very firmly believe it. They may accept it provisionally, as the best hypothesis at present, but they feel about it as they cannot help feeling as to an army which has always been beaten ; however strong it seems they think it will be beaten again."

The venerable gentlemen who constitute the elder school tell us that motion is not persistent ; that *energy* constitutes a class of things including two groups, the forces on the one hand and the motions on the other ; that the total amount of energy is persistent, but that the total amount of motion is changeable. And by their definition force is that which produces motion, *i. e.* force can create or destroy motion. But manifestly where there is more motion there must be less force, therefore force can destroy itself ; and when there is more force and less motion, force can create itself.

The moon that passes through the sky of the gentlemen of the old school is moon from the eastern to the western horizon. Then the dragon, which exists not, destroys the moon and thus creates itself, and passing through the cave from west to east it mounts to their horizon, and in the twinkling of an eye commits suicide by creating a moon. It is not strange that the thaumaturgics of such philosophy should lend signal aid to its rhetoric.

The use of hypothesis in science is not only legitimate but an absolute necessity. The science of psychology, as distinguished from metaphysic speculation, points out this fact : that all increase of knowledge is dependent upon hypothesis. Objective impressions made by the phenomena of the universe upon the organ of the mind are discerned only by the aid of comparison, and are added to knowledge only by being combined with previously discerned phe-

nomena. Phenomena imperfectly discerned are such as are combined by superficial analogies; phenomena clearly discerned are such as are combined by essential homologies. With all discernment, therefore, there is comparison, and comparison is reflection and reflection is reason. Now, scientific research is not random observation and comparison, but designed discernment and classification; it is research for a purpose, and the purpose is the explanation of imperfectly discerned phenomena. Phenomena not understood, because imperfectly discerned and classified, are made the subject of examination by first inventing a hypothetic explanation of the same. With this, the investigator proceeds to more careful observation and comparison, devising new methods of discrimination and of testing conclusions. Under the impetus of this hypothetic explanation, discernment and comparison proceed, and additions to knowledge are made thereby, and it matters not whether the hypothesis be confirmed or overthrown.

On this rock much research is wrecked. When an hypothesis gains such control over the mind that phenomena are subjectively discerned, that they are seen only in the light of the preconceived idea, then research but adds to vain speculation. A mind controlled by an hypothesis is to that extent insane; the rational mind is controlled only by the facts, and contradicted hypotheses vanish in their light.

There is another rock on which research is wrecked—the belief which oftentimes takes possession of the mind that the unknown is unknowable, that human research can penetrate into the secrets of the universe no farther. It is the despondency of unrewarded mental toil.

Yet another rock on which research is wrecked is the definition of the unknown. Phenomena appear, but whence is not discovered, and resort is had to verbal statement, and the verbal statement oft repeated comes to be held as a fact itself. This is the vice of all metaphysics, by which *words* are held to be *things*—spectral imaginings that haunt the minds of introverted thinkers as devils possess the imaginations of the depraved.

In the midst of the sea of the unknown stand the three rocks: the controlling hypothesis, the unknowable unknown, and the verbal definition, and in the waters about them are buried many wrecks.

COMBINATION OF MATTER.

When the various bodies known to mind are resolved into their constituent parts to the utmost of art and knowledge, such parts are found to be so minute as almost to disappear in the perspective toward the infinitesimal. The molecular bodies thus dimly discerned are combined and re-combined, until substances are produced that come distinctly within the cognizance of our senses, so that we are able to observe their forms and motions. These molar bodies are again combined, until at last bodies of such magnitude are produced that they are but dimly discerned in the perspective toward the infinite—stellar systems that appear not to the eye, but only to the mind's eye.

INORGANIC COMBINATION.

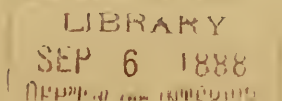
Matter is primarily combined by chemical affinity. The substances thus produced appear in three states: gaseous, fluid, and solid, but are not clearly demarcated. That chemically combined matter which is found in the solid state is further combined by crystallization and lithification. It may be that these methods are parts of the same process, and further, that they are one with chemical affinity; at any rate it is impossible clearly to demarcate them. They are also influenced by gravity, and to a large extent act under its control. Thus it is that gravity, and affinity with its concomitants, unite in molecularly combining matter into inorganic substances. Again, these bodies are mechanically combined into geologic formations, bodies of water, and bodies of air, and such combinations result from gravity. Finally they are all combined into an aggregate, the earth itself, solid, fluid, and gaseous. This also results from gravity.

In the succession of combinations thus briefly reviewed, the first natural aggregate reached is the earth. Below that we have chemical and mechanical substances, which do not constitute integers, but only integral parts. The earth itself is a whole—an aggregation, as the term is here used.

Again, the earth is one of the bodies of the solar system, which is a combination of worlds. This aggregation, also, is controlled by gravity. Other higher astronomic aggregates may exist.

ORGANIC COMBINATION.

Portions of the matter combined by affinity and gravity are seg-



regated to be combined by vitality, giving organic bodies or aggregates, as plants and animals. These bodies do not permanently remain such, as the matter of which they are composed sooner or later returns to the condition of combination due solely to affinity and gravity. They live and die.

SUPERORGANIC COMBINATION.

There are certain biotic bodies whose activities are combined. The first step in combination is the biologic differentiation of the sexes, giving a group of co-operative individuals for the activities of reproduction—male and female, parent and child. This initial combination is crudely developed into still larger combinations of co-operative individuals among the lower animals. With mankind it is developed to a much higher degree, resulting in a great variety of co-operative activities.

There is found, then, a variety of methods of combination, included under three classes: physical, due to affinity and gravity; biotic, due to vital organization; and anthropic, due to related activities. Physical combinations result in the production of *substances* and *aggregates*, and the existence of a physical body is preserved by preserving identity of form and identity of constituent matter. Biotic combination also produces substances and aggregates, and the existence of a biotic body is continued by the preservation of identity of form, but not of identity of constituent matter. In anthropic combination, substances and aggregates, as the terms are here used, are not produced, but biotic aggregates are interrelated in their activities through the agency of mind.

In physical aggregates the relation of parts is that of interdependence, so that the constitution and form of each part are dependent on the constitution and form of every other part. This interdependence may be better comprehended by means of an illustration. In the aggregate the earth, the interdependence is exhibited in the relations existing between the incompletely aggregated bodies of minerals, known as geologic formations; the incompletely aggregated bodies of water, known as seas, lakes, streams, and clouds; and the incompletely aggregated bodies of air, known as winds. Air-currents gather the waters from the seas and pour them upon the lands. Rains and rivers disintegrate the rocks and carry them to the sea. Currents in the sea distribute the detritus over

the bottom. By the loading of areas of sea-bottom they are depressed, and by the degradation of land-areas they are unloaded and rise. Change in the geography of the land effects a change in wind-currents and in bodies of water, and a change in the latter effects a change in sedimentation. In like manner, throughout all physical nature, an interdependence of parts is exhibited. Part acts *on* part.

In biotic aggregates the same interdependence of parts is shown. Any change affecting the digestive apparatus affects the circulatory apparatus, and these again are influenced by the respiratory apparatus. But in addition to this interdependence of parts, there is also an organization of parts—that is, special functions are performed by the several parts, and each is the organ of its function. And this organization is of such a nature that each works for the others. The digestive apparatus digests for itself and all the organs, the heart propels for all the body, the eye sees for all the body, the ear hears for all the body, the hand touches for all the body. Thus the organic parts act *on* and *for* one another.

In activital combination, aggregates, as the term is here used, do not appear, but the same interdependence is observed. By association the sanitary state of the husband affects that of the wife, and the condition of the mother affects the child; and on through the different combinations of animals and men this interdependence is observed. The relation of organization also exists by the differentiation of industries. The husband brings food to the wife and children, and the wife prepares the food. And this differentiation of industries, or “division of labor” as it is termed in political science, is carried on to an elaborate condition in civilized life. Then men are related to one another as constituent members of society; one commands and another obeys. Then men are related to one another through language; one speaks, another hears; one writes, another reads. Then men are related to one another through opinions; having common opinions, they form common designs and act for common purposes. It will thus be seen that superorganic or anthropic combination arises from the establishment of four classes of relations, corresponding to the four classes of activities represented by arts, institutions, languages, and opinions. The arts are human activities directed to the utilization of the materials of nature and the control of its powers, for the purpose of securing happiness. Institutions are human activities arranged for the purpose of securing

peace and establishing justice, and thereby increasing happiness. Languages are activities devised for the purpose of communicating thought, and thereby securing happiness. Opinions arise from psychic activities, the purpose of which is to learn the truth, that happiness may ensue.

In physical, biotic, and anthropic combinations the parts control one another. It will therefore be convenient to speak of three kingdoms of matter: the mineral or physical kingdom, the organic or biotic kingdom, and the anthropic or activital kingdom.

MODES OF MOTION.

All bodies, however combined, are discovered to be in motion.

Among the bodies of the mineral kingdom, a variety of modes of molecular motion are exhibited, having various distinguishing characteristics. These are heat and light, electricity and magnetism, then sound and that motion in gases by which through impact they retain their rarefied state. Again, a variety of molar motions are observed in gases, liquids, and solids; and finally stellar motions are observed in astronomic systems.

In the biotic kingdom plants and animals exhibit many varieties of organic motions, called *functions*. These are superadded to the physical motions, which appear alike in the physical and biotic kingdoms. Physical bodies exhibit motions; biotic bodies exhibit motions and functions, the latter being highly organized motions.

In the anthropic kingdom there is a complexity of motions arising from biotic functions, which are arranged and combined so as to produce *activities*. These activities are represented by arts, institutions, languages, and opinions.

Thus there are three great classes of motions corresponding to the three great classes of combinations, namely, physical motions; biotic motions, or functions; and anthropic motions, or activities.

THE RELATION OF MOTION TO COMBINATION.

It will at once be seen that anthropic combination is such by virtue of human activities. Activital combination is manifestly composed motion.

Again, biotic aggregates are such by virtue of continuous combination and dissolution. Within proper limits a biotic body may be compared to a river; it is a form through which matter passes. In

plants some of this passing matter becomes fixed for a time, but eventually returns from the biotic to the mineral kingdom. Among animals this passage of physical matter through the biotic form is more rapid. The organic functions, also, of these bodies are but arranged or organized motions. Life is motion—the specific motion called *function*.

Again, among the aggregations of the physical kingdom, stellar systems are aggregates by virtue of motion. The combination observed is due to composed motion. Of the mechanical combinations, that exhibited in the atmosphere is such by virtue of motion—that is, the gaseous state is preserved by the interference of molecular motions, and the bodies into which it is imperfectly differentiated, *i. e.*, currents of air, are such by virtue of motion. Again, the imperfectly aggregated bodies of water are such by virtue of motion. This is seen to be true of the clouds floating in the air, and of rivers rolling to the seas. Lakes with outlets are bodies of water in motion, forever fed from the clouds, forever discharging into the sea; and mediterranean seas without outlet are perpetually receiving and discharging their waters; and so far as the sea is differentiated into currents, these are bodies imperfectly aggregated by motion.

There yet remain certain molecular combinations of inorganic substances, due to affinity and gravity, the nature of which is not so immediately perceived. Now, as all societies and other anthropic combinations are such by virtue of their motions, known as activities, and as all biotic bodies are such by virtue of their functions, and as all stellar combinations are such by virtue of stellar motion, and as finally all mechanical combinations are such by virtue of motion, it is at once suggested as an inductive hypothesis that those combinations the nature of which is yet unknown are also such by virtue of motion. It is an hypothesis worthy of consideration, that affinity and gravity are also due to motion. It has even been supposed by some that chemical and barologic methods of combination are but diverse modes of the same process; that affinity and gravity constitute but one method of combination, and that we call it *affinity* when the combination involves minute bodies, below our sense perceptions, and *gravity* when larger bodies are involved.

An attempt has thus been made to define the three kingdoms of matter in terms of matter and motion, showing that there are three

methods of combination, and that the parts combined are related by three corresponding methods, and that in each kingdom motions of a distinctive class are discovered. The constitution of physical bodies is due to composed motion; the constitution of biotic bodies is due to composed transmutations of motion; anthropic combinations are due to related activities.

In order that there be evolution, there must be change in combination of matter and in mode of motion. The sole property of matter is motion, and motion itself is change of position. But this change of position results in change of combination, and change of combination results in change of mode of motion. These changes must now be set forth.

CHANGE OF COMBINATION.

If the mind could discern and classify all the bodies of the universe at any one moment, only space conditions would enter therein; but bodies change from time to time, so that there are sequences of combination. Substances and aggregates of matter are such by reason of an arrangement in position of their constituent parts. Substances and bodies change in external relations and in internal relations. Change in external relations is change of position in relation to external things. Change in internal relations is the change in relative arrangement of constituent parts. And this change of position is always motion, the first and only property of matter.

Chemical, crystalline, and lithical combinations are decomposed and otherwise re-composed, mechanical combinations are broken up and otherwise re-arranged, and stellar aggregates are believed to have been gradually formed. With physical bodies internal change is the direct result of external change. This is their distinctive characteristic, that all their changes of constitution result directly from agencies without themselves.

Biotic bodies exhibit the same changes as mineral bodies, and also a series peculiar to themselves. First, biotic substances are segregated from the mineral kingdom—*i. e.*, mineral substances are changed into biotic substances. Second, biotic bodies begin, grow, decline, and die. This is a progressive change of structure. Third, the structure of biotic bodies is preserved by continuous change in their constituent matter. Form and structure are preserved while the matter is forever changing. Life is a determined, systematic sequence of transmutations of motion, transformations of matter, and

transfigurations of body. Life is change. Fourth, as the individuals are not persistent, the method of aggregation continues by the processes of reproduction of like forms. But these like forms are made unlike—*i. e.*, changed—by two processes. In the biotic reproduction of the higher forms the bisexual method prevails, so that each individual is the offspring of two parents, like both so far as they are alike, but differing from the one or the other so far as they are unlike. Fifth, the individual has its constitution determined by its parents, but subject to changes which may be brought about by external relations differing from those to which the parents were subjected; and within limits these are transmitted to offspring. Thus it is seen that biotic changes are caused by external and internal agencies.

This may be put in another form. In mineral bodies the same matter is changed in structure. In biotic bodies the same or nearly the same structure remains and the constituent matter changes; yet there is a slow change in structure from birth to death, and a still further change in structure from generation to generation; but there is more rapid change of constituent matter. Anthropic aggregates arise, not by a combination of matter, but by a combination of the activities of biotic bodies. These biotic bodies themselves change, as individuals disappear and new ones take their places. Thus family group succeeds family group, and generations of people succeed generations of people. In the same manner arts change. Old arts are abandoned and new arts appear. Various societies cease to exist and new societies are organized. The organization due to the differentiation of operations steadily increases by the division of labor; and the grouping of bodies of men into states, *i. e.*, tribes and nations, is in constant flux. So, languages change—they grow and die. And opinions change with each individual and from generation to generation. All these changes are determined by the will of the individual units who are actors—that is, activities change because the actors so desire. Anthropic change is due to psychic agencies.

CHANGE OF MOTION.

That motion is persistent is a fundamental axiom. But while it does not change in quantity it changes in quality in diverse ways. First, motion may be changed in direction. Simple motion is the motion of a body in a straight line, and change of such motion of

the lowest order is change in direction, and this is accomplished by the combination of two or more motions having different directions. Then motion may be transmitted from one body to another. The molecular motions—heat, light; electricity, sound, etc.—are motions propagated by transmission from molecule to molecule. In the kinematic hypothesis of gravity it is held that atomic motion is transmitted from atoms to combined and aggregated bodies by impact; and here we reach another method of change—that by transmutation. One mode of motion may be transmuted into another, as molar motion into heat, and heat into electricity.

By the combination of matter motion is composed. Mineral substances and aggregates exhibit this composition of diverse modes of motion. Biotic bodies exhibit composition of modes of motion, and also composition of transmutations of motion, and it is this latter characteristic which distinguishes biotic from physical motion. Activital combinations exhibit a composition of modes of motion, and a composition of the transmutations of motion, and a composition by co-operative action. It is the last characteristic which distinguishes activital motion from biotic.

The changes of motion exhibited in the mineral kingdom are changes in direction by combination, changes in relative quantity by transmission, changes in mode of motion through transmutation, and changes in the combination of modes of motion.

In the biotic kingdom the same changes are found as in the mineral kingdom, but to them are added changes in the composition of transmutations of motion.

In the anthropic kingdom all the changes in the other kingdoms appear, together with changes in the composition of activities.

EVOLUTION DEFINED.

As matter is indestructible, when one combination or aggregation is dissolved some other must appear, and *vice versa*. Existing bodies must have antecedents. In tracing backward the history of bodies, lines of sequences are followed. Many such are known, and the first important characteristic to be noted of them is *they are orderly*. Like bodies have like antecedents. From this results one of the highest inductions of science, namely, that from consequents antecedents can be restored, and from antecedents consequents can be predicted. The second important characteristic of these sequences

of change is that *many are in a definite direction*, which is gradually becoming known. This general course of change is denominated Evolution, and the term must be defined.

Evolution is progress in systemization. It must be noted that not all changes are progressive; some are retrogressive. It is only progressive change that is here called evolution; retrogressive change is dissolution. As the term is here used, a System is an assemblage of interdependent parts, each arranged in subordination to the whole so as to constitute an integer. Evolution may therefore be defined in another way. It is progress in differentiation by the establishment of unlike parts, and in the integration of these parts by the establishment of interdependence. Dissolution is retrogression by the lapsing of integration through the destruction of interdependence, and the lapsing of differentiation through the loss of heterogeneity in parts.

EVOLUTION IN THE PHYSICAL KINGDOM.

Under the kinematic hypothesis, which embraces the ethereal and nebular hypotheses, portions of discrete matter have been segregated to be combined and aggregated. The process precedent to evolution, then, is combination and aggregation, by which substances and integers are produced.

Whatever may be the fate of the explanation of the origin of substances and aggregates through the kinematic and concomitant hypotheses, the fact remains that such bodies exist, and the evolution of matter, as it is hereafter dealt with, starts from this point. Given substances and aggregates as they are known to exist in nature, and given changes which they are known to undergo, it is proposed to point out by what methods evolution is attained.

The terms *substance* and *aggregate* have been used as distinguishing two orders of combination. It should be noted that they cannot be clearly demarcated. Substances are composed of homogeneous, non-interdependent parts, but this homogeneity is never absolute, and some slight degree of interdependence may always be discovered. Aggregates, on the other hand, are composed of heterogeneous, interdependent parts, but degrees of heterogeneity and interdependence appear. Combination is the bringing together of dissociated matter; and it is in the combinations, separations, and re-combinations of matter that evolution appears.

In mineral bodies combinations proceed by molecular, molar, and stellar methods. It has been shown that the changes in these bodies are due to external conditions or forces. If a given body be in harmony with external conditions no change occurs in its constitution, but if it be out of harmony the impinging agencies effect such modifications as will produce harmony. This may be done by a change in the body as a substance or aggregate, or by its separation and re-combination in some more harmonious form. The evolution of mineral bodies is thus accomplished by direct adaptation to external conditions.

If it is permitted hypothetically to conceive of a universe of ethereal matter—*i. e.*, matter composed of discrete atoms in motion, such atoms would remain in an attenuated condition by atomic impact. In matter thus constituted, motion could be transmitted from atom to atom, but no new mode of motion would result therefrom. The mass of matter thus constituted would be absolutely homogeneous. But if by some method several such atoms should be combined, so as to move together as a common body, and so that their interspaces could not be penetrated by other atoms, the motion of an impinging atom would not only be transmitted to the larger body, but it would also be transmuted into another mode or kind of motion. If other such molecules were formed by the segregation of atoms from the homogeneous mass, the new kind of motion would be set up in all the matter thus segregated, and the motions of these bodies would react one upon another. If, again, some of these molecules were segregated, to be combined in larger bodies, with or without such a diminution of interspaces as to prevent the interpenetration of atoms, a third mode of motion would be established; and if diverse methods of aggregation should occur, diverse modes of motion would be established thereby; and in all combining and re-combining, aggregating and re-aggregating, new modes and complexities would arise.

It is a well-known law that a moving body passes in the direction of the least resistance. Diverse modes of motion may exist in a body, due to the complexities of its organization. In the transmission of motion to such a body from another by impact, the motion transmitted is transmuted into that mode which gives it the least resistance. This is illustrated on every hand. When a smaller body impinges against a larger, the inequality between the two may be so great that molar motion is not set up in the

larger body, but the whole of the imparted motion is transmuted into heat or some other molecular motion.

This law, that motion passes in the direction of least resistance, is the equivalent of the law of adaptation in the evolution of matter. When evolution is considered from the standpoint of matter, it is convenient to use the term *Adaptation*; when considered from the standpoint of motion, it is more convenient to use the term *Least Resistance*.

EVOLUTION IN THE BIOTIC KINGDOM.

In biotic bodies it has been seen that change is the result of internal as well as external conditions. As external conditions, or the environment, are changing, these bodies change to a limited extent, in the same manner as do mineral bodies; but there is also a change brought about indirectly by the environment, through certain internal changes in the constitution of biotic bodies. Through this internal constitution individuals are changed in time—one generation dies and another succeeds.

There is yet another method of change in biotic bodies, which steadily increases from the lowest to the highest—that is, the change in their constituent matter. While structure changes slowly from birth through growth and decadence to death, the constituent matter changes with much greater rapidity. In this change the minute elements of structure change much more rapidly than the larger into which they are compounded; so that every part of the organ must be supplied with new material to replace that which is steadily becoming effete and passing away. Now the rate of this change in any integral part of an organism is dependent upon the activity of the organ. Exercise increases the rate of change in the constituent matter of a biotic organ, and thus the slow change in its structure, which proceeds from life to death, is accelerated. This accelerated change results in increased differentiation of the organ, and it thereby becomes more and more efficient in the performance of its function. This change, therefore, results from exercise. Organs that are exercised increase in efficiency, by non-exercise they decrease in efficiency. This change in the organization of any one individual is but slight, but as the slight changes pass from one generation to another, continuous exercise of one set of organs greatly modifies them; continuous neglect of exercise in another set modifies them also, until at last they are atrophied. Thus by exercise and non-

exercise important structural changes are produced when conjoined with the changes due to heredity.

All these changes result in progress, from the fact that those individuals whose change is in a direction out of harmony with the environment ultimately perish, while those whose change is in a direction in harmony with the environment survive. This method of adaptation or evolution in biology is called "the survival of the fittest."

The rate of evolution by survival is greatly accelerated by another condition. Each pair of biotic bodies reproduce a large number of new bodies, so that reproduction from generation to generation is in a high geometric ratio. The earth having become occupied with all the biotic beings that can derive sustentation therefrom, but a small fraction of the beings produced in a generation can live. Few survive, many succumb. Survival by adaptation is therefore made more efficient by competition.

There are other changes in the biotic kingdom brought about by adaptation. The multiplicity of biotic beings, causing over-population, has crowded them into every conceivable habitat—in the air, on the land, and in the water; and living beings have become adapted thereto by the development of wings, legs, fins, and correlative organs. Thus by exercise organs have been developed, and by non-exercise other organs have been atrophied, until living beings have become specialized for a vast diversity of habitats—for life on the mountain and in the valley, in the light and in the dark, in the cold and in the heat, in humid regions and in arid regions. Living beings have also been adapted to various kinds of food and to various methods of acquisition—in fine, to a great variety of conditions.

This specialization by development, through exercise and non-exercise, must be clearly distinguished from the processes of evolution. The heterogeneous living beings thus produced are but multiplied and diverse forms, animals and plants alike being as often degraded as evolved in the processes of specialization. Degradation is especially to be noticed in parasitic animals and others adapted to extremely abnormal habitats; but it should be understood that a form thus produced may, in the process of its production and subsequent existence, make progressive change in the system of its structure by the methods of evolution already characterized.

Specialization is greatly accelerated by a peculiar method. As

all the higher animals are physically discrete, psychic relations must be established, in order that they may meet for the act of reproduction. These psychic relations gradually develop into choice, or sexual selection, and by methods which have been clearly pointed out by biologists the minute increments of change that result therefrom eventually accumulate into strong variations, always adapted to the conditions of the environment. Thus the survival of the fittest is accelerated by sexual selection.

EVOLUTION IN THE ANTHROPIC KINGDOM.

If attention is directed exclusively to animal life, we notice that evolution has proceeded *pari passu* with specialization. Of the forms that have been specialized from time to time some have become extinct, some have been degraded, and some have been evolved in varying degree. One form, not the most specialized, made the greatest progress in evolution, until an organism was developed of so high a grade that this species became more independent of environment than any other, and, by reason of its superiority, spread widely throughout the land portion of the globe. This superior animal was early man, when he first inhabited all the continents and the great islands. The production of this superior, *i. e.* more highly systematized organism, was the antecedent to the inauguration of new methods of evolution.

It has been shown that the great efficiency of the biotic method of evolution by survival depends upon competition for existence in enormously overcrowded population. Man, having acquired superiority to other animals, passed beyond the stage when he had to compete with them for existence upon the earth and into the stage where he could utilize plants and animals alike for his own purposes. They could no longer crowd him out, and to that extent the law of the survival of the fittest in the struggle for existence was annulled in its application to man. He artificially multiplies such of the lower animals as are most useful to him, and domesticates them, that they may be more thoroughly under his control, and modifies them, that they may be more useful, and uses such as he will for beasts of burden; and the wild beasts he destroys from the face of the earth. In like manner he cultivates useful plants, and destroys such as are worthless to him. He does not compete with other biotic species, but utilizes them for his welfare. Yet

the law of the survival of the fittest applies in so far as it is not dependent upon competition, and slow evolution may still result therefrom. But at this stage new methods spring up of such great efficiency that the method by the survival of the fittest may be neglected because of its insignificance.

In anthropic combinations the units are men, and men at this stage are no longer passive objects, but active subjects; and instead of man being passively adapted to the environment, he adapts the environment to himself through his activities. This is the essential characteristic of anthropic evolution. Adaptation becomes active instead of passive. In this change certain parts of the human organism are increasingly exercised from generation to generation. This steadily increasing exercise results in steadily increasing development, and the progress of the unit—man—in this higher organization depends upon development through exercise. But the progress by exercise depends upon the evolution of activities.

Man is an animal, and may be studied as such; and this branch of science belongs to biology. But man is more than an animal. Though an animal in biotic function, he is man in his anthropic activities; for by them men are combined—*i. e.*, interrelated—so that they are not discrete beings, but each acts on, for, and with, his fellow-man in the pursuit of happiness. Human activities, thus combined and organized, transcend the activities of the lower animals to such a degree as to produce a new kingdom of matter. The nature of these activities must here be set forth.

The first grand class is composed of those which affect the external world, and by them men are interrelated through their desires. These activities are the Arts. The arts have been evolved by human invention, and man has been impelled thereto by his endeavor to supply his wants. In the course of the evolution of the arts, man has progressively obtained control over the materials and powers of nature. All the arts of all the human period are the inventions of men. But invention has proceeded by minute increments of growth. A vast multiplicity of arts have been devised, of which comparatively few survive in the highest civilization. As the inventions have been made, the best in the average has been chosen. Man has therefore exercised choice. The evolution of the arts has thus been by the method of invention and choice, in the endeavor to gratify desire, and by them man has adapted the environment to himself.

Second. There is a grand class of activities through which men

are interrelated in respect to their conduct. These activities result in Institutions. Through them men are associated for a variety of purposes. Every institution is an organization of a number of individuals, who work together for a common purpose, as, for example, to prosecute some industrial enterprise, to co-operate in the pursuit of pleasure, to promote some system of opinions, or to worship together under the forms of some religion. All such institutions constitute a class denominated Operative Institutions. A second class are the institutions which man has organized for the direct regulation of conduct. These are States and their subordinate units, with their special organs of government, and rules for the regulation of conduct, called Laws.

Institutions have been developed from extreme simplicity to extreme complexity. They are all the inventions of mankind, and their evolution has been by minute increments of growth. Their invention has been wrought out that men might live together in peace and render one another assistance; and gradually, by the consideration of particulars of conduct as they have arisen from time to time, men have sought to establish justice, that they might thereby secure peace. Of the vast multiplicity of institutions—forms of state, forms of government, and provisions of law—which have been invented, but few remain in the highest civilization, and these few have been selected by men. Men have thus exercised choice. Institutions, therefore, have been developed by invention and the choice of the just in the endeavor to secure peace.

Third. There is another fundamental group of activities through which men are interrelated in respect to their thoughts. These are the activities of mental intercommunication, and result in Languages. Languages, also, are inventions by minute increments of growth. Many languages have been invented, and in each language many words and many methods of combining linguistic devices have been invented. In the languages of the most civilized peoples, but few of these survive; and there are spoken by all the peoples of the earth but few languages in comparison to the many that existed in the early history of mankind; and the method of survival, when analyzed, is found also to be choice. Men have chosen the economic in the expression of thought. Languages, therefore, have developed by invention and choice in the struggle for expression.

Fourth. There is a grand class of activities by which men are interrelated in respect to their designs. Men arrive at Opinions, and

these have always reacted upon languages, institutions, and arts, and largely led them in their courses of progress. Because of their opinions, men are willing to work together, and thus have common designs. There have been many opinions and many systems of philosophy. Of all that have existed, but few remain in the highest civilization. A careful analysis of the facts relating to the growth of opinions reveals this truth, that opinions also are invented, and that the final survival of the few has been due to the human act of choice in the selection of the truth. Opinions, therefore, have been developed by invention and choice in the struggle to know.

Fifth. Opinions are formed as the direct activities of the Mind. Languages, institutions, and arts have arisen through the action of the mind and the exercise of other corporeal functions. All these activities, therefore, are dependent upon the mind. On the other hand, these objective activities react upon the mind, so that mental operations are controlled thereby. Through the exercise of the mind in the prosecution of activities it is developed. These mental activities are perception and comparison, or reflection, as it is more usually called. The subjective evolution of the mind is therefore the product of the objective evolution of activities.

These five great classes of activities are interdependent in such a manner that one is not possible without the others; they arise together, and their history proceeds by a constant interchange of effects. All the five classes of activities react upon man as an animal in such a manner that his biotic history subsequent to his differentiation from the lower animals is chiefly dependent thereon. The evolution of man as a being superior to the beast is therefore due to the organization of activities.

It has been shown that man does not compete with the lower animals for existence. In like manner, man does not compete with man for existence; for by the development of activities men are interdependent in such a manner that the welfare of one depends upon the welfare of others; and as men discover that welfare must necessarily be mutual, egoism is transmuted into altruism, and moral sentiments are developed which become the guiding principles of mankind. So morality repeals the law of the survival of the fittest in the struggle for existence, and man is thus immeasurably superior to the beast. In animal evolution many are sacrificed for the benefit of the few. Among mankind the welfare of one depends upon the welfare of all, because interdependence has been established.

It has thus been shown that there are three stages in the combination of matter and motion, and that each stage is characterized by a clearly distinct method of evolution. These may be defined as follows :

First, physical evolution is the result of direct adaptation to environment, under the law that motion is in the direction of least resistance.

Second, biotic evolution is the result of indirect adaptation to the environment by the survival of the fittest in the struggle for existence.

Third, anthropic evolution is the result of the exercise of human faculties in activities designed to increase happiness, and through which the environment is adapted to man.

These may be briefly denominated: evolution by adaptation, evolution by survival of the fittest, and evolution by endeavor.

Civilized men have always recognized to some extent the laws of human evolution,—that activities are teleologically developed, and that happiness is increased thereby. In the early history of mankind the nature of teleologic endeavor was so strongly impressed upon the mind that the theory was carried far beyond the truth, so that all biotic function and physical motion were interpreted as teleologic activity. When this error was discovered, and the laws of physical and biotic evolution established, vast realms of phenomena were found to have been entirely misunderstood and falsely explained, and teleologic postulates have finally fallen into disrepute. Men say there is progress in the universe by reason of the very laws of nature, and we must let them alone. Thus, reaction from the ancient false philosophy of teleology has carried men beyond the truth, until they have lost faith in all human endeavor; and they teach the doctrine that man can do nothing for himself, that he owes what he is to physical and biotic agencies, and that his interests are committed to powers over which he has no control.

Such a philosophy is gradually gaining ground among thinkers and writers, and should it prevail to such an extent as to control the actions of mankind, modern civilization would lapse into a condition no whit superior to that of the millions of India, who for many centuries have been buried in the metaphysical speculations of the philosophy of ontology. When man loses faith in himself, and worships nature, and subjects himself to the government of the

laws of physical nature, he lapses into stagnation, where mental and moral miasm is bred. All that makes man superior to the beast is the result of his own endeavor to secure happiness.

Man, so far as he is superior to the beast, is the master of his own destiny, and not the creature of the environment. He adapts the natural environment to his wants, and thus creates an environment for himself. Thus it is that we do not discover a biotically aquatic variety of man, yet he dwells upon the sea and derives sustentation from the animals thereof by means of his arts. A biotically arboreal variety of man is not discovered, but the forest are used in his arts and the fruits of the forests for his sustentation. An aërial variety of man is not discovered, but he uses the winds to propel his machinery and to drive his sails; and, indeed, he can ride upon the air with wings of his own invention. A boreal variety of man is not discovered, but he can dwell among the everlasting snows by providing architectural shelter, artificial warmth and bodily protection.

Under the influences of the desert a few plants secure a constitution by which the moisture imbibed during brief and intermittent rains is not evaporated; they become incrustated with a non-porous glaze, or contract themselves into the smallest space and exist without life until the rain comes again. Man lives in the desert by guiding a river thereon and fertilizing the sands with its waters, and the desert is covered with fields and gardens and homes. Everywhere he rises superior to physical nature. The angry sea may not lash him with its waves, for on the billows he builds a palace, and journeys from land to land. When the storm rises it is signaled from afar, and he gathers his loved ones under the shelter of his home, and they listen to the melody of the rain upon the roof. When the winds of winter blow he kindles fossil sunshine on his hearth, and sings the song of the Ingleside. When night covers the earth with darkness he illumines his path with lightning light. For disease he discovers antidote, for pain nepenthe, and he gains health and long life by sanitation; and ever is he utilizing the materials of nature, and ever controlling its powers. By his arts, institutions, languages, and philosophies he has organized a new kingdom of matter, over which he rules. The beasts of the field, the birds of the air, the denizens of the waters, the winds, the waves, the rivers, the seas, the mountains, the valleys, are his subjects; the powers of nature are his servants, and the granite earth his throne.

BULLETIN

OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON.

GENERAL MEETING.



BULLETIN
OF THE
GENERAL MEETING.

227TH MEETING.

JANUARY 13, 1883.

The President in the Chair.

Twenty-six members present.

Mr. H. FARQUHAR completed a communication begun at the 224th meeting on

EXPERIMENTS IN BINARY ARITHMETIC,

in which he showed that simple addition involved carrying on several distinct mental operations almost simultaneously and a capital of more than fifty propositions committed to memory. Believing that the difficulty in mastering, and the mental strain and liability to error in conducting, this most important of mathematical processes could be proved to be unnecessarily great, he had compared the time occupied in adding a few dozen numbers of six or eight figures each with that required when these numbers were expressed in powers of 2, the mental work being, in the latter case, reduced to counting similar marks and halving their sums. He had found it best to give different forms to the marks denoting neighboring powers, so as to avoid confusion of columns, and had combined two or more of them into one written figure for brevity of expression. About seventy combinations of various shapes had been tried, but very few of them found economical. In the best notation, however, the addition required only three-fourths the time taken with the ordinary figures. Had the computer practised as many weeks with the new notation as years with the old, the difference would have been much more marked; as it was in fact when one unskilled in arithmetic, to whom the binary notation had just been taught, tried the two additions. The gain in accuracy, with this observer, was even

more striking than the gain in speed. There could be very little doubt, therefore, that a fair degree of skill in arithmetic with a binary notation could be acquired by many to whom it is impossible under the present system.

The only practicable division of arcs and angles, and the most natural division of all things, is by continued bisections. This is shown by the ratio of value in our coins, weights, and capacity measures; by any table of prices; and by the prevalent subdivision of lowest nominal units, as of the carpenter's inch into eighths and sixteenths, and of percentages into quarters, etc., in stock quotations, where convenience of calculation by our present arithmetic seems almost gratuitously sacrificed. The American coinage is inconvenient in practice, because of the awkward fractional ratio $2\frac{1}{2}$, which it introduces between successive pieces; and there would be the same difficulty in a decimal system of weights or of measures, should it be imposed upon us. We have thus another powerful reason for endeavoring to introduce a binary arithmetic.

In the remarks which followed, Mr. E. B. ELLIOTT expressed the hope that Congress would adopt the metric system of weights and measures for international purposes. It would be better to secure what advantage could be gained from uniformity and consistency, even though the basis of consistency was an arithmetic not ideally the best attainable. Such a course would not prevent, but might pave the way for a better arithmetic.

Mr. W. B. TAYLOR said the world was losing so much by the employment of the denary arithmetic that he thought even a single generation might find economy in substituting the octonary. The introduction of decimal measures, while it would aid the computer, would injure the remainder of the community. The paper of Mr. Farquhar had an especial value, in that it proved the ability of binary systems to compete with the established system in rapidity of computation.

Other remarks were made by Messrs. HARKNESS, MUSSEY, POWELL, and GILBERT.

The next communication was by Mr. S. M. BURNETT on

REFRACTION IN THE PRINCIPAL MERIDIANS OF A TRIAXIAL ELLIP-
SOID; REGULAR ASTIGMATISM AND CYLINDRICAL LENSES;

and he was followed by Mr. W. HARKNESS on

THE MONOCHROMATIC ABERRATION OF THE HUMAN EYE IN
APHAKIA.

These two papers are complementary, and are published in the *Archives of Ophthalmology*, Vol. XII, No. 1.

228TH MEETING.

JANUARY 27, 1883.

The President in the Chair.

Thirty-seven members present.

The Auditing Committee, appointed at the Annual Meeting, reported through its chairman, Mr. Antisell, that it had examined the accounts of the Treasurer for 1882, and found them correct.

The report was accepted.

The communication of the evening was by Mr. H. H. BATES on

THE NATURE OF MATTER,

and was discussed by Mr. W. B. TAYLOR and Mr. POWELL.

This paper is published in the *Popular Science Monthly* for April, 1883.

229TH MEETING.

FEBRUARY 10, 1883.

The President in the Chair.

Forty-two members and visitors present.

It was announced that reports of the scientific proceedings would hereafter be furnished to Science.

Mr. W. H. DALL announced that an opportunity would be afforded members to contribute to the Balfour Memorial Fund.

A communication was then read by Mr. A. F. A. KING on

THE PREVENTION OF MALARIAL DISEASES, ILLUSTRATING, *inter alia*,
THE CONSERVATIVE FUNCTION OF AGUE.

[Abstract.]

The various theories thus far presented in explanation of the

phenomena of malaria were unsatisfactory and insusceptible of scientific demonstration.

According to the best medical authorities the most generally admitted facts upon which the present orthodox theory of malaria rests were as follows: 1. Malaria affects by preference low and moist localities. 2. It is almost never developed at a lower temperature than 60° F. 3. Its evolution or active agency is checked by a temperature of 32° F. 4. It is most abundant and most virulent as we approach the equator and the sea-coast. 5. It has an affinity for dense foliage, which has the power of accumulating it, when lying in the course of winds blowing from malarious localities. 6. Forests or even woods have the power of obstructing and preventing its transmission under these circumstances. 7. By atmospheric currents it is capable of being transported to considerable distances—probably as far as five miles. 8. It may be developed in previously healthy places by turning up of the soil, as in making excavations for the foundations of houses, tracks for railroads, and beds for canals. 9. In certain countries it seems to be attracted and absorbed by bodies of water lying in the course of such winds as waft it from the miasmatic source. 10. Experience alone can enable us to decide as to the presence or absence of malaria in any given locality. 11. In proportion as countries, previously malarious, are cleared up and thickly settled, periodical fevers disappear, in many instances to be replaced by typhoid fever (?) 12. Malaria usually keeps near the surface of the earth. It is said to “hug the ground,” or “love the ground.” 13. It is most dangerous when the sun is down, and seems almost inert during the day. 14. The danger of exposure after sunset is greatly increased by the person exposed *sleeping* in the night air. 15. Of all human races the white is most sensitive to marsh fevers, the black least so. 16. In malarial districts the use of fire, both indoors and to those who sleep out, affords a comparative security against malarial disease. 17. The air of cities in some way renders the poison innocuous; for, though a malarial disease may be raging outside, it does not penetrate far into their interior. 18. Malarial diseases are most prevalent towards the latter part of summer and in the autumn. 19. Malaria is arrested not only by trees, but also by walls, fences, hills, rows of houses, canvas curtains, gauze veils, mosquito nets, and probably by fishing nets. 20. Malaria spares no age, but it affects infants much less frequently than adults.

These generally admitted facts were insusceptible of scientific explanation by the marsh fever hypothesis of Lanciscisci; but were capable of explanation by the theory that marsh fevers are produced by the bites of proboscidian insects, notably in this and in some other countries by mosquito bites.

A review of the natural history, habits, and geographical distribution of the mosquito was next presented in explanation of the twenty statements above quoted.

In discussing statement 15, it was maintained that the comparative immunity of the black races was largely due to color, the dark complexion of the skin being another illustrative instance of "protective coloring" so often observed in other animals, and by which, in this instance, the negro was protected from the *sight*, and consequently from the *bite* of the mosquito; a similar protection being further secured by the offensive odor and greasiness of his cutaneous secretions, aided by artificial inunction of the body with grease, paint, pitch, &c., which last probably constituted the initial step in the evolution of dress. Hence malarial melanosis was considered to be the designed natural termination of ague—its conservative function—destined to modify the individual by defensive adaptation against the mosquito, whose penetrating proboscis, like an inoculating needle, infected the body with malarial poison, no matter whether this last was mosquitual saliva, the *Bacillus malarie* of Klebs and Crudelli, or some other element as yet unknown.

The spleen, whose function is not yet settled by physiologists, was regarded as the chief *pigment-forming organ*, and was *designed for this purpose in the economy of the organism*. Generally considered a superfluous organ, capable of removal without any great interference with the functions of the organism, it was naturally designed to *meet the emergency of variation in skin-color* to secure "protective coloring" against fever-producing proboscidian insects, as before indicated. The natural process, however, required exposure of the naked body to the sun during the chill stage, in order to secure deposit of the newly formed pigment in the skin. Nature had not anticipated the artificial appendage of dress, and the organism had not inherited from ancestral progenitors any provision for so unexpected an addition. Chills do not occur at night, but only between the rise and setting of the sun; sunlight during the chill stage being a necessary requirement, in order that nature's design of cutaneous chromatogenesis may be consummated. Other racial

differences between the whites and blacks—such as even cerebral capacity and variations in the skeleton—might be susceptible of explanation by blood changes resulting from malaria. The marrow of bones was also a pigment-forming tissue, and the aching of bones during ague, especially in so-called “break-bone” fever, suggested congestion and modified nutrition in the osseous structures, such as might eventually lead to modification in the skeleton. The inhabitants of oriental countries especially were more vigorous and intelligent if they lived in elevated regions, than were others inhabiting mosquito-infected lowlands and sea coasts.

In further support of the mosquital origin of malarial fevers numerous noted medical authorities were cited, showing that, in all parts of the world where these diseases prevail, immunity was secured by protecting the body from mosquito bites. The geographical distribution and seasonal evolution of mosquitoes and other proboscidian insects were shown partially to agree with the times and places in which malarial diseases prevail; though from lack of information conclusive evidence on this point was yet wanting. There was, however, a general admission on the part of medical authorities that swarms of these insects in almost any locality were a pretty sure sign of malignancy.

On the other hand numerous instances were adduced from “Narratives” and “Travels” in which the bodies of persons had been covered with pustules, “resembling small-pox,” from mosquito bites without any subsequent occurrence of fever having been *recorded* by the narrating authors.

This opposing evidence was inconclusive, (1) because the authors cited were not in search of medical information; (2) because the period of incubation, being often long and uncertain, fever *may* have occurred after the mosquito bites had been forgotten; (3) the insect proboscis (like a vaccine lancet unarmed with virus) might be uncontaminated with fever poison, or fever germs; and (4) *successful* inoculations of specific germ poisons are *not* usually followed by immediate local suppuration at the point of puncture, but only after a certain period of incubation, the *immediate* local inflammation being rather *preventive* of subsequent blood infection.

The possible spread of yellow-fever contagion by the inoculating proboscis of the mosquito carrying infecting matter drawn from the blood of yellow-fever patients to unaffected persons was suggested. In epidemics, the spread of the disease stopped as soon as a freezing temperature paralyzed the mosquito, &c.

The spread of spotted-fever, typhus-fever, in jails, ships, &c., was referred to the inoculating instrument of fleas, &c.—these insects usually prevailing among filthy people thickly crowded together.

That malarial diseases were ever produced solely by the *inhalation* of supposed poisonous vapors was held to be untenable. Experimenters, who had demonstrated the existence of specific poisons for special fevers, had equally proven that the mode by which such poisons, when obtained, could be introduced into the body for the artificial production of disease, was by *inoculation through the skin*. These experiments were imitations of insect inoculation. The proboscis of the mosquito was Nature's inoculating needle.

The *modus operandi* of the eucalyptus tree in preventing malarial diseases was ascribed tentatively to the tree being destructive to, or interfering directly or indirectly with, the propagation and development of mosquitoes.

From the foregoing conceptions as to the origin of malarial disease, the following prophylactic measures were deducible:

1st. *Personal* protection from all winged insects, especially during evening and night, by gauze curtains, veils, window-blinds, or clothing impenetrable by the proboscis of inoculating insects; and further, personal protection both from these and all creeping insects, especially during epidemics, endemics, and in crowded jails, ships, &c., by daily inunction of the whole body with some terebinthinate, camphorated, or eucalyptalized ointment or liniment.

2d. *Domiciliary* protection (*a*) *exteriorly*, by screens of trees, walls, fences, &c., interposed at some distance between dwellings and the supposed sources of malaria, or mosquito nurseries; and with fires or lamps arranged as traps for the attraction and destruction of such winged insects as may encroach nearer. A further protection (*b*) in the *interior* of dwellings being secured by the use of smoke (as of tobacco or prethrum) or of some volatile aromatic substance, as of camphor, assafoetida, garlic, &c., which may be offensive to proboscidian intruders.

3. *Municipal* protection by groves of trees (pines, cedars, or eucalyptus) planted between cities and the sources of malaria and mosquitoes, together with cordons of electric or other lights, between said grove and the marsh, the lights to be arranged as fly-traps for the retention and destruction of such winged insects as may be thus secured.

With relation to the city of Washington, it was suggested that the Washington monument would afford a good opportunity (by placing illuminated fly-traps at different elevations on its exterior) for ascertaining the height at which mosquitoes fly, or are brought by the wind from the adjacent Potomac flats. The proposed reclamation of the flats could scarcely do more than mitigate malarial disease, so long as our summer and autumn southern breezes come, laden with mosquitoes, from the miles of unreclaimed swamps farther down the river, as at Four-mile Run and other nearer localities.

Mr. BILLINGS remarked that, since ague did not invariably result from insect bites, the most that could be claimed was that they accomplished an accidental inoculation with malarial poison.

The subject was also discussed by Messrs. DOOLITTLE, TONER, and ANTISELL.

The meeting closed with an exhibition by Mr. C. E. DUTTON of a series of oil paintings illustrative of the Hawaiian Islands.

230TH MEETING.

FEBRUARY 24, 1883.

Vice-President BILLINGS in the Chair.

Thirty members and visitors present.

The Chair announced the election of Mr. THOMAS RUSSELL to membership.

The first communication was by Mr. G. K. GILBERT on

THE RESPONSE OF TERRESTRIAL CLIMATE TO SECULAR VARIATIONS
IN SOLAR RADIATION.

[Abstract.]

Secular variations of climate may theoretically be caused (1) by the internal heat of the earth and (2) by changes in the constitution or volume of the atmosphere. They have unquestionably been wrought (3) by changes in the limits and configuration of ocean bottoms and land surfaces, (4) by changes in the movements of the earth with reference to celestial bodies, and (5) by variations of

solar radiation. Attention will here be restricted to the last-mentioned cause.

An augmentation of the strength of solar radiation (*a*) will cause a general rise in the temperature of the atmosphere, (*b*) will heighten the contrast between warm and cold regions, thereby stimulating oceanic and atmospheric circulation, and (*c*) will heighten the contrast between wet and dry regions, making the wet wetter and the dry drier. (*d*) It will also diminish glaciation. This has been disputed by some writers, but is sustained by a quantitative discussion. A computation, based on the annual curves of precipitation and temperature at St. Bernard, close to the glaciers of the Alps, shows that a general rise in the temperature of the air, while it will increase the total precipitation, will slightly diminish the snow-fall; that it will very greatly increase the rate of melting. The ratio of snow-fall to evaporation is reduced one-half by 6° C rise of temperature; the ratio of snow-fall to melting is reduced one-half by a rise of $1\frac{1}{2}^{\circ}$; and, assuming that evaporation actually dissipates twice as much snow as does melting, the ratio of snow-fall to snow dissipation (or the tendency to glaciation) is reduced one-half by $4\frac{1}{2}^{\circ}$ rise of temperature.*

(*e*) Increase of solar radiation will also, through its general effects, influence the distribution of winds, and thus produce secondary effects of a local nature.

Mr. DALL remarked that ice was rendered more plastic and fluent by the presence of water; so that the movement of ice and the consequent extent of glaciers are favored by rain. If Mr. Gilbert by the term "glaciation" referred to the *extent* of glaciers, some limitation of his conclusions might be necessary.

Other remarks were made by Messrs. ANTISELL, DOOLITTLE, H. FARQUHAR, and ELLIOTT.

The next communication was by Mr. J. W. CHICKERING ON

THE THERMAL BELTS OF NORTH CAROLINA.

[Abstract.]

In the agricultural volume of the Patent Office Report for 1861 is an article written by Mr. Silas McDowell, of Franklin, Macon county, N. C., bearing this title. He was a man of much intelli-

* The computation is given in full in "Science" for March 16, 1883.

gence, an enthusiastic student in geology and botany, a companion and guide of several botanists in their early explorations of the southern Appalachians, and a farmer by profession. He died in 1882, at the ripe old age of 87.

He states that in the valley of the Little Tennessee river, in Macon county, lying about 2,000 feet above tide water, when the thermometer in the morning indicates a temperature of about 26°, the frost line extends about 300 feet in vertical height, but that then comes a belt extending about 400 feet in vertical height up the mountain side, within which no frost is seen, delicate plants remaining untouched. Above this, frost again appears. So sharp is the dividing line that sometimes one-half of a shrub may be frost killed, while the other half is unaffected.

A small river, having its source in a high plateau 1,900 feet above this, runs down into this valley, breaking through three mountain barriers, and consequently making three short valleys, including the plateau, rising one above the other, each of which has its own vernal zone, traversing the hillsides that enclose it, and each beginning at a lesser elevation above the valley, as the valleys mount higher in the atmosphere, so that around the plateau, a beautiful level height, containing 6,000 acres of land, and lying 3,900 feet above tide water, the lower edge of the thermal belt is not more than 100 feet above the common level of the plateau.

Not only does vegetation within this zone remain untouched by frost, so that the Isabella, the most tender of all the native grapes, has not failed to produce abundant crops in twenty-six consecutive years, but mildew, blight, and rust, which often attack vines in the lower valleys, are here unknown, while the same purity and dryness of the air which favor the grape, make this a refuge for the consumptive, as diseases of the lungs have never been known to originate among the inhabitants.

Mr. McDowell adds: "The thermal belt must exist in all countries that are traversed by high mountains and deep valleys, and the only reason why its visible manifestations are peculiar to our southern Alleghanies, is the fact that their precocious spring vegetation is sometimes killed by frost, while the same thing does not happen in the mountains further north."

These statements are corroborated by similar testimony respecting another such belt along the Tryon mountain range in Polk county, N. C.; the specific claim being that such a belt is found

for eight miles in length, extending from 1,200 feet to 2,200 feet above tide water, within which the leaves of plants, shrubs, and flowers remain untouched by frost until the latter part of December, and after a snow storm not a particle of snow remains within the belt, while the tops and sides of the mountains above and the valleys below will be covered.

The verification of these alleged facts would be matters of interest in their economical and sanitary aspects, and would supply data for some interesting researches respecting the nocturnal stratification of the atmosphere.

It is earnestly to be hoped that at some time we may have reliable and continuous thermometrical observations at these and similar stations, to determine the existence, extent, and temperature of such belts.

Remarks were made on this communication by Mr. ALVORD.

Mr. C. E. DUTTON then made a communication on the

GEOLOGY OF THE HAWAIIAN ISLANDS.

[Abstract.]

On the slopes of Mauna Loa are sea beaches, terraces, coral sands, and other evidences of shore action at various levels. The highest that can be positively announced has an altitude of 2,800 feet above the ocean. It can be traced a large part of the way around the island, being discernible even when covered by more recent lava. It does not now lie horizontal, but descends from 2,800 to 400 feet, while on the adjoining island, Maui, there is evidence of submergence. On the farther (western) side of Maui, and on other islands beyond, there is again evidence of upheaval.

All the lavas of the islands are basaltic. Those of Mauna Loa and Kilauea are abnormally basic and are related to certain lavas of New Zealand, called by Mr. Judd "ultra-basalts." The New Zealand rock consists chiefly of olivine; that of Mauna Loa is sometimes more than half olivine, and contains much magnetite and hematite. A Greenland lava, classed also as ultra-basalt, contains the only known native iron of telluric origin. As this suggests the iron meteorites, so the basalts of New Zealand and Mauna Loa suggest the stony meteorites.

The volume of the eruptions of Mauna Loa is enormous; that of 1855 would nearly build Vesuvius, and two of prehistoric date

were greater still. The lava has a high liquidity and flows forty to fifty-five miles, spreading at the base of the cone into a broad sheet. There are no explosive phenomena and no fragmental products. The slope of the mountain is 4° along the major and 7° along the minor axis. Kilauea has a few cinder cones on its flanks. Mauna Kea consists chiefly of them, and has an average slope of $7\frac{1}{2}^{\circ}$ to 11° .

Kilauea is always active, maintaining lakes of liquid fire. Over one of these a crust is formed, black, but flexible, which after a while breaks up and suddenly sinks, the process being repeated at intervals of $1\frac{1}{2}$ to $2\frac{1}{4}$ hours. The great interior pit described by observers from 1823 to 1841 is now filled.

Mauna Loa is not active more than one-third or one-fourth of the time, but compensates by the magnificence of its phenomena. Great fountains of lava are projected hundreds of feet into the air.

Mr. Dutton's communication was interrupted by the arrival of the hour for adjournment. In response to a question by Mr. TAYLOR, he stated that the crust over a lava lake acquired a thickness of five or six inches before breaking up.

Mr. ANTISELL inquired whether there is any basalt on the islands, and Mr. Dutton explained that they are composed exclusively of that material.

231ST MEETING.

MARCH 10, 1883.

Vice-President WELLING in the Chair.

Thirty-four members and visitors present.

The Chair announced that Messrs. ALBERT WILLIAMS, Jr., JOHN HENRY RENSHAW, and HENRY FRANCIS WALLING had been elected to membership.

Mr. M. H. DOOLITTLE read a communication on

SUBSTANCE, MATTER, MOTION, AND FORCE,

which was discussed by Messrs. W. B. TAYLOR, ELLIOTT, HARNESSESS, and WELLING.

Mr. E. B. ELLIOTT then communicated

FORMULAS FOR THE COMPUTATION OF EASTER.

In the calendar the vernal equinox is considered as invariably occurring on the 21st of March.

The Paschal full moon is the full moon which (according to the calendar) occurs on or first after the 21st of March.

Easter Sunday in any year is the first Sunday which occurs *after* the Paschal full moon; that is, first after the full moon which, according to the calendar, occurs *on or first after* March 21st.

To find the date of Easter Sunday for any year, A. D., New Style.

Let c denote the complete hundreds of years in the number denoting any year, and y the number of remaining years. Thus in the year 1883, $c = 18$ and $y = 83$, the number for the entire year, 1883, being denoted by $100 c + y$.

In the following formulas w , as a subscript after a division, denotes that only the whole number of the quotient is to be retained, and r , as a subscript, denotes that only the remainder after the division is to be retained; thus $\left(\frac{18}{4}\right)_w = 4$; and $\left(\frac{18}{4}\right)_r = 2$.

$$\begin{aligned} & n \text{ (the golden number less one)} \\ = & \left(\frac{\text{year}}{19}\right)_r = \left(\frac{100 c + y}{19}\right)_r = \left(\frac{5 c + y}{19}\right)_r = \left(\frac{5 c + y}{20 - 1}\right)_r \\ & = \frac{1}{19} \left[5 \left(\frac{c}{19}\right)_r + \left(\frac{y}{19}\right)_r \right]_r \end{aligned}$$

This number (n) pertains to a lunar cycle of 19 years.

$$s = \overline{c - 8} - \left(\frac{c}{4}\right)_w - \left(\frac{c + 1 - \left(\frac{c + 8}{25}\right)_w}{3}\right)_w$$

Inspection of the formula for s will show that, for any year from 1700 A. D. New Style to 1899 A. D., both inclusive, the value of s is zero (0). For any year Old Style the value of s is the constant number 22.

$$\begin{aligned} q & = \left(\frac{23 + s + 19 n}{30}\right)_r ; \text{ also,} \\ & = \left(\frac{23 + s - 11 n}{30}\right)_r \\ h & = \left(\frac{q}{29}\right)_w + \overline{29 - q} \left(\frac{q}{28}\right)_w \left(\frac{n}{11}\right)_w \end{aligned}$$

The value of h may be shown to be zero (0) for any year from 1700 A. D. to 1899 A. D., both inclusive, during New Style, and for all years during Old Style.

$p = q - h$ = the interval in days from March 21st to the date of the Paschal full moon, or the number of days to be added to March 21st to find the date of the Paschal full moon.

If $p =$ zero (0), the Paschal full moon accordingly falls on the 21st of March.

$$L = \left(\frac{1 + 2 \left(\frac{c}{4} \right)_r - y - \left(\frac{y}{4} \right)_w + \left(\frac{c}{40} \right)_w}{7} \right)_r$$

L denotes the number (in alphabetical order) of the Dominical or Sunday letter. Thus, the number corresponding to the Dominical letter A is 1, to B is 2, to C is 3, to D is 4, to E is 5, to F is 6, and to G is 7 or 0 (zero).

The term $\left(\frac{c}{40} \right)_w$ gives a correction to the Gregorian value when the year exceeds 4000 A. D.; for any year less than 4000 the value of this corrective term is obviously zero (0).

$$t - 1 = \left(\frac{3 - p + L}{7} \right)_r = \left(\frac{3 + 6p + L}{7} \right)_r$$

t denotes the number of days which elapse after the date of the Paschal full moon to the date of Easter Sunday.

$$\begin{aligned} \text{Easter Sunday} &= \text{March } (21 + 1 + p + \overline{t - 1}) \\ &= \text{March } (21 + p + t) \\ &= \text{April } (p + t - 10) \end{aligned}$$

To find the date of Easter Sunday for any year, A. D., Old Style.

$$n = \left(\frac{\text{year}}{19} \right)_r = \left(\frac{100c + y}{19} \right)_r$$

The formula for n is the same as in New Style.

$$q = p = \left(\frac{23 + 22 + 19n}{30} \right)_r = \left(\frac{15 + 19n}{30} \right)_r = \left(\frac{15 - 11n}{30} \right)_r$$

$$L = \left(\frac{3 + c - y - \left(\frac{y}{4} \right)_w}{7} \right)_r$$

$$t - 1 = \left(\frac{3 - p + L}{7} \right)_r = \left(\frac{3 + 6p + L}{7} \right)_r$$

$$\begin{aligned} \text{Easter Sunday} &= \text{March } (21 + 1 + p + \overline{t-1}) \\ &= \text{March } (21 + p + t) \\ &= \text{April } (p + t - 10) \end{aligned}$$

EXAMPLE 1.—Required the day of the month on which Easter Sunday falls in the year 1883 A. D., New Style.

$$n = \left(\frac{5c+y}{19}\right)_r = 5 \left(\frac{c}{19}\right)_r + \left(\frac{y}{19}\right)_r$$

$$\left(\frac{18}{19}\right)_r = 18 \text{ or } -1; \quad 5 \left(\frac{18}{19}\right)_r = 90 \text{ or } -5$$

$$\left(\frac{83}{19}\right)_r = \left(\frac{4 \times 19 + 7}{19}\right) = 7$$

$$n = -5 + 7 = 2$$

$$20n = 40$$

$$19n = 20n - n = 38$$

$$s = \overline{18} - 8 - \left(\frac{18}{4}\right)_w - \left(\frac{18 + 1 - \left(\frac{18+8}{25}\right)_w}{3}\right)_w$$

$$= 10 - 4 - \left(\frac{19-1}{3}\right)_w = 10 - 4 - 6 = 0$$

$$q = \left(\frac{23+s+19n}{30}\right)_r = \left(\frac{23+0+38}{30}\right)_r = 1$$

$$h = \left(\frac{1}{29}\right)_w + \overline{29-1} \left(\frac{1}{28}\right)_w \left(\frac{2}{11}\right)_w = 0 + 28 \times 0 \times 0 = 0 + 0 = 0$$

$$p = q - h = 1 - 0 = 1$$

$$L = \left(\frac{1 + 2 \left(\frac{18}{4}\right)_r - 83 - \left(\frac{83}{4}\right)_w + \left(\frac{18}{40}\right)_w}{7}\right)_r$$

$$= \left(\frac{1 + \overline{2 \times 2} - 83 - 20 + 0}{7}\right)_r = \left(\frac{1 + 4 - 6 - 6}{7}\right)_r = 0$$

$$t - 1 = \left(\frac{3 - p + L}{7}\right)_r = \left(\frac{3 - 1 + 0}{7}\right)_r = 2$$

$$\begin{aligned} \text{Easter Sunday} &= \text{March } (21 + 1 + p + \overline{t-1}) \\ &= \text{March } (22 + 1 + 2) \\ &= \text{March } 25 \end{aligned}$$

EXAMPLE 2.—Required the date of Easter Sunday for the year 1884
A. D., New Style.

$$5 \left(\frac{18}{19} \right)_r = -5$$

$$\left(\frac{84}{19} \right)_r = 8$$

$$n = 8 - 5 = 3$$

$$20n = 60$$

$$20 - n = 19n = 57$$

$$s = 0$$

$$q = \left(\frac{23 + 0 + 57}{30} \right)_r = 20$$

$$h = \left(\frac{20}{29} \right)_w + \overline{29 - 20} \left(\frac{20}{28} \right)_w \left(\frac{3}{11} \right)_w$$

$$= 0 + 9 \times 0 \times 0 = 0 + 0 = 0$$

$$p = q - h = 20 - 0 = 20$$

$$L = \left(\frac{1 + 2 \left(\frac{18}{4} \right)_r - 84 - \left(\frac{84}{4} \right)_w + \left(\frac{18}{40} \right)_w}{7} \right)_r$$

$$= \left(\frac{1 + 4 - 0 - 0 + 0}{7} \right)_r = 5$$

$$t - 1 = \left(\frac{3 - 20 + 5}{7} \right)_r = \left(\frac{8 - 6}{7} \right)_r = 2$$

$$\begin{aligned} \text{Easter Sunday} &= \text{March } (21 + 1 + 20 + 2) \\ &= \text{March } 44 \\ &= \text{April } (44 - 31) \\ &= \text{April } 13 \end{aligned}$$

EXAMPLE 3.—Required date of Easter Sunday for the year 3966
A. D., New Style.

$$2 \times 19 = \begin{array}{r} 39 \mid 66 \\ 38 \mid 57 \\ \hline 1 \mid 9 \end{array} = 3 \times 19$$

$$n = \left(\frac{5c + y}{19} \right)_r = \left(\frac{5 \times 1 + 9}{19} \right)_r = 14$$

$$20n = 280$$

$$19n = 20n - n = 266$$

$$s = \overline{39 - 8} - \left(\frac{39}{4}\right)_w - \left(\frac{\overline{39 + 1} - \left(\frac{39 + 8}{25}\right)_w}{3}\right)_w$$

$$= 31 - 9 - \left(\frac{40 - 1}{3}\right)_w = 31 - 9 - 13 = 9$$

$$q = \left(\frac{23 + s + 19n}{30}\right)_r = \left(\frac{23 + 9 + 266}{30}\right)_r = 28$$

$$= h \left(\frac{28}{29}\right)_w + \overline{29 - 28} \left(\frac{28}{28}\right)_w \left(\frac{14}{11}\right)_w$$

$$= 0 + 1 \times 1 \times 1 = 0 + 1 = 1$$

$$p = q - h = 28 - 1 = 27$$

$$L = \left(\frac{1 + 2 \left(\frac{39}{4}\right)_r - 66 - \left(\frac{66}{4}\right)_w + \left(\frac{39}{40}\right)_w}{7}\right)_r$$

$$= \left(\frac{1 + 2 \times 3 - 3 - 2 + 0}{7}\right)_r = 2$$

$$t - 1 = \left(\frac{3 - p + L}{7}\right)_r = \left(\frac{3 - 27 + 2}{7}\right)_r = 6$$

$$\text{Easter Sunday} = \text{March } (21 + 1 + 27 + 6)$$

$$= \text{March } 55$$

$$= \text{April } (55 - 31 =) 24$$

EXAMPLE 4.—Required the date of the Paschal full moon (March $\overline{21 + p}$), and the date of Easter Sunday (March $\overline{21 + p + t}$ or March $\overline{21 + 1 + p + (t - 1)}$) for the year 2152 A. D., New Style.

$$\left(\frac{2152}{19}\right)_r = 5 = n$$

$$19n = 95$$

$$s = 1$$

$$23 = 23$$

$$19n + s + 23 = 119$$

$$q = \left(\frac{19n + s + 23}{30}\right)_r = \left(\frac{119}{30}\right)_r = 29$$

$$h = 1 + \overline{0 \times 0 \times 0} = 1$$

$$p = q - h = 28$$

Paschal full moon = March (21 + 28 =) 49

= April (49 - 31 =) 18

$$L = \left(\frac{1 + 2 \left(\frac{21}{4} \right)_r - 52 - \left(\frac{52}{4} \right)_w + \left(\frac{21}{40} \right)_w}{7} \right)_r$$

$$= \left(\frac{1 + 2 \times 1 - 52 - 13 + 0}{7} \right)_r$$

$$= \left(\frac{1 + 2 + 0 - 3 - 6}{7} \right)_r = \left(\frac{3 - 2}{7} \right)_r = 1$$

$$t - 1 = \left(\frac{3 - 28 + 1}{7} \right)_r = 4$$

Easter Sunday = March (21 + 1 + 28 + 4 =) 54

= April (54 - 31 =) 23

The Julian or Old Style Calendar was established by the Council of Nice A. D. 325; the first year of the Gregorian or reformed calendar was A. D. 1582, and the first year in which the reformed calendar was adopted in England was A. D. 1752.

In Russia, and in other countries where the religion of the Greek Church now obtains, the New Style of reckoning has *not* been adopted, but the Old Style is still in force.

In Alaska, Old Style was employed until after the cession of that country by Russia to the United States in the year 1869.

EXAMPLE 5.—*Find the date of Easter Sunday for the year 1582 A. D., Old Style.*

$$\begin{array}{r|l} 15 & 82 \\ 5 + 15 & = 75 \\ 20 - 1) & 157 \quad (7 \\ & \underline{140 - 7} \\ & 17 + 7 = 24 = 19 + 5 \\ & n = 5 \end{array}$$

$$19n = (20 - 1)n = 100 - 5 = 95 = 3 \times 30 + 5$$

$$q = \left(\frac{19n + 15}{30} \right)_r = \left(\frac{5 + 15}{30} \right)_r = 20$$

$$L = \left(\frac{3 + 15 - 82 - 20}{7} \right)_r$$

$$= \left(\frac{18 - 5 - 6}{7} \right)_r = \left(\frac{18 - 11}{7} \right)_r = 0$$

$$t - 1 = \left(\frac{3 - 20 + 0}{7} \right)_r = 4$$

Easter Sunday = March (22 + 20 + 4 =) 46
 = April (46 - 31 =) 15

232D MEETING.

MARCH 24, 1883.

Vice-President WELLING in the Chair.

Forty-three members and visitors present.

The first communication was by Mr. J. R. EASTMAN ON

THE FLORIDA EXPEDITION FOR OBSERVATION OF THE TRANSIT
 OF VENUS.

[Abstract.]

The observing station of the Florida expedition was upon Way Key, the largest of the group of islands known as Cedar Keys.

The principal instruments employed were a portable transit, a five-inch equatorial telescope, and a photoheliograph. The first two require no description. The photoheliograph consisted of an objective of five inches aperture and about forty feet focus, a heliostat for throwing the sun's rays on the objective, and a plate holder at the focus of the objective. The accessory apparatus consisted of a measuring rod, permanently mounted, for accurately measuring the distance from the objective to the photograph plate; a movable slide with a slit of adjustable width, for exposing the plates; and a circuit connecting with a chronograph, so arranged that when the exposing slide was moved to expose the plate, and when the center of the slit was opposite the center of the plate-holder, the circuit was broken and the record made on the chronograph. A black disk was painted on one side of the slide, and so placed that when the slide was at rest at one end of its course and the image of the sun was adjusted concentric with this disk, it would fall on the center of the plate-holder when the slide was moved. The adjustments having been completed the exposing of the plates was a simple matter. The image of the sun was thrown by the heliostat upon the black disk and centered, the sensitive plate was fixed in

the plate-holder, the operator moved the exposing slide, and the time of exposure was recorded on the chronograph.

For observing contacts I used an eye piece, magnifying 216 diameters, attached to a Herschel solar prism, and a sliding shade-glass with a density varying uniformly from end to end. The time of my signals was taken by assistant astronomer Lieut. J. A. Norris, U. S. N., from a chronometer; while, with an observing key, I also made a record on the chronograph as a check.

About 40 seconds before the computed time of first contact a narrow stratus cloud passed on to the southeastern edge of the sun and shut out all the light. The cloud remained about 3 minutes, and when it passed off, the notch in the sun's limb was plainly marked. Two photographs were taken to test the apparatus and the plates, and then the time before *second* contact was devoted to an examination of the limbs of Venus and the sun. Both were perfectly steady. In observations of the sun for the last twenty years I never saw it better. At about 13 minutes after first contact the outline of the entire disk of Venus could be seen, and seemed perfectly circular. About 2 minutes later a faint, thin rim of yellowish light appeared around the limb yet outside the sun. This rim was at first broadest near the sun's limb, but soon the width of the light became uniform throughout. The light was wholly exterior to the limb of Venus; that is, the black limb of Venus on the sun and the dark limb outside formed a perfectly circular disk, with the rim of light or halo, outside the portion off the sun. As the time of second contact approached, Lieutenant Norris again took up his station at the chronometer. As the limbs neared geometrical contact, the cusps of sunlight began to close around Venus more rapidly; and the perfect definition of the limbs and the steady, deliberate, but uniformly increasing motion of the cusps, convinced me instantly that the phenomena attending the contact would be far more simple than I had ever imagined. I had only to look steadily to see the cusps steadily but rapidly extend themselves into the thinnest visible thread of light around the following limb of Venus and remain there without a tremor or pulsation. At the moment the cusps joined I gave the signal and also made the record on the chronograph. Still keeping my eye at the telescope, I saw nothing to note save the gradually increasing line of light between the limbs of the two bodies. The disk of Venus on the sun was black.

A re-examination was then made of all the photographic apparatus, and about 10 minutes after the second contact the principal photographic work was commenced; and this was continued with slight interruption until about 10 minutes before third contact; 150 dry plates and 30 wet ones being exposed. One of the interruptions was for the purpose of making measurements of the diameter of Venus, which was done with a double-image micrometer attached to the 5-inch telescope.

On going to the telescope to observe the last contacts, I found the limbs of Venus and the sun as steady as in the morning, and though there was now some haze over the sun it did no harm. The third contact was observed with great accuracy, nothing occurring to obstruct or complicate the very simple and definite phenomena, which were in the reverse order of those seen at second contact. The rim of light appeared around Venus as soon as the limb was visible beyond the sun, and was seen for nearly 10 minutes. The complete outline of Venus was visible for 2 minutes longer. No phenomena worthy of note were seen between third and fourth contacts. The lapping of the limb of Venus over that of the sun gradually but steadily decreased until the final separation, which was observed with great accuracy for such a phenomenon. Soon after the last contact the entire apparatus was again carefully examined and the necessary observations made to determine the errors of the chronometers.

In the observations of interior contacts there was no trace of any tremor or fluctuation of the light in the cusps as they closed around the limb of Venus; and it is almost needless to say that there was no trace of a shadow or a black drop or ligament between the limbs at second and third contacts. The probable error for the second and third contacts was estimated at $0''.3$; for fourth contact, $0''.5$.

Observers of transits of Venus and Mercury have written so much in regard to the obstacles encountered from the apparition of the shadow, or black drop, between the limbs of the two bodies at *second* and *third* contacts, and so full has been the testimony in favor of the existence and the almost necessary occurrence of this phenomenon, that at the transit of Mercury, in 1878, many observers claimed, as evidence of their skill, that they *did* see it; while others, less fortunate, apologized for *not* seeing it. Observers of the black drop were so generally confined to those with imperfect

apparatus or to those unaccustomed to observation of the sun's limb or disk that the true nature of the obstacle was pretty well understood before it was carefully investigated. It is now quite well settled that the "black drop" is due to bad eyes, imperfect apparatus, or the inexperience of the observer. With good eyes and proper apparatus a good observer never should see the black drop. When it is seen there is something wrong; it is a spurious phenomenon.

One of the negatives was exhibited to the Society.

In reply to a question by Mr. E. J. FARQUHAR, Mr. EASTMAN said the halo about Venus was believed to be due to the atmosphere of the planet.

The next communication was by Mr. CLEVELAND ABBE on

DETERMINING THE TEMPERATURE OF THE AIR.

He stated that the question now to be considered is not where to place a thermometer so as to obtain the temperature most proper for the use of the meteorologist, but is rather the purely physical question of how to determine the temperature of the air at any given location. He described the methods and defects of the former and present meteorological methods of exposure, viz: (1) Thermometers hung in the open air. (2) Those placed in shady locations. (3) The Glaisher screen. (4) The Stevenson screen and the double louvre screens in general. (5) The double metallic cylindrical shelters of Jelinek and Wild. (6) The silver thimble screen of Regnault. (7) The whirling thermometer of Saussure, Arago, Bravais, and the French observers (exhibiting Babinet's arrangement as made by Casella.) (8) Joule's method, depending on a balance in the temperature and density of two columns of the air.

He then gave a description of the method devised by him in 1865 and used for a short time at Poulkova; this consisted in constructing a very perfect louvre screen, within which were established black bulb and bright or silvered bulb thermometers having very diverse coefficients of radiation and conduction. These thermometers were in air, not *in vacuo*, as this latter arrangement was proper only for the determination of the direct solar radiation, as in the Arago-Davy method, whereas in the present case the temperature of the air and the radiation from terrestrial objects were the special objects of study.

The air temperature (t_a) was found from the indications of the bright and black bulbs (t_s and t_b) by the empirical formula

$$t_a = t_s + C (t_b - t_s)$$

where C is a small coefficient, to be determined experimentally, and is nearly constant. This arrangement of bright and black bulbs can be used by meteorologists and physicists without a screen, and even in the sunlight, if the theory of the action of the bright and black bulbs is perfectly understood. A similar formula will give the temperature (T) of a single radiating body whose effect is equal to the total effect that is shown by the black bulb :

$$T = t_b + C' (t_b - t_s)$$

He then stated that the theoretical basis of this method has quite recently been further elucidated by Professor Ferrel, who has shown that the approximate nature of the relation between the above constant C , the radiating, absorbing, and conducting powers of the thermometers, and the velocity of the wind is given by the following equation :

$$C = \frac{1 + \frac{Br_b}{B' + B''v}}{\frac{r_b}{r_s} - 1}$$

where r_b and r_s are the radiating (and absorbing) powers of the blackened and silvered bulbs, respectively, v is the velocity of the wind or currents flowing past the bulbs, and $B B' B''$ are constant coefficients depending on the size, conductivity, and specific heat of the substance of the bulbs.

In reply to a question of Mr. GILBERT, he stated that the difference between the bright and black bulbs had rarely exceeded a few tenths of a degree in the delicate shelter made of oiled paper, as used by him at Poulkova, the maximum occurring February 22, 1866, at 10 a. m., when, the louvre box being in the full sunshine, the bright bulb was at $14^{\circ}.9$ Cent. and the black bulb at $14^{\circ}.3$, showing that the latter had been slightly warmed by the warm sides of the box.

In reply to a question of Mr. HARKNESS, the author explained, that although it was conducive to accuracy that these thermometers should be placed within a shelter, yet this was not necessary; if we take advantage of the more accurate method of determining

the co-efficient constant C , as given by Prof. Ferrel's theory, the two thermometers placed anywhere within doors or without would still give data for determining temperatures of the location; it should be borne in mind that the temperature thus obtained belongs specifically to the air in contact with the thermometers and is not an average value for any extensive portion of the atmosphere. As it is an advantage to conduct observations under uniform conditions, it is recommended that a pair of bright and black bulb thermometers be attached to the whirling table, whereby the effect of a current of air may be on the one hand determined and on the other hand kept as uniform as possible.

Mr. HARKNESS said that the object practically sought by meteorologists was to learn the average temperature of a considerable body of air, but their efforts were thwarted by the irregularity and inconstancy of the distribution of temperature. So long as the air in contact with the thermometer is not precisely representative of the air of the vicinage it was useless to refine methods of observation, unless by that refinement errors of a constant nature were eliminated. For the determination of mean monthly or annual temperatures he considered the reading of the nearest half degree as sufficient, and regarded the reading of the tenths of a degree as a useless refinement.

The advantage of reading to tenths was further discussed by Messrs. ABBE, DOOLITTLE, and KUMMELL. Mr. KUMMELL pointed out that where a difference of temperature is observed as an indication of the moisture of the air, the tenths are worthy of record.

The following communication by Prof. CHARLES E. MUNROE, of Annapolis, Md., was then read by the Secretary :

DETERMINATION OF THE SPECIFIC GRAVITY OF SOLIDS BY THE
COMMON HYDROMETER.

Having occasion some time since to devise methods for the examination of coal on board ship, I was obliged, as my first consideration, to work with such materials and apparatus as are usually found in ships' stores, and then to arrange the methods so that they could be used under the restricted conditions which prevail. The unsteadiness of the ship makes balance methods for the determination of specific gravities difficult, even when a suitable balance is at

hand, while hydrometers may be steadied so that the instrument may be read with a reasonable degree of precision, as is shown in its constant use in the determination of the degree of saturation of the water in the steam-boiler, and in other instances.

To use the hydrometer for the determination of the specific gravities of solids I take advantage of the fact that, when a body floats in a liquid in which it is wholly immersed, the specific gravities of the liquid and the solid are the same, and we have simply to determine the value for one of them.

The process is carried out by taking a dense solution, dropping in it the solid to be determined, (which must be light enough to float on the surface,) and then diluting slowly with water until the solid floats immersed, stirring the mixture constantly. The solid is now removed and the hydrometer inserted and read. For the determination of the specific gravities of the bituminous coals and lignites a thick solution of cane sugar was used, while for the heavier anthracite concentrated sulphuric acid, diluted with dilute sulphuric acid, was employed. The increase in temperature in the latter case causes no appreciable error if the reading is quickly taken. The following results were obtained by the method described, the specific gravity of each specimen having first been determined by Jolly's balance:

	By Jolly's balance.	By mixture.
Anthracite -----	1,5640	1,560
Bituminous coal -----	1,3008	1,310
Bituminous coal -----	1,3000	1,300
Gas coal -----	1,2790	1,285
Cannel coal (ligniform) -----	1,1550	1,155
Cannel coal -----	1,1292	1,120
Lignite -----	1,0909	1,090

Mr. DUTTON remarked that the same principle had recently been successfully applied to the separation of the component minerals of crystalline rocks. A sample is powdered and then placed in a very heavy liquid (a solution of mercuric iodide and potassium iodide), the density of which is gradually diminished, until the particles of the heaviest mineral sink to the bottom. A repetition of the process eliminates each mineral in turn.

233D MEETING.

APRIL 7, 1883.

Mr. WM. H. DALL in the Chair.

Thirty-six members and visitors present.

The Chair announced that Messrs. EDWARD SANDFORD BURGESS and SUMNER HOMER BODFISH had been elected members.

The General Committee reported to the Society that "a Mathematical Section had been organized by the election of Mr. ASAPH HALL as Chairman and Mr. HENRY FARQUHAR as Secretary. All members of the Society who are interested in mathematics are invited to attend and take part in its meetings, announcements of which will be sent to those who notify the Secretary of a desire for them."

The first communication was by Prof. W. C. KERR on

THE GEOLOGY OF HATTERAS AND THE NEIGHBORING COAST.

[Abstract.]

The notable projection of Hatteras, beyond the general line of trend of the Atlantic coast, has, of course, a geological origin. The study of the changes now taking place, and of the phenomena which have left their recent traces on the surface, readily furnish the data for the solution of the problem. Nearly one-half of this eastern inter-sound region of North Carolina is water surface, and the land surface lies for the most part below ten feet (much of it below five.)

A large part of this low-lying surface is covered with beds of peat, which thicken towards the centre on the divides or swells between the bays and sounds, rising, in some cases, to ten and fifteen feet, and in the Dismal Swamp on the northern border of the State to twenty-two feet. These beds of peat are in process of forming by the decay of plants growing on the surface, chiefly cypress and juniper. Many tiers of the undecayed logs of these timbers are piled upon one another through the whole thickness of the deposit, which is soft and yielding, so that a fence-rail may be thrust down beyond its length. Vast tracts of such peat swamps (and of marsh and savanna on which only water grasses and small shrubs and scrub pines grow and decay) are found throughout this coast region. Here we have the first stage in the formation of a coal bed. Another notable fact is that many of the rivers which empty into the sounds

increase in depth of channel at a distance from their mouths; while the sounds are 12 to 15 and 20 to 22 feet deep, the rivers are often 30 and 40 feet and upwards. This can only be accounted for by supposing a subsidence of the region to be in progress, the sounds and open bays being silted up by the deposits brought down by the floods of the Roanoake and other large rivers, while no particle of sediment can reach the sheltered depths of the narrow windings of the upper reaches of these minor streams. This theory of subsidence is abundantly confirmed by the disappearance under water of large tracts of swamp bordering the rivers, as the Chowan, within the observation of men now living, and by the existence of rooted stumps of cypress and juniper in the bottom of the bays and sounds, even to the depth of 15 and 20 feet, and also by the vertical and crumbling shores of the sounds, undermined and eroded by the advancing waves.

The Atlantic ocean is walled off from this region by a narrow fringe of sand islands, or dunes, blown shoreward by the wind and thrown up into reefs and hillocks like snow-drifts 50, 80, and even more than 100 feet high. The movement of these sand waves being inland, the sounds are silting up next the sea, and are in many places converted into marshes 3 to 5 miles wide. The reef is increasing in continuity and breadth, most of the inlets above Hatteras that were open 300 years ago being closed and obliterated. An inspection of the form of the curves of the submarine contours off Hatteras and adjoining coasts will show that the action of the tides and ocean currents, the Gulf stream and Arctic current meeting at this point, accumulate upon Hatteras the river silt which reaches the sea by way of the Chesapeake as well as that of the rivers which discharge their burdens through the inlets about this point and southwards. Which amounts to this—that Hatteras may be described as a sort of *delta*, whose materials are derived from the drainage of more than 100,000 square miles of the Atlantic slope.

A subsidence of about 20 feet would bring the sea again over the entire Sound region and carry the shore 75 miles inland, bringing Hatteras to coincide with Cape Lookout. A sand reef, like that north of Hatteras, marks the line of the ancient shore, when these conditions obtained. A depression of fifty feet would move the shore 100 miles west of Hatteras and carry the point of meeting of the conflicting ocean currents and waves to Cape Fear. A subsidence of 500 feet, as in the glacial period, would carry

Hatteras more than 200 miles west of its present position. This horizon is marked by an immense sand reef, still retaining its wind and wave marks, and rising to a height of more than 500 feet above tide, the reef itself being at least 100 feet deep and many miles in length. The sea must have remained at this level for a very long period.

But Hatteras is not a modern phenomenon. It is at least as old as the cretaceous; the quaternary as well as the tertiary of this coast region of North Carolina are laid down upon an eroded surface of cretaceous rock, while the artesian borings, at Charleston, reach this formation at 700 feet, and at the mouth of the Chesapeake they do not seem to have touched it at 1,000 feet.

Mr. WARD remarked that, in traversing the Jericho canal of the Dismal Swamp in a row boat, he had observed an outward flow at both ends of the canal, showing that, by continuous water passage, a divide was crossed between Lake Drummond and the James river.

He criticised the doctrine taught in text-books and popular writings that the preservation of leaves in a fossil state is due ordinarily to river action and delta formation. More favorable conditions are to be found in swamps.

Other remarks were made by Messrs. DUTTON and HOUGH.

The second communication was by Mr. H. F. WALLING on

TOPOGRAPHICAL INDICATIONS OF A FAULT NEAR HARPER'S FERRY.

[Abstract.]

A description was given of a break in the continuity of the Blue Ridge, where its disconnected portions, extending side by side for a few miles, are cut by the Potomac river, near Harper's Ferry, the gorges so formed presenting a striking feature of the scenery.

The two ridges, here about 12,000 feet apart, stretch for hundreds of miles in nearly parallel directions, one to the south and the other to the north; the latter being known in Pennsylvania as the South Mountain. The strike of the rocks is parallel to the ridges, about N. 30° E., and the prevailing dip is eastward; averaging not more than 30°. The ridges are composed of hard sand-rock; the adjacent region, of lime-stone and other rocks more easily disintegrated or dissolved.

Supposing the sand-rock of the Blue Ridge and South Mountains to have been originally a continuous formation, it will be readily

seen that a vertical fault in easterly dipping strata, having its direction somewhat nearer the meridian than the present strike and its downthrow on the west side of the fault, would produce a lateral discontinuity like that here observed, the upthrown part of any stratum cropping out on the east of the downthrown part at a distance depending upon the amount of the vertical displacement.

All this would depend upon whether the sand rocks were originally continuous in the two ridges—a question which was left for the geologists to decide. The writer, however, took occasion to suggest that great longitudinal faults might be formed near coast lines when the gradual overloading of the balanced crust by depositions of sediment produced a strain too great to be relieved by flexure. A rupture would then occur, the strata going down on the overloaded side of the fault and up on the other until equilibrium of pressure upon the yielding magma below was restored by lateral displacement of the magma. The fault so formed would present a diminished resistance to dislocation, and if the action which originated it should continue, it would be likely to increase in dimensions both in length and in the amount of vertical displacement. This action might even continue after the emergence of the region above the surface of the water, provided a more rapid denudation of the landward than of the seaward side of the fault took place, in which case a continued disturbance of equilibrium would be accompanied by vertical yielding, increasing the amount of dislocation, and by subterranean movements of the supporting magma, whereby a restoration of material would be effected from overloaded to denuded areas.

Moreover, the hypothesis of a constant restoration of disturbed equilibrium makes it easier to understand why the folding of strata should grow steeper, even to a *folding under*, as the axis of a mountain chain is approached. A diagram exhibiting the so-called "fan-like structure of the Alps," enlarged from a figure by Rogers, (see Rogers' Report on the Geology of Pennsylvania, Vol. II, p. 902,) was shown in illustration. The gradual subterranean movements inward under a mountain chain, as the upper portions were removed and the remainder elevated, would carry the strata along on a support of diminishing width until they were folded upward and backward.

The gradual increase towards the east in the amount of corrugation and steepness of dips, together with the supposed reversed folding by which the rocks of the eastern part of the Appalachian region seem to

dip under older rocks, still further east appear, therefore, to favor the notion that the paleozoic rocks of the Appalachian region and the eastern part of the Mississippi basin were derived from the erosion of highlands formerly existing east of the Appalachian chain, now, perhaps, submerged in the Atlantic ocean. The downthrow of a fault, if formed in the manner supposed in the region under consideration, would accordingly be on its western side, as suggested above.

The third communication was by Mr. S. F. EMMONS on

ORE DEPOSITION BY REPLACEMENT.

[Abstract.]

After a few introductory remarks upon the relatively unsatisfactory condition of that branch of geology which treats of ore deposits, considering the early date at which it was taken up, the speaker briefly reviews the existing theories and classifications, and shows that they are mainly based on the idea that each ore deposit is the filling of some pre-existing cavity or opening in the rock in which it is now found; that so-called fissure veins, for instance, were once actually open cracks, and that irregular deposits in limestone have been made by the filling up of open caves, such as so frequently occur in these rocks. The result of his studies of the so-called "carbonate deposits" of Leadville, Colorado, has been to show that they are *not* the filling up of pre-existing cavities; the caves there have been formed since the ore was deposited, as is proved by their crossing indiscriminately ore bodies and limestone. They belong to a class of deposits for which he proposes the name *metamorphic deposits*, or those which have been formed by a metamorphic interchange between the vein and original rock material. In Leadville the principal deposits are an actual replacement of the limestone itself at or near the contact of this stratum with an overlying sheet of porphyry. This replacement action has in places proceeded so far that the entire stratum of ore-bearing limestone or dolomite, originally 150 to 200 feet thick, has been changed into vein material, which consists of silica and metallic minerals. This vein material was brought in solution by percolating waters, which had taken it up during their circulation through the adjoining and generally overlying eruptive rocks. A more detailed description of the phenomena of these deposits will be found in his paper en-

titled "Abstract of a Report on the Geology of Leadville," in the Second Annual Report of the Director of the United States Geological Survey.

While the speaker's studies have thus far been mainly confined to limestone deposits, he has reason to believe that essentially the same process has produced a large proportion of ore deposits in crystalline and eruptive rocks, and that to the class of metamorphic deposits belong most of the so-called fissure veins of the Rocky Mountain region. That is, that they are not the filling in of pre-existent open fissures by vein materials foreign to the adjoining rocks, but simply a metamorphic change of these rocks themselves along channels of easy access to percolating waters; and according to the character of the material held in solution by these waters, these rocks have been more or less changed into quartz and metallic minerals, to a greater or less width, as the case may be. Numerous instances of such veins will be found in the forthcoming Census Report upon the Statistics and Technology of the Precious Metals, by Mr. G. F. Becker and the speaker.

234TH MEETING.

APRIL 21, 1883.

Vice-President BILLINGS in the Chair.

Forty members present.

The Chair announced that Messrs. WASHINGTON CARRUTHERS KERR and SAMUEL FRANKLIN EMMONS had been elected members.

Mr. W. H. DALL addressed the Society on

GLACIATION IN ALASKA,

illustrating his remarks by maps of the territory and of the glacial areas of the St. Elias Alps and Kachekmak Bay, Cook's Inlet, the latter being from surveys made by him under the direction of the U. S. Coast Survey.

He called attention in the first place to the wide differences in the character of the masses of ice resulting from the consolidation of snow by gravity (which would usually be classed as glaciers), as observed by him during nine years' exploration in Alaska.

These might be classed under several heads: as plateau-ice, filling

large areas of depression and without motion as a whole, but when sufficiently accumulated overflowing the edges of its basin in various directions; as valley-ice, filling wide valleys of gentle incline both as to their axes and their lateral slopes, producing masses of ice moving in a definite direction but without lateral and sometimes even without terminal moraines; as ice-cascades, formed in sharp narrow ravines of very steep inclination, usually without well-defined surface moraines; as typical glaciers, showing névé and lateral and terminal moraines; and lastly, as effete or fossil glaciers, whose sources have become exhausted, whose motion has therefore ceased, and whose lower portions have become smothered by the accumulation of non-conducting débris. The very existence of one of these last has remained unknown for half a century, though the plateau underwhich it is buried has been described and mapped by explorers.

Another form under which ice appears in Alaska is that of solid motionless layers, sometimes of great thickness, interstratified with sand, clay, etc. A deposit probably of this character is described by Nordenskiöld, on the Asiatic coast, near Bering Strait. In Alaska this formation, in which ice plays the part of a stratified rock, extends from Kotzebue sound, where the greatest known thickness of the ice-layer, about three hundred feet, has been noted, around the Arctic coast, probably to the eastern boundary. In Kotzebue Sound the ice is surmounted by about forty feet of clay containing the remains of fossil horses, buffaloes (*Bos latifrons*, etc.), mountain sheep, and other mammals. Farther north the ice is covered with a much thinner coat of mineral matter or soil, usually not exceeding two or three feet in thickness, and rarely rises more than twelve or fifteen feet above high water mark on the sea coast. Its continuity is broken between Kotzebue Sound and Icy Cape by rocky hills composed chiefly of carboniferous limestones, which bear no glaciers and do not seem to have been glaciated. The absence of boulders and erratics over all this area has been noted by Franklin, Beechey, and all others who have explored it. The remarkable extent and character of the formation was unknown previous to the speaker's investigations, though the ice cliffs of Kotzebue Sound had attracted attention from the time of their first discovery.

Mr. DALL desired especially to emphasize the distinction between these strata of pure ice and the "frozen soil" so often alluded to by arctic explorers. The absence of frozen soil in the alluvium

of the Yukon Valley, far north of Kotzebue Sound, was noted, as well as the fact that this valley has, for some unexplained reason, a mean temperature considerably above the normal, so that its forests extend well beyond the Arctic circle.

The distribution of glaciers, properly so-called, in Alaska, as far as our present knowledge goes, is confined to the region of the Alaskan range and the ranges parallel with it south of the Yukon Valley, but particularly to the coast mountains bordering on the Gulf of Alaska and the Alexander Archipelago, of which the Saint Elias Alps form the most conspicuous uplift.

The distribution of stratified ice is all north of the Yukon Valley, which divides the two regions. Hence, for the glacial epoch, it may be presumed that the one is the equivalent of the other, and the fact that Arctic Alaska is marked by stratified ice, rather than glaciers such as those of Greenland, must be due to local geological and climatic peculiarities existing at the time. On the Asiatic coast, especially at Holy Cross Bay, in nearly the same latitude and with not very different topographic conditions, glaciers are abundant at the present time.

On the mainland, facing the Alexander Archipelago, especially toward Lynn Canal, Icy Strait and the Stikine region, local glaciers are abundant, and traces of others, now dissolved, may be found on the lowlands of most of the islands. That these were always local, though doubtless very extensive, and that they were the progeny of the topography instead of being its parent, is obvious to anyone who has seen the coasts of Maine or Norway, which have been submitted to general glaciation, and will compare their rounded, worn, and *moutonnée* aspect with that of the sharp cliffs, beetling crags, narrow valleys, and scanty lowlands of the Alaskan islands.

The speaker concluded, from his observations, that the extent of the Alaskan glaciers is greatly diminished from its former state, and is probably still diminishing; that the southern portion of the Territory is probably nearly or quite stationary, while the northern part is undergoing elevation; and that, from the nature of the case, the area of stratified ice cannot be expected to increase or diminish materially without changes in geological or climatic conditions too great to be anticipated.

Mr. ALVORD remarked that on Point Barrow frozen ground had been penetrated to a depth of thirteen feet.

In reply to a question by Mr. ANTISELL, Mr. DALL said that little was known of the humidity of the interior of Alaska; 23 inches of precipitation, nearly all in snow, had been observed in a single year at one point and 12 inches at another.

Mr. F. B. HOUGH then read a paper on

THE CULTIVATION OF THE EUCALYPTUS ON THE ROMAN
CAMPAGNA,

which was discussed by Messrs. E. B. ELLIOTT and H. FARQUHAR. It is published in the American Journal of Forestry for June, 1883.

235TH MEETING.

MAY 5, 1883.

Vice-President BILLINGS in the Chair.

Twenty-seven members and visitors present.

The Chair announced the election to membership of Messrs. WILLIAM THOMAS SAMPSON, JOHN OSCAR SKINNER, and THOMAS CROWDER CHAMBERLIN.

The first communication was by Mr. H. A. HAZEN on
HYGROMETRIC OBSERVATIONS.

[Abstract.]

After describing the various devices by which the moisture of the air has been measured, and especially the novel and valuable apparatus of Crova, the speaker illustrated the difficulty of the subject by contrasting synchronous determinations made at four points within a radius of two miles, and then described some experiments tending to show the inaccuracy of the wet and dry bulb hygrometer, as ordinarily observed. The value of the wet bulb reading is enhanced by blowing on the bulb with a bellows, or otherwise subjecting it to a brisk current of air.

Mr. HARKNESS remarked first, that Mr. Hazen's experiments appeared to prove the insufficiency of Regnault's formula, for they showed the difference between the indications of the wet bulb and dry bulb to be a function not only of the humidity, but of the velocity of wind; second, that height of station above the ground

was a condition to which too little attention had been given; and third, that there seemed a possibility of obtaining a slightly erroneous vapor tension with Crova's apparatus.

Mr. E. J. FARQUHAR then read a paper on

DREAMS IN THEIR RELATION WITH PSYCHOLOGY.

[Abstract.]

Several theories of dreams were considered and none found entirely sufficient; not because a new and complete one was to be proposed, but because all seemed a little too partial and limiting in their scope. After touching on the relation of dreams to sleep and to waking, as intermediate between them, discrediting many recorded experiments on the ground of their being vitiated by a special purpose latent in the mind, and pointing out that the usual supposition of our being often waked by the intensity of a dream appears to put cause for effect, since it must be the fact of waking that effects the dream, perhaps by slow degrees—the character of mental operations in dreams was discussed. Dissent was expressed from the opinion that the dreaming state is devoid of such originating power as belongs to the waking; this position was maintained by showing first, the extreme vividness and lastingness of impression often pertaining to dreams, apart from any features of horror; then the coherence, far from being unknown among them, yet of a peculiar kind; and, finally, the true significance occasionally appearing in them, generally by figurative shape, amounting sometimes to a real enlightenment of the mind. Regarding the faculties or aspects of mind most apt to display themselves in dreams, it was held that all were liable to the exercise in turn, though some of the higher ones, especially the moral sense and judgment, less than others; since these expressed a rarer and more distinctive force evolved and laid up by and for our relations with actual life, while other powers whose exercise is less of an expenditure from the most important vitalities of mind were freer at the time—the principles of conservation and struggle for existence being thought to apply among the mental elements. Thus, to a certain degree, the mind may be seen more clearly in its true character by means of dreams than awake, though in very partial views at a time. Unconscious mental action was reviewed in this connection, and it was held that not only the lower processes, called reflex, but many of the highest functions

largely partake of this attribute. A great number of other points in regard to dreams were merely named as illustrating the fertility of the subject.

236TH MEETING.

MAY 19, 1883.

Vice-President HILGARD in the Chair.

Forty members and visitors present.

It was announced from the General Committee that the following rules had been adopted:

I. If the author of any paper read before a section of the Society desires its publication, either in full or by abstract, it shall be referred to a committee, to be appointed as the section may determine.

The report of this committee shall be forwarded to the Publication Committee by the secretary of the section, together with any action of the section taken thereon.

II. Any paper read before a section may be repeated, either entire or by abstract, before a general meeting of the Society, if such repetition is recommended by the General Committee of the Society.

Mr. ROBERT FLETCHER made a communication entitled

RECENT EXPERIMENTS ON SERPENT VENOM.

It is published in the *American Journal of the Medical Sciences* for July, 1883.

Mr. H. FARQUHAR then made a communication on

FURTHER EXPERIMENTS IN BINARY ARITHMETIC,

showing that the relation between the vertical and horizontal dimensions of the characters used in the binary notation is a factor in determining its economic value. He presented, also, the results of a series of comparative tests showing that the binary notation enables some persons, after brief practice, to perform addition more rapidly than with denary notation, while with others it requires a longer time. The latter class includes practiced computers, generally, and the former those less accustomed to the use of figures.

Mr. DOOLITTLE remarked that the most instructive results would be obtained by experimenting with young persons; and the subject was further discussed by Messrs. W. B. TAYLOR, E. B. ELLIOTT, and C. A. SCHOTT.

237TH MEETING.

JUNE 2, 1883.

Vice-President HILGARD, and afterward Mr. HARKNESS, in the Chair.

Twenty-two members present.

It was announced that the next meeting would be held October 13th.

Mr. W. LEE made a communication, with illustrations, entitled
 SKETCHES FROM MEDALLIC MEDICAL HISTORY.

[Abstract.]

The paper was prefaced by remarks on the value of coin and medal collecting as a profitable means of instruction, and by a recognition of the danger to which collectors are exposed of developing a mania for collecting odd and curious things which cease to be instructive. An extended interest in numismatics commenced to show itself in this country in 1858, at which time there were probably not as many as one hundred coin collectors in the United States. The interest has grown rapidly, however, until now there must be on the books of the United States Mint the names of at least one thousand collectors who receive yearly the issue of the mint, with a special proof polish. In New York alone, during the year 1882, there were thirty-nine collections sold at public auction, the amount realized being \$68,441.36. The largest of these was the Bushnell collection, which realized \$13,900.47. Several of our large cities have numismatic societies, some of which are designated as numismatic and archæological societies; and a number of periodicals devoted simply to the interest of numismatics obtain a satisfactory circulation.

The modes of striking off coins and medals were given somewhat in detail, and attention was then called to the important part which medals struck in honor of medical men and to commemorate im-

portant events bearing directly upon the history of medicine have played throughout the history of the world. The illustrations of the paper included a hundred and fifty examples of the medals themselves, in regular sequence, from the days of Roman and Greek medicine down almost to the date of the paper itself, an interesting commemoration of events and individuals marking epochs in the history of medicine. These medals were taken up *seriatim*, references were made to the lives of individuals and the scientific work done by them, and descriptions were given of the occasions which called for the striking of medals.

The paper closed with an expression of hope that the Society might be stimulated at the sight of so many handsome and permanent memorials of the men and times of the past, to attempt to preserve the features of its first president, Joseph Henry, in a similar enduring form.

The bibliography of the subject was discussed at some length, and the following works were referred to :

- MEAD, Richardi.—Dissertatio de Nummis quibusdam a Smyrnaeis in medicorum honorem percussis. Naples, 1752.
- RUDOLPHI, C. A.—Index numismatum in virorum de rebus medicis vel physicis meritorum memoriam percussorum. Berlin, 1st edition 1823, 2d edition 1825, 12mo., XII, 131 pp, 3d edition 1828, 4th edition 1829. (This work (2d edition) comprises the description of 523 medals struck in honor of 350 scientific and medical men.)
- RENAULDIN, Leop. Jos.—Études historiques et critiques sur les Médecins Numismatistes, contenant leur biographie et l'analyse de leurs écrits. Paris, 1851, 8°, XVI, 574 pp. (This work contains the names of 61 physicians).
- CHÉREAU (A).—Les mereaux et les getons de l'ancienne faculté de médecine de Paris. L'Union Médicale. Paris, 1873, 3 Series, XV, pp. 309, 321.
- PFEIFFER, (L) und RULAND (C).—Pestilentia in Nummis. Geschichte der grossen Volkskrankheiten in numismatischen Documenten. Ein Beitrag zur Geschichte der Medicin und der Cultur. Tubingen, 1882, 8° X, 189 pp. Mit zwei Tafeln Abbildungen in lichtdruck.
- WROTH, Warwick.—Asklepios and the Coins of Pergamon. From the Numismatic Chronicle and Journal of the Numismatic Society. London, 1882, Part I, Third Series, No. 5, pages 1 to 51, plates 3.
- MOEHSSEN, J. C. G.—The exact title of this author's work is not known to the writer of the paper; it was written in German,

and embodies a description of a collection of medals in Berlin struck in honor of physicians, giving 200 medals struck after the 15th century.

GROTEFEND, C. L.—Die Stempel der Römischen Augenärzte. Hannover, 1867.

Mr. T. N. GILL then made a communication on

ANALOGUES IN ZOO-GEOGRAPHY.

238TH MEETING.

OCTOBER 13, 1883.

The Society, in accordance with the notice of adjournment at the June meeting, resumed its sessions.

The President in the Chair.

Forty-four members and visitors present.

It was announced that during the vacation the Society had lost by death Surgeon General C. H. CRANE, one of its Vice-Presidents; Admiral B. F. SANDS, one of its founders; and Dr. JOSIAH CURTIS.

It was further announced from the General Committee that Mr. GARRICK MALLERY had been appointed Vice-President to fill the vacancy occasioned by the death of Mr. CRANE, and that Mr. C. V. RILEY had been added to the General Committee to complete its number.

Mr. WILLIAM B. TAYLOR read a paper entitled

NOTE ON THE RINGS OF SATURN.

[Abstract.]

After an historic sketch of the varying and apparently incongruous observations by astronomers on the markings and aspects of the Saturnian rings, down to those of Schiaparelli of the Milan Observatory, (published in June last,) Mr. TAYLOR remarked that since the mathematical discussion by Prof. J. Clerk Maxwell, in 1857,* both the rigid and the fluid ring theories have been abandoned; and the discrete or meteoric constitution of the rings is now accepted by all physical astronomers as conclusively established.

* *On the Stability of the Motion of Saturn's Rings.* 4to. 71 pp. and 1 plate. Cambridge, Eng., 1859.

Reference was then made to the startling announcement by Otto Struve, in 1851, that a careful comparison of the earlier with the later measurements showed that during the two hundred years of observation the rings had been widening, and the inner edge steadily approaching the body of the planet.* Considering the necessarily vast antiquity of the Saturnian system, such a change during the brief interval of human existence seems *à priori* almost infinitely improbable. The hypothesis of some that a meteoric ring has been drawn in by Saturn's attraction, within comparatively recent ages, seems entirely negatived by the circular symmetry of the system. It is not surprising, therefore, that Struve's inference has been received with an almost universal incredulity by the astronomical world. Robert Main, of the Greenwich Observatory, from a discussion of his own measurements taken in the winter of 1852-'3, and in 1854, disputed the accuracy of Struve's measures; and concluded that "no change has taken place in the system since the time of Huyghens."† And Prof. F. Kaiser, in a paper on "The Hypothesis of Otto Struve respecting the gradual increase of Saturn's Ring," etc., arrives at the same conclusion, and believes "there exists no reason whatever for supposing that the compound ring of Saturn is gradually increasing in breadth."‡

There seems to be little doubt of some unintentional exaggeration in Struve's tabulated results, which range from 4".6 : 6".5 for the ratio of ring breadth to space between ring and ball, in the time of Huyghens, 1657, to 7".4 : 3".7 for the ratio of breadth to space, by his own observation in 1851. Nevertheless it is a noteworthy fact that all the early drawings of Saturn made in the seventeenth century (many of which are figured by Huyghens in his *Systema Saturnium*, 1659) plainly exhibit the width of the ring as sensibly less than the dark space within; while all modern observers would agree that the bright ring is now wider than the dark space, in about the ratio of 3 : 2; or were we to take the average of the esti-

* *Recueil des Mémoires présentés* [etc.] *par les Astronomes de Poulkova*. 4to. St. Petersburg, 1853. Vol. I, pp. 349-385. "Sur les Dimensions des Anneaux de Saturne." (Memoir read before Acad. Sci.) A brief abstract of the memoir is given in the *Monthly Notices, R. A. S.*, November 12, 1852. Vol. XIII, pp. 22-24.

† *Monthly Notices, R. A. S.*, December 14, 1855. Vol. XVI, pp. 30-36.

‡ *Mem. Acad. Sci., Amsterdam*, 1858. A translation of the memoir is given in the *Monthly Notices, R. A. S.*, January 11, 1856. Vol. XVI, pp. 66-72.

mates of the last century, it would probably not vary far from $5''.25:5''.75$; while the general average for the present century would probably be about $6''.5:4''.5$. There seems, therefore, to be a real difference, not accounted for by inferiority of earlier instruments and estimates, nor by the existing uncertainties of modern measurements. The question will probably be definitely settled in less than a century. Meanwhile there is a need of some explanation of the apparently systematic and progressive divergence first pointed out by Struve; and we naturally ask, What indications are afforded by theory?

The elder Herschel, in 1789, (at the Saturnian equinox, when the edge of the ring was presented to view,) from supposed observation of protuberances moving on the line, believed that he had detected a rotation, whose period he estimated at 10h. 32m. 15s., for the outer edge of the ring.* The correctness of this interpretation was controverted by Schroeter, from observations at Lilienthal, on the next passage of Saturn's equatorial node in 1803; as it was afterward questioned by Prof. G. P. Bond, of Harvard Observatory, from observations in 1848.† It is scarcely doubtful that Herschel's period was derived from an entire misconception of the nature of the ring—which he firmly held to be solid—and that it possesses no scientific value whatever. A. Secchi, from certain recurrent irregularities of phase observed at Rome in 1854, 1855, and 1856, inferred a rotation period of 14h. 23m. This is doubtless a nearer approximation (for the outer edge of the ring) than Herschel's estimate. It is not probable, however, that the period of any portion of the ring will be determined by observation.

Accepting the meteoric theory of the rings as now established, we may by Kepler's law compute with confidence the period of rotation of any part of the ring; and we thus find—

From the period of the inner Satellite (<i>Mimas</i>)---	22h.	37½m.—
The period of outer edge of ring -----	14h.	30 m.
“ dividing stripe -----	11h.	20 m.
“ inner edge of bright ring -----	7h.	12 m.
“ inner edge of dusky ring -----	5h.	45 m.
Mean period of ring (supposed solid) about -----	10h.	50 m.

The period of the planet Saturn is . . . 10h. 14m.

* *Phil. Trans. Roy. Soc.* 1790: Vol. LXXX, p. 479; and 1792: Vol. LXXXII, p. 6.

† Gould's *Astronomical Journal*. 1850. Vol. I, pp. 20, 21.

Thus regarding each constituent element of the ring as having its own independent rotation, (a condition absolutely essential to the stability of the system,) we may consider that from the complicated and variable perturbations by the exterior satellites, no one particle can revolve in a circular orbit, and hence that in a space so crowded there must be a considerable amount of interference. The collisions at intersecting orbits may result in heat or in disintegration; but in any event they must tend to a degradation of motion, and hence to a slightly shortened mean radius-vector and a shortened period.

Theoretically then such an effect as that indicated by Struve would seem inevitable, whether as a matter of fact it has been sufficient in a couple of centuries to be detected or not. And this involves a modified conception as to the earlier condition of the Saturnian rings. To suppose a fine web of nebulous matter continuously spun out from Saturn's equator, with an unchanging balance of centrifugal and centripetal forces during the long ages while the planet was slowly contracting to one-half its radius, is certainly no easy task or plausible theory. If, however, we are now beholding but a stage of transitional development of the ring, we shall have to imagine its primitive radius considerably larger, and its width as probably very much narrower—so narrow indeed as to have a planetary or satellitic status, revolving in a single definite period—possibly that of *Mimas* the nearest satellite. Such a ring would present a condition of comparatively great stability; and it may have been that only the secular recurrence of rare and remarkable conjunctions commenced upon it the work of disturbance and disintegration.

When Galileo, the first to see the strange appendages to Saturn, (though without being able to distinguish the *ansæ* as parts of a ring,) observed, in 1612, that they had entirely disappeared, he wrote in some dismay, "Has Saturn possibly devoured his own children?"* So may perhaps the future astronomer, seeing but an airy trace of the historic ring, repeat the saying, Saturn has indeed devoured his offspring; not indeed completely, for a part will probably still remain; nor with violent catastrophe, for the scattered fragments falling by their eccentricity will be absorbed as gently as are the meteors daily falling on our earth.

* Third letter to Marc Velsler, December 1, 1612. *Opere di Galileo*. 4to. 4 vols. Padua, 1744: Vol. II, p. 123.

A subsidiary point deserving of notice is the certainty that the inner portions of the bright ring (and still more those of the dusky ring) are revolving in periods three or four hours shorter than that of Saturn himself. When Professor Hall made his brilliant discovery of the satellites of Mars, and announced that the inner satellite (*Phobos*) was found to have the short period of 7h. 38m. (or less than one-third of that of Mars) the fact was at once proclaimed by some as incompatible with the "nebular hypothesis." Everybody knows that the rotation periods of the sun and planets do not conform to the third law of Kepler. Our own moon has an actual velocity in its orbit more than double that of our terrestrial equator. And had the moon a little less than one-third its present distance, (that is, were its radius-vector less than 70,000 miles,) its *angular* velocity would exceed that of the earth, or its period would be less than 24 hours. Or, stated in another way, our earth, if expanded to the orbit of the moon, (under the most favorable disposition of form and of homogenous density,) would occupy considerably more than a year in completing its rotation. The supposed nebular difficulty is therefore just as pertinent to our own satellite as to those of Saturn or of Mars. The obvious solution is, that all the planets (without exception) have lost a very large amount of rotatory energy; and this may be largely or chiefly ascribed to the retarding effects of internal friction resulting from solar tides. And, given time enough, the rotation of every planet should be finally reduced to the lunar condition of a precise accord of its diurnal and annual periods. On any hypothesis whatever, it is certain that the rotations of the planets are very much slower (notwithstanding too the acceleration due to contraction) than they originally were. This fact certainly offers no objection to the nebular hypothesis.

Mr. DUTTON questioned the validity of Ennis' hypothesis, that the rotation of a nebular mass could be initiated by purely internal movements.

Other remarks were made by Mr. FRISBY.

Mr. S. M. BURNETT then made a communication on

THE CHARACTER OF THE FOCAL LINES IN ASTIGMATISM,

showing that the two lines which limit the focal interval of Sturm have been erroneously assumed to be straight. There is only one

special case of the triaxial ellipsoid in which they are straight. In all other cases they are curved.

The full text of this paper may be found in the *Archives of Ophthalmology*, Vol. XII, Nos. 3 and 4.

Mr. H. A. HAZEN followed with a communication on

THERMOMETER EXPOSURE.

[Abstract.]

Without entering upon the question, Where in any locality shall the air temperature be observed, it is proposed to discuss the even more important question, What shall be the environment of a thermometer that it may give the true temperature. The practice has been very various: in England the Stevenson shelter is regarded as a standard: this is a double-louvred frame, wholly of wood, 18 x 10 x 18 inches, and placed about 4 feet above grass. In Russia we find a large wooden outside shelter of single louvres open to the north, inside of which is placed a metallic screen, the whole being exposed 12 or 13 feet above grass. In any exposure we should seek, first, to allow the freest possible access of the outer air, and second, to screen the thermometer from direct sun heat, from precipitation, and from radiation, whether (*a*) from surrounding objects by day or (*b*) to the sky at night.

It is important that we adopt some ready means of accurately determining the air temperature which may answer as a standard of comparison. This we have in the swung thermometer, which, by its free motion through a large body of air shaded from direct sunlight in the daytime, is calculated to give good results.

Experiments have been tried with a so-called "Pattern" shelter constructed of wood, of single louvres, inclined 30° to the horizontal, thus giving a good air circulation. The size is 4 x 3 x 3 feet, and it is erected at a height of 13 feet above a tin roof. In order to determine the least admissible size for a shelter, thermometers were placed in the Pattern 5 inches apart and running in an east and west direction, and these were observed morning and afternoon. It has been found that with a hot sun and still air the heat from the louvres rapidly diminishes with distance and becomes insensible at 15 inches. Comparisons have also been made for several weeks between the Russian and Pattern shelters; and the means of 100 sets of continuous observations on a still day, and again on a windy day, are shown in the following table:

	Dry ther- mometer.		Wet ther- mometer.		Relative humidity; per cent.	
	Russian.	Pattern.	R.	P.	R..	P
Still air-----	74°.8	73°.5	64°.0	62°.7	52.4	51.1
Light south wind--	77 .2	77 .1	62 .0	61 .0	36.7	34.1

These results show directly the advantage of a good circulation of air, and that after shielding from the sun and radiation to the sky with a shelter at least 3 feet long, we may neglect other considerations.

Experiments are still in progress to determine the proper height above sod or roof, the proper exposure for a north window, and so forth.

Mr. ANTISELL, referring to the general theme rather than to the special subject of the paper, took occasion to note that the practice of conducting meteorologic observations on the tops of high houses, while it may well subserve the special purposes of the Signal Service, renders their work of materially less value to the medical profession. There is so much change, especially of the moisture element, in the first few feet from the ground upward that no observations can be depended upon as reporting the conditions of the phenomena of disease unless they are made in the layer actually occupied by man.

Mr. TAYLOR asked whether there might not be an error arising from the set given to the glass of the bulb by the pressure of the mercury of a whirled thermometer.

Mr. HAZEN replied that he had tested the effect of pressure applied to the bulb with the finger, and found that the set produced was of very brief duration. He had also tested the thermic effect of the friction on the atmosphere incurred by rapid whirling, and found it inappreciable with a velocity of about fourteen miles an hour. On whirling a black bulb thermometer, he observed a change of several tenths of a degree, which appeared clearly referable to the greater coefficient of friction of the surface roughened by lamp-black.

Mr. GRAHAM BELL remarked that if we eliminate radiation and learn the absolute temperature of the air at the point of observation, our knowledge is still limited to that point only, whereas for meteorologic purposes it is important to ascertain the average temperature of a body of air. He suggested the possibility of utilizing for this purpose a measurement of the velocity of sound, which

velocity is dependent on atmospheric temperature and independent of barometric pressure.

Mr. DUTTON thought that the extreme delicacy of this observation would involve an uncertainty greater than the one which now inheres in the determination.

239TH MEETING.

OCTOBER 27, 1883.

The President in the Chair.

Forty-seven members and guests present.

The Chair announced the death of two members since the last meeting—LEONARD DUNNELL GALE and ELISHA FOOTE.

Announcement was also made of the election to membership of CHARLES DOOLITTLE WALCOTT.

Mr. T. N. GILL made a communication on

ICHTHYOLOGICAL RESULTS OF THE VOYAGE OF THE ALBATROSS.

Mr. ALEXANDER GRAHAM BELL made the following communication on

FALLACIES CONCERNING THE DEAF, AND THE INFLUENCE OF SUCH
FALLACIES IN PREVENTING THE AMELIORATION
OF THEIR CONDITION.

It is difficult to form an adequate conception of the prevalence of deafness in the community. There is hardly a man in the country who has not in his circle of friends and acquaintances at least one deaf person with whom he finds it difficult to converse excepting by means of a hearing-tube or trumpet. Now is it not an extraordinary fact that these deaf friends are nearly all adults? Where are the little children who are similarly afflicted? Have any of us seen a child with a hearing-tube or trumpet? If not, why not? The fact is that very young children who are hard of hearing, or who cannot hear at all, do not naturally speak, and this fact has given origin to the term "deaf-mute," by which it is customary to designate a person who is deaf from childhood.

"But are there no deaf children," you may ask, "excepting those whom we term deaf-mutes?" No; none. In the tenth census

of the United States (1880) persons who became deaf under the age of sixteen years were returned as "deaf and dumb." Such facts as these give support to the fallacy that deafness, unaccompanied by any other natural defect, is confined to adult life, and is specially characteristic of advancing old age.

So constant is the association of defective speech with defective hearing in childhood that if one of your children whom you have left at home, hearing perfectly and talking perfectly, should, from some accident, lose his hearing, he would also naturally lose his speech. Why is this, and why are those who are born deaf always also dumb?

Fallacies Concerning the Dumbness of Deaf Children.

The most ingenious and fallacious arguments have been advanced in explanation. George Sibscota,* in 1670, claimed that the nerves of the tongue and larynx were connected with the nerves of the ear, "and from this Communion of the vessels proceeds the sympathy between the Ear, the Tongue and Larynx, and the very affection of those parts are easily communicated one with the other. Hence it is that the pulling of the Membrane of the Ear causeth a dry Cough in the party; and that is the reason most deaf men * * * are Dumb, or else speak with great difficulty; that is, are not capable of framing true words or of articulate pronunciation by reason, of the want of that convenient influx of the animal spirits; and for this cause also, it is that those who are thick of Hearing have a kind of hoarse speech."

The value of Sibscota's reasoning may be judged of by the further information he gives us concerning the uses of the Eustachian tube. "By this it is," he says, "that Smokers, puffing up their Bheeks, having taken in the fume of Tobacco, send it out at their Ears. Therefore the opinion of *Alcmaeon* is not ridiculous, who held that she-Goats did breathe thorough their Ears," &c., &c.

It is easy for us to laugh at the fallacies of the past, but are we ourselves any less liable to error on that account? The majority of people at the present day believe that those who are born deaf are also dumb *because of defective vocal organs*. Now let us examine

* I have been informed that Sibscota's work, "The Deaf and Dumb Man's Discourse," from which the above extracts are taken, is in reality a translation of another work by Anthony Densing, published in 1656.

this proposition. It is a more ridiculous and absurd fallacy than that of Sibscota and more easily disposed of.

The hypothesis that congenitally deaf children do not naturally speak because their vocal organs are defective involves the assumption that were their vocal organs perfect such children *would* naturally speak. But why should they speak a language they have never heard? Do we speak any language that we have not heard? Are our vocal organs defective because we do not talk Chinese? It is a fallacy. The deaf have as perfect vocal organs as our own, and do not naturally speak because they do not hear. I have myself examined the vocal organs of more than 400 deaf-mutes without discovering any other peculiarities than those to be found among hearing and speaking children. The deaf children of Italy and Germany are almost universally taught to speak, and why should we not teach ours? Wherever determined efforts have been made in this country success has followed and articulation schools have been established.

Fallacy Concerning the Intelligence of Deaf Children.

The use of the word "mute" engenders another fallacy concerning the mental condition of deaf children. There are two classes of persons who do not naturally speak—those who are dumb on account of defective hearing and those who are dumb on account of defective minds. All idiots are dumb.

Deaf children are gathered into institutions and schools that have been established for their benefit away from the general observation of the public, and even in adult life they hold themselves aloof from hearing people; while idiots and feeble-minded persons are not so generally withdrawn from their families. Hence the greater number of "mutes" who are accessible to public observation are dumb on account of defective minds, and not of defective hearing. No wonder, therefore, that the two classes are often confounded together. It is the hard task of every principal of an institution for the deaf and dumb to turn idiots and feeble-minded children away from his school—children who hear perfectly, but cannot speak. Although it is evidently fallacious to argue that, because all deaf infants are dumb, and all idiots are dumb; therefore all deaf infants are idiots: still this kind of reasoning is unconsciously indulged in by a large proportion of our population; and the majority of those who for the first time visit an institution

for the deaf and dumb express unfeigned astonishment at the brightness and intelligence displayed by the pupils.

Why Hearing Children who become Deaf also become Dumb.

I have stated above that children who are born deaf do not naturally speak because they cannot hear. For the same reason children who lose their hearing after having learned to speak naturally tend to lose their speech. They acquired speech through the ear by imitating the utterances of their friends and relatives, and when they become deaf they gradually forget the true pronunciation of the words they know, and have naturally no means of learning the pronunciation of new words; hence their speech tends to become more and more defective until they finally cease to use spoken words at all.

Adults who become deaf do not usually have defective speech, for in their case the habit of speaking has been so fully formed that the mere practice of the vocal organs in talking to friends prevents loss of distinctness. We can learn, however, from the case of Alexander Selkirk how important is constant practice of the vocal organs. This man, after about one year's solitary residence upon an island, was found to have nearly forgotten his mother tongue; and we find that deaf adults who shrink from society and use their vocal organs only on rare occasions acquire peculiarities of utterance that are characteristic of persons in their condition, although the general intelligibility of their speech is not affected.

Fallacies Regarding the Nature of Speech.

The fallacies I have already alluded to respecting the difference between those who become deaf in' childhood and those who become deaf in adult life have their origin in a fallacy concerning the nature of speech itself. To most people, who do not reflect upon the subject, it appears that speech is acquired by a natural process similar to that by which we acquire our teeth. At a certain age the teeth make their appearance, and at another age we begin to talk. To unreflecting minds it appears that we *grow into speech*; that speech is a natural product of the vocal organs, produced without instruction and education; and this leads directly to the fallacy that where speech is wanting or imperfect the vocal organs are defective.

I have already stated that this cause has been assigned in expla-

nation of the dumbness of children who are deaf. The idea gives rise also to the popular notion that stammering and other defects of speech are diseases to be "cured," and the attempt has been made to do so, even by heroic treatment. It is not so very long ago that slices have been cut from the tongue of a stammerer, in the vain hope of "curing" what was, after all, but a bad habit of speech. I have myself known of cases where the uvula has been excised to correct the same defect. The dumbness of the deaf and the defective speech of the hearing are some of the penalties we pay for acquiring speech ignorantly, by mere imitation. If parents realized that stammering and other defects of speech were caused by ignorance of the actions of the vocal organs, and not necessarily through any defect of the mouth, they would have their children taught the use of the vocal organs by articulation teachers, instead of patronizing the widely-advertised specialty physicians, who pretend by secret means to "cure" what is not a disease. Speech is naturally acquired by imitation, and through the same agency defects of speech are propagated. A child copies the defective utterance of his father. A school-fellow mocks a stammering companion, and becomes himself similarly affected. In the one case the fallacy that the supposed disease is hereditary prevents attempts at instruction and correction, and in the other the idea that the affliction is the judgment of God in the way of punishment discourages the afflicted person and renders him utterly hopeless of any escape excepting by a miracle.

A practical illustration of the fact that defective speech is propagated by imitation is shown in my own case. When I was a boy my father was a teacher of elocution, and had living with him at one time one or two pupils who stammered. While under the care of my father, these boys spoke clearly and well, without any apparent defect, but, owing to his being called away for a protracted period of time, his pupils relapsed, and the boys commenced to stammer as badly as at first. Upon my father's return he found a house full of stammerers. *His own sons were stammering too!* I can well remember the process of instruction through which I went before the defect was corrected in my own case.

Ignorance the Real Difficulty in the Way of Teaching Deaf Children to Speak.

Speech is the mechanical result of certain adjustments of the

vocal organs, and if we can teach deaf children the correct adjustments of the perfect organs they possess, they will speak. The difficulty lies with us. We learn to speak by imitating the sounds we hear, in utter ignorance of the action of the organs that accompanies the sounds. I find myself addressing an audience composed of scientific men, including many of the most eminent persons in the country, and I wonder how many there are in this room who could give an intelligible account of the movements of their vocal organs in uttering the simplest sentence? We must study the mechanism of speech, and when we know what are the correct adjustments of the organs concerned, ingenuity and skill will find the means of teaching *perfect* articulation to the deaf.

The Old Fallacy—"Without Speech, no Reason."

I have already stated that children who are born deaf are also always dumb. How, then, can they think? It is difficult for us to realize the possibility of a train of thought being carried on without words; but what words can a deaf child know, who has never heard the sounds of speech?

When we think, we think in words, though we may not actually utter sounds. Let us eliminate from our consciousness the train of words, and what remains? I do not venture to answer the question; but it is this, and this alone, that belongs to the thoughts of a deaf child.

It is hardly to be wondered at, therefore, that the fallacy should have arisen in the past that there could be no thought without speech; and this fallacy prevented for hundreds of years any attempt at the education of the deaf. Before the end of the last century deaf-mutes were classed among the idiots and insane; they had no civil rights, could hold no property; they were irresponsible beings. Even those interested in the religious welfare of the world consigned their souls to the wrong place, for "faith comes by hearing," and how could a deaf child be saved? I say that for hundreds of years the old fallacy, that "without speech there could be no reason," hindered and prevented any attempt at the amelioration of the condition of the deaf. But, strange to say, it was this very fallacy that first led to their education. It was attempted, by a miracle to teach them to speak.

In Bede's History of the Anglo-Saxon church we read "How Bishop John cured a dumme man with blessing him."

“And when one weeke of Lent was past, the next sounday he willed the poore man to come unto him; when he was come, he bydd him put out his tounge and show it unto him, and taking him by the chinne, made the signe of the holy crosse upon his tounge, and when he had so signed and blessed it, he commaunded him to plucke it in again, and speake saying, speake, me one word, say *gea, gea*, which in the english tounge is a worde of affirmation and consent in such signification as *yea, yea*.* Incontinent the stringes of his tounge were loosed, and he said that which was commanded him to say. The bishopp added certain letters by name, and bid him say A; he said A; say B, he said B, and when he had said and recited after the bishopp the whole cross rewe he put upon him sillables and hole wordes to be pronounced. Unto which when he answered in all pointes orderly, he commaunded him to speake long sentences, and so he did; and ceased not all that day and night following, so longe as he could hold up his head from sleepe (as they make report that were present) to speake and declare his secret thoughtes and purposes, which before that day he could never utter to any man.”†

Now, stripped of the miraculous, this is simply a case of articulation teaching. In the other countries of Europe the first attempts at the education of the deaf were also made by teaching them to speak, and as the early teachers were monks of the Roman Catholic Church, it is probable that these schools resulted from the attempts to perform the miracle of healing the dumb. A large proportion of the deaf and dumb who were thus brought together were successfully taught to articulate.

But now comes a marvel: It was found by the old monks that their pupils came to understand the utterances of others by watching the mouth. Such a statement appears more marvelous to those who understand the mechanism of speech than to those who are ignorant of it; and there is a general tendency to consider this accomplishment as among the fictitious embellishments of the old narratives. But the experience of modern teachers confirms the fact. John Bulwer, who is said to have been the earliest English writer upon the subject of the instruction of the deaf and dumb, published

* It will be remembered that the original of this was in Latin, and that “the english tounge” here means what we now call the Anglo Saxon.

† American Annals of the Deaf and Dumb, vol. I, p. 33 (1848).

in the year 1648 a treatise entitled "Philocophus; or, the Deaf and Dumbe Man's Friend. Exhibiting the Philosophicall verity of that subtile Art, which may inable one with an *observant Eie*, to *Heare* what any man speaks by the moving of his lips. Upon the same Ground, with the advantage of an Historicall Exemplification, apparently proving, That a Man Borne Deafe and Dumbe may be taught to *Heare* the sound of *words* with his *Eie*, and thence learn to speak with his tongue."

Articulation Teaching in America.

In Europe at the present time deaf children are much more commonly taught to speak and understand speech than in this country.

In the majority of our schools and institutions articulation and speech-reading are taught to only a favored few, and in these schools no use is made of articulation as a means of communication. A considerable number of the deaf children in our institutions could once hear and speak, and those pupils who retain some knowledge of spoken language have their vocal organs exercised for an hour or so a day in an articulation class under a special articulation teacher, but this is not enough exercise to retain the speech. I have seen a boy who became deaf at 12 years of age, and who had previously attended one of our public schools, go into an institution for the deaf and dumb talking as readily as you or I *and come out a deaf mute.*

Few, if any, attempts are made to teach articulation to those who have not naturally spoken, except at the special request of parents who desire that the experiment shall be tried with their children.

I have seen a congenital deaf mute, who also had a sister deaf and dumb, who was taught to speak in adult life, and I found upon experiment that he could understand by ear the words and sentences that he had been taught to articulate when they were spoken in an ordinary tone of voice about a foot behind his head, yet this young man had been educated at one of our best institutions without acquiring articulation, and as a consequence he grew up a deaf mute and married a deaf mute. He informed me himself that he could hear the people talking in the workshop where he was employed, but did not understand what they said.

As a matter of personal observation I am convinced that a large proportion of the congenitally deaf are only hard of hearing, and this belief is supported by the fact that it used to be the custom in

some of our institutions to summon the pupils from the play-ground *by the ringing of a bell!* Does this not indicate that a large number of the pupils could hear the ringing of the bell, and that they told the others who could not hear at all? Such pupils could have been taught to speak at home by their friends if artificial assistance had been given to their hearing. There was no necessity for their ever becoming deaf and dumb.

It is only within the last fifteen years or thereabouts that schools have been established in the United States where all the deaf children admitted are taught articulation and speech-reading, but such schools are rapidly increasing in number. Still, it is not generally known that the experimental stage has passed, and that all deaf mutes can be taught intelligible speech. This is now done in Italy and Germany, and the international conventions of teachers of the deaf and dumb held recently at Milan and Brussels have decided in favor of articulation for the deaf.

I have stated before that the difficulties in the way of teaching articulation are external to the deaf. They lie with us and in our general ignorance of the mechanism of speech. A teacher who does not himself understand the mechanism of speech is hardly competent to produce the best results. So dense is the general ignorance upon this subject that it is probable that of the 50,000,000 of people in this country the number of persons who are familiar with all that is known concerning the mechanism of speech might be numbered on the two hands. Considering this, the success obtained in our articulation schools is gratifying and wonderful.

Upon the Art of Understanding Speech by the Eye.

It has been found in the articulation schools of this country that deaf children can acquire the art of understanding by eye the utterances of their friends and relatives, and this fact has led some teachers to suppose that speech is as clearly visible to the eye as it is to the ear, and this fallacy tends to hinder the acquisition of the art by their pupils.

When we examine the visibility of the elementary sounds of our language we find that the majority can not be clearly distinguished by the eye. How then, you may ask, can a deaf child who cannot distinguish the elements understand words which are combinations of these elements?

When the lips are closed we cannot see what is going on inside

the mouth. The elementary sounds of our language, represented by the letters P, B, and M, involve a closure of the lips. Hence the differences of adjustment that originate the differences of sound are interior and cannot be seen. But while the deaf child may not be able to say definitely whether the sound you utter is P, B, or M, he knows certainly that it must be one of these three, for no other sounds involve a closure of the lips. And so with the other elements of our language. While he may not be able to tell definitely the particular element to which you give utterance, he can generally refer it to a group of sounds that present the same appearance to the eye. In the same manner he may not be able to tell the precise word that you utter, but he can refer it to a group of words having the same appearance. For instance, the words "pat," "bat," and "mat" have the same appearance to the eye. While he cannot tell which of these words you mean when it is uttered singly, he readily distinguishes it in a sentence by the context. For instance, were you to say that you had wiped your feet upon a "mat," the word could not be "pat" and it could not be "bat."

Here we come to the key to the art of understanding speech by the eye—Context. But this involves, as a prerequisite, a competent knowledge of the English language; and we may particularly distinguish those children who have acquired the art from those who have not, by their superior attainments in this respect. We can, therefore, see why children who have become deaf after having learned to speak, naturally acquire this power to a greater extent than those who are born deaf.

There are many cases of congenitally deaf children who have acquired this art as perfectly as those who have become deaf from disease; but in every case such children have been thoroughly familiar with the English language, at least in its written form.

Fallacies Regarding Speech-reading.

The fallacy that speech is as clearly visible to the eye as it is audible to the ear hinders the acquisition of the art by causing the teacher to articulate slowly and word by word, even opening the mouth to its widest extent to make the actions of the organs more visible. When we realize that context is the key to speech-reading, theory asserts that ordinary conversational speech should be more intelligible than slow and labored articulation. This is amply proved by the experience of the most accomplished speech-readers.

I have been told by one who has acquired this art that when introduced to strangers their speech is more readily understood if they are not aware they are speaking to one who cannot hear. The moment they are told they commence to speak slowly and open their mouths to an unnatural extent, thus rendering their articulation partially unintelligible. The change brought about by the knowledge that the listener could not hear was sometimes sudden and great.

I have lately made an examination of the visibility of all the words in our language contained in a small pocket dictionary, and the result has assured me that there are glorious possibilities in the way of teaching speech-reading to the deaf, if teachers will give special attention to the subject.

One of the results of my investigation has been that the ambiguities of speech are confined to the little words, chiefly to monosyllables. The longer words are nearly all clearly intelligible. The reason is obvious, for the greater number of elements there are in a word the less likelihood is there that another word can be found that presents exactly the same outline to the eye.

We need never be afraid, therefore, of using long words to a deaf child, if they are within his comprehension. We are apt to have the idea that short words will be simpler, and we sometimes try to compose sentences consisting as much as possible of monosyllabic words, under the impression that such words are easy for the pupil to pronounce and read from the mouth. It is more common, therefore, to present such sentences to beginners than to more advanced pupils. Now, I do not mean to say that these sentences may not be easier for a child to pronounce, but the words used are the most ambiguous to the eye. Such a simple word as "man," for instance, is homophenous with no less than thirteen other words.

A few years ago I dictated a string of words to some pupils, with the object of testing whether they judged by context or were able to distinguish words clearly by the eye. The results are instructive. Among the words dictated occurred the following: "Hit—rate—ferry—aren't—hat—four—that—reason—high—knit—donned—co." I told the pupils not to mind whether they understood what I said or not, but simply to write down what they thought the words looked like, and what do you think they wrote? Upon examining their slates I found that nearly every child had written the following sentence: "It rained very hard, and for that reason

I did not go." I told the pupils to be very careful to observe whether they could distinguish any difference between the words I uttered and the words they wrote. I therefore went over the whole string of words again, articulating them one by one very distinctly. No difference whatever was detected.

The mother of one of my pupils was present, and was greatly astonished to see her daughter writing down words so different from those I had pronounced. She said that she could not have believed that her daughter could have been so stupid; but her surprise was increased when she found that the other children had written the same sentence. I told her that there was no difference in appearance between the words I had uttered and the words they had written. She desired to test the matter herself with her own child. She asked her daughter to repeat after *her* the words I had written, but the result was the same. The last part of the sentence she repeated at least a dozen times, without shaking her daughter's confidence in the belief that the words she had uttered were precisely the same as those spoken by her mother. To one who could hear, it was a startling revelation to observe the confidence of the child in the accuracy of her replies.

"Repeat after me," said the mother, as she pronounced the words singly and with deliberate distinctness: "high;" answer, "I;" "knit," ans., "did;" "donned," ans., "not;" "co," ans., "go." "Are you sure you have pronounced the words exactly as I have said them?" Ans. "Yes; perfectly certain." "Try again." "Knit," answer, "did;" "donned," answer "not." "Are you *sure* I said that?" Ans. "Yes; absolutely sure." "Try again," and here the mother mouthed the word "donned," ans., "not." The mother was convinced, and she left the room with the remark that she felt that she had been very cruel to her child through ignorance of the fact that words that were very different to her ear looked alike to her child, and could not possibly be distinguished, excepting by context.

I have seen a teacher attempting to impart instruction to a deaf child by word of mouth. She would speak word by word, and the pupil would repeat after her. Upon one occasion the pupil gave utterance to a very different word from that which had been spoken by the teacher. The latter repeated the word a number of times, opening her mouth to the widest extent, and the boy each time repeated the incorrect expression. The teacher grew annoyed at the supposed stupidity of the pupil, and the pupil grew sulky, and was

discouraged in his attempt to read from the mouth ; whereas, in reality, it was not the stupidity of the boy that was in the way of his progress, but the ignorance of the teacher, who did not know that the words that were so different to her ear were absolutely alike to his eye.

Some teachers, in their anxiety to teach speech-reading to their pupils, have the idea that they should refrain from every other mode of communication, so that their pupils may be forced to observe the movements of the mouth, and the mouth alone. For instance, it is easy to write an ambiguous word or to spell it by a manual alphabet, but some teachers refrain from doing so, under the impression that this practice leads the pupil to depend upon the hand instead of the mouth.

Again, deaf persons gather an idea of the emotion that actuates a speaker by the expression of his countenance. In fact facial expression is to the eye what the modulation of the voice is to the ear. It gives life to the inaudible utterances of the mouth ; but there are some teachers who are so afraid that their pupils may come to depend upon the face instead of the mouth, that they think they should assume an impassive countenance from which nothing could be inferred.

Requisites to the Art of Speech-reading.

If we examine the visibility of speech and the causes of its intelligibility, we shall find that there are three qualifications that must be possessed by a deaf child in order that he may understand readily the utterances of his friends. Omit any one of these qualifications and good speech-reading is an impossibility :

I. The eye must be trained to recognize readily those movements of the vocal organs that are visible. Has this ever been done? Have not pupils been required to grapple with all the difficulties of speech-reading at once, and to observe not only the movements of the vocal organs, but to find out the meaning of what is said?

II. I have already explained that certain words have the same appearance to the eye, and it is necessary, if the pupil is to understand general conversation, that he shall know the words that look alike, so that a given series of movements of the vocal organs shall suggest to his mind not a single word, but a group of words, from which selection is to be made by context.

An illustration will explain what I mean. There are many

words which have the same sound to the ear, but different significations. For instance, were I to ask you to spell the word "râne," you could not tell whether I meant "rain," "rein," or "reign." These words sound alike, but they lead to no confusion, for they are readily distinguished by context. In the same way "homophenous words," or words that have the same appearance to the eye, are readily distinguished by context.

As a general rule when a teacher finds that her pupil does not understand a given word, she supposes the non-comprehension to be due to an untrained eye, and this leads to the patient repetition of the word with widely opened mouth, to make the action of the organs more visible. This, unintentionally, enables the pupil to acquire a knowledge of homophenous words; for, when he fails to understand in the first instance, he is requested to try again. He then guesses at the meaning. He thinks of all the words that past experience has taught him looked something like the word proposed, and after a series of guesses generally succeeds in his attempt to unravel the meaning.

In this way success comes at last, not in consequence of the pupil seeing more than he saw at first, but in consequence of knowledge gained by experience of failure. He learns what words present the same appearance to the eye. Let teachers find out the words that look alike, and teach them in groups to their pupils. In this way instruction will take the place of painful experience.

III. The third requisite to good speech-reading is familiarity with the English language. Familiarity with our language, either in its written or spoken form, is absolutely essential in order that a deaf person may make use of context in his attempt to decipher our speech. It is a mental problem that the deaf child has to solve and not solely a problem of vision. The eyes of the congenitally deaf, if there is any difference at all, are rather stronger and better than the eyes of those who become deaf from disease; and yet, as a class, the congenitally deaf acquire the art of speech-reading with much more difficulty than those who could speak before they became deaf. The reason is, that, as a class, the former have not a vernacular knowledge of our language even in its written form, while the latter have. Children who become deaf in infancy from disease are at as great a disadvantage in this respect as the congenitally deaf, and for the same reason.

I shall inquire more particularly into the cause of this lack of

familiarity with the English language, and I shall show that it results from a wide-spread fallacy regarding the nature of language and the means by which our language should be taught. In the meantime I shall simply direct attention to the fact that those who are deaf from infancy do not, as a general rule, become familiar with the English language even in its written form.

It is obvious that if we talk to deaf children by word of mouth, and refrain from explaining, by writing or some other clearly visible means, the words that are ambiguous, those pupils who are already familiar with the language have very great advantages over the others. They have a fund of words from which to draw, they can guess at the ambiguous word and substitute other words within their knowledge so as finally to arrive at the correct meaning. But young children who have been deaf from infancy and who never, therefore, have known our language, are not qualified at once for this species of guess-work. They know no words excepting those we teach them, and have, therefore, no fund to draw upon in case of perplexity. If we commence the education of such children by speech-reading alone they are plunged into difficulties to which they have not the key.

To such children it becomes a matter of absolute necessity that our language should be presented to them in an unambiguous form. With such pupils, writing should be the main reliance, and speech-reading can only be satisfactorily acquired by the constant accompaniment of writing, or its equivalent—a manual alphabet. I have no hesitation in saying that the attempt to carry on the general education of young children who are deaf from infancy by means of articulation and speech-reading alone, without the habitual use of English in a more clearly visible form, would tend to retard their mental development. I do not mean to say that this is ever actually done, but I know there is a tendency among teachers of articulation to rely too much upon the general intelligibility of their speech. Let them realize that the intelligibility is almost entirely due to context, and they will rely more upon writing and less upon the mouth in their instructions to young congenitally deaf children.

After a probationary period, pupils who could speak before they became deaf become so expert in speech-reading that the regular instruction of the school-room can be carried on through its means without detriment to the pupil's progress. The exceptional cases of congenitally deaf persons who have become expert in this art

assures us that, with all who are deaf from infancy, we can certainly achieve the same results if only we can give them a sufficient knowledge of our language, at least in its written form. In the early stages of the education of the congenitally deaf it appears to me that written English should be made the vernacular of the school-room, and that all words or sentences written should also be spoken by the teacher and read by the pupils from the mouth. When the English language has become vernacular there is no reason why instruction should not also be given by word of mouth alone (as in the case of those who could speak before they became deaf) without interfering with mental development.

Before leaving this subject I would say that it is of importance to remember that speaking and understanding speech by the eye are two very different things. We can all of us speak very readily, but I fancy it would puzzle most of us to be called upon to tell what a speaker says by watching his mouth. The congenitally deaf can certainly be taught to speak intelligibly even by persons unfamiliar with the mechanism of articulation. Such pupils should therefore be taught to articulate, and their vocal organs should be continually exercised in the school-room by causing them to speak as well as to write. The congenitally deaf can be taught to articulate even *before* they are familiar with English, but I do not think they can acquire the power of understanding ordinary conversational speech by watching the mouth, at least to any great extent, until *after* they have become familiar with our language.

Gesture Language.

I have already stated that the old fallacy, "without speech there can be no reason," prevented for hundreds of years any attempt at the education of the deaf and dumb, and now I come to the memorable experiment that forever exploded the fallacy. Towards the latter end of the last century the Abbe de l'Epee, during the course of his ministration in Paris, entered a room in which two girls were sewing. He addressed some remarks to them, but received no reply. These girls were deaf and dumb. At once the kind heart of the good Abbe was touched, and he determined to devote his life to the amelioration of the condition of the deaf and dumb.

He gathered together quite a number of deaf children, who made their home with him. He spent his time in their society and devoted to their comfort all that he possessed, reducing himself even

to poverty for their sake. He soon observed that these children were communicating with one another, but not by speech. They were inventing a language of their own, unlike any of the spoken languages of the earth—a language of gestures. These children were reasoning by means of this language; they were thinking in gestures instead of in words, and the idea occurred to the Abbe de l’Epee that the old dogma that had for so many hundred years prevented the education of the deaf was a fallacy. Here was nature developing an instrument of reason with which speech had nothing to do. Why should he not study this gesture language and assist these children in their attempts to perfect a means of communication of this kind, and why should he not use this means of communication so as to lead their minds to higher and ever higher thoughts? He did so and succeeded in developing the “sign language” that is now so extensively employed in this country in the education of the deaf. The experiment at once attracted attention. Kings and Emperors visited the humble abode of the Abbe de l’Epee and were astonished by what they saw. He conversed with his pupils in the gesture language, and he taught them through its means the meaning of written French, so that they were enabled to communicate with hearing persons by writing.

The Fallacy that a Gesture Language is the only Form of Language that is Natural to the Congenitally Deaf.

The old fallacy was done away with, but a new one immediately took its place, which has been introduced into our country with the language of signs, and is now the main obstacle to the acquisition of English by the congenitally deaf. The fallacy to which I allude is that this gesture language is the only language that is natural to the congenitally deaf, and that therefore such children must acquire this language as their vernacular before learning the English language, and must be taught the meaning of the latter through its means. To my mind such a statement consists of a succession of fallacies, each one resting on the preceding. The proposition that the sign language is the only language that is natural to congenitally deaf children is like the proposition that the English language is the only language that is natural to hearing children. It is natural only in the same sense that English is natural to an American child. It is the language of the people by whom he is surrounded. A congenitally deaf child who for the first time enters an insti-

tution for the deaf and dumb finds the pupils and teachers employing a gesture language which he does not understand; but in time he comes to understand it, and learns by imitation to use it, just as an American child in Germany comes in time to understand and speak German.

Although congenitally deaf children, when they enter an institution, do not understand or use the sign language as there employed, they each know and use a gesture language of some kind, which they employ at home in communicating with their friends and relatives. Hence it is argued that if the "sign language" employed in our institutions is not the only one, a gesture language of some kind is necessarily the vernacular of the congenitally deaf child. The scope of the statement is thus widened, and the proposition we have now to consider may be thus expressed: Gesture language, in the wider sense, is the only form of language that is natural to those who are congenitally deaf.

It is a matter of great importance to the 34,000 deaf-mutes of this country, and to their friends and relatives, as well as to all persons who are interested in the amelioration of the condition of the deaf and dumb, that we examine this proposition with care and decide whether it is a fallacy or not. To my mind it is a fallacy based upon another concerning the nature of language itself, namely, that there is such a thing as a natural language. Such an idea has led to errors in the past, and will ever continue to do so. We have all read of the monarch of ancient times, who is recorded to have shut up a number of little children by themselves, and to have given orders to their attendants to hold no communication with them, so that he might observe what language they would naturally speak as they grew up. It is recorded that the first word uttered was a Greek word, from which it was argued that the Greek language was the natural language of mankind.

In the seventeenth century the ingenious Van Helmont was imbued with the idea that the Hebrew language was of divine origin, from which he argued that Hebrew was the natural language of mankind, and that the shapes of the Hebrew letters had some natural relation to the sounds they represented; that they pictured, in fact, the positions of the vocal organs in forming the sounds. The latter idea led him to employ the characters as a means of teaching articulation to a deaf-mute; but the former idea led him to teach his deaf-mute Hebrew, instead of his native tongue.

When we examine the languages of the world that are naturally acquired by hearing children, we fail to discover any natural connection between the sounds of the words and the things they represent; everything is arbitrary and conventional.

Origin and Mode of Growth of a Gesture Language.

Now, let us examine for a moment the nature of a gesture language and the manner in which it comes into existence. You are, we shall suppose, a farmer, and your little deaf boy comes running into the house in great excitement, anxious to tell you something he has observed. How does he do so?

We shall imagine a case. He commences by placing his hands above his head, bowing low, and marching about the room, after which he points out of the window.

You shake your head; you have not the remotest idea what he means.

His face assumes an anxious look, and down he goes upon his hands and knees, and scrambles over the floor, touching the carpet with his mouth from time to time, and then again points out of the window.

Still you do not comprehend.

A look of perplexity crosses his face. What can he do to make you understand? At last his face lights up, as a new thought comes into his mind, and he touches the bridge of his nose and again points out of the window.

But, alas! alas! you cannot understand.

The little fellow is perplexed and troubled. At last, in despair, he takes hold of your coat and pulls you out of the door, around the corner, and *you find your cow in the turnip patch.*

Now you begin to understand what it was he meant to say; he had tried to picture the cow, and to imitate its actions. The hands held above the head had indicated the horns; the scrambling on the floor on his hands and knees had imitated the action of a four-footed animal, and his mouth to the carpet meant the cow eating the turnips.

But how about the bridge of his nose?

You will probably observe that the cow to which he referred had some white spot or other mark upon the nose, and the gesture of the child had not indicated a cow in general, but your black cow "Bessie," with the white spot on her nose, in particular.

Having advanced thus far in the comprehension of his meaning, do you think that the child will take the trouble to go through this same pantomime the next time he wishes to tell you about your cow? No. He may commence such a pantomime, but before he gets half through you understand what he means, and he never completes it. A process of abbreviation commences, until finally a touch on the bridge of his nose alone becomes the name of your black cow "Bessie," and the simple holding of his hands above his head conveys to your mind the idea of a cow in general.

By a natural process of abbreviation the child arrives at a simple gesture or sign for every object or thing in which he is interested.

But there are many thoughts he desires to express which are abstract in their nature. How, for instance, can he indicate by any sign the color of an object? Suppose, by way of illustration, that he desired to communicate to you the idea that he had seen in the road a cow that was perfectly white?

I shall try to depict the conversation between yourself and your deaf boy as it might actually have occurred.

THE BOY. The boy points to the road, touches his teeth, and holds his hands above his head.

You gather from this a vague idea of some connection between that road, the boy's teeth, and a cow.

Here is a problem: What did he mean? It is pretty clear that he had seen a cow in the road, but what connection had his teeth with that? Perhaps the cow's teeth were peculiar. You think you had better get him to explain, so—

THE FATHER. You touch your teeth with an interrogative and puzzled look.

THE BOY. The boy responds by showing you his shirt sleeve and pointing to the road.

Can he mean that there was any connection between his shirt sleeve and the cow. To clear this point—

THE FATHER. You touch his shirt sleeve and raise your hands above your head with a look of interrogation.

THE BOY. The boy nods vigorously, raises his hands above his head, and makes his sign for "snow," followed by other signs for objects that are white.

After he has presented a sufficient number of such signs, you perceive that the one thing common to them all was their color—they

were white. And thus you gain the idea that the cow was white.

Do you suppose he goes through this process every time he desires to communicate the idea of white? No; he remembers the object which had conveyed to your mind the idea that that cow was white, and the sign for this object is ever after used as an adjective, qualifying the object the whiteness of which he desires to indicate. Of course you cannot predicate what this particular sign may be. I have seen children who have conveyed the idea by touching their teeth; others who expressed it by an undulatory downward movement of the hand, expressive of the way in which a snow-flake falls to the ground.

It will thus be understood that a deaf child first commences to express his ideas by pantomime, and that by a process of abbreviation pantomimic gestures come to be used in a conventional manner. Pantomime is no more entitled to the name of language than a picture is, although many ideas can be conveyed through its means. In proportion as it becomes more conventional and arbitrary it becomes more and more worthy of the name of language.

The Sign-Language of Our Institutions.

Now, when the deaf children who lived with the Abbe de l'Epee were first brought together, each of them used a gesture-language he had invented for himself as a means of communicating with his friends at home. Thus there were as many gesture-languages as there were children. The only element common to these languages was probably the pantomime from which they had all sprung. But now what happened? Association and the necessity of intercommunication led to the adoption of common signs. Each child presented his gestures to his fellows, and by a process of selection those signs that appeared to the majority to be most fitting survived, and were adopted by the whole; and the synonymous signs, which were not so well fitted, were either forgotten by disuse or used in a new meaning to express other ideas.

I do not wonder at the interest displayed in this growth by the Abbe de L'Epee and his contemporaries. To my mind it was the most interesting and instructive spectacle that has ever been presented to the mind of man—the *gradual evolution of an organized language from simple pantomime.*

When, in 1817, the first school for the deaf and dumb was opened in America, the sign-language as used in the school of the Abbe de

l'Epee (then under the charge of his successor, the Abbe Sicard) was imported from France, and became the medium of instruction. The teachers trained in this school naturally became the principals of other institutions established upon its model, and thus the sign-language has been diffused over the length and breadth of our land.

I heartily agree with all that experienced teachers of the deaf have urged concerning the beauty and great interest of this gesture language. It is indeed interesting to observe how pantomimic gestures have been abbreviated to simple signs expressive of concrete ideas; how these have been compounded or have changed their meaning to indicate abstract thoughts; and how the sequence of the sign-words has to a certain extent become obligatory, thus forming a sort of gesture syntax or grammar.

The original stock or stocks from which our languages are derived must have disappeared from earth ages before historic times; but in the gesture speech of the deaf we have a language whose history can be traced *ab origine*, and it has appeared to me that this fact should give it a unique and independent value. In the year 1878, in a paper read before the Anthropological Society of London, I advocated the study of the gesture language by men of science; for it seemed to me that the study of the mode in which the sign language has arisen from pantomime might throw a flood of light upon the origin and mode of growth of all languages.

You may ask why it is that, with my high appreciation of this language *as a language*, I should advocate its entire abolition in our institutions for the deaf.

I admit all that has been urged by experienced teachers concerning the ease with which a deaf child acquires this language, and its perfect adaptability for the purpose of developing his mind; but after all it is not the language of the millions of people among whom his lot in life is cast. It is to them a foreign tongue, and the more he becomes habituated to its use the more he becomes a stranger in his own country.

This is not denied by teachers of the deaf and dumb, but the argument is made, as I have stated above, that it is the only language that is natural to congenitally deaf children, or that at all events, some form of gesture language must necessarily be their vernacular, and be employed to teach our English tongue.

The Fallacy that a Gesture Language is the only form of Language in which a Congenitally Deaf Child can Think.

Now what do we mean by a language being "natural" or not? I cannot believe that in this 19th century any one really entertains the fallacy that there is a natural language *per se*. So I presume that that language is considered natural to a person in which he thinks. Under this meaning the proposition assumes this shape: The sign language taught in our institutions, or a gesture language of some kind, is the only form of language in which a congenitally deaf child can think; that is, it is the only language of which the elements can be associated directly with the ideas they express.

In this form the fallacy is easily exploded, for in the course of the last one hundred years so many experiments have been made in the education of the deaf that we now know with absolute certainty that deaf children can be taught to associate written words directly with the ideas they represent; and when they are taught to spell these words by a manual alphabet, the movements of the fingers become so natural a method of giving vent to their thoughts that even in sleep their fingers move when they dream.

Not only has written English been made the vernacular of congenitally deaf children, but the same result has been achieved with written French, German, Spanish, Dutch, and other languages.

Congenitally deaf children who have been taught articulation move their mouths in their sleep and give utterance to words when they dream.

Laura Bridgman, the blind deaf-mute, was taught by the late Dr. Howe to gather ideas through the sense of touch. English words printed in raised letters were presented to her sense of touch in connection with the objects which they represented, and she associated the impressions produced upon the ends of her fingers with the objects themselves. The English language in a *tangible* form became her vernacular.

All these facts assure us that any form of language may become natural to a deaf child by usage, so long as it is presented to the senses he possesses. There is only one way that language is naturally acquired, and that is by usage and imitation. Any form of language that can be clearly appreciated by the senses the deaf child possesses, will become his vernacular if it is used by those about him.

Why the Deaf employ a Gesture Language.

A gesture language is employed by a deaf child at home, not because it is the only language that is natural to one in his condition, but because his friends neglect to use in his presence any other form of language that can be appreciated by his senses. Speech is addressed to his ear; but his ear is dead, and the motions of the mouth cannot be fully interpreted without previous familiarity with the language. On account, therefore, of the neglect of parents and friends to present to his eye any clearly visible form of language, the deaf child is forced to invent such a means of communication, which his friends then adopt by imitation. I venture to express the opinion that no gesture language would be developed at home by a deaf child if his parents and friends habitually employed, in his presence, the English language in a clearly visible form. He would come to understand it by usage, and use it by imitation.

An old writer, George Dalgarno, in 1680, expressed the opinion, in which I fully concur, that "there might be successful addresses made to a dumb child even in its cradle, *risu cognoscere matrem*, if the mother or nurse had but as nimble a hand as usually they have a tongue."

When deaf children enter an institution they find the other pupils and the teachers using a form of gesture language which they do not understand. For the first time in their lives they find a language used by those about them that is addressed to the senses they possess. After a longer or shorter time they discard the language that they had themselves devised, and acquire, *by imitation*, the sign language of the institution.

Harmful Results of the Sign Language.

After a few months residence in the institution, the children return to their friends in the holidays using easily and fluently a language that is foreign to them, while of the English language they know no more than the average school boy does of French or German after the same period of instruction. The only language they can employ in talking to their friends is the crude gesture language of their own invention, which they had long before discarded at school; and they perpetually contrast the difficulty and slowness of comprehension of their friends with the ease with which their school fellows and teachers could understand what they mean. They have

learned by experience how sweet a thing it is to communicate freely with other minds, and they are continually hampered and annoyed by the difficulty they meet with in conversing with their own parents and friends.

Can it be wondered at, therefore, that such a child soon tires of home? He longs for the school play-ground, and the deaf companions with whom he can converse so easily. Little by little the ties of blood and relationship are weakened, and *the institution becomes his home*.

Nor are these all the harmful effects that are directly traceable to the habitual use in school, as a means of communication, of a language foreign to the mass of the people. Disastrous results are traceable inwards in the operation of his mind, and outwards in his relation to the external world in adult life. He has learned to *think* in the gesture-language, and his most perfected English expressions are only translations of his sign speech.

As a general rule, when his education is completed, his knowledge of the English language is like the knowledge of French or German possessed by the average hearing child on leaving school. He cannot read an ordinary book intelligently without frequent recourse to a dictionary. He can understand a good deal of what he sees in the newspapers, especially if it concerns what interests him personally, and he can generally manage to make people understand what he wishes by writing, but he writes in broken English, as a foreigner would speak.

Let us consider for a moment the condition of a person whose vernacular is different from that of the people by whom he is surrounded. Place one of our American school boys just graduated from school in the heart of Germany. He finds that his knowledge of German is not sufficient to enable him to communicate freely with the people. He thinks in English, and has to go through a mental process of translation before he can understand what is said, or can himself say what he means. Constant communication with the people involves constant effort and a mental strain. Under such circumstances what a pleasure it is for him to meet with a person who can speak the English tongue. What a relief to be able to converse freely once more in his own vernacular. Words arise so spontaneously in the mind that the thought seems to evoke the proper expression.

But mark the result: the more he associates with English-

speaking people the less desire does he have to converse in German. The practice of the English language prevents progress in the acquisition of German. I have known of English people who have lived for twenty years in Germany without acquiring the language.

If our American school boy desires to become familiar with the German language, he must resolutely avoid the society of English-speaking people. He then finds that the mental effort involved in conversation becomes less and less, until, finally, he learns to think in German, and his difficulties cease.

Now consider the case of a deaf boy just graduated from an institution where the sign language has been employed as a means of communication. His vernacular is different from that of the people by whom he is surrounded. He thinks in the gesture language and has to go through a mental process of translation before he can understand what is said or written to him in English, and before he can himself speak or write in English what he desires to say. He finds himself in America, in the same condition as that of the American boy in Germany. If he avoids association with those who use the sign language, and courts the society of hearing persons, the mental effort involved in conversation becomes less and less, and finally he learns to think in English and his difficulties cease.

But such a course involves great determination and perseverance on the part of the deaf boy, and few, indeed, are those who succeed.

Not only do the other deaf-mutes in his locality have the same vernacular as his own, but they were his school fellows, and they have a common recollection of pleasant years of childhood spent in each other's society. Can it be wondered at, therefore, that the vast majority of the deaf graduates of our institutions keep up acquaintance with one another in adult life? The more they communicate with one another the less desire they have to associate with hearing persons, and the practice of the gesture language forms an obstacle to further progress in the acquisition of the English language.

These two causes (*a*) previous exclusive acquaintance with one another in the same school, and (*b*) a common knowledge of a form of language specially adapted for the communication of the deaf with the deaf, operate to attract together into the large cities large numbers of deaf persons, who form a sort of deaf community or society, having very little intercourse with the outside world.

They work at trades or businesses in these towns, and their leisure hours are spent almost exclusively in each other's society. Under such circumstances can we be surprised that the majority of these deaf persons marry deaf persons, and that we have as a result a small but necessarily increasing number of cases of hereditary deafness due to this cause. Such unions do not generally result in the production of deaf offspring, because the deafness of the parents in a large proportion of cases is of accidental origin, and accidental deafness is no more likely to be inherited than the accidental loss of a limb. Still I would submit that the constant selection of the deaf by the deaf in marriage is fraught with danger to the community.

Why the English Language should be Substituted for the Sign Language as a Vernacular.

If we examine the position in adult life of deaf children who have been taught to speak, or who have acquired the English language as a vernacular, whether in its written or spoken forms, we find an entirely different set of tendencies coming into play, especially if these persons have not been forced in childhood to make the acquaintance of large numbers of other deaf children, by social imprisonment for years together in the same school or institution apart from the hearing world.

Their vernacular use of the English language renders it easy for them to communicate with hearing persons by writing, or by word of mouth if they have been taught to articulate; and hearing persons can easily communicate with them by writing, or by word of mouth if they have been taught the use of the eye as a substitute for the ear. The restraints placed upon their intercourse with the world by their lack of hearing leads them to seek the society of books, and thus they tend to rise mentally to an ever higher and higher plane. A cultivated mind delights in the society of educated people, and their knowledge of passing events derived from newspapers forms an additional bond of union between them and the hearing world.

If they have formed in childhood few deaf acquaintances, they meet in after life hundreds of hearing persons for every deaf acquaintance, and if they marry, the chances are immensely in favor of their marrying hearing persons.

There is nothing in the deaf-mute societies in the large cities to

attract them, and much to repel them; for the more highly educated deaf-mutes in these societies speak what is to them a foreign language; while the greater number of the deaf-mutes to be found there are so ignorant that self-respect forbids them from mingling with them.

Thus the extent of their knowledge of the English language is the main determining cause of the congregation or separation of the deaf in adult life. A good vernacular knowledge of the English language operates to effect their absorption into society at large, and to weaken the bonds that tend to bring them together; whereas, a poor knowledge of the language of the country they live in causes them to be repelled by society and attracted by one another; and these attractive and repulsive tendencies are increased and intensified if they have been taught at school a language foreign to society and specially adapted for intercommunication among themselves. I say, then, let us banish the sign language from our schools. Let the teachers be careful in their intercourse with their pupils to use English and English alone. They can write, they can speak by word of mouth, they can spell the English words by a manual alphabet, and by any or all of these methods they can teach English to their pupils as a native tongue.

Conclusion.

In conclusion allow me to say:

1. That those whom we term "deaf-mutes" have no other natural defect than that of hearing. They are simply persons who are deaf from childhood and many of them are only "hard-of-hearing."

2. Deaf children are dumb, not on account of lack of hearing, but of lack of instruction. No one teaches them to speak.

3. A gesture language is developed by a deaf child at home, not because it is the only form of language that is natural to one in his condition, but because his parents and friends neglect to use the English language in his presence in a clearly visible form.

4. (a) The sign language of our institutions is an artificial and conventional language derived from pantomime.

(b) So far from being natural either to deaf or hearing persons, it is not understood by deaf children on their entrance to an institution. Nor do hearing persons become sufficiently familiar with the language to be thoroughly qualified as teachers until after one or more years' residence in an institution for the deaf and dumb.

(c) The practice of the sign language hinders the acquisition of the English language.

(d) It makes deaf-mutes associate together in adult life, and avoid the society of hearing people.

(e) It thus causes the intermarriage of deaf-mutes and the propagation of their physical defect.

5. Written words can be associated directly with the ideas they express, without the intervention of signs, and written English can be taught to deaf children by usage so as to become their vernacular.

6. A language can only be made vernacular by constant use as a means of communication, without translation.

7. Deaf children who are familiar with the English language in either its written or spoken forms can be taught to understand the utterances of their friends by watching the mouth.

8. The requisites to the art of speech-reading are :

(a) An eye trained to distinguish quickly those movements of the vocal organs that are visible (independently of the meaning of what is uttered.)

(b) A knowledge of *homophenes* ;* that is, a knowledge of those words that present the same appearance to the eye ; and

(c) Sufficient familiarity with the English language to enable the speech-reader to judge by context which word of a homophonous group is the word intended by the speaker.

If we look back upon the history of the education of the deaf, we see progress hindered at every stage by fallacies. Let us strive, by discussion and thought, to remove these fallacies from our minds so that we may see the deaf child in the condition that nature has given him to us. If we do this, I think we shall recognize the fact that the afflictions of his life are *mainly due to ourselves*, and we can remove them.

Nature has been kind to the deaf child, man cruel. Nature has inflicted upon the deaf child but one defect—imperfect hearing ; man's neglect has made him dumb and forced him to invent a language which has separated him from the hearing world.

Let us, then, remove the afflictions that we ourselves have caused.

* This word was suggested to me some years ago by Mr. Homer, lately Principal of the Providence (R. I.) School for Deaf-Mutes, and has now been permanently adopted.

1. Let us teach deaf children to think in English, by using English in their presence in a clearly visible form.
2. Let us teach them to speak by giving them instruction in the use of their vocal organs.
3. Let us teach them the use of the eye as a substitute for the ear in understanding the utterances of their friends.
4. Let us give them instruction in the ordinary branches of education by means of the English language.
5. And last, but not least, let us banish the sign language from our schools.

If it were our object to fit deaf children to live together in adult life and hold communication with the outside world as we hold communication with other nationalities than our own, then no better plan could be devised than to assist the development of a special language suitable for intercommunication among the deaf.

But if, on the other hand, it is our object to destroy the barriers that separate them from the outside world and take away the isolation of their lives, then I hold that our energies should be devoted to the acquisition of the English language as a vernacular in its spoken and written forms. With such an object in view we should bring the deaf together as little as possible and only for the purpose of instruction. After school hours we should separate the deaf children from one another to prevent the development of a special language and scatter them among hearing children and their friends in the outside world.

The subject being presented to the Society for discussion, Mr. E. M. GALLAUDET spoke, in substance, as follows:

I have listened with great interest to the remarks of Mr. Bell this evening, and am ready to agree in many particulars with the views he has so well presented.

I am, however, compelled to differ with him at several points; and as these involve matters of vital importance in the treatment of the deaf, I will beg the indulgence of the Society for a short time, while I attempt to show to what extent some of Mr. Bell's views are erroneous.

In proving the generally received opinion that the vocal organs of persons deaf from infancy are defective, to be a fallacy, Mr. Bell declared that difficulties encountered by such persons in acquiring speech are wholly external to themselves, and that all

persons so situated can, with proper instruction, be taught to speak and to understand the motions of the lips of others.

That this is a grave error has been proved by the experience of more than a century of oral teaching in Germany.

The late Moritz Hill, of Wessenfels, Prussia, a man of the widest experience and highest standing among the oral teachers of Europe, expressed to me the opinion a few years since that out of one hundred deaf-mutes, including the semi-mute and semi-deaf, only "eleven could converse readily with strangers on ordinary subjects" on leaving school. Of course a much larger number would be able to converse with their teachers, family, and intimate friends on common-place subjects; but it would be found that very many could never attain to any ready command of speech.

The explanation of this lies in the fact that a child, deaf from infancy, in order to succeed with speech and lip-reading must possess a certain quickness of vision, a power of perception, and a control over the muscles of the vocal organs, by no means common to all such children.

Mr. Bell's view has been held by many instructors with more or less tenacity, and *this* fact is explained by a readiness on their part to argue from the particular to the general. Having attained marked success with certain individuals, they draw, in their enthusiasm, the mistaken conclusion that success is possible in the case of every other deaf child, overlooking the fact that many things, besides the mere deafness of the child, may affect the result. Experience has demonstrated that in attempting to teach the deaf to speak, failure in many cases must be anticipated.

Mr. Bell is mistaken in supposing ignorance as to the mechanism of the vocal organs to be a prominent cause of failure to impart speech to the deaf. It is no doubt true that among persons unfamiliar with the training of the deaf, few have made the mechanism of speech a study; but in Germany, Italy, and France, not to speak of our own country, many are to be found who may be said to have mastered this subject. The results of their labors have been made available to instructors of the deaf, and all the best oral schools are profiting thereby.

Mr. Bell is also mistaken when he says that "in a majority of our schools and institutions articulation and speech-reading are taught to only a favored few, and in these schools no use of articulation is made as a means of communication," and that "few, if

any, attempts are made to teach articulation to those who have not naturally spoken." In most of the larger institutions for the deaf in this country, every pupil is afforded an opportunity to acquire speech, and instruction in this is discontinued only when success seems plainly unattainable.

It is a great error to suppose it to be true of a deaf person educated on what Mr. Bell calls the sign-method, that, "as a general rule, when his education is completed, his knowledge of the English language is like the knowledge of French or German possessed by the average hearing child on leaving school," or to say that "he cannot read an ordinary book intelligently without frequent recourse to a dictionary." On the contrary, a majority of persons thus educated have a good knowledge of their vernacular, are able to use it readily as a means of communication with hearing persons, and *are* able to read intelligently without frequent recourse to the dictionary.

When Mr. Bell has become familiar with the peculiarities of the deaf by personal contact with a large number of this class of persons, I am confident he will not repeat his assertion that "nature has inflicted upon the deaf child but one defect—imperfect hearing." For he will then have discovered, what has long been known to teachers of experience, that deaf children, in addition to their principal disability, are often found to be lacking in mental capacity, or in the imitative faculty, in the power of visual or tactile perception, and in other respects; all of which deficiencies, though they do not amount even to feeble-mindedness, much less to idiocy, do operate against the attainment of success in speech, as well as in other things which go to complete the education of such children.

Passing over several points of relatively small importance, in regard to which I believe Mr. Bell's views to be subject to criticism, I come to his characterization as a fallacy of the opinion held by many "that the language of gestures is the only language natural to the child born deaf or who has become deaf in infancy."

I think that in order to sustain his view that this is a fallacy Professor Bell gives a strained and very unusual meaning to the words "natural language." If, as he explains, a natural language is any one that a child may happen to be first taught by those with whom he is associated, then I should have no controversy with him. But I understand a natural language to be one that is mainly spontaneous, and not at all one that is borne in upon a child from without.

Moritz Hill, to whom I have already alluded, speaks of the language of signs as "one of the two universally intelligible innate forms of expression granted by God to mankind," the other being speech. Now it is hardly necessary to urge that speech is the form of expression natural to hearing persons, and I think a little reflection will satisfy most persons that with the deaf the language of signs is the only truly natural mode of expressing their thoughts.

Mr. Bell urges that the use of signs in the education of the deaf is a hinderance rather than a help, and that it would be better to banish them altogether. To this view I must give my earnest dissent.

I might, of course, cite the opinions of very many successful instructors of the deaf, who have followed only the sign method, to sustain my position, but I prefer to call in again the testimony of Moritz Hill, a man whose whole life was devoted to the instruction of the deaf by the oral method. In an exhaustive work on the education of the deaf,* Hill says, speaking of those who pretend that in the "German method" every species of pantomimic language is proscribed :

"Such an idea must be attributed to malevolence or to unpardonable levity. This pretence is contrary to nature and repugnant to the rules of educational science.

"If this system were put into execution the moral life, the intellectual development of the deaf and dumb, would be inhumanly hampered. It would be acting contrary to nature to forbid the deaf-mute a means of expression employed by even hearing and speaking persons. * * * It is nonsense to dream of depriving him of this means until he is in a position to express himself orally. * * * Even in teaching itself we cannot lay aside the language of gestures (with the exception of that which consists in artificial signs and in the manual alphabet—two elements proscribed by the German school), the language which the deaf-mute brings with him to school, and which ought to serve as a basis for his education. To banish the language of natural signs from the school-room and limit ourselves to articulation is like employing a gold key which does not fit the lock of the door we would open and refusing to use the iron one made for it. * * * At the best, it would be *drilling* the deaf-mute, but not *moulding* him intellectually or morally."

* Der gegenwärtige Zustand des Taubstummen Bildungswesens in Deutschland; von Hill, Inspector der Taubstummen Anstalt zu Wettsenfels; Ritter des St. Olafs, &c. Weimar, H. Böhlau, 1866.

Hill then follows with thirteen carefully formulated reasons why the use of signs is important and even indispensable in the education of the deaf.

Mr. Bell is in error when he supposes that in the so-called sign-schools verbal language is only imparted through the intervention of the sign-language. In many well-ordered schools of this class, language is taught without the use of signs, and in such schools the language of signs is kept in its proper position of subordination. It goes without saying that in schools for the deaf there may be an injudicious and excessive use of signs. This is always to be guarded against, and when it is, I am convinced that no harm, but great good, results from the use of signs in teaching the deaf.

Furthermore, it is well known that the attempt to banish signs from a school for the deaf rarely succeeds. Miss Sarah Porter, for three years an instructor in the Clarke Institution at Northampton, Mass., an oral school in which most excellent results have been attained, shows candor as well as judgment when she says, in a recent article in the *American Annals of the Deaf and Dumb*, "Every oral teacher knows that fighting signs is like fighting original sin. Put deaf children together and they will make signs secretly if not openly in their intercourse with each other."

It is not true as a matter of fact that the use of signs necessarily prevents the deaf from acquiring an idiomatic use of verbal language and from thinking in such language. Large numbers of them who have never been taught orally have come into such a use of verbal language, and while it is granted that many educated under the sign system do not use verbal language freely and correctly, the same is found to be true of very many who have been educated entirely in oral schools.

In one important particular the language of signs performs a most valuable service for the deaf, and one of which nothing has yet been found to take the place. Through signs large numbers of deaf persons can be addressed, their minds and hearts being moved as those of hearing persons are by public speaking in its various forms.

Having seen the good effects on the deaf of the discreet use of the sign-language through a period of many years, I am confident that its banishment from all schools for the deaf would work great injury to this class of persons intellectually, socially, and morally.

The Hon. GARDINER G. HUBBARD being present, was invited by the chair to participate in the discussion. He said he had been connected with the Clark Institution for many years. The deaf pupils in that school are taught entirely by articulation.

From recent inquiries which had been made to ascertain how far the graduates had profited by instruction in articulation, it appeared that in almost in every instance they could carry on conversation with others sufficiently to engage in many kinds of business from which they would have been excluded if they had only used signs.

It was true, as Mr. Gallaudet said, the congenitally deaf were frequently able to articulate more distinctly than those who lost their hearing at an early age, but this arises from the fact that the disease that caused the deafness affected the organs of articulation to a greater or less degree; but the congenitally deaf do not make as rapid progress in their studies as those who had once spoken, for these have a knowledge of language which the former could obtain only by long protracted study.

Mr. Hubbard believed that the pupils at the Clark Institution made at least as rapid progress in all their studies as those taught by signs; while, at the same time, they acquired the power of reading from the lips and speaking, in which those taught by signs were deficient.

When the first application was made to the Legislature of Massachusetts for the incorporation of the Clark Institution, Mr. Dudley, of Northampton, chairman of the committee to whom the petition was referred, had a congenitally deaf child under instruction at Hartford. The petitioners were opposed by the professors from the asylum, as they believed an articulating school would retard the education of the deaf, as it was impractical to teach the deaf by articulation, that system having been tried and proved a failure, and the new method was stigmatized as one of the visionary theories of Dr. Howe, (the principal of the Perkins Institute for the Blind, and the teacher of Laura Bridgeman, the blind deaf mute,) who was associated with the petitioners in the hearing.

The application was rejected through the influence of these professors and of Mr. Dudley, who 'knew, from experience with his own child, that it was impossible to teach the congenitally deaf to talk.'

Two years after, our application was renewed and with better success.

Mr. Hubbard in the meantime, with the aid of Miss Rogers, had opened a small school where the deaf were taught to speak. This school was visited and examined by the committee, and the progress made was so great that Mr. Dudley became a warm convert, convinced that the impossible was possible, and the application was granted, although again opposed by the gentlemen from Hartford. The school was opened at Northampton, and has been in operation for nearly fifteen years, and teaching by articulation has ceased to be a visionary theory.

Many of the warmest friends of the Institution now are, like Mr. Gallaudet, connected with institutions where signs are used. In almost every institution for the deaf classes are now taught to articulate, though articulation is not used as the instrument for instruction.

Mr. Gallaudet had taken exception to the remark of Mr. Bell, that idiots were born dumb, and said that in every school for idiots there were many feeble-minded children who could talk readily; but Mr. Bell used the word idiot not as simply a feeble-minded person, but according to its ordinary meaning, "a human being destitute of reason or the ordinary intellectual powers of man."

It has always been the policy at Northampton to prevent, as far as possible, marriages of deaf with deaf, for the records show that the children of such intermarriages are often deaf; and even where a congenitally deaf person marries a hearing person, the children sometimes are deaf.

The tendency of the intermarriage of the deaf would be to raise a deaf race in our midst.

About one in 1,500 of the population are deaf; but if these intermarriages should take place and a deaf race be created, the proportion would rapidly increase. The object of all friends of the deaf should be to prevent the deaf from congregating, and to induce them to associate with hearing people. In bringing the deaf together in institutions, where they are taught by signs, the tendency is to make the deaf deafer and the dumb more dumb.

It was originally intended to have only a family or small school at Northampton, but it was soon found that signs could not be excluded from the play-ground, as the young children could not communicate in any other way. The plan was changed, the number of pupils was largely increased, and a preparatory department established, in which signs were tolerated on the play-ground. On

the removal of the pupils to the higher departments, the use of signs is forbidden, and they are rarely used on the play-ground or between the pupils, either in or out of school hours.

In the later years of instruction they acquire great facility in articulation and reading from the lips, though there is almost always some difficulty for a stranger to understand them.

Mr. Gallaudet had referred to the International Convention of deaf-mute teachers and their friends, at Milan, three years ago. Mr. Hubbard was present at the convention held this year at Brussels, and was there informed that a delegate had been sent from France to attend the convention at Milan and investigate the method of instruction in Italy, where articulation was used, for the purpose of deciding whether the instruction in the French schools should continue to be by signs, or instruction by articulation be substituted for signs.

The preference of the delegate had been for signs, but on witnessing the results obtained in the Italian schools and hearing the discussion, he was led to advise that the instruction in the French schools hereafter be by articulation, instead of signs, and such a change has, Mr. Hubbard understands, been made in most of the schools of France.

Mr. Hubbard learned from the reports at Brussels that almost all the European schools were taught by articulation, and that this means of instruction was being rapidly substituted for the sign language in England as well as in France.

Mr. BELL, in reply to the remarks of Mr. Gallaudet, said:

There are signs *and* signs. There is the same distinction between pantomime and the sign-language that there is between a picture and the Egyptian hieroglyphics.

Pictures are naturally understood by all the world, but it would be illogical to argue from this that a picture-language, like that developed by the ancient Egyptians, must also be universally intelligible. Pantomime is understood by all the world, but who among us can understand the sign-language of the deaf and dumb without much instruction and practice?

No one can deny that pantomime and dramatic action can be used, and with perfect propriety, to illustrate English expressions so as actually to facilitate the acquisition of our language by the deaf; but the abbreviated and conventionalized pantomime, known

as the "sign-language," is used *in place* of the English language, and becomes itself the vernacular of the deaf child.

Judging from the quotations given by Dr. Gallaudet, Moritz Hill himself makes a clear distinction between pantomime and the sign-language, retaining the former and proscribing the latter. "Every species of pantomimic language is not proscribed," he says. "Natural signs," or "signs employed by hearing and speaking persons," are retained, while "artificial signs" are proscribed.

All the arguments that have been advanced regarding pantomime and a pantomime language are equally applicable to pictures and a picture-language. For instance, we may say that a picture-language is more natural than any of the spoken languages of the world, because pictures are naturally understood by all mankind. We may even arrive, by a further process of generalization, at the idea that picture-language, in the wider sense, really constitutes the only form of language that is natural at all, for all the other languages of the world appear to be entirely arbitrary and conventional. If we pursue the parallel we shall arrive at the conclusion that a picture-language of some kind must necessarily become the vernacular of our pupils, through which the other more conventional languages may be explained and taught.

It is immaterial whether such statements are fallacious or not, so long as we do not apply them to educational purposes. But let us see how they work in practice. The exhibition of a picture undoubtedly adds interest to the fairy tale or story that we tell a child. It illustrates the language we use, and it may be of invaluable assistance to him in realizing our meaning. But is that any reason why we should teach him Egyptian hieroglyphics? Granting the premises: Is the conclusion sound that we should therefore teach him English *by means* of hieroglyphics?

If such conclusions are illogical, then the fundamental ideas upon which our whole system of education by signs is based are also fallacious and unsound.

One word in conclusion regarding speech.

The main cause of the fallacies that fog our conception of the condition of the deaf child is *his lack of speech*. A deaf person who speaks is regarded by the public more as a foreigner than as a deaf mute. Speech, however imperfect, breaks through the barriers of prejudice that separate him from the world, and he is recognized *as one of ourselves*.

Mr. Gallaudet under-estimates the value of speech to a deaf child. He seems to think that speech is of little or no use, unless it is as perfect as our own. The fact is that the value of speech to a deaf child must be measured by its *intelligibility* rather than by its perfection.

It is astonishing how imperfect speech may be and yet be intelligible. We may substitute a mere indefinite murmur of the voice for all our vowel sounds, without loss of intelligibility. (Here Mr. Bell spoke a few sentences in this way, and was perfectly understood.) Here at once we get rid of the most difficult elements we are called upon to teach. If now we examine the relative frequency of the consonantal elements, we shall find that 75 per cent. of the consonants we use are formed by the point of the tongue, and that the majority of the remainder are formed by the lips. The consonants that are difficult to teach are chiefly formed by the top or back part of the tongue; but, on account of their comparative rarity of occurrence, they may be very imperfectly articulated without loss of intelligibility. Hence I see no reason why, in spite of the general ignorance of teachers respecting the mechanism of speech, we may not hope to teach all deaf children an intelligible pronunciation.

Let teachers appreciate the value of intelligible speech to a deaf child, and they will make the attempt to give it to him. At the present time, lack of appreciation operates to prevent the attempt from being made upon a large scale. Skilled teachers of articulation will become more numerous as the demand for their service increases, and their ingenuity, intelligently applied, will increase the perfection of the artificial speech obtained.

In the meantime, do not let us discard speech from the difficulty of obtaining it in perfection. Do not let us be misled by the idea that intelligible but defective speech is of no use, and must necessarily be painful and disagreeable to all who hear it. Those who have seen the tears of joy shed by a mother over the first utterances of her deaf child will tell you a different tale. None but a parent can fully appreciate how sweet and pleasant may be the imperfect articulation of a deaf child.

240TH MEETING.

NOVEMBER 10, 1883.

The President in the chair.

Forty-eight members present.

Announcement was made of the election to membership of
ETHELBERT CARROLL MORGAN.

It was announced from the General Committee that invitation had been extended to the members of the Anthropological and Biological Societies to attend the meeting of December 8th, for the purpose of listening to the annual address of the President.

Mr. EDWIN SMITH exhibited a

SEISMOGRAPHIC RECORD OBTAINED IN JAPAN,

describing the apparatus by which it was made, and giving a brief account of the seismographic investigations of Professor J. A. Ewing.

Remarks were made by Mr. ANTISELL.

Mr. C. E. DUTTON made a communication, entitled

THE VOLCANIC PROBLEM STATED.

[Abstract.]

It is sufficiently obvious that the volcano is a heat problem, or a thermo-dynamic problem. All volcanic activity is attended with manifestations of great energy. This energy is due to the elastic force of considerable quantities of water occluded in red-hot or yellow-hot lavas. The problem is to find a satisfactory explanation of the origin of the heat, the origin of the occluded water, and their modes of reaction.

In attempting this solution, various explanations have been conjectured. The first to be noticed, and the one which, in various forms, has met with the most favor from geologists and physicists, is that the source of heat is primordial—*i. e.*, it is the remains of a large amount of heat contained by the entire earth-mass in its supposed primordial condition, according to the nebular hypothesis; that water has penetrated from above, either from the ocean or from lakes; and that the contact of cold water with the hot magmas within the earth is a summary explanation of the phenomena. This view is supported by the following considerations: 1st, the contact of water with intensely hot bodies and the resulting generation of great explosive force is matter of the commonest experience; 2d, the outer rocks and strata are known to be full of fissures, and the ocean bottom and lake bottoms are, therefore, presumably very leaky; 3d, nearly all active volcanoes are situated either within, or

in the neighborhood of, large bodies of water; 4th, volcanoes near the sea often deliver salts which may reasonably be supposed to be the same as those contained in the ocean; 5th, the analogy of geysers gives us a series of phenomena which seem to be, in many respects, quite parallel, and which have been satisfactorily explained in a similar way.

To this view of the origin and causation of volcanic activity there are some objections. There is difficulty in understanding how water obtains access to hot magmas. No doubt the rocks are full of fissures, but we cannot, by any means, confidently infer that these fissures extend sufficiently deep to afford free or even capillary passages to melted magmas beneath. We should more legitimately infer that the heat increases gradually with the depth. At a depth of a few miles the rocks presumably have a temperature which, though high, is still below fusion, and at such temperatures it is well known that all the siliceous or rocky materials we are acquainted with are viscous. Remembering the immense statical pressure due to a thickness of a single mile of rocks, all fissures at such depths would be closed, as if the rocks were wax or butter.

2d. Although the contact of cold water with intensely hot masses will surely produce a violent explosion, we are not at liberty to admit offhand that cold water does obtain such contact in the volcanoes. On the contrary, as it penetrates it takes up the heat of the rocks through which it passes. But water is believed by all physicists to have what is technically termed a critical temperature, *i. e.*, a temperature at which it can exist only in the form of vapor however great the pressure, and this temperature is computed theoretically to be about 772° F., which is far below that of melted rock. If therefore, water could reach the liquid lavas below, it would reach them only in the form of vapor. There is indeed no difficulty in supposing that the vapor of water may, under great statical pressure, be forced into the rocks, passing between inter-molecular spaces. This is but one aspect of the phenomena of the diffusion and occlusion of gases in solids, and we know that water-vapor in large quantities is readily occluded by lava. But this is evidently no explanation of the explosive action. It is in the broadest possible contrast with the gross conception of the sudden access of cold water to hot bodies. The presumption is, under the process here suggested, that the vapor of water might penetrate slowly into regions of great heat until the hot magmas were saturated, and then the

process would come to a standstill. But there would be no volcano in this case, for the supposed condition is evidently statical and stable. For the pressure which is supposed to force the vapor in is that due to the hydrostatic pressure of a column of water. The pressure which keeps it from blowing out is that due to an equally high or even higher column of rock, the density of which is at least two and a half times greater.

3d. The analogy of the geyser thus fails to become a true homology, or an epitome of the volcano. For the geyser is due to the access of cold water to a cavity walled by hot rocks and its vaporization; the volcano, if due to the penetration of water, is due to penetration in the form of vapor in the first instance; and the difference is radical.

4th. The proximity of volcanoes to large bodies of water does not necessarily imply a logical and causal relation, and is not necessarily the true law of distribution. Another and perhaps a more rational law of distribution may be given. As a matter of fact all active volcanoes are not situated near seas or lakes, though in truth the exceptions are at the present time few, as for instance, Sangay, in the eastern Cordilleras of Peru, and the volcanoes of Central Asia. It seems as if Darwin had acutely divined the true association, viz: that volcanoes are situated in areas which are undergoing elevation. So far as we know this rule is without exception, but there are many cases where the verification of the elevation is wanting. So far, however, as the test has hitherto been applied it has approved the rule. This is especially conspicuous in the western half of our own country when applied to the late Tertiary and Post Tertiary volcanoes, and it is true, so far as known, of the Andes, Java, Phillipines, and Mediterranean, and I have recently been able to verify it in the case of the Hawaiian volcanoes. It happens that elevations, as well as subsidences, are much more frequent and extensive near coast lines than in continental interiors, whence the proximity of volcanoes to the sea becomes a secondary rather than a primary relation. But elevations also occur in continental interiors, though less frequently. And when they do occur, we find associated phenomena of volcanism as abundant and forcible as in littoral regions. This has been the case in the great Tertiary elevation of the Rocky Mountains, of the Alps, and of the Himalayan plateau. Darwin's law of the distribution of volcanoes is as thoroughly sustained by geological history as by modern instances;

while the other law, though largely predominant at the present period, shows a few conspicuous failures at the present time, but a very large number of them in times past.

Another hypothesis to account for volcanic energy supposes the interior of the earth to consist of unoxidized elements, which gradually become oxidized by the penetration of oxygen from the atmosphere.

The objections to this hypothesis are as follows: On the assumption that the earth acquires no oxygen from space, the primitive atmosphere would have been many thousand times greater than at present; but the geological record argues strongly in favor of an atmosphere which may indeed have varied in quantity and composition, but nowhere near so greatly as the hypothesis implies. Any such extravagant difference would have recorded itself legibly in the strata. Furthermore, on this view, the end of all volcanic activity is close at hand. Only three pounds of oxygen to the square inch of terrestrial surface are left. A few hundred or thousand centuries and the last volcanic beacon is extinguished, and with it all organic life.

But suppose the earth gathers up oxygen in its march through space. This may be true, but we can make any supposition on this point which pleases our fancy and feel sure that no prudent scientific man will dispute it.

A third hypothesis is that of the late Robert Mallet, which assumes the earth to be contracting interiorly by a secular loss of primitive heat. As the interior cools and shrinks, the external shell is crushed and crumpled together, and this mechanical crushing is a sufficient source of heat.

To this hypothesis there are many answers. The most direct one is that the very facts which are relied upon to prove that there is any interior cooling at all now going on also prove that the amount hitherto has been exceedingly small, and has been limited as yet to a thin external shell, not exceeding 150 miles in thickness, while the great interior is about as hot as ever; but, by the terms of the hypothesis, if the interior has not cooled there has been no interior contraction. The hypothesis is refuted by taking its own premises and pushing them to their inevitable conclusions.

There is a fourth hypothesis, which cuts the Gordian knot instead of untying it. It assumes, as the result of causes unexplained, heat is generated locally within the earth, and such local movements

of heat are the cause of volcanism. This is an arbitrary postulate, which, by its own terms, precludes discussion. Nevertheless it is the one which I believe agrees best, and perhaps perfectly, with observed facts. It undoubtedly sweeps away the difficulties which encumber all other hypotheses, but unfortunately it is an appeal to mystery, and therefore substitutes a single difficulty as great as, if not greater, than all the other difficulties put together.

There is a fifth hypothesis, which takes account of the fact that many bodies which are solid under great pressure are immediately liquefied when the pressure is removed, heat being neither lost nor gained. The removal of pressure by denudation of the surface above the seat of lavas may thus determine volcanic action. The reply to this is that volcanoes do not always, nor even generally, occur where such denudation and consequent relief of pressure, are in progress. The true law of the distribution of volcanoes appears to be the one given by the late Charles Darwin, viz., that they occur in areas which are undergoing elevation.

There are several broad facts, or categories of facts, which a true theory of the volcano must cover, and which will be recited briefly.

1. Lavas, in their subterranean seat, could not possibly have been in a highly elastic explosive condition from the earliest epochs of the earth's evolution, and only waiting a convenient season to break forth. We have no alternative but to regard them as being inert and inexplusive in their primitive condition, and as having acquired explosive energy just before the epoch of eruption. To assume that they have always been in the condition they present while pouring forth, and that the opening of a fissure has been the accident which determined the eruption, is reasoning in a circle. It is the energy of the lavas which causes the fissure, and not the fissure which causes the lavas to extrude. The lavas extrude themselves by virtue of their acquired elastic force. The theory must explain how materials which antecedently were inert, passive, incapable of eruption, may become active, dynamical, eruptible.

2. Another broad fact, closely related to the foregoing, is the intermittent action of volcanoes. These vents do not discharge all their available products at once, but by repeated spasms of activity, separated by longer intervals of repose. If these fiery explosive liquids had lain so long in the earth, chock-full of energy and only awaiting the opening of a passage-way, how happens it that when

a vent *is* once opened they do not all rush forth at once, and continue to outpour until the reservoir is completely exhausted, and why does not the vent thereafter close up forever? In a word, why should a volcano dole out its products in driblets, instead of sending forth one stupendous belch, equal to all the driblets combined? The answer here proposed is that it is because lavas, in their primitive condition, do not have sufficient potential energy, in the form of elastic force, to break open the covering which keeps them in; but they gradually acquire that energy in a portion of the reservoirs at a time, and when a sufficient portion of them has acquired it the covering is ruptured, and the whole of this energetic portion is extravasated. The vent then closes, and the process is repeated upon a second installment. The agency which thus progressively develops this force is the missing factor, and when we discover it we shall discover the secret of the volcano.

The third general fact to be taken account of is the enormous quantity of heat given off by volcanoes through long periods of time without any sign of exhaustion. The quantity of heat brought up by the lavas themselves is but a fraction of the whole amount dissipated. Kilauea wastes many times more heat by quiet radiation from the surfaces of its lava lakes and by steaming and by numberless modes of escape than by actual eruption of lavas. Mauna Loa also dissipates the greater part of its heat in the same way, and the same fact is wholly or partially true of all other active or intermittent volcanoes. And yet for very long periods, for thousands of centuries, these great volcanoes show no sign of heat-exhaustion; on the contrary, such indications as we have suggest the conclusion that the earth beneath them is hotter than before.

A fourth general fact is that volcanoes are located in areas which have recently been or are now undergoing elevation.

All these facts suggest the action of some cause generating heat within the earth. This cause, if such it be, is for the present wholly mysterious and unknown.

Mr. POWELL, referring to the relation between volcanic eruption and elevation, said that the typical, secular sequence of geologic events was, first, elevation, resulting in, second, degredation, accompanied by, third, extravasation, followed sooner or later by, fourth, subsidence, resulting in, fifth, sedimentation. There are numerous regions in which this circle of events has been recorded, and in some places it has been repeated two or three times.

Mr. F. W. CLARKE suggested that the difficulty in the way of a chemical explanation of volcanic phenomena was due to our ignorance of chemical force under high pressures. Spring has lately shown that chemical union could be brought about by pressure alone. Hence, water coming in contact with molten rock matter in the interior of the earth might be prevented from dissociating. If, however, dissociation takes place, we may conceive that water may play the following part in volcanic explosions. Gradually filtering through the surface rocks to the hot lava, it would undergo slow decomposition, and great quantities of mixed oxygen and hydrogen would thus slowly accumulate. Now let a process of cooling begin. Soon the temperature at which oxygen and hydrogen unite would be reached, and explosive union would occur. This may account for volcanic explosions, at least in part. By such a process, potential energy is gradually stored up, to be later, suddenly or instantaneously, released. This hypothesis does not account for volcanic heat, but presupposes its existence.

Mr. WHITE, referring to Mr. Powell's remarks on the instability of continental areas, said that the prevalent doctrine of the permanence of oceans, and the gradual development of the continents, was not sustained by paleontology. Continents were needed somewhere to develop the land plants and land mammals which appeared during the emergence of the known continents.

Mr. HARKNESS pointed out that Mr. White was postulating unknown continents to support the Darwinian hypothesis, to which Mr. White assented.

Mr. POWELL added, that in detailing the great cycle of geologic events, he should have included metamorphism as a sixth term, resulting from burial by sediment; and Mr. DUTTON remarked that he had included this consideration in a paragraph contained in his written manuscript, but not read.

Mr. MCGEE made a communication on

THE DRAINAGE SYSTEM AND THE DISTRIBUTION OF THE LOESS OF
EASTERN IOWA.

[Abstract.]

The most conspicuous geographic feature of eastern Iowa is the remarkable parallelism among its water-ways. Yet the region comprises two essentially distinct geologic tracts; and the coincidence

in direction of drainage in these is fortuitous: 1. The Wisconsin Driftless Region so far extends into the northeastern corner of Iowa as to include all of the triangular area bounded on the southwest by the elevated Niagara escarpment extending from the extreme eastward projection of the state northwestwardly to the Minnesota line, fifty miles west of the Mississippi. Within this tract, the drainage was originally determined by general surface slope and by rock-structure, and the present topography, which is varied and picturesque, was developed by sub-ærial erosion. 2. Within the far more extensive tract formed by the glacial drift and its derivatives, the surface is a gently undulating plain, over which the general relief is inconspicuous, and the local topography faintly defined though singularly uniform and symmetric in character; and here the parallelism in drainage is prevalent and characteristic. There are, indeed, both local and general exceptions to this parallelism, which exemplify a variety of types of aberrant behavior of the streams; but while these impair the geographic symmetry of the drainage system, they add much more largely to its geologic significance. Putting together the instances of accordant, and neglecting the instances of aberrant extension of water-lines, a *normal direction of drainage* for the whole of the drift-formed tract might be empirically determined; which normal direction is represented by a symmetric series of slightly divergent and slightly curved lines, concave to the northeastward, radiating from a point north of the state in a general southeasterly direction, toward the Mississippi. Probably nowhere else on the surface of the globe does so symmetric a normal drainage system exist, and assuredly nowhere else does the sum of directions of stream-flow over so considerable an area present so few examples of departure from the normal.

The broader topographic features of eastern Iowa are dependant upon geologic structure. The dip of the rocks is to the southwest, and the outcrops of the several formations represented form successive approximately parallel zones (trending northwest and southeast), of which those of the Niagara and Hamilton are widest. Now the Niagara rocks resisted well the planation of the pre-quaternary eons, and their eastern margin is accordingly defined by a prominent escarpment varying from 1,000 to 1,350 feet in altitude, from which there is a steep northeasterly slope to the Mississippi, and a gentle inclination, corresponding to the dip of the strata, in the opposite direction. The Hamilton rocks, on the other hand, have so

yielded to erosion that their area is topographically represented by a broad, shallow trough, of which the altitude is only from 600 to 1,000 feet, and of which the sides rise and culminate in the Niagara escarpment on the east and in the Mississippi-Missouri water-shed on the west. There is, however, a subordinate general topographic feature which is independent of geologic structure. A wide, gentle, indefinitely outlined depression extends directly across the great eastward projection (the "Cromwell's Nose") of Iowa and diagonally across the Upper Silurian, Devonian, and Carboniferous rocks alike, in the line of the general course of the Mississippi, from near the mouth of the Turkey to the mouth of the Iowa. It is manifestly of great antiquity.

Thus, in its general topography, eastern Iowa is characterized, primarily, by an elevated escarpment near its eastern border, by a broad depression intersecting its western portion diagonally, and by a general southwesterly slope extending over most of its area; and secondarily, by an indefinite ancient valley cutting off its eastern projection. And its general drainage system is almost absolutely independent of this general topography; for not only do the principal streams flow at right angles to the prevailing slope and cut through the elevated escarpment when it lies in their way, but, with the single exception of the Cedar, they preserve their courses directly across the ancient valley.

In their relation to minor topographic features the rivers of eastern Iowa conform to two diametrically opposite laws: 1. for two-thirds or three-fourths of their combined length they flow in the axes of the ill-defined, shallow valleys which characterize the drift-plain; and, 2, for the remaining portion of their courses they flow in narrow gorges which they have excavated for themselves in the axes of the elongated ridges that constitute the leading features in the local topography of the region. Moreover, they have in many instances, at the same time gone out of their direct courses, and deserted valleys already prepared for them, to attain the anomalous positions assumed under the second law of association. And let it be noted that in every such case the gorges have demonstrably been carved by the streams themselves through the quaternary and older formations alike; that the pre-existent valleys which they avoided have not been appreciably eroded since the quaternary; and that there has been no localized orographic movement in the region since long antecedent to the quaternary.

The principal tributaries entering the rivers from the right similarly conform to two antagonistic laws in their relation to topography: 1. Most of them flow throughout their courses in directions coincident with local and general slopes, and avoid elevations in their vicinity; and, 2. Many of them originate with directions approaching those normal to their localities, but curve more and more to the left toward their mouths, until they flow directly against the general slope, and enter the rivers at large angles; and all such streams have high north banks which they closely hug, and low south banks which they avoid.

So the drainage system of eastern Iowa is essentially independent of the more general topographic features, though affected by local topography; and the relations of the waterways to local topography are largely anomalous, and without parallel elsewhere.

Though essentially continuous stratigraphically, and of unquestionable genetic unity, the loess of eastern Iowa is variable in many characters, and may be separated into three geographic divisions; viz: 1, the Driftless Region division; 2, the Riparian division; and, 3, the Southern division. That of the first division forms the surface throughout the Driftless Region, as it exists in Iowa, and everywhere overlaps the eastern border of the drift; it is generally rather coarse, heterogeneous, and non-calcareous, and yields depauperate fossils of characteristic species; it reposes upon or graduates into a thin stratum of water-worn erratic materials, which, in turn, rests upon either the residuary clays of the Driftless Region or the margin of the drift-sheet; its western border is exceedingly sinuous, affects the greatest altitudes, and invariably overlooks the contiguous drift-plain; and, in capping the elevated Niagara escarpment, it forms the highest land within hundreds of miles, except in northerly directions. The loess of the Riparian division occurs chiefly in the elongated ridges so common and so intimately associated with the waterways in eastern-central Iowa; it is often fossiliferous, and its characters are generally typical; it usually graduates downward into stratified sands or gravels, which may or may not merge into drift; and it invariably seeks the highest summits in the region;—for the ridges in which the rivers have carved their cañons are always loess-topped; wherever streams avoid low-lying valleys for high-lying plateaus, the plateaus are of loess exteriorly; and the high northern banks of the aberrant tributaries are generally loess-capped. The loess of the Southern division prevails

over southeastern Iowa ; it abounds in characteristic fossils (which may or may not be depauperate), in loess-kindchen, and in calcareous tubes ; it is fine, homogeneous, and vertically cleft ; it generally graduates into the subjacent drift so imperceptibly that neither geographic nor stratigraphic separation of the formations, by other than a purely arbitrary line, is possible ; and it occurs indiscriminately at all levels.

So, in its distribution, the loess of eastern Iowa is intimately connected with the Driftless Region, with the drainage, and with the topographic configuration ; but in its disposition to seek the greatest altitudes in the north, and to merge into the drift in the south, its behavior is as anomalous as is that of the rivers of the same region.

Mr. POWELL remarked that these peculiarities of drainage were different from those observed in the drainage systems of mountain regions and demanded a different explanation, which was not yet forthcoming. It was probable, however, that not enough allowance was made for the differential effects of general degradation subsequent to the determination of the drainage.

Mr. GILBERT, after defining antecedent and super-imposed drainage, said that Mr. McGee's description definitely negated the hypothesis of antecedent drainage, and rendered the hypothesis of super-imposed drainage in the ordinary sense equally untenable. The most plausible alternative is the hypothesis suggested by Mr. McGee in one of his earlier papers, that the drainage was super-imposed by the ice-sheet, the distribution of loess having been determined at the same time and by the same causes.

Mr. WHITE regretted that Mr. McGee's special investigations did not include the portion of Iowa draining to the Missouri. The details of drainage in that region are equally interesting, and, in his opinion, do not admit of the explanation mentioned by Mr. Gilbert. The direction of the rivers diverges at right angles from that of the Mississippi tributaries, and their valleys are excavated from loess except along their upper courses.

Mr. POWELL said that on the Illinois side of the Mississippi River many of the features described in the paper are repeated. The loess hills follow the river courses, and in the opposite directions overlook plains. The explanation of the phenomena is problematic, but the theory advocated by Mr. Gilbert does not appear sufficient.

241ST MEETING.

NOVEMBER 24, 1883.

Vice-President BILLINGS in the Chair.

Fifty-three members and guests present.

It was announced by the Chair that the next meeting would be held in the Lecture Hall of the National Museum, that the members of the Anthropological and Biological Societies were invited to be present, and that the members of all three societies were requested to invite their friends.

Opportunity was afforded for the introduction of amendments to the Constitution, but none were offered.

Mr. C. D. WALCOTT made a communication on

THE CAMBRIAN SYSTEM IN THE UNITED STATES AND CANADA.

[Abstract.]

Defining the Paleozoic period as has been done by Geikie in his *Text-Book of Geology*, it will include all the older sedimentary formations containing organic remains, up to the top of the Permian. Upon the paleontologic evidence it may be divided into an "older and newer division, the former (from the base of the Cambrian to the top of the Silurian system) distinguished more especially by the abundance of its graptolitic, trilobitic, and brachiopodous fauna, and by the absence of vertebrate remains; the latter (from the top of the Silurian system to the top of the Permian system) by the number and variety of its fishes and amphibians, the disappearance of graptolites and trilobites, and the abundance of its cryptogamic terrestrial flora." The two divisions may be still further subdivided; the upper into the Carboniferous and Devonian, the lower into the Silurian above and the Cambrian beneath. It is the Cambrian division we now have to consider.

Stratigraphically it is difficult to fix any definite upper limit to the Cambrian system, owing to local causes having affected the conditions of sedimentation and consequent extinction or continuance of the fauna. Upon the evidence of the section in New York State on the western side of Lake Champlain, the Potsdam sandstone closes the period stratigraphically and paleontologically, the Calciferous formation forming little more than a closing deposit of the Potsdam; and the large Chazy fauna appearing suddenly in the overlying limestone is entirely distinct from that of the Potsdam. In central

Nevada the section passes through limestones marked by the presence of a typical Potsdam fauna and on up to one that has the general facies of that of the Trenton Lower Silurian fauna. Midway of these passage beds occur layers of rock that carry representatives of both the Cambrian and Silurian faunas. Above this band the Cambrian fauna gradually disappears, and below it soon predominates to the exclusion of the Silurian types. In this section we have an illustration of the gradual extinction of an older fauna as a new one is introduced, the sedimentation continuing and no physical disturbance occurring to change the conditions necessary for the presence of animal life. It is the ideal section uniting the faunas of two periods, and if we had the blanks filled in between all the groups, as the blank between the Potsdam and Chazy in New York is filled in by the Nevada section, the Paleozoic would be a record of continuous connected organic life from the base of the Cambrian to the summit of the Permian.

It is convenient for stratigraphic geologic work to separate the Paleozoic series into subdivisions, and, as this is almost necessarily done on paleontologic evidence, I would separate the Cambrian as one characterized by what Barrande has named the first fauna.* Applying this to the Nevada section already mentioned, the line between the Cambrian and Silurian would be drawn where the types of the second fauna begin to predominate. With this definition of the Cambrian system, the strata referred to it in the United States and Canada will be briefly noticed.

In the Grand Cañon of the Colorado the top of the Cambrian is the Tonto formation, a series of sandy calcareous strata 1,000 feet in thickness. The contained fauna is closely allied to that of the Potsdam sandstone and continues up to the summit of the formation, the overlying Devonian rocks resting directly above strata containing *Lingulepis*, *Iphidea*, *Conocephalites*, *Dicellosephalus*, etc. The Tonto rests uncomfortably on strata that were extensively eroded prior its deposition. This lower series comprises over 11,000 feet of unmetamorphosed shales, limestones, and sandstones, with 1,000 feet of interbedded lavas. It forms the Grand Cañon and Chu-ar' groups of Powell and is characterized by the presence of a few fossils that enable us to refer it to the Cambrian but not to define its stratigraphic horizon. That is done on the evidence of the position it occupies with reference to the Tonto.

* The paleontologic evidence and discussion will appear in a future paper.

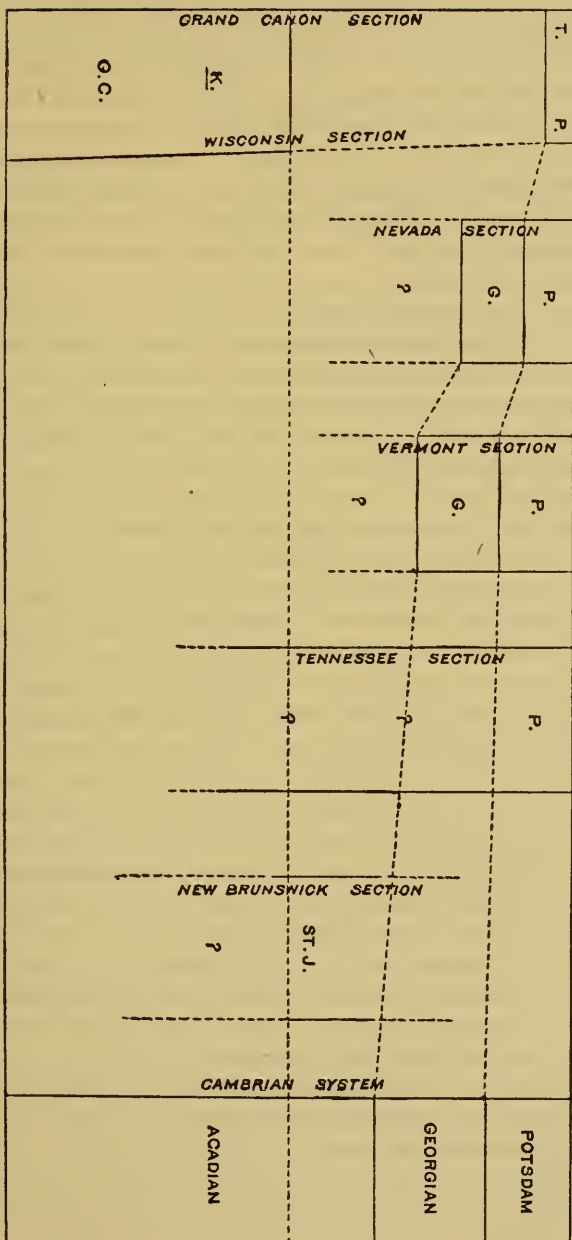
The relations of the Grand Cañon section are shown in the first column of the page of sections.

The Potsdam sandstone in Wisconsin occupies the same relative stratigraphic position as the Tonto formation, except that the break above the Tonto and between it and the Devonian is filled in by the Calciferous and other Silurian formations. As has already been said, the faunas of the Potsdam and Tonto are very much the same in general character. The Potsdam formation here overlies unconformably a series of strata that are directly comparable with the Grand Cañon and Chu-ar' series. The Keweenawan series, according to Chamberlin, has about 10,000 feet of sedimentary strata distributed through 30,000 feet of eruptive rocks. In all this great mass no decisive evidence of organic life has been discovered, but knowing that the series is unconformably overlain by the Potsdam formation and that it in turn rests unconformably on the Archæan, as does the Grand Cañon series, we feel justified in correlating the Grand Cañon and Wisconsin sections and they are united in the first column of the page of sections.

The upper part of the Nevada section has already been mentioned. Below the Potsdam horizon there occurs a distinct fauna, characterized by a considerable development of the trilobitic genus *Olenellus*, a genus that in the embryonic development of several of its species proves that it is derived from the *Paradoxides* family and is consequently of later date. This section is readily correlated with that of the Georgian group of Vermont, as there we have the Potsdam sandstone above the *Olenellus* horizon, and in the downward section both stop at nearly the same relative horizon. The position of the Georgian formation in Nevada and Vermont, in relation to the Potsdam, leads to the view that it represents a portion of the period of erosion between the Tonto formation and the Grand Cañon series and also the Potsdam formation and the Keweenawan series.

The upper portion of the Tennessee Cambrian, the Knox shale, is correlated with the Potsdam sandstone, and so is the Knox sandstone. The Chilhowee sandstone and Ocoee conglomerate and slates cannot be directly connected with the Georgian horizon, since the paleontologic data are insufficient. From their position beneath the Knox shale with its Potsdam fauna they are extended downward past the Georgian and into the Paradoxidian or St. Johns horizon. Their total thickness (Geology of Tennessee, pp. 158, 159) is nearly 15,000 feet.

TYPICAL CAMBRIAN SECTIONS.



T. = Tonto. G. C. = Grand Cañon. P. = Potsdam. G. = Georgian. St. J. = St. Johns. K. = Keweenaw.

Maximum thickness of Cambrian = 50,000 + feet.

There is still another group, the St. Johns or Acadian, that occupies an horizon below the Georgian and may fill in a portion of the period of erosion between the pre-Potsdam and Keweenawan and the Tonto and Grand Cañon series, or it may represent some of the upper portions of the Grand Cañon and Keweenawan series. In the geologic sections it is placed beneath the Georgian and as above or passing down into the lower groups. For the present both it and the Paradoxidian argillites of Braintree must be left in doubt with regard to their relations to the lower Cambrian of Wisconsin and northern Arizona.

Of the Canadian survey sections, the one on the north side of the Straits of Belle Isle is most interesting as it gives the Georgian horizon, but unfortunately an interval of ten miles in width is occupied by the straits before the section is again continued. In this interval the Potsdam group is lost, but farther along the coast there occurs, below limestones referred to the Calciferous horizon, a mass of sandstone that may be assigned to the Potsdam formation—giving, in connection with the *Olenellus* or Georgian horizon, a section not unlike that of Central Nevada.

No other section that has been determined in the British Provinces throws much light on the stratigraphic succession of the Cambrian rocks. At Point Levis a curious mingling of the Cambrian and Silurian faunas has been said to occur, but this is rather to be attributed to error in the interpretation of the stratigraphy in a much disturbed area than to a break in the sequence of organic remains, elsewhere so uniform. I prefer to accept the interpretation given by M. Jules Marcou, who says (*The Taconic and Lower Silurian Rocks of Vermont and Canada*, Proc. Bos. Soc. Nat. Hist., Vol. VIII, p. 252, 1862,) that the primordial or Cambrian types are associated together and occur in a belt of limestone that contains no traces of the second or Silurian fauna.

The accompanying table of sections gives a general outline of the Cambrian. Numerous local sections of the Potsdam series are not mentioned, as they do not add materially to the general information in regard to the system in its vertical range.

The geographic range is great, extending as it does from Newfoundland to Montana on the northern line, and thence south to Nevada, Texas, and Alabama.

Mr. JOHN JAY KNOX made a communication on
THE DISTRIBUTION OF THE SURPLUS MONEY OF THE UNITED STATES
AMONG THE STATES.

[Abstract.]

President Jackson, in his message to Congress in 1829, referred to the difficulty in adjusting the tariff, so that the revenues of the Government should be but slightly in excess of its expenditures. He considered the appropriation of money for internal improvements, by Congress, as unconstitutional, but suggested that, if the anticipated surplus in the Treasury should be distributed among the States, according to their ratio of representation, such improvements could then be made by the States themselves. If necessary it would be expedient to propose to the States an amendment to the Constitution, authorizing such legislation.

In his message for the following year he again suggested the same proposition.

The receipts from sales of public lands for the three years, 1834, 1835, and 1836, were \$44,492,381—slightly less than the total receipts from this source for the thirty-eight years previous, from 1796 to 1834. On January 1, 1835, the country was virtually out of debt, and the receipts of the Government largely exceeded the previous estimates of the Secretary. The amount of surplus on January 1, 1835, was \$8,892,858, and at the same date in 1836 \$26,749,803. On January 1, 1837, it amounted to more than forty-two millions.

In 1834-5-6, the public money, which had heretofore been deposited in the Bank of the United States, was deposited in favorite State banks by order of General Jackson. The deposit of the revenues in these banks was followed by financial distress, and during the year 1834, and previous thereto, propositions were made in the public press for distribution of the surplus revenue among the States as a measure of relief. These propositions were first in the form of a distribution of the revenue from public land; then a distribution of the lands themselves; and finally a distribution of the surplus. During the session of 1835, a select committee was appointed in the Senate, which reported a resolution to amend the Constitution so that the money remaining in the Treasury at the end of each year, until the first of January, 1843, should annually be distributed among the States and Territories. Both General

Jackson and Secretary Woodbury were opposed to this proposition, as the withdrawal of public moneys would deprive the State banks of the deposits, and would be likely to increase the financial troubles. A bill to distribute the surplus was, however, introduced in the Senate, and passed by a vote of 25 to 20. It was evident that this bill could not pass the House, as a majority of its members considered the bill, in the form of a distribution, as unconstitutional. The friends of the measure in the Senate determined to change its form so as to remove the difficulty. A bill then pending in the Senate was so amended as to change the proposition for distribution to a proposition for deposit with the States, and in this form it passed the Senate, and subsequently the House by a large majority, 155 to 38.

This act of June 23, 1836, provided for the deposit with the treasurers of the several States of 37 millions (\$37,468,859) in four instalments during the year 1837—the Secretary of the Treasury to receive certificates of deposit therefor signed by competent authority, in such form as he should prescribe, which certificates should express the usual legal obligation, and pledge the faith of the State for the safe keeping and repayment of the deposit, from time to time, whenever the same should be required. The first three installments were deposited. Before the last installment, payable on the 1st day of October, was transferred, a series of financial disasters culminated in the crisis of 1837, and there was no surplus to deposit. Further legislation was deemed necessary in this emergency, and an extra session of Congress was called by President Van Buren. During this session, on September 11, 1837, a bill was reported from the Finance Committee of the Senate, providing that the transfer of the fourth installment should be indefinitely postponed. The opposition to this bill was persistent, and there was a long debate, which was participated in by Webster, Clay, Calhoun, Buchanan, Benton, Silas Wright, Caleb Cushing, and others of the Senate; and in the House by Adams, Fillmore and Sibley of New York, Bell of Tennessee, Wise of Virginia, and many others.

A bill was finally passed, providing for the postponement of the deposit of the fourth installment until January 1, 1839. It passed the House by a vote of 119 to 117, and contained an amendment proposed by Mr. Buchanan, providing that the deposits should not be subject to the requisition of the Secretary of the Treasury, but should remain until called for by Congress. On the 1st of Jan-

uary, 1839, there were no funds in the Treasury available for the payment of the fourth installment, and since that date there has never been a surplus in the Treasury above the debts and estimated expenditures of the Government.

The amount of the three installments was \$28,101,645, and the amount placed in the Treasury of each State has since been carried among "unavailable funds of the general Treasury," as may be seen by reference to the annual reports of the Treasurer of the United States.

The fourth installment, amounting to \$9,367,215, has never been transferred or deposited, and recently the State of Virginia, through the action of its Legislature, and the State of Arkansas, through the action of its treasurer and one of its United States Senators, has applied to the Secretary of the Treasury for the payment of this last instalment.

It is generally believed that the moneys deposited by the Government with the different States were, for the most part, wasted or employed in works of internal improvement which were unnecessary. The data for a full investigation of this subject are not at hand, but it is known that the States of Massachusetts, Connecticut, New York, New Jersey, Pennsylvania, Delaware, Maryland, North Carolina, Illinois, Indiana, Kentucky, Ohio, and Missouri appropriated a considerable portion of the income from this fund to the support of public schools; and that in many of these States the income from the whole fund has been from the commencement, and still is, devoted to the education of the people.

A bill was introduced by Senator Logan, during the first session of the last Congress, providing that the entire income derived from the internal-revenue tax on the manufacture and sale of distilled spirits shall be appropriated and expended for the education of all children living in the United States, as shown by the census of 1880 and each succeeding census. The bill also provides that the States shall be required, before receiving the benefits of the act, to make school attendance obligatory upon all children between the ages of seven and twelve years, for at least six months in each year.

Mr. ALVORD inquired as to the present status of the Smithsonian fund, amounting to about half a million of dollars, which was invested in the bonds of the State of Arkansas.

Mr. KNOX said that the Government has assumed the Arkansas

bonds formerly held by the Smithsonian Institution, and that the Government also held quite a large amount of the bonds of the States of Virginia and Arkansas in the Indian Trust Fund. If legislation should be obtained authorizing the payment of the fourth instalment to these States, such legislation should provide that the payment be made in the bonds now held by the Government.

Mr. ALVORD said that the history of agricultural college grants was not thus far very encouraging. It would have been better if Congress had provided that the agricultural colleges should never be united with other colleges. The union was apt to lead to confusion and controversies, and lower the standard and prestige of both. Witness the case of Dartmouth College. In this reference Mr. MUSSEY concurred.

The Hon. HUGH McCULLOUGH, being invited by the Chair to participate in the discussion, said that in Indiana the application of the money deposited by the United States had occasioned a long debate, which had resulted in its division. One half, by means of a system of commissioners, was loaned to individuals on land and mortgage; the other half was put into stock of the State Bank, with which the speaker was at that time connected. In a financial crisis the first half was practically lost, probably less than one-twentieth part being recovered; but the loss was fortunately made good by the bank stock, upon which dividends were regularly paid, and by which the investment was eventually doubled. Since the closing of the bank, this money has constituted the school fund of Indiana.

Mr. R. D. CUTTS made a communication on

THE ACTION OF THE INTERNATIONAL GEODETIC ASSOCIATION AS TO
AN INITIAL MERIDIAN AND UNIVERSAL TIME.

[Abstract.]

The International Geodetic Association of Europe, formed for the purpose of connecting the systems of triangulation executed by the different States of Europe, and hence for the measurement of arcs, and for the discussion of all questions of science comprised within the term Geodesy, has been in active existence for many years. The meeting in 1882 was held at The Hague, and before adjournment it was decided that the seventh conference should meet at Rome, in October, 1883.

In the meantime, all governments in diplomatic relations with the United States were invited by the President, in accordance with the act of Congress, August 3, 1883, to send delegates to Washington for the purpose of fixing upon a meridian proper to be employed as a common zero of longitude and standard of time, reckoning throughout the globe. More than twenty of these countries had signified, before October last, their acceptance of the invitation, but these did not include many of the principal governments of Europe. The delay in forwarding their definitive replies was due to their desire to have the advice, before committing themselves, of the European Geodetic Association. Hence it was at the request of many of these governments that the Association took up the subject of the unification of longitudes, and of the introduction of a universal time.

So soon as it was decided to take such action, General Ibanez, of Spain, the then President of the Association, addressed a letter to the Superintendent of the Coast and Geodetic Survey, urging him in strong terms to send a delegate to the meeting at Rome. So short a notice was given, however, that the delegate selected had to start at once, reaching Rome only on the morning of the first day's session, October 15th.

After a full discussion of the different views presented, the following resolutions were almost unanimously passed on October 24th. It must be borne in mind that they are merely of an advisory character, sanctioned and urged, nevertheless, by the highest scientific authority. It is the function of the convention to be held at Washington next year to take official and decisive action on the subject in all its details.

Resolutions of the International Geodetic Commission in relation to the Unification of Longitudes and of Time.

The seventh general conference of the International Geodetic Association, held at Rome, and at which representatives of Great Britain, together with the directors of the principal astronomical and nautical almanacs, and a delegate from the Coast and Geodetic Survey of the United States, have taken part, after having deliberated upon the unification of longitude by the adoption of a single initial meridian, and upon the unification of time by the adoption of a universal hour, have agreed upon the following resolutions :

I. The unification of longitude and of time is desirable, as much in the interest of science as in that of navigation, of commerce, and of international communication. The scientific and practical utility of this reform far outweighs the sacrifice of labor and the difficulties of adaptation which it would entail. It should, therefore, be recommended to the Governments of all the States interested, to be organized and confirmed by an International Convention, to the end that hereafter one and the same system of longitudes shall be employed in all the institutes and geodetic bureaus, for the general geographic and hydrographic charts, as well as in the astronomical and nautical almanacs, with the exception of those made to preserve a local meridian, as, for instance, the almanacs for transits, or those which are needed to indicate the local time, such as the establishment of the port, &c.

II. Notwithstanding the great advantages which the general introduction of the decimal division of a quarter of the circle in the expressions of the geographical and geodetic co-ordinates, and in the corresponding time expressions, is destined to realize for the sciences and their applications, it is proper, through considerations eminently practical, to pass it by in considering the great measure of unification proposed in the first resolution.

However, with a view to satisfying, at the same time, very serious scientific considerations, the Conference recommends, on this occasion, the extension by the multiplication and perfection of the necessary tables, of the application of the decimal division of the quadrant, at least, for the great operations of numerical calculations, for which it presents incontestable advantages, even if it is wished to preserve the old sexagesimal division for observations, for charts, navigation, &c.

III. The Conference proposes to the Governments to select for the initial meridian that of Greenwich, defined by a point midway between the two pillars of the meridian instrument of the Observatory of Greenwich, for the reason that that meridian fulfils, as a point of departure for longitudes, all the conditions demanded by science; and because being at present the best known of all, it presents the greatest probability of being generally accepted.

IV. It is advisable to count all longitudes, starting from the meridian of Greenwich, in the direction from west to east only.

V. The Conference recognizes for certain scientific wants and for the internal service in the chief administrations of routes of com-

munication, such as the railroads, steamship lines, telegraphic and post routes, the utility of adopting a universal time, along with local or national time, which will necessarily continue to be employed in civil life.

VI. The Conference recommends, as the point of departure of universal time and of cosmopolitan date, the mean noon of Greenwich which coincides with the instant of midnight, or with the commencement of the civil day, under the meridian situated 12 hours or 180 degrees from Greenwich.

It is agreed to count the universal time from 0^h to 24^h.

VII. It is desirable that the States which, for the purpose of adopting the unification of longitudes and of time, find it necessary to change their meridians, should introduce the new system of longitudes and of hours as soon as possible.

It is equally advisable that the new system should be introduced without delay in teaching.

VIII. The Conference hopes that if the entire world should agree upon the unification of longitudes and of time by accepting the meridian of Greenwich as the point of departure, Great Britain will find in this fact an additional motive to make, on its part, a new step in favor of the unification of weights and measures, by acceding to the *Convention du Mètre* of the 20th May, 1875.

IX. These resolutions will be brought to the knowledge of the Governments and recommended to their favorable consideration, with the expression of a hope that an International Convention, confirming the unification of longitudes and of time, shall be concluded as soon as possible, by means of a special conference, such as the Government of the United States has proposed.

Mr. HILGARD said that while the report of the Association did not conform in some of its details to the desires and interests of this country, nevertheless our principal object had been gained by the endorsement of the Association for the International Conference on the subject of standard time, to be held in Washington.

The selection of the meridian of Greenwich as the starting point for longitudes, was more convenient for us than for Europeans; Europeans alone are liable to the confusion arising from the numerical identity of meridians east and west of Greenwich. It will be impossible, however, for us to agree to the rule which counts all longitudes from west to east.

Mr. ELLIOTT opposed the establishment of noon as the initial hour of the day. It seemed to be proposed in the interest of astronomers, who work at night, and would not be submitted to by the people at large.

He exhibited a map showing a grouping of the railroads of the country under the recently adopted time schedule.

Mr. CUTTS said that the resolutions of the Geodetic Association do not appertain to civil time. The "universal time" they advocate is for the use only of astronomers and great transportation corporations.

Other remarks were made by Mr. NEWCOMB.

242D MEETING.

DECEMBER 8, 1883.

By permission of the Secretary of the Smithsonian Institution, the Society occupied for the evening the Lecture Hall of the National Museum.

The President called Vice-President MALLERY to the Chair.

There were present about three hundred members and guests.

By invitation, the Presidents of the Biological and Anthropological Societies occupied seats on the platform.

The President of the Society, Mr. J. W. POWELL, delivered the annual address, taking for his subject

THE THREE METHODS OF EVOLUTION.

[The address is printed on pages XXVII-LII, *ante*.]

The Chair invited the members of the Society and their friends to remain for a period after adjournment, for the purpose of social intercourse.

The Society then adjourned.

243D MEETING.

DECEMBER 22, 1883.

THE THIRTEENTH ANNUAL MEETING.

The President in the chair.

Thirty-four members present.

The minutes of the 226th, 241st, and 242d meetings were read.

The Chair announced the death, since the last meeting, of General R. D. CUTTS.

The Chair announced the election to membership of Messrs. ROBERT SIMPSON WOODWARD, DANIEL ELMER SALMON, and JOHN MILLS BROWNE.

The Secretary's report on the membership of the Society was read. During the year the Society received seventeen new members, lost eight by death, and lost three by resignation.

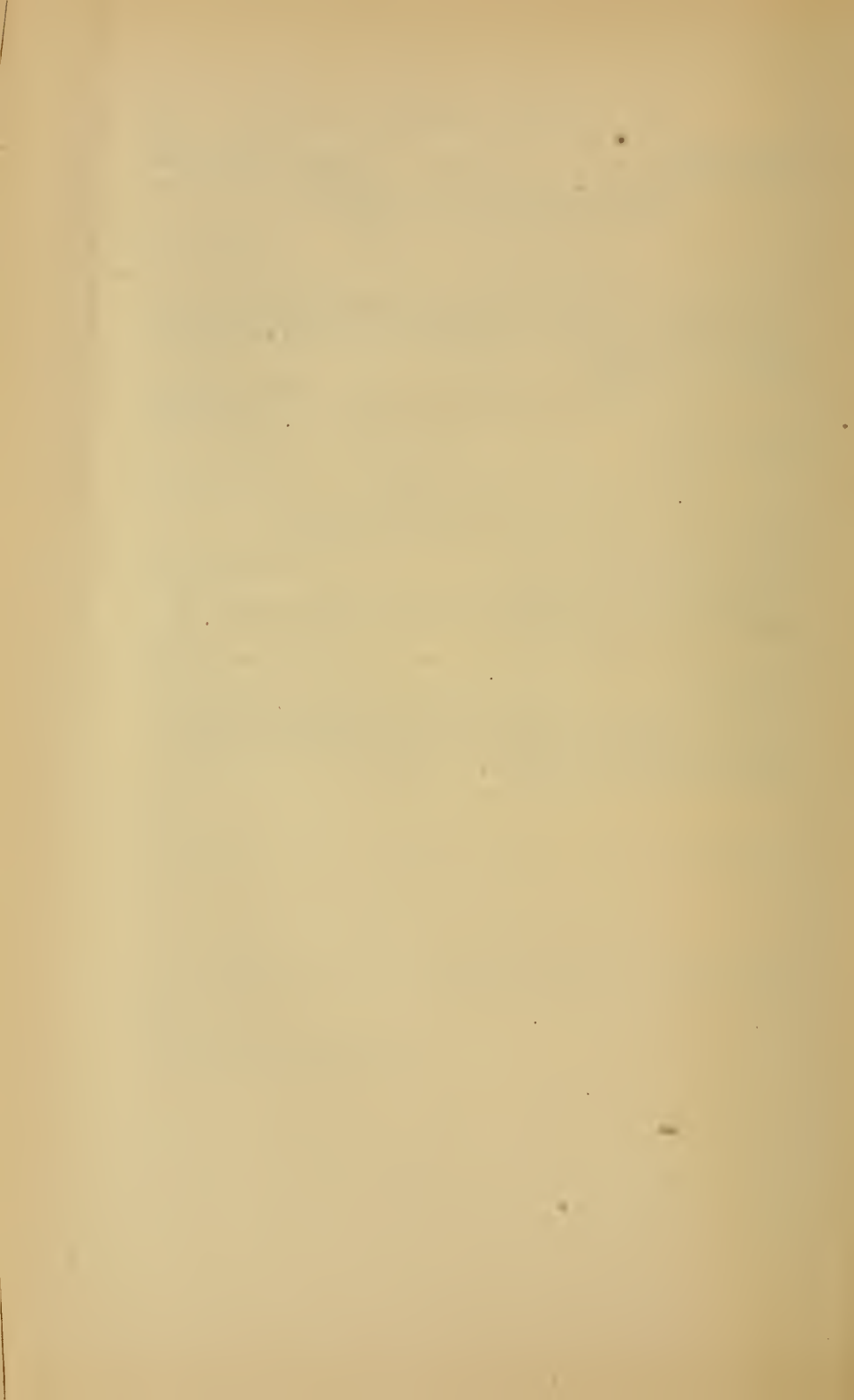
The Treasurer not being present, the Chair appointed Mr. Henry Farquhar Treasurer *pro tempore*.

The officers for the ensuing year were then elected by ballot. (The list is printed on page xv.)

On motion of Mr. JENKINS, the vote for President was made unanimous.

The Chair appointed Messrs. C. A. White, S. Newcomb, and H. C. Yarrow a committee to audit the annual report of the Treasurer.

The Society then adjourned.

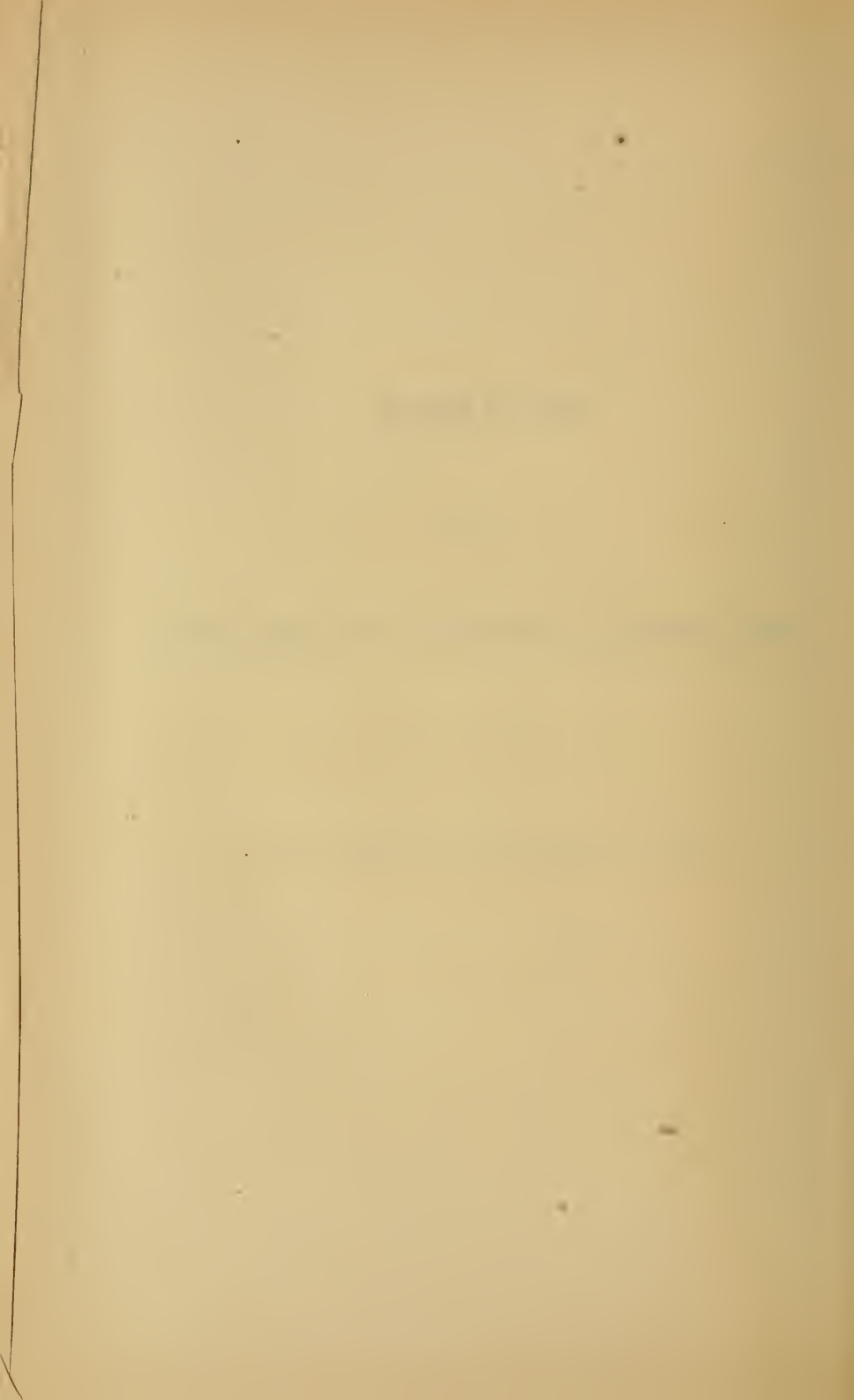


BULLETIN

OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON.

MATHEMATICAL SECTION.



STANDING RULES
OF THE
MATHEMATICAL SECTION.

Adopted March 24, 1883.

1. The object of this Section is the consideration and discussion of papers relating to pure or applied mathematics.

2. The special officers of the Section shall be a Chairman and a Secretary, who shall be elected at the first meeting of the Section in each year, and discharge the duties usually attaching to those offices.

3. To bring a paper regularly before the Section it must be submitted to the Standing Committee on Communications for the stated meetings of the Society, with the statement that it is for the Mathematical Section.

4. Meetings shall be called by the Standing Committee on Communications whenever the extent or importance of the papers submitted and approved appear to justify it.

5. All members of the Philosophical Society who wish to do so may take part in the meetings of this Section.

6. To every member who shall have notified the Secretary of the General Committee of his desire to receive them, announcements of the meetings of the Section shall be sent by mail.

7. The Section shall have power to adopt such rules of procedure as it may find expedient.

LIST OF MEMBERS

WHO RECEIVE ANNOUNCEMENT OF MEETINGS OF THE
MATHEMATICAL SECTION.

ABBE, C.	GORE, J. H.
ALVORD, B.	GREEN, B. R.
AVERY, R. S.	HALL, A.
BABCOCK, O. E.	HARKNESS, W.
BAKER, M.	HAZEN, H. A.
BATES, H. H.	HILGARD, J. E.
BILLINGS, J. S.	HILL, G. W.
BURGESS, E. S.	KING, A. F. A.
CHRISTIE, A. S.	KUMMELL, C. H.
COFFIN, J. H. C.	LEFAVOUR, E. B.
DELAND, T. L.	PEIRCE, C. S.
DOOLITTLE, M. H.	RITTER, W. F. M'K.
EASTMAN, J. R.	SMILEY, C. W.
ELLIOTT, E. B.	TAYLOR, W. B.
FARQUHAR, H.	UPTON, W. W.
FLINT, A. S.	WALLING, H. F.
GILBERT, G. K.	WINLOCK, W. C.
NEWCOMB, S.	

INAUGURAL ADDRESS

OF THE

CHAIRMAN OF THE MATHEMATICAL SECTION,

BY ASAPH HALL.

GENTLEMEN OF THE MATHEMATICAL SECTION:

I thank you for the honor you have conferred on me by my election as Chairman of this Section, and the best return that I can make is to do my utmost to render our meetings as interesting and successful as possible.

Although my duties have been such that I have not been able to take a very active part in the proceedings of the Philosophical Society, it is easy to understand how a need has been felt for a more full and frequent discussion of mathematical questions. Mathematics has indeed been called the queen of the sciences, but the rigor and dryness of its methods make it distasteful to many. The fact seems to be that as any branch of knowledge advances and finally is reduced to law, it loses in a large degree its attractiveness and popularity. Then, it is only with the indefinite outlines and the obscure boundaries of this science that most people like to deal; and this may be natural and right, since nearly all advancement originates in speculation and doubt, which lead to investigation, and which, by a variety of motives, spur men on to labor. But the science of mathematics, though old, is yet young and vigorous. We have now six journals of the highest rank, which are devoted almost exclusively to pure mathematics—two in Germany, two in France, one in England, and, I am glad to say, one in our own country. These journals are devoted to the discussion of the highest conceptions of space and number, treating chiefly of the laws and forms of analytical expressions, and generally they touch lightly on any practical application of the science. Such discussions prepare the way, however, for better and more general practical methods, and in our own country they have, I think, another value. For one, I can hardly accept the doctrine, advocated in some quarters, that the American scientific man of the future should

be distinguished by his facility in getting a patent on his discovery, in forming joint stock companies and watering stock, and in suddenly becoming rich at the expense of his fellow-men. Such a career may be a natural result of our present system of sociology, but it does not seem to be in harmony with scientific thought and research, and our social need is for men of a different character. Far nobler is the life of one who devotes himself to the study of the most abstract forms of science; winning for us, if haply he may, another forward step up the hill of knowledge.

But when we come to the field of applied mathematics we soon learn how necessary are the studies of the pure mathematician. Nearly all the researches in natural philosophy, where the action of forces is concerned, require the formation and solution of differential equations, and hence the theory of such equations becomes important, and in some cases almost essential, for the advancement of physical investigations. It is not, of course, to be supposed that experiment and observation are to be done away with or neglected, or that mere skill in differentiating, integrating, and solving equations can supply the place of correct thinking. In fact, we may be sure that Leibnitz was mistaken when he declared that the invention of the differential calculus had made known that royal road to knowledge for which the king had inquired in vain of Euclid. But still it remains true that this calculus forms the most powerful engine we have for the solution of questions in natural philosophy. It enables us to adopt the old maxim, "*divide et impera.*" If we can reduce the problem to its elements, and can form its true differential equation, the rest of the work is purely mathematical. Unfortunately, the differential equations that occur in the problems of nature are very different from those given in our text-books, and their exact solution is in most cases impossible. Here we must rely chiefly on that happy device of the variation of constants, by means of which the solution of simpler forms is extended to the more complex.

One of the great advantages of putting a question in a mathematical form is the precision with which it can be stated. If we are right, the truth of our assertion will be the sooner acknowledged, and if we are wrong, our error can be the more easily detected. Frequently it has seemed to me that disputes would be avoided in the meetings of our scientific societies if men would take the trouble to put their assertion into a formula and write it on the blackboard;

and certainly there would be a clearness and meaning that are so often wanting. Thus, if any one asserts that when a planet comes to its perihelion it ought to fall into the sun, the law of gravitation being true, he is not worth listening to unless he will put his assertion into a formula; and when he is able to do this he will probably find out his own error. There will be so much gain by simply reducing the problem to its elements and giving it a correct form. Again, where scientific statements *may be* true, there will be a gain in giving them, when possible, a mathematical expression. Thus, when we are told that the fixed star 1830 Groombridge is running away, disobedient to the law of gravitation, how much better it would be if we could see on the blackboard the mathematical proof of this assertion, so that we could judge for ourselves on what assumption it is based. The subject of impulsive forces is one that we hear disputes about in our own society, and it seems to be a fair field for a mathematical exposition. How often do we see such phrases as "energy," "potential energy," "kinetic energy," "conservation of energy," "work," "virial," &c. Could not some one of our members give us a clear account of these terms, show us how they are connected with the general equations of mechanics, what new ideas they contain, and on what limitations they may be based? As the application of mathematics is extended, sounding phrases are sure to come into use, and it is well to test them and know what they mean.

In the discussions of this Section, while all are invited to be critical, I trust that we shall all be kind and good tempered. We come together for discussion and mutual improvement, and while error is not to be spared we must be charitable to each other's faults.



BULLETIN

OF THE

MATHEMATICAL SECTION.

A communication signed by Mr. J. E. Hilgard and nineteen other members of the Philosophical Society, asking that a Section in Mathematical Science be formed, as provided in Paragraph 6 of the Standing Rules of the Society, was presented to the General Committee at its regular meeting January 27, 1883. The proposition was agreed to, and Mr. Hilgard was empowered to call a special meeting for the purpose of organizing such a section; the call being extended to all members of the Society.

1ST PRELIMINARY MEETING.

FEBRUARY 17, 1883.

Twelve members met in the library of the Army Medical Museum, in answer to the first call.

Mr. HILGARD not being present, Mr. E. B. ELLIOTT was called to the Chair.

An informal discussion followed, which brought out a unanimous sentiment in favor of forming the Section.

With some differences of opinion as to details, it was agreed to postpone formal action, and the meeting adjourned subject to call.

2D PRELIMINARY MEETING.

MARCH 5, 1883.

Mr. HILGARD in the Chair.

Fifteen members present.

A plan of organization was adopted, and referred to the General Committee of the Society for consideration.

1ST REGULAR MEETING.

MARCH 29, 1883.

Fourteen members present.

In the absence of Mr. HILGARD, who had presided over the meeting for organization, Mr. G. W. HILL was called to the Chair.

The standing rules for the government of the Section, as adopted at the last meeting of the General Committee of the Society, were read.

The Section then proceeded to elect officers for the year 1883. On motion of Mr. WINLOCK the rules of the Society at its Annual Meeting were followed.

Mr. ASAPH HALL was chosen Chairman and Mr. H. FARQUHAR Secretary.

A letter from Mr. MARCUS BAKER, dated Los Angeles, Cal., was read by Mr. CHRISTIE. It expressed a strong interest in the Section, recommending that it should be conducted as nearly as possible on the plan devised by the late Prof. Henry for the Society itself, by which business and science are kept apart. A free use of pencil and paper at the meetings, and seats around a table, were further suggested. The letter closed by advocating the foundation of a new mathematical journal.

Mr. CHRISTIE then made a communication on

A QUASI GENERAL DIFFERENTIATION.

The paper was discussed by Messrs. KUMMELL, ELLIOTT, HILL, and DOOLITTLE. The author reserves it from publication to await further research.

A resolution was passed, requesting the committee in charge of the matter to call meetings of the Section on Wednesday evenings.

2D MEETING.

APRIL 11, 1883.

The Chairman, Mr. HALL, presided.

Present, ten members and two invited guests.

It was announced that the Editor of "Science" would publish brief reports of the meetings of the Section.

The Chairman read an inaugural address, [given in full on pp. 117 to 119 *ante*.]

Mr. C. H. KUMMELL then began a paper on

ALIGNMENT CURVES,

which was not finished at the time of adjournment.

3D MEETING.

APRIL 26, 1883.

The Chairman presided.

Present, sixteen members and one invited guest.

Mr. KUMMELL completed his paper, begun at the second meeting, on

ALIGNMENT CURVES ON ANY SURFACE, WITH SPECIAL APPLICATION TO THE ELLIPSOID.

[Abstract.]

The attempt to put a number of points in line on a curved surface whose normals are supposed to be given (abstraction is made of deviations of the plumb-line and lateral refraction) gives rise to various curves, which I call alignment curves. There are two classes—alignment curves with two given termini and those with a starting point only. There are three distinct curves of the first class, viz. : 1. The normal section, if the surveyor directs his assistant to place staffs in line from one end of the line. 2. A curve described if the surveyor would align a point near him, then move up to this point, thence align another point, etc., until the terminus is reached. This process is that used in chaining, or more roughly by a pedestrian going towards a point, and is characterized by requiring only foresights. I call it *proorthode* ($\pi\rho\theta, \partial\rho\theta\delta\varsigma, \partial\delta\acute{\omicron}\varsigma$).* 3. A curve resulting if a backsight is also taken. This curve is therefore defined by the condition that the normal plane at any point of it which passes through one end also passes through the other. I call it *diorthode* ($\delta\iota\acute{\alpha}, \partial\rho\theta\delta\varsigma, \partial\delta\acute{\omicron}\varsigma$), because it may be con-

* This and other names of curves were coined by my friend, Mr. Wm. R. Galt, of Norfolk, Va.

sidered straight *all through* at any of its points. This curve may be considered the ideal curve of a primary base line. Various names have been given to it when on the terrestrial spheroid. Dr. Bremiker, who appears to have first considered it (in his *Studien ueber hoehere Geodæsie*, 1869), proposed the name "Feldlinie"; that is, field line. He thinks it should be adopted as the geodetic line, because both linear and angular measurements conform to it. Clarke, Zachariæ, and Helmert have also mentioned it, the latter, however, only in a note, where he remarks that it deserves no consideration in geodesy.

To the second class belong two curves: 1. A curve described as follows: The surveyor at the starting point takes his directions from a staff at short distance and directs his assistant to place a staff in the prolongation. Repeating this operation from the first staff, from the second staff, etc., he describes a curve which is well known to be the shortest curve between any of its points. It is usually called the geodetic line. However, since this name would apply at least equally well to the three curves already considered, I propose the name *brachisthode* ($\beta\rho\acute{\alpha}\chi\iota\sigma\tau\omicron\varsigma$). The properties of this curve need not be considered here, such mathematicians as Gauss, Hansen, Bessel, and others, having perfected its theory. Helmert, in his "*Hoehere Geodæsie*," makes this curve the basis of nearly all geodetic computations. The brachisthodic process on a plane evidently results in a straight line, and on a sphere in a great circle. If, on these surfaces, it is in starting directed to a distant point, that point will be reached (disregarding errors of observation). Not so on other curved surfaces; there, in general, the first element of the brachisthode is not in direction to any of its points at a finite distance. 2. The *loxodrome* being a curve which has a constant inclination to a given direction, may, perhaps, be mentioned as belonging to this class.

The general equations of the two-end curves on any surface may be developed as follows:

Let the equation of the surface be:

$$u = f(x, y, z) = 0 \quad (1)$$

then if (ξ, η, ζ) is any point in the normal at the surface point (x, y, z) , we have its equations:

$$\frac{\xi - x}{\left(\frac{du}{dx}\right)} = \frac{\eta - y}{\left(\frac{du}{dy}\right)} = \frac{\zeta - z}{\left(\frac{du}{dz}\right)} \quad (2)$$

and the equation of a normal plane at the surface point (x, y, z) and passing through (x_2, y_2, z_2) , (not necessarily a surface point, but considered so here), is :

$$\begin{aligned}
 0 &= \left[(\xi - x) \left(\frac{du}{dz} \right) - (\zeta - z) \left(\frac{du}{dx} \right) \right] \left[(y_2 - y) \left(\frac{du}{dz} \right) - (z_2 - z) \left(\frac{du}{dy} \right) \right] \\
 &\quad - \left[(\eta - y) \left(\frac{du}{dz} \right) - (\zeta - z) \left(\frac{du}{dy} \right) \right] \left[(x_2 - x) \left(\frac{du}{dz} \right) - (z_2 - z) \left(\frac{du}{dx} \right) \right] \\
 &= [(y_2 - y) (\xi - x) - (x_2 - x) (\eta - y)] \left(\frac{du}{dz} \right) \\
 &\quad + [(z_2 - z) (\eta - y) - (y_2 - y) (\zeta - z)] \left(\frac{du}{dx} \right) \\
 &\quad + [(x_2 - x) (\zeta - z) - (z_2 - z) (\xi - x)] \left(\frac{du}{dy} \right) \tag{3}
 \end{aligned}$$

If in this we replace the surface point (x, y, z) by the surface point (x_1, y_1, z_1) and (ξ, η, ζ) by the surface point (x, y, z) we obtain :

$$\begin{aligned}
 0 &= [(y_2 - y_1) (x - x_1) - (x_2 - x_1) (y - y_1)] \left(\frac{du}{dz_1} \right) \\
 &\quad + [(z_2 - z_1) (y - y_1) - (y_2 - y_1) (z - z_1)] \left(\frac{du}{dx_1} \right) \\
 &\quad + [(x_2 - x_1) (z - z_1) - (z_2 - z_1) (x - x_1)] \left(\frac{du}{dy_1} \right) \tag{4}
 \end{aligned}$$

which, if combined with the equation of the surface, gives the normal section at (x_1, y_1, z_1) through (x_2, y_2, z_2) .

If, however, we replace in (3) (ξ, η, ζ) by the surface point (x, y, z) we obtain :

$$\begin{aligned}
 0 &= [(y_2 - y) (x_1 - x) - (x_2 - x) (y_1 - y)] \left(\frac{du}{dz} \right) \\
 &\quad + [(z_2 - z) (y_1 - y) - (y_2 - y) (z_1 - z)] \left(\frac{du}{dx} \right) \\
 &\quad + [(x_2 - x) (z_1 - z) - (z_2 - z) (x_1 - x)] \left(\frac{du}{dy} \right) \tag{5}
 \end{aligned}$$

and this, combined with the equation of the surface, gives the diorthodic curve.

As we move along the diorthode, (5) may be considered a plane which turns about the chord (1, 2) as an axis, so as to be always normal to the surface. It follows that the normals at any point of the diorthode are constrained to pass through the chord. They will thus generate a ruled surface, whose equation is not (5) however.

The equation of this ruled surface is obtained by eliminating x, y, z from (1), (2), and (5). It is important to remark that the diorthode does not consist of parts which are diorthodes with respect to their termini, otherwise the normals would at the same time pass through two chords from the same point and the curve would be a plane curve. Dr. Bremiker had erroneously supposed that the diorthode was touched by the normal planes. This is only the case at the termini. He has been criticized by Dr. Bruns of Pulkowa and by Helmholtz, but neither critic has shown the existence of a curve possessing this property, namely, the proöorthode, in which the normal plane at any of its points passes through the consecutive point and the forward terminus, but not in general through the starting point. If then in (5) we replace (x_1, y_1, z_1) by $(x + dx, y + dy, z + dz)$ we have:

$$\begin{aligned}
 0 &= [(y_2 - y) dx - (x_2 - x) dy] \left(\frac{du}{dz} \right) \\
 &+ [(z_2 - z) dy - (y_2 - y) dz] \left(\frac{du}{dx} \right) \\
 &+ [(x_2 - x) dz - (z_2 - z) dx] \left(\frac{du}{dy} \right) \\
 &= \left[(y_2 - y) \left(\frac{du}{dz} \right) - (z_2 - z) \left(\frac{du}{dy} \right) \right] dx \\
 &+ \left[(z_2 - z) \left(\frac{du}{dx} \right) - (x_2 - x) \left(\frac{du}{dz} \right) \right] dy \\
 &+ \left[(x_2 - x) \left(\frac{du}{dy} \right) - (y_2 - y) \left(\frac{du}{dx} \right) \right] dz \qquad (6)
 \end{aligned}$$

By means of the equation of the surface (1) and its differential equation

$$0 = \left(\frac{du}{dx} \right) dx + \left(\frac{du}{dy} \right) dy + \left(\frac{du}{dz} \right) dz \qquad (7)$$

any one of the variables with its differential can be eliminated. The resulting differential equation being integrated so as to contain the starting point (x_1, y_1, z_1) , will be the equation of a projection of the proöorthode on a coördinate plane.

The proöorthode being differently related to its ends, will be different forward and backward, while the diorthode is the same forward and backward.

The following diagram will illustrate the relative course of these curves :



Any surface of the second degree may be represented by

$$u = 0 = \left(\frac{x-a}{a}\right)^2 + \frac{y^2}{p} + \frac{z^2}{q} - a \quad (8)$$

The origin is taken at one of its real vertices, so that $(a, 0, 0)$ is its centre. The equation of the diorthode is then by (5), if we write $x_2 - x_1 = \Delta x$; $y_2 - y_1 = \Delta y$; $z_2 - z_1 = \Delta z$,

$$\begin{aligned} 0 &= [(y_2 - y)(x_1 - x) - (x_2 - x)(y_1 - y)] \frac{z}{q} \\ &+ [(z_2 - z)(y_1 - y) - (y_2 - y)(z_1 - z)] \frac{x-a}{a} \\ &+ [(x_2 - x)(z_1 - z) - (z_2 - z)(x_1 - x)] \frac{y}{p} \\ &= (y_2 x_1 - y_1 x_2 + y \Delta x - x \Delta y) \frac{z}{q} \\ &+ (z_2 y_1 - z_1 y_2 + z \Delta y - y \Delta z) \frac{x-a}{a} \\ &+ (x_2 z_1 - x_1 z_2 + x \Delta z - z \Delta x) \frac{y}{p} \\ &= \Delta x \left(\frac{1}{q} - \frac{1}{p}\right) yz + \Delta y \left(\frac{1}{a} - \frac{1}{q}\right) xz + \Delta z \left(\frac{1}{p} - \frac{1}{a}\right) xy \\ &+ (z_2 y_1 - z_1 y_2) \frac{x-a}{a} \\ &+ (x_2 z_1 - x_1 z_2 + p \Delta z) \frac{y}{p} + (y_2 x_1 - y_1 x_2 - q \Delta y) \frac{z}{q} \quad (9) \end{aligned}$$

The equations of the chord (1, 2) may be written :

$$\frac{x_2 - x}{x_1 - x} = \frac{y_2 - y}{y_1 - y} = \frac{z_2 - z}{z_1 - z} \quad (10)$$

Every point of the chord, therefore, satisfies (9), and since that

represents a surface of the second degree, it must be a hyperboloid of one sheet, for this and its varieties are the only ruled surfaces of that order. In the general form (9) it has a center in finite space. It is then the elliptic hyperboloid; but if $a = p$ (or $a = q$ or $p = q$), it has its center at an infinite distance, and it is a parabolic hyperboloid. In this case the base surface becomes:

$$0 = \frac{(x-a)^2 + y^2}{a} + \frac{z^2}{q} - a \quad (11)$$

which is a surface of revolution of the second degree.

If $a = p = q$, then (9) becomes a plane and the base surface a sphere. (9) is evidently satisfied by the center $(a, 0, 0)$, therefore the intersecting surface always passes through the center of the base surface.

I consider now the ellipsoid:

$$0 = \frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} - 1 \quad (12)$$

We have then the intersecting surface of the diorthode:

$$0 = (z_2 y_1 - z_1 y_2 + z \Delta y - y \Delta z) \frac{x}{a^2} + (x_2 z_1 - x_1 z_2 + x \Delta z - z \Delta x) \frac{y}{b^2} \\ + (y_2 x_1 - y_1 x_2 + y \Delta x - x \Delta y) \frac{z}{c^2} \quad (13)$$

Let $(0, y_x, z_x)$ be the point where the chord (1, 2) pierces the yz -plane

$$\begin{array}{ccccccc} (x_y, 0, z_y) & \text{“} & \text{“} & \text{“} & \text{“} & \text{“} & z_x - \text{“} \\ (x_z, y_z, 0) & \text{“} & \text{“} & \text{“} & \text{“} & \text{“} & x_y - \text{“} \end{array}$$

then we can easily verify the relations:

$$y_x = \frac{x_2 y_1 - x_1 y_2}{\Delta x}; \quad z_x = \frac{x_2 z_1 - x_1 z_2}{\Delta x} \quad (14_x)$$

$$z_y = \frac{y_2 z_1 - y_1 z_2}{\Delta y}; \quad x_y = \frac{y_2 x_1 - y_1 x_2}{\Delta y} \quad (14_y)$$

$$x_z = \frac{z_2 x_1 - z_1 x_2}{\Delta z}; \quad y_z = \frac{z_2 y_1 - z_1 y_2}{\Delta z} \quad (14_z)$$

and if we assume:

$$\alpha_b^2 = 1 - \frac{a^2}{b^2}; \quad \alpha_c^2 = 1 - \frac{a^2}{c^2} \quad (15_a)$$

$$\beta_c^2 = 1 - \frac{b^2}{c^2}; \quad \beta_a^2 = 1 - \frac{b^2}{a^2} \quad (15_b)$$

$$\gamma_a^2 = 1 - \frac{c^2}{a^2}; \quad \gamma_b^2 = 1 - \frac{c^2}{b^2} \quad (15_c)$$

(13) will take either of the following equivalent forms :

$$0 = \Delta z (y_z - \alpha_b^2 y) \frac{x}{a^2} + \Delta x (z_x - \beta_a^2 z) \frac{y}{b^2} + \Delta y (x_y - \gamma_a^2 x) \frac{z}{c^2} \quad (13^I)$$

$$0 = \Delta y (z_y - \alpha_c^2 z) \frac{x}{a^2} + \Delta z (x_z - \beta_a^2 x) \frac{y}{b^2} + \Delta x (y_x - \gamma_b^2 y) \frac{z}{c^2} \quad (13^{II})$$

The following relations will be much referred to :

$$0 = \frac{y_z}{\Delta y} + \frac{z_y}{\Delta z} = \frac{z_x}{\Delta z} + \frac{x_z}{\Delta x} = \frac{x_y}{\Delta x} + \frac{y_x}{\Delta y} \quad (16)$$

$$\frac{x_y - x_z}{x_y} = \frac{y_z}{y_x} = \frac{z_y}{z_x - z_x} ; \quad \frac{y_z - y_x}{y_z} = \frac{z_x}{z_z} = \frac{x_z}{x_z - x_y} ;$$

$$\frac{z_x - z_y}{z_x} = \frac{x_y}{x_z} = \frac{y_x}{y_x - y_z} \quad (17)$$

$$0 = x_y y_z z_x + y_x z_y x_z \quad (18)$$

Replacing in these $\Delta x, \Delta y, \Delta z$; y_x, z_y, x_z ; z_x, x_y, y_z

$$\text{by } \frac{1}{a^2}, \frac{1}{b^2}, \frac{1}{c^2} ; \alpha_b^2, \beta_a^2, \gamma_a^2 ; \alpha_c^2, \beta_a^2, \gamma_b^2 \quad (19)$$

$$\text{we have: } 0 = \frac{\gamma_b^2}{c^2} + \frac{\beta_c^2}{b^2} = \frac{\alpha_c^2}{a^2} + \frac{\gamma_a^2}{c^2} = \frac{\beta_a^2}{b^2} + \frac{\alpha_b^2}{a^2} \quad (16^I)$$

$$\frac{\beta_a^2 - \gamma_a^2}{\beta_a^2} = \frac{\gamma_b^2}{\alpha_b^2} = \frac{\beta_c^2}{\beta_c^2 - \alpha_c^2} ; \quad \frac{\gamma_b^2 - \alpha_b^2}{\gamma_b^2} = \frac{\alpha_c^2}{\beta_c^2} = \frac{\gamma_a^2}{\gamma_a^2 - \beta_a^2} ;$$

$$\frac{\alpha_c^2 - \beta_c^2}{\alpha_c^2} = \frac{\beta_a^2}{\gamma_a^2} = \frac{\alpha_b^2}{\alpha_b^2 - \gamma_b^2} \quad (17^I)$$

$$0 = \beta_a^2 \gamma_b^2 \alpha_c^2 + \alpha_b^2 \beta_c^2 \gamma_a^2 \quad (18^I)$$

and these relations also will be found correct.

Because in the equation of the diorthodic surface the terms in x^2, y^2, z^2 are wanting, there must be lines, perpendicular to the coordinate planes, lying wholly in the surface. To determine those perpendicular to the xy -plane, I place = 0 the term in (13^I) dependent on z and that in (13^{II}) independent of z , or

$$0 = -y \Delta x \frac{\beta_c^2}{b^2} + \frac{\Delta y}{c^2} (x_y - \gamma_a^2 x)$$

$$= -\frac{\gamma_b^2}{\gamma_a^2} \cdot \frac{x_y}{y_x} y + \left(\frac{x_y}{\gamma_a^2} - x \right) \text{ by (16) and (16}^I)$$

$$0 = \Delta y z_y \frac{x}{a^2} + \Delta z (x_z - \beta_a^2 x) \frac{y}{b^2}$$

$$= \frac{y_z}{\alpha_b^2} x + \left(\frac{x_z}{\beta_a^2} - x \right) y \text{ by (16) and (16}^I)$$

Substituting the value of y from the first into the second equation we have :

$$\begin{aligned} 0 &= \frac{y_z}{\alpha_b^2} x + \frac{\gamma_a^2}{\gamma_b^2} \cdot \frac{y_x}{x_y} \left(\frac{x_y}{\gamma_a^2} - x \right) \left(\frac{x_z}{\beta_a^2} - x \right) \\ &= \frac{\gamma_b^2}{\alpha_b^2 \gamma_a^2} \cdot \frac{y_z x_y}{y_x} x + \left(\frac{x_y}{\gamma_a^2} - x \right) \left(\frac{x_z}{\beta_a^2} - x \right); \text{ or,} \\ 0 &= \frac{\beta_a^2 - \gamma_a^2}{\beta_a^2 \gamma_a^2} (x_y - x_z) x + \left(\frac{x_y}{\gamma_a^2} - x \right) \left(\frac{x_z}{\beta_a^2} - x \right) \text{ by (17}_1\text{) and (17}_1^1\text{)} \\ &= x^2 - \left(\frac{x_y}{\beta_a^2} + \frac{x_z}{\gamma_a^2} \right) x + \frac{x_y}{\beta_a^2} \cdot \frac{x_z}{\gamma_a^2} \cdot x = \frac{x_z}{\gamma_a^2} \text{ or } x = \frac{x_y}{\beta_a^2} \end{aligned}$$

Corresponding to the first value we have :

$$y = \frac{\gamma_a^2}{\gamma_b^2} \cdot \frac{y_x}{x_y} \cdot \frac{x_y - x_z}{\gamma_a^2} = \frac{y_x}{\gamma_b^2} \cdot \frac{x_y - x_z}{x_y} = \frac{y_x}{\gamma_b^2} \text{ by (17}_1\text{)}$$

and corresponding to the second :

$$y = \frac{\gamma_a^2}{\gamma_b^2} \cdot \frac{y_x}{x_y} \cdot x_y \left(\frac{1}{\gamma_a^2} - \frac{1}{\beta_a^2} \right) = \frac{y_x}{\gamma_b^2} \cdot \frac{\beta_a^2 - \gamma_a^2}{\beta_a^2} = \frac{y_x}{\alpha_b^2} \text{ by (17}_1^1\text{)}$$

Denoting these constants by x_c, x_b, y_c, y_a , respectively, we have then the equations of a pair of generatrices of the hyperboloid (13) perpendicular to the xy - plane :

$$x = \frac{x_z}{\gamma_a^2} = x_c; \quad y = \frac{y_x}{\gamma_b^2} = y_c \quad (20_2)$$

$$x = \frac{x_y}{\beta_a^2} = x_b; \quad y = \frac{y_x}{\alpha_b^2} = y_a \quad (20_2^1)$$

Similarly the pair of generatrices perpendicular to the yz - plane:

$$y = \frac{y_x}{\alpha_b^2} = y_a; \quad z = \frac{z_x}{\alpha_c^2} = z_a \quad (20_x)$$

$$y = \frac{y_z}{\gamma_b^2} = y_c; \quad z = \frac{z_y}{\beta_c^2} = z_b \quad (20_x^1)$$

and that perpendicular to the zx - plane :

$$z = \frac{z_y}{\beta_c^2} = z_b; \quad x = \frac{x_y}{\beta_a^2} = x_b \quad (20_y)$$

$$z = \frac{z_x}{\alpha_c^2} = z_a; \quad x = \frac{x_z}{\gamma_a^2} = x_c \quad (20_y^1)$$

Now the second line of each pair intersects the chord, as may be proved thus: The equations of the chord (1, 2) are any two of the following three equations:

$$\frac{x}{x_y} + \frac{y}{y_x} - 1 = 0 \quad (21_2)$$

$$\frac{y}{y_x} + \frac{z}{z_y} - 1 = 0 \tag{21_x}$$

$$\frac{z}{z_x} + \frac{x}{x_z} - 1 = 0 \tag{21_y}$$

Now $\frac{x_b}{x_y} + \frac{y_a}{y_x} - 1 = \frac{1}{\beta_a^2} + \frac{1}{\alpha_b^2} - 1 = \alpha_b^2 + \beta_a^2 - \alpha_b^2 \beta_a^2 = 0$

and (21_x) or (21_y) can always be satisfied for some value of z ; therefore (20_z¹) intersects the chord. In the same manner it may be proved that (20_x¹) and (20_y¹) intersect the chord. It follows, then, that (20_x), (20_y), and (20_z) cannot intersect the chord, and hence belong to the same system of generation.

The equations of a pair of lines intersecting in a given point of the hyperboloid and belonging to different systems of generation can be easily found by the condition that one of them must intersect (20) and the other (20¹). I omit this, but give a remarkable symmetrical form of the equation of the hyperboloid :

$$\begin{aligned} 0 &= (x - x_b)(y - y_c)(z - z_a) - (x - x_c)(y - y_a)(z - z_b) \tag{22} \\ &= x(y_c z_a - y_a z_b) + y(z_a x_b - z_b x_c) + z(x_b y_c - x_c y_a) \\ &- xy(z_a - z_b) - yz(x_b - x_c) - zx(y_c - y_a), \text{ because } x_b y_c z_a = x_c y_a z_b \\ &\text{by (18) and (18¹)} \end{aligned}$$

It is immediately evident that this equation is satisfied by equations (20). It is not uninteresting to prove that it also satisfies (21), or that it contains the chord, since it shows the remarkable pliability of these forms by virtue of the relations (16), (17), (18), (16¹), (17¹), (18¹).

The points (x_c, y_c, z_a) , (x_c, y_c, z_b) , (x_b, y_c, z_b) , (x_b, y_a, z_b) , (x_b, y_a, z_a) , (x_c, y_a, z_a) form a warped hexagon, which lies wholly in the hyperboloid, and its sides may be considered six intersecting edges of a characteristic parallelepipedon. These edges are :

$$A = \frac{1}{2}(x_b - x_c); \quad B = \frac{1}{2}(y_c - y_a); \quad C = \frac{1}{2}(z_a - z_b) \tag{23}$$

and the co-ordinates of its center are :

$$x_o = \frac{1}{2}(x_b + x_c); \quad y_o = \frac{1}{2}(y_c + y_a); \quad z_o = \frac{1}{2}(z_a + z_b) \tag{24}$$

and these must be those of the center of the hyperboloid also.

Transferring the origin of co-ordinates to this center, we have the equation of the hyperboloid regarding (23) :

$$0 = (x - A)(y - B)(z - C) - (x + A)(y + B)(z + C) \tag{25}$$

From this equation we soon find by familiar processes the lengths and directions of the principal axes.

As to the question, Which of the alignment curves should be used in geodesy? I observe that between two intervisible points on the terrestrial spheroid the difference between the course of these curves is so extremely minute that they are practically identical; we can use then that method of tracing which is most convenient. For the distance of non-intervisible stations I consider the brachisthode the *geodetic* line as heretofore, because 1st, the diorthode becomes impracticable; and 2d, it cannot be divided into portions which are themselves diorthodes. As Assistant Wm. Eimbeck, of the United States Coast and Geodetic Survey, suggested to me, the diorthode proper cannot even be traced between very distant stations, which are intervisible only from very elevated positions, such as high peaks or the usual wooden structures. This led me to consider a new class of alignment curves—the apparent horizon alignment curves. The *a. h.* pro-orthode would be the locus of all points for which the tangent cuts the normal at the forward end; while the *a. h.* diorthode is a curve, at any point of which a tangent to the surface, which passes through the normal at one end, also passes through that at the other end. The equation (3) being adapted to these changed conditions will furnish also the equations of these curves; and I have thus found that the *a. h.* diorthode on an ellipsoid has an intersecting surface of the fourth order.

Messrs. HARKNESS and DOOLITTLE made remarks on this paper.

Mr. ASAPH HALL then made a communication on

THE DETERMINATION OF THE MASS OF A PLANET FROM OBSERVATIONS OF TWO SATELLITES.

[Abstract.]

M. Struve recommends that the position angle and distance of one satellite from another satellite be measured, instead of referring the place of each to the center of the primary planet; and a series of such measurements on satellites of Jupiter has been begun under his direction at Pulkowa. These observations are found to occupy one-third the time, and are considered two or three times as accurate as those where the planet is used. The most important advantage of the new method is its freedom from the unknown constant errors attending the old, due to the great difference in size and bright-

ness of the objects measured. The price to be paid for this advantage is a greatly increased complexity in the computation; for the elements of both orbits now enter into each equation of condition, and there are therefore twelve normal equations instead of six to solve. The comparative difficulty may be estimated by the number of auxiliary quantities that must be computed in the solution of n equations, namely:

$$\frac{1}{6} n (n + 1) (n + 5),$$

which amounts to 77 for $n = 6$, and to 442 for $n = 12$; a value nearly six times as great. But it is worth while to bear in mind that the twelve equations, by giving the elements and mean distance of each satellite, give two values of the planet's mass.

Mr. HARKNESS called attention to the advantage of substituting an accidental error, be it even a large one, for an unknown constant error.

Mr. TAYLOR criticised the designations usually given to the apsides of satellites orbits as being particular when they should be general. He suggested the terms *peri-apsis* and *apo-apsis*, or *aphapsis*.

Remarks were also made by Messrs. KUMMELL and HILL.

Before adjournment the Chairman replied to some questions as to the new object glass for the Imperial Observatory at Pulkowa; and gave a short explanation of the difficulty of calculating the true anomaly in elliptic orbits.

4TH MEETING.

MAY 9, 1883.

The Chairman presided.

Present: twelve members and one guest.

The report of a committee appointed by the General Committee of the Society to consider matters pertaining to Sections was read.

Mr. DOOLITTLE read a paper entitled

INFINITE AND INFINITESIMAL QUANTITIES.

[Abstract.]

An infinitesimal may be defined as the result of infinite division;

but the term *infinite division* probably does not represent the same conception to all mathematicians. If we suppose a quantity divided into a number of parts, and each of these parts subdivided, and similar subdivisions to go on forever, each requiring finite time, we have a conception to which the name *infinite division* may be given with some appropriateness, but which might better be called *eternal division*. Such division never reaches a result. But if we suppose the time of each subdivision to be proportional to the magnitude of each part, the entire process is completed in finite time, although no limit can be given to the number of subdivisions. If a point be supposed to have passed with constant velocity over a given distance, there was a time when it had passed over half the distance; afterward a time when the remaining distance was one-fourth of the original distance; the number of such successive halvings is certainly unlimited; and the result is that there is no remaining distance. This is division infinite but not eternal, and the result seems to be zero.

As a point is defined to be position without magnitude, so may an infinitesimal be defined to be quantitative relation without magnitude. The terms *infinitesimal*, *differential*, *nothing*, and *zero*, are not synonyms. They have the same logical denotation but differ in connotation. Mathematicians usually speak of "the value" or "the true value" of a vanishing fraction, as though any quantity whatever were not a true value. The term *serial value* is proposed as conducive to clearness of thought. A differential coefficient is the serial value of a vanishing fraction; and a differential or infinitesimal may be further defined as zero in serial relation to continuously diminishing quantity.

The term *infinitesimal* is however frequently employed like other terms to denote the symbol of its exact signification. We speak of drawing and erasing lines, meaning the visible symbols of Euclidean lines. Even in our purely mental processes we give the name *points* to the imagined small volumes that symbolize positions without magnitude. In like manner the term *infinitesimal* is employed to denote the imagined small quantity in approximate relation that symbolizes a relation which becomes exact only when magnitude disappears.

A line is infinite relatively to a point, but infinitesimal, *i. e.*, zero, relatively to a surface or volume. Every quantity is finite relatively to other quantities of its own order—zero relatively to orders

above and infinite relatively to orders below. A volume is integrated from surfaces, a surface from lines, and a line from points. Each integral is infinite relatively to the magnitudes from which it is integrated. As momentum is integrated from motion-generating force, it is infinite relatively thereto. Momentum may also be dissipated by infinitesimal decrements; and it is possible that momentum is always thus dissipated and re-integrated whenever motion is communicated from one body to another; but the principles of mathematics are equally consistent with the hypothesis that actual contact sometimes occurs, in which case motion is directly and instantaneously transmitted without dissipation or re-integration. Granting that infinitesimal time requires infinite force, momentum satisfies that condition.

This paper gave rise to considerable discussion, in which Messrs. TAYLOR, HILL, KUMMELL, and LEFAVOUR maintained the legitimacy of the notion of infinitesimals as real elements out of which quantity is built up; Messrs. ELLIOTT, DOOLITTLE, and FARQUHAR took the opposite ground, preferring the Newtonian view of the Calculus; while Mr. CHRISTIE, while preferring the infinitesimal method, maintained that no evaluation of continuous quantity, in terms of units as it must necessarily be, could ever be precise or entirely satisfactory, to however small a compass the uncertainty be reduced. Mr. CHRISTIE also pointed out some paradoxes to which the usual definitions of curves and tangents appeared to lead.

Mr. ELLIOTT then exhibited some tables to serve as a perpetual calendar, and gave a full explanation how by means of them the day of the week corresponding to that of the month for any year, New or Old Style, B. C. or A. D., could be found.

5TH MEETING.

MAY 23, 1883.

The Chairman presided.

Twenty members and guests present.

The appointment of the committee called for under the new Standing Rule relating to papers read before Sections of the Society was considered. Mr. TAYLOR moved that the committee consist of the Chairman and Secretary and a third member to be

appointed by the Chair. After some discussion by Messrs. HARKNESS and ELLIOTT it was so ordered, with the additional provision that this appointment be made for each paper separately.

Mr. G. W. HILL made a communication on

PLANETARY PERTURBATIONS OF THE MOON,

which was yet unfinished when he yielded the floor to Mr. G. K. GILBERT, who made a communication on

GRAPHIC TABLES FOR COMPUTING ALTITUDES FROM BAROMETRIC DATA.

This paper will appear in the Bulletins of the U. S. Geological Survey.

6TH MEETING.

JUNE 6, 1883.

The Chairman presided.

Present, sixteen members and guests.

Mr. G. W. HILL concluded his paper on

CERTAIN POSSIBLE ABBREVIATIONS IN THE COMPUTATION OF THE LONG-PERIOD PERTURBATIONS OF THE MOON'S MOTION DUE TO THE DIRECT ACTION OF THE PLANETS.

[Abstract.]

Hansen has characterized the calculation of these inequalities as extremely difficult. However, it seems to me that if the shortest methods are followed there is no ground for such an assertion. The work may be divided into two portions independent of each other. In one the object is to develop, in periodic series, certain functions of the moon's coördinates, which in number do not exceed five. This portion is the same whatever planet may be considered to act, and hence may be done once for all. In the other portion we seek the coefficients of certain terms in the periodic development of certain functions, five also in number, which involve the coördinates of the earth and planet only. And this part of the work is very similar to that in which the perturbations of the earth by the planet in question are the things sought. And as the multiples of the mean motions of these two bodies, which enter into the expres-

sion of the argument of the inequalities under consideration, are necessarily quite large, approximate values of the coefficients may be obtained by semi-convergent series similar to the well-known theorem of Stirling. This matter was first elaborated by Cauchy,* but in the method as left by him we are directed to compute special values of the successive derivatives of the functions to be developed. Now it unfortunately happens that these functions are enormously complicated by successive differentiation, so that it is almost impossible to write at length their second derivatives. Manifestly then, it would be a great saving of labor to substitute for the computation of special values of these derivatives a computation of a certain number of special values of the original function, distributed in such a way that the maximum advantage may be obtained. This modification has given rise to an elegant piece of analysis.

It will be noticed that in this method it is necessary to substitute in the formulæ, from the outset, the numerical values of the elements of the orbits of the earth and planet. There seems to be no objection to this on the practical side, as for the computation of the inequalities sought no partial derivatives of R , with respect to these elements, are required.

The paper is printed in full in the *American Journal of Mathematics*, Vol. VI.

Mr. E. B. ELLIOTT made a communication on

UNITS OF FORCE AND ENERGY, INCLUDING ELECTRIC UNITS.

SEVENTH MEETING.

NOVEMBER 21, 1883.

The Chairman presided.

Thirteen members present.

* Mémoire sur les approximations des fonctions de très-grands nombres, and Rapport sur un Mémoire de M. Le Verrier, qui a pour objet la détermination d'une grande inégalité du moyen mouvement de la planète Pallas. Comptes Rendus de l'Académie des Sciences de Paris. Tom. XX, pp. 691-726, 767-786, 825-847.

Mr. C. H. KUMMELL read a communication entitled
 THE THEORY OF ERRORS PRACTICALLY TESTED BY TARGET-
 SHOOTING.

[Abstract.]

Sir John Herschel treats a special case in which shots of equal probability are in circles. According to Liagre's theory target shooting is compounded of two distinct operations, viz., sighting and leveling, each of which is liable to errors, independently following the ordinary linear law of error. Some reasons for the independence of these operations are that for sighting the direction of the wind, which does not affect the leveling, must be regarded; and that, on the other hand, leveling only is affected by the range. The consequences of Liagre's theory will now be developed.

Let x = error of sighting and ε_x its mean error;
 y = error of leveling and ε_y its mean error;
 then it follows that

$$\frac{dx}{\varepsilon_x \sqrt{2\pi}} e^{-\frac{x^2}{2\varepsilon_x^2}} = \text{probability to hit anywhere at distance } x \text{ from} \\ \text{sighting axis.} \quad (1_x)$$

$$\frac{dy}{\varepsilon_y \sqrt{2\pi}} e^{-\frac{y^2}{2\varepsilon_y^2}} = \text{probability to hit anywhere at distance } y \text{ from} \\ \text{leveling axis.} \quad (1_y)$$

$$\therefore \frac{dxdy}{2\varepsilon_x \varepsilon_y \pi} e^{-\frac{x^2}{2\varepsilon_x^2} - \frac{y^2}{2\varepsilon_y^2}} = \text{probability to hit the point } (x, y). \quad (2)$$

This probability is the same for any point on the ellipse:

$$\frac{x^2}{\varepsilon_x^2} + \frac{y^2}{\varepsilon_y^2} = \frac{r^2}{\varepsilon^2}, \text{ where } \varepsilon^2 = \frac{1}{2}(\varepsilon_x^2 + \varepsilon_y^2) \quad (3)$$

This I shall call, then, an equal probability ellipse; its semi-axes are:

$$\frac{\varepsilon_x}{\varepsilon} r \text{ and } \frac{\varepsilon_y}{\varepsilon} r \quad (4)$$

and r = mean semi-diameter (which is equal to its conjugate).

$$\text{Assume} \quad x_r = \frac{\varepsilon}{\varepsilon_x} \quad \text{and} \quad y_r = \frac{\varepsilon}{\varepsilon_y} y \quad (5)$$

then every point on the equal probability ellipse (3) corresponds to a point (x_r, y_r) on the circle: $x_r^2 + y_r^2 = r^2$, (6)
 which is the reduced equal probability circle.

Counting directions from the right of the x - axis, let

$$\alpha = \text{direction of } (x, y) \tag{7}$$

$$\alpha_r = \text{ " " } (x_r, y_r), \text{ or reduced direction of } (x, y) \tag{8}$$

$$\text{then } \tan \alpha = \frac{y}{x} = \frac{\epsilon_y}{\epsilon_x} y_r \div \frac{\epsilon_x}{\epsilon_x} x_r = \frac{\epsilon_y}{\epsilon_x} \tan \alpha_r \tag{9}$$

$$\text{also } x = \frac{\epsilon_x}{\epsilon} r \cos \alpha_r \tag{10_x}$$

$$y = \frac{\epsilon_y}{\epsilon} r \sin \alpha_r \tag{10_y}$$

$$\text{whence } dx = \frac{\epsilon_x}{\epsilon} \cos \alpha_r dr - \frac{\epsilon_x}{\epsilon} r \sin \alpha_r d\alpha_r$$

$$dy = \frac{\epsilon_y}{\epsilon} \sin \alpha_r dr + \frac{\epsilon_y}{\epsilon} r \cos \alpha_r d\alpha_r$$

Transforming, then, (2) to the new variables, r and α_r , we must replace:

$$dx dy \text{ by } \frac{\epsilon_x \epsilon_y r dr d\alpha_r}{\epsilon^2}$$

and thus obtain

$$\frac{r dr d\alpha_r}{2\pi \epsilon^2} e^{-\frac{r^2}{2\epsilon^2}} = \text{probability to hit a point of which } (r, \alpha_r) \tag{11}$$

is the reduced point.

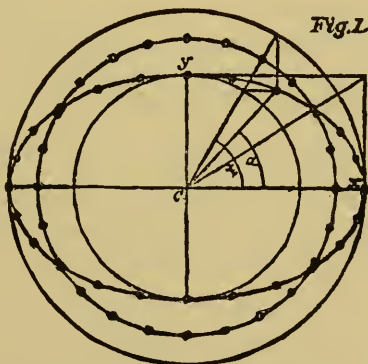


Fig. 1 exhibits 24 shots of equal probability, on an equal probability ellipse, and their reduced positions evenly distributed over the reduced circle.

The probability to hit anywhere on the perimeter of an equal probability ellipse of mean semi-diameter, r , is found by integrating (11), with respect to α , through a circumference. It is

$$P_r = \frac{rdr}{\epsilon^2} e^{-\frac{r^2}{2\epsilon^2}} \quad (12)$$

Let n_r = number of shots on area of equal probability ellipse of semi-diameter r , and n = total number; then

$$\frac{n_r}{n} = \int_0^r \frac{rdr}{\epsilon^2} e^{-\frac{r^2}{2\epsilon^2}} = 1 - e^{-\frac{r^2}{2\epsilon^2}} \text{ or } \frac{n - n_r}{n} = e^{-\frac{r^2}{2\epsilon^2}} \quad (13)$$

Let $r = \rho$; if $n_r = \frac{1}{2}n$, then $\frac{1}{2} = e^{-\frac{\rho^2}{2\epsilon^2}} \therefore \rho = \epsilon \sqrt{2l2}$ (14)
The ellipse :

$$\frac{x^2}{\epsilon_x^2} + \frac{y^2}{\epsilon_y^2} = 2l2 \quad (15)$$

is then an even chance ellipse, which is hit or missed with equal probability. Eliminating ϵ between (13) and (14), we obtain:

$$\left(\frac{n - n_r}{n}\right) \rho^2 = \left(\frac{1}{2}\right) r^2 \quad (16)$$

$$\therefore \rho = r \sqrt{\frac{\log 2}{\log \left(\frac{n}{n - n_r}\right)}} \quad (17)$$

These formulæ agree with Herschel's in form, and have, also, the same signification, in case the precisions of sighting and leveling are equal, for in that case the ellipses (3) and (15) become circles and r, ρ their radii, respectively. Herschel employs these formulæ for determining the skill of a marksman, which he defines to be $= \frac{1}{\rho}$, from the number of shots that have fallen on a circle of radius r .

Correspondingly, we should have to count the shots that have fallen on an equal probability ellipse, the axes of which have the unknown ratio $\frac{\epsilon_y}{\epsilon_x}$, which, as yet, we have no method of finding; therefore formulæ (14) and (17) cannot be employed in their general signification. If, nevertheless, we count the shots on a circle of radius r and compute a value for ρ and ϵ , we shall come as near to their true values as the problem requires, especially if the precisions of sighting and leveling are not very different. This can be

shown analytically by proving that the probability of hitting the area of the circle

$$x^2 + y^2 = r^2$$

differs from that of hitting the equal probability ellipse

$$\frac{x^2}{\epsilon_x^2} + \frac{y^2}{\epsilon_y^2} = \frac{r^2}{\epsilon^2}$$

by terms of the fourth order, with respect to the difference between the mean errors of sighting and leveling.

In computing ρ by (17) the radius (or mean semi-diameter) r is left arbitrary; it is, however, not at all indifferent; for if we take it very small or very large it will give very unreliable values of ρ .

There must then be a certain magnitude of r giving the most re-

liable value of ρ , and it is that which makes $P_r = \frac{rdr}{\epsilon^2} e^{-\frac{r^2}{2\epsilon^2}}$ a

maximum. This gives the condition: $0 = \frac{1}{\epsilon^2} - \frac{r^2}{\epsilon^4} \therefore r = \epsilon$

Thus the most favorable value of r for determining ρ is the

mean error ϵ and the ellipse $\frac{x^2}{\epsilon_x^2} + \frac{y^2}{\epsilon_y^2} = 1$ (18)

is the ellipse of the most probable shot.

Placing $r = \epsilon$ in (13), we have

$$\frac{n - n_\epsilon}{n} = e^{-\frac{1}{2}} = 0.60653 \dots$$

$$\therefore n_\epsilon = \left(1 - e^{-\frac{1}{2}}\right) n = 0.39347 \dots n = 0.4n \text{ nearly} \quad (19)$$

The most probable shot is, therefore, the distance of the $(0.4n)$ th shot from the center nearly; also the mean of the $(0.4n + m)$ th, and the $(0.4n - m)$ th shot should, if m is not too large, give a fair value of the most probable shot.

Solving (13) for ϵ , we have also

$$\epsilon = \frac{r}{\sqrt{2l \frac{n}{n - n_r}}} \quad (20)$$

From the definition of ϵ_x and ϵ_y it is obvious that

$$\epsilon_x = \sqrt{\frac{[x^2]}{n}}; \quad \epsilon_y = \sqrt{\frac{[y^2]}{n}} \quad (21)$$

which formulæ afford a comparison between the precisions of sighting and leveling. We have then

$$\epsilon = \sqrt{\frac{[s^2]}{2n}} \text{ if } s = \sqrt{x^2 + y^2} \quad (22)$$

This formula, although laborious for practical use, is the most rigorous measure of skill in shooting, and there is no need of other formulæ except when shots are lost. In that case it requires an important modification, whereby it loses in rigor if the number of lost shots is considerable. Assuming the precisions of sighting and leveling equal, then the reduced distance r in (12) will be the actual distance s of a shot; and if the target is circular, of limiting radius R , we have

$$[s^2]_1^n R = n \int_0^R s^2 \frac{sd s^*}{\epsilon^2} e^{-\frac{s^2}{2\epsilon^2}}$$

$$= n \left\{ -R^2 e^{-\frac{R^2}{2\epsilon^2}} + 2\epsilon^2 \left(1 - e^{-\frac{R^2}{2\epsilon^2}} \right) \right\}$$

Now by (13) $n_R = n \left(1 - e^{-\frac{R^2}{2\epsilon^2}} \right)$

therefore $[s^2]_1^n R = 2n_R \epsilon^2 - (n - n_R) R^2$

and $\epsilon^2 = \frac{[s^2]_1^n R + (n - n_R) R^2}{2n_R} \quad (23)$

This formula reverts, of course, to (22), if $n = n_R$, and it makes the most probable sum of the squares of the lost shots

$$[s^2]_n^n R = \frac{n}{n_R} (n - n_R) R^2$$

and since $(n - n_R) R^2$ is the smallest possible actual value of this quantity; this expression for it is quite plausible.

The targets used by the National Rifle Association are rectangular. (At long range they are 12 feet wide and 6 feet high).

Let a ($= 6$ feet) be the limiting value of x and b ($= 3$ feet) that for y , then we have, if n_{ab} is the number of hitting shots

$$n_{ab} = n \int_{-a}^a \frac{dx}{\epsilon_x \sqrt{2\pi}} e^{-\frac{x^2}{2\epsilon_x^2}} \int_{-b}^b \frac{dy}{\epsilon_y \sqrt{2\pi}} e^{-\frac{y^2}{2\epsilon_y^2}} = n P t_a P t_b \quad (24)$$

The integral $P t_a = \int_{-a}^a \frac{dx}{\epsilon_x \sqrt{2\pi}} e^{-\frac{x^2}{2\epsilon_x^2}} = \frac{2}{\sqrt{\pi}} \int_0^a dt e^{-t^2}$, and

similarly $P t_b$, is tabulated in Chauvenet's Method of Least Squares (Table IX, appendix, to the argument t), and is therefore known.

We have further :

$$\begin{aligned} [x^2]_I^{n_{ab}} &= n \int_{-a}^a x^2 \frac{dx}{\epsilon_x \sqrt{2\pi}} e^{-\frac{x^2}{2\epsilon_x^2}} \int_{-b}^b \frac{dy}{\epsilon_y \sqrt{2\pi}} e^{-\frac{y^2}{2\epsilon_y^2}} \\ &= n P t_b \left\{ - \left[\frac{\epsilon_x x}{\sqrt{2\pi}} e^{-\frac{x^2}{2\epsilon_x^2}} \right]_{-a}^a + \epsilon_x^2 \int_{-a}^a \frac{dx}{\epsilon_x \sqrt{2\pi}} e^{-\frac{x^2}{2\epsilon_x^2}} \right\} \\ &= n \epsilon_x^2 P t_b (P t_a - t_a P t_a) \end{aligned} \quad (25_x)$$

Here $P t_a$ denotes $\frac{dP t_a}{dt_a} = \frac{2}{\sqrt{\pi}} e^{-t_a^2}$ and can also be taken from Chauvenet's table, being $100 \times$ difference. Similarly,

$$[y^2]_I^{n_{ab}} = n \epsilon_y^2 P t_a (P t_b - t_b P t_b) \quad (25_y)$$

By virtue of (24) we have also

$$\epsilon_x^2 = \frac{[x^2]_I^{n_{ab}}}{n_{ab} \left(1 - t_a \frac{P t_a}{P t_b} \right)} \quad (25'_x)$$

$$\epsilon_y^2 = \frac{[y^2]_I^{n_{ab}}}{n_{ab} \left(1 - t_b \frac{P t_b}{P t_a} \right)} \quad (25'_y)$$

and these formulæ may be used to compute ϵ_x and ϵ_y by an obvious approximative process. They show that $\epsilon_x^2 > \frac{[x^2]_I^{n_{ab}}}{n_{ab}}$, as it should

be; but it may, or rather must, happen sometimes that the most probable increase of the sum of x^2 and y^2 or $[x^2]_{\substack{n \\ n_{ab}}} + [y^2]_{\substack{n \\ n_{ab}}}$ consistent with (25') is $< (n - n_{ab}) b^2$, b being the smaller limit. Such a result cannot be accepted, being contradictory to the fact that there are $n - n_{ab}$ shots at a greater distance than b . The following method gives plausible results in that case. Assume

$$(\varepsilon_y^2) = \frac{[y^2]_{\substack{n_{ab} \\ I}} + (n - n_{ab})b^2}{n} \quad (b < a) \quad (25_y'')$$

as first approximate value in (25_y'), and if $\varepsilon_y < (\varepsilon_y)$ adopt (ε_y) as final value of ε_y : but if $\varepsilon_y > (\varepsilon_y)$, then proceed in approximating to ε_y by (25_y'). The solution of (25_x') gives, as heretofore, the best value of ε_x . Among the target records of the international shooting match of 1874, at Creedmoor, there are 9 with lost shots, 5 of which give too small an increase of sum of squares, and this means that from the record of the hitting shots it would not appear probable that so many shots were lost.

Instead of the squares, we may, however, employ first powers of distances; and I shall develop the requisite formulæ for a circular target and equal precisions.

$$\begin{aligned} \text{We have } [s]_I^{nR} &= n \int_0^R s \frac{sd s}{\varepsilon^2} e^{-\frac{s^2}{2\varepsilon^2}} \\ &= n \left(-Re^{-\frac{R^2}{2\varepsilon^2}} + \varepsilon \sqrt{\frac{\pi}{2}} Pt_R \right) \\ &= -(n - n_R)R + n\varepsilon \sqrt{\frac{\pi}{2}} Pt_R \quad \text{by (13)} \\ \therefore \varepsilon &= \frac{[s]_I^{nR} + (n - n_R)R \sqrt{\frac{2}{\pi}}}{nPt_R} \quad (26) \end{aligned}$$

$$\text{If } n_R = n, \text{ this becomes } \varepsilon = \frac{[s]}{n} \sqrt{\frac{2}{\pi}} \quad (27)$$

$$\text{The quantity } r_o = \frac{[s]}{n} = \varepsilon \sqrt{\frac{\pi}{2}} \quad (28)$$

which may be called the *average shot*, has been recently introduced by the United States Ordnance Department, under the name "radius of the circle of shots," in place of the extremely defective quantity, the mean absolute deviation, the insufficiency of which was pointed out by Henry Metcalfe, Captain of Ordnance, in the Report of the Chief of Ordnance of 1882. Thus the adopted method of discussion of the precision of firearms, as used by that department, is in agreement with Liagre's theory, only the shots are not referred to the true center, but to the "center of shots," viz.: their center of gravity.

We have, now, the following three quantities, each of which may be used as a measure of precision, sighting and leveling being equally good.

1, the even chance shot, ρ .

2, the most probable shot, ε , (or mean error of sighting and leveling).

3, the average shot, r_0 , also called radius of the circle of shots; and they are related to each other as follows :

$$\frac{\rho}{\sqrt{2/2}} = \varepsilon = r_0 \sqrt{\frac{2}{\pi}} \quad (29)$$

The preceding formulæ I regard as complete, for practical discussion of target records, provided there is no evidence for a constant vitiating cause. If, for example, during a shooting match the wind is blowing constantly in the same direction, the effect of this might be partially revealed by computing for the whole match the quantity :

$$x_0 = \frac{[x]}{n} \quad (30)$$

If the sign of this quantity is consistent with the observed direction of the wind, it might, perhaps, be proper to refer the shots to a new center, to the right or left of the true center, by this quantity. In that case we have, however,

$$\varepsilon_x = \sqrt{\frac{[x^2] - nx_0^2}{n-1}} \quad (31)$$

In leveling there may be a somewhat constant individual habit of holding too high or too low, which, however, ought not to be eliminated in a fair discussion of a match, although it would be of interest to compute the quantity

$$y_0 = \frac{[y]}{n}$$

for each marksman and for a whole team.

Much less proper, it would seem to me, to regard the position of the axes unknown, and to compute their most probable position. If center and axes are to be determined, x' y' denote the co-ordinates of a shot from a random origin and position of axes, and w the angle of turning the latter into their most probable direction; then the most probable co-ordinates of a shot are:

$$x = x_0 + x' \cos w + y' \sin w; \quad y = y_0 + y' \cos w - x' \sin w.$$

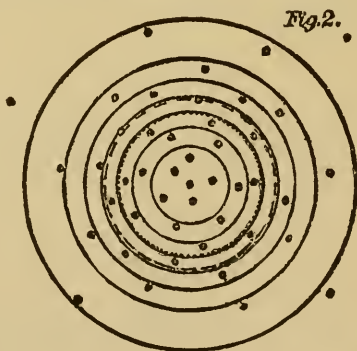
Imposing the conditions of a minimum for $[x^2]$ and $[y^2]$, we find

$$\left. \begin{aligned} x_0 &= -\frac{1}{n} ([x'] \cos w + [y'] \sin w); \\ y_0 &= -\frac{1}{n} ([y'] \cos w - [x'] \sin w) \end{aligned} \right\} (33)$$

$$\tan 2w = \frac{[x'y'] - \frac{1}{n} [x'] [y']}{[x'^2] - \frac{1}{n} [x']^2 - [y'^2] + \frac{1}{n} [y']^2} \quad (34)$$

These formulæ have, however, their proper place in the theory of Andræ's "Fehler-ellipse."

Fig. 2 exhibits an ideal distribution of 45 shots. Each ring contains 6 shots, leaving 3 shots between the outer ring and infinity. The dotted circle is that of the most probable shot, and the dashed one that of the even chance shot.



The following table refers to the combined target record of the Irish team at 800 yards range, in the international shooting match of 1874, at Creedmoor:

Irish Team at 800 yards: $\epsilon = 1.3095$ ft.; 90 shots, 88 hits.

Radii.	No. of shots on circle.		Discrepancy.	No. of shots on ring.		Discrepancy.
	Theory.	Actual.		Theory.	Actual.	
<i>Fect.</i>						
0.5	6.3	5	+1.3	6.3	5	+1.3
1.0	22.8	22	+0.8	16.5	17	-0.5
1.5	43.3	47	-3.7	20.5	25	-4.5
2.0	62.0	58	+4.0	18.7	11	+7.7
2.5	75.5	74	+1.5	13.5	16	-2.5
Leveling limit-- 3.0	83.5	83	+0.5	8.0	9	-1.0
3.5	87.5	87+?	+0.5?	4.0	4+?	0.0?
4.0	89.2	87+?	?	1.7	?	?
4.5	89.8	88+?	?	0.6	1+?	-0.4?
				89.8	88+2	

A target of 50 pistol shots at 50 yards range shows similar discordance between theory and practice, which, on an average, may be taken less than 5 per cent.

Target of pistol shots at 50 yards range: $\epsilon = 0.167$ ft.; 50 shots,
no misses.

Radii.	No. of shots on circle.		Discrep'y.	No. of shots on ring.		Discrep'y.
	Theory.	Actual.		Theory.	Actual.	
<i>in.</i>						
0.5	1.5	1	+0.5	1.5	1	+0.5
1.0	5.9	8	-2.1	4.4	7	-2.6
1.5	12.2	14	-1.8	6.3	6	+0.3
2.0	19.7	23	-3.3	7.5	9	-1.5
2.5	27.0	28	-1.0	7.3	5	+2.3
3.0	33.7	33	+0.7	6.7	5	+1.7
3.5	39.6	37	+2.6	5.9	4	+1.9
4.0	43.2	41	+2.2	3.6	4	-0.4
4.5	46.0	46	0.0	2.8	5	-2.2
5.0	47.8	47	+0.8	1.8	1	+0.8
5.5	48.8	49	-0.2	1.0	2	-1.0
6.0	49.4	50	-0.6	0.6	1	-0.4
				49.4	50	

Mr. ELLIOTT gave an example of remarkably close agreement between the distribution of errors by theory and by observation of the chest measurements of 1,516 United States soldiers, reported by Dr. Bulkley at the Berlin Statistical Congress. In five groups the greatest difference was four-tenths per cent.

EIGHTH MEETING.

DECEMBER 5, 1883.

The Chairman presided.

Fourteen members and guests present.

Mr. ALVORD discussed

A SPECIAL CASE IN MAXIMA AND MINIMA,

the problem being to find the radius of the sphere that will displace the maximum quantity of liquid from a conical wine glass full of water.

The differential co-efficient, when put equal to zero, is in the form of two factors. Equating each to zero, one gives the radius of the maximum sought; the other gives a still larger radius, which proves to be the radius of the sphere just tangent to the centre of the base of the cone, and to the sides of the cone, extended upwards. This gives the minimum displacement equal to zero. Calling a the radius of the base, b the height, and c the slant height of the cone, the radius of the sphere producing maximum displacement equals

$\frac{abc}{(c-a)(2a+c)}$; the radius corresponding to minimum displacement equals $\frac{ab}{c-a}$.

When the radius is still greater, the sphere does not reach the surface of the liquid, but displaces an imaginary quantity of the same. An analytical expression for this case was sought in vain; the result above is simple, and no square root of a negative quantity appears. By some device in the mode of investigation, this imaginary case might appear, as in the question to obtain the radical axis of two circles, discussed by Salmon.

Mr. KUMMELL suggested that the close relation between the circle $x^2 + y^2 = R^2$ and the equilateral hyperbola $x^2 - y^2 = R^2$, each of which could be regarded as an imaginary branch of the other, might help us to understand many of such difficulties. He showed that the radical axis of two circles not intersecting was the common chord of two equilateral hyperbolas whose major axes were those diameters of the circles which lie in the same straight line.

Mr. ELLIOTT read a communication on

A FINANCIAL PROBLEM,

in which he gave formulæ for calculating the advantage of in-

vestment in United States Government bonds, at six or at four per cent., and making use of the banking privileges thus available, over investment at a higher rate without such privileges. The restrictions caused by the high premium on Government bonds, the bank tax, and the necessary specie reserve were all allowed for.

This paper was discussed by Messrs. HARKNESS, DE LAND, SMILEY, and others.

Mr. H. FARQUHAR presented the following

FORM OF LEAST-SQUARE COMPUTATION.

Suppose four unknown constants, A, B, C and D, are to be calculated from equations of condition of the form

$$aA + bB + cC + dD = y.$$

Arrange columns in order (1) a^2 , (2) ab , (3) ac , (4) ad , (5) ay , (6) b^2 , (7) bc , (8) bd , (9) by , (10) c^2 , (11) cd , (12) cy , (13) d^2 , (14) dy .

Add up first five columns and place under (2) to (5) the quotients of their sums divided by $\Sigma(1)$.

Put the product $\frac{\Sigma(2)}{\Sigma(1)} \Sigma(2)$ under (6), $\frac{\Sigma(2)}{\Sigma(1)} \Sigma(3)$ under (7), $\frac{\Sigma(2)}{\Sigma(1)} \Sigma(4)$ under (8), $\frac{\Sigma(2)}{\Sigma(1)} \Sigma(5)$ under (9), $\frac{\Sigma(3)}{\Sigma(1)} \Sigma(3)$ under (10), $\frac{\Sigma(3)}{\Sigma(1)} \Sigma(4)$ under (11), $\frac{\Sigma(3)}{\Sigma(1)} \Sigma(5)$ under (12), $\frac{\Sigma(4)}{\Sigma(1)} \Sigma(4)$ under (13), and $\frac{\Sigma(4)}{\Sigma(1)} \Sigma(5)$ under (14), *reversing the sign in every case.*

Then add up (6) to (9), placing under the sums of (7) to (9) their quotients divided by $\Sigma'(6)$.

Put the product $\frac{\Sigma'(7)}{\Sigma'(6)} \Sigma'(7)$ under (10), $\frac{\Sigma'(7)}{\Sigma'(6)} \Sigma'(8)$ under (11), $\frac{\Sigma'(7)}{\Sigma'(6)} \Sigma'(9)$ under (12), $\frac{\Sigma'(8)}{\Sigma'(6)} \Sigma'(8)$ under (13), and $\frac{\Sigma'(8)}{\Sigma'(6)} \Sigma'(9)$ under (14), *reversing each sign.*

Add (10) to (12), putting quotients $\frac{\Sigma''(11)}{\Sigma''(10)}$ and $\frac{\Sigma''(12)}{\Sigma''(10)}$ under the sums.

Put the product $\frac{\Sigma''(11)}{\Sigma''(10)} \Sigma''(11)$ under (13) and $\frac{\Sigma''(11)}{\Sigma''(10)} \Sigma''(12)$ under (14), *reversing the signs.*

Add (13) and (14); when $\frac{\Sigma''(14)}{\Sigma''(13)} = D$.

Then, under (12), enter $\frac{\Sigma''(12)}{\Sigma''(11)} - \frac{\Sigma''(11)}{\Sigma''(10)} D = C$.

Next, under (9), enter $\frac{\Sigma''(9)}{\Sigma''(6)} - \frac{\Sigma''(8)}{\Sigma''(6)} D - \frac{\Sigma''(7)}{\Sigma''(6)} C = B$.

Lastly, under (5), enter $\frac{\Sigma''(5)}{\Sigma''(1)} - \frac{\Sigma''(4)}{\Sigma''(1)} D - \frac{\Sigma''(3)}{\Sigma''(1)} C - \frac{\Sigma''(2)}{\Sigma''(1)} B = A$.

NOTES.—[1] The sign of summation is distinguished by an additional stroke for every additional quantity introduced under the column added up.

[2] These additional quantities, under the columns of squares, (6), (10), and (13), will evidently all be negative.

[3] This form may be extended to any number of unknown quantities, by insertion of *ae*, etc., between (4) and (5), *be*, etc., between (8) and (9), and so on. Modifications where there is a smaller number of unknown constants, and where one of them has the coefficient always unity, will be obvious.

[4] One of the quantities *a*, *b*, etc., will, in many computations, be zero when another one is significant, and *vice-versa*; as when one unknown quantity changes in the course of a series of observations. In this case we may save some columns by arranging our equation thus: $a_1 A_1 + a_2 A_2 + b B + \text{etc.} = y$ (where $a_1 a_2 = 0$, always). Here two sums are found under columns (1) to (5), two quotients under (2) to (5), and two additional quantities placed under each of the other columns before they are summed up. The remainder of the work then proceeds as before, except that the *last* step will be duplicate.

[5] It will be found advisable always to make Σa , Σb , etc., as nearly zero as possible, so that the products will be smaller and there will be less danger of error.

[6] The computation is to be checked by applying *A*, *B*, etc., and finding the residuals of *y*. Then $\Sigma(a \Delta y)$, $\Sigma(a \Delta b)$, etc., should all be zero.

[7] Where but two unknown quantities are to be found, one of them with the constant coefficient unity (as $A + b B = y$), other methods will usually be preferable. Two of these will be given.

I. If the values of *b* are symmetrical, so that $b = \beta \pm b'_1, \beta \pm b'_2, \beta \pm b'_3$, etc., here all that is necessary to find *B* is to subtract the

value of y for every $\beta - b'$ from that for $\beta \mp b'$, to multiply the remainders by b' , to find $\Sigma (b' \Delta y)$ and divide it by $2 \Sigma (b'^2)$, when the quotient will be B. If A should be wanted also—as is very often not the case—then Σy must also be found, and $A = \frac{\Sigma y}{n} - \beta B$, where n equals the number of equations.

II. In all cases we may obtain the required values by taking the difference of b and of y from the mean of the column, multiplying the residual by the former difference, thus forming columns of $(b - \frac{\Sigma b}{n})^2$ and $(b - \frac{\Sigma b}{n})(y - \frac{\Sigma y}{n})$ adding these and dividing the second sum by the first. That is,

$$B = \frac{\Sigma \left\{ \left(b - \frac{\Sigma b}{n} \right) \left(y - \frac{\Sigma y}{n} \right) \right\}}{\Sigma \left\{ \left(b - \frac{\Sigma b}{n} \right)^2 \right\}}; \text{ when } A = \frac{\Sigma y}{n} - \frac{\Sigma b}{n} B.$$

NINTH MEETING.

DECEMBER 19, 1883.

The Chairman presided.

Sixteen members and guests present.

Mr. H. FARQUHAR furnished a

NOTE ON THE PROBLEM DISCUSSED BY MR. ALVORD,

in which he showed that the volume of a spherical segment of height h , $\pi h^2 (R - \frac{1}{3}h)$, being real for all values of h , both positive and negative, was to be interpreted for $h < 0$ or $h > 2R$ as the volume of the segment of the equilateral hyperboloid of two sheets whose axes equal R ; this volume being taken with a negative sign. It was positive for negative values of h , since it must become zero when $h = 0$ by negative increments; hence the minimum of the function when $h = 0$ in such problems as the one discussed.

Mr. DOOLITTLE read a communication on

THE REJECTION OF DOUBTFUL OBSERVATIONS.

[Abstract.]

For the purposes of this discussion we may divide errors into

two grand classes, and name them, from their consequences, *instructive errors* and *uninstructive errors*. The latter class includes blunders in recording, pointing on wrong objects, &c. The former consists of errors that indicate error in other observations.

I once tried the experiment of dropping a short straight piece of wire five hundred times upon a sheet of ruled paper and counting the number of intersections of the wire with a ruled line. When the end of the wire touched or nearly touched a line, and intersection was doubtful, I counted it as half an intersection. I recorded the number of intersections in groups of fifty trials, as follows: 23, 26, 28.5, 24, 31.5, 28, 27, 14, 25, 28.5. These numbers may be regarded as observations from which may be deduced the probable ratio of the length of the wire to the distance between two consecutive lines; and it seems impossible to account for the remarkable smallness of the eighth number by any supposition of uninstructive error. It is almost certain that a ratio deduced from it alone is largely in error; but it indicates that the other nine observations are somewhat in error, and that its error is needed to counterbalance theirs. If we retain it, and regard the mean of all as the most probable truth, we infer that this observation is 11.55 units in error. If we reject it, and take the mean of the other nine as the most probable truth, we infer that this observation is 12 5-6 units in error. It should be remembered that the rejection of an observation does not sweep from existence the fact of its occurrence; but merely increases its already large estimate of error. Because an error of 11.55 units is so large as to be very improbable, shall we therefore infer that an error of 12 5-6 units is more probable?

It seems very clear to me that the larger an instructive error is the more instructive it is, and the more important is it that the observation containing it *should not* be rejected. The mean of all the ten above-described observations being regarded as the most probable truth, any one of the other nine could be better spared than the eighth. On the other hand, the larger an uninstructive error is, the more important it is that the observation *should* be rejected. Whenever an observation is intelligently rejected, there is a comparison of two antecedent probabilities, viz.: that of the occurrence of an instructive error of the magnitude involved and that of the occurrence of an uninstructive error of the same magnitude. When an error is evidently so large that it cannot possibly belong to the instructive class, the antecedent probability of such

an instructive error is 0; the antecedent probability of an un-instructive error is always greater than 0; and the observation should certainly be rejected. But since the theory of least squares allows no limit whatever to the possible magnitude of instructive errors, such rejection involves the admission that the method of least squares is not applicable to the case. When an observation involves a merely suspicious error, which is neither so large that instructiveness is impossible nor so small as to pass without question, it would seem reasonable that the observation should be weighted according to the relative magnitudes of the two antecedent probabilities which I have mentioned; but this can never be determined with any approach to mathematical precision.

In order to make this matter clear, let us suppose for example that ninety-nine observations of equal weight and known to be free from un-instructive error are separately written on as many cards; that the number 25 is arbitrarily written on a similar card; that these hundred cards are thoroughly shuffled; and that ten cards being then drawn at random, the following numbers appear on them: 15, 18, 14, 25, 17, 16, 15, 18, 16, 17. Let it be required to determine from these data, according to the theory of least squares, the probability that the number 25 on the fourth card drawn is the record of an observation. Here the antecedent probability of an un-instructive error is by hypothesis equal to 1-10.

I commence by assuming a value of the required probability, and weight the doubtful observation accordingly. I then proceed in the ordinary method and determine an approximation to the antecedent probability of the occurrence of a genuine observation

giving the value 25 by integrating $\frac{1}{\sqrt{\pi}} \int e^{-t^2} dt$ between the

limits corresponding to 24.5 and 25.5, since the observations are taken to the nearest unit. This integral is the antecedent probability of an instructive error of the given magnitude, tainted with the incorrectness of the assumption with which I began. Call this

integral p . Then $\frac{p}{\frac{1}{10} + p}$ is the resulting required probability. If

it agrees with my original assumption, the problem is solved. If it does not agree, I have data for a better assumption according to the well-known method of trial and error. After a few repetitions of the process, as I have found by experiment, an assumption can be made that will be verified by agreement with the result.

In practical problems the antecedent probability of blunders and other uninformative errors is never known, and is only matter of exceedingly vague conjecture. Perhaps if a very large number of observations were examined, and the proportion of evidently uninformative errors ascertained, a somewhat intelligent estimate might be made of the proportion of those that exist but are not evident; and data of some little value might be gathered toward a scientific method of weighting. But I have no faith that the result would be any where near worth the labor. At present, the best that a computer can do is to reject entirely, or retain entirely, or assign a simple weight, such as $\frac{1}{2}$, $\frac{1}{3}$, or $\frac{2}{3}$, in sheer desperation, and with the feeling that his judgment is nearly or quite worthless. It would be utter folly to assign weights upon a centesimal scale; and it would also be utter folly to conjecture an antecedent probability and proceed according to the method just set forth.

It is well known that the method of least squares gives very untrustworthy information in regard to the antecedent probability of large instructive errors. In regard to the other antecedent probability required for an intelligent solution of the problem, it gives no information whatever. So far as I can understand Prof. Peirce's method of arriving at a criterion, he takes two probabilities, both functions of probabilities of instructive error, and balances them against each other. This procedure reminds me of what sometimes happens in war, when two detachments of the same army meet in the dark and fire into each other, each supposing the other to belong to the common enemy. Prof. Peirce also seems to me to violate the fundamental principle of the science of probabilities, that probabilities must be independent in order that their product shall equal concurrent probability.

If a computer resorts to the criterion when he feels that his own judgment is worthless, and only then, the criterion is harmless; since it is of no importance whether a decision is made by a worthless judgment or a worthless criterion.

In the discussion that followed, Mr. A. HALL gave a brief account of the literature of the criteria which have been proposed for the rejection of doubtful observations. In addition to the criterion proposed by Prof. Peirce, which had been discussed by Mr. Doolittle, that of Mr. E. J. Stone was mentioned; and also the proofs of a criterion given by Chauvenet and Watson. The advocacy of Peirce's criterion by Gould, Winlock, Bache, Coffin, and Schott

was noticed, and also its criticism by Airy, Stone, and Glaisher, together with Glaisher's approval of De Morgan's method of treating observations. In conclusion, Mr. HALL said:

The general result of what has been done in this matter appears to be as follows:

Every one can devise a criterion that suits himself, but it will not please other people.

Now there seems to be a good reason underlying this. The attempt to establish an arbitrary and general criterion for the discussion and rejection of observations is an attempt to eliminate from this work the knowledge and judgment of the investigator. Such an attempt ought to fail, and it certainly will fail at length, no matter by what personal influence it may be supported. It is true that no proof has been given of the principle of the arithmetical mean for a finite number of observations, such as the practical cases that always come before us; but we assume this principle as leading to the most probable result. When we depart from this principle, it must be done, I think, for reasons that are peculiar to each case, and there can be no better guide than the judgment of the investigator. It may be said that if the criteria that have been proposed be carefully managed they will do little harm, since the result of the arithmetical mean will be altered very little; and in fact this is their chief recommendation. But by diminishing the value of the real probable error the criteria give to the observations a fictitious accuracy and a weight they do not deserve.

The paper was also discussed by Messrs. HILL, ELLIOTT, FARQUHAR, WOODWARD, and others, including Mr. JAMES MAIN, a visitor—all agreeing, on essential points, with Mr. Doolittle's view.

Mr. R. S. WOODWARD then discussed

THE SPECIAL TREATMENT OF CERTAIN FORMS OF
OBSERVATION-EQUATIONS.

[Abstract.]

In a set of observation-equations whose type is

$$x_0 + (t - t_0) y - n = v \text{ with weight } p,$$

in which t_0 is an arbitrary constant, the same for each equation, and in which the residuals, v , are supposed to arise solely from errors in the observed quantities, n , it will be best to make

$$t_0 = \frac{[pt]}{[p]}$$

This value of t_0 makes the co-efficient of y in the first normal equation and the co-efficient of x_0 in the second normal equation, zero, and hence gives directly

$$x_0 = \frac{[pn]}{[p]}$$

$$y = \frac{[p(t-t_0)n]}{[p(t-t_0)^2]}$$

The weight of this value of x_0 is a maximum; *i. e.*, the value of x_0 corresponding to $t_0 = \frac{[pt]}{[p]}$ has a greater weight than the value of x_0 corresponding to any other value of t_0 .

The probable error of the function $x_0 + \mu y$ is given by the simple formula.

$$\sqrt{\varepsilon_{x_0}^2 + \mu^2 \varepsilon_y^2}$$

in which ε_{x_0} and ε_y are the probable errors of x_0 and y , respectively.

The investigation shows that, when several standards of length are to be intercompared two and two, in order to obtain the length of some one of them, it will be conducive to accuracy to have the mean temperatures of the several sets of comparisons equal.

Remarks were made upon this communication by Mr. KUMMELL.

Mr. ALEX. S. CHRISTIE made a communication on

CONTACT OF PLANE CURVES.*

[Abstract.]

Let $0 = f(x, y)$, (1), $0 = \varphi(x, y)$, (2), and $y = \psi(x)$, (3) be the equations of plane curves. Transferring the origin to (ξ, η) , where $\eta = \psi(\xi)$, writing f, φ for $f(\xi, \eta)$, $\varphi(\xi, \eta)$, respectively, and u_n for

$$\frac{1}{n!} \frac{\partial^n f}{\partial \xi^n}, v_n \text{ for } \frac{1}{n!} \frac{\partial^n \varphi}{\partial \xi^n}, \text{ we have}$$

from (1), $0 = \sum_0^\infty \left(\frac{y^n}{n!} \frac{\partial^n}{\partial \eta^n} \cdot \sum_0^\infty (x^r u_r) \right)$, (1'), from (2),

$$0 = \sum_0^\infty \left(\frac{y^n}{n!} \frac{\partial^n}{\partial \eta^n} \right) \cdot \sum (x^r v_r), \text{ (2'), and from (3), } y = x \frac{d\eta}{d\xi} + \frac{x^2}{2!} \frac{d^2\eta}{d\xi^2}$$

$$+ \frac{x^3}{3!} \frac{d^3\eta}{d\xi^3} + \&c. \tag{3'}$$

* Throughout this paper, δ , for lack of sorts, is put for round d , and denotes partial differentiation.

Writing (3') in the form $y = xw_1 + x^2w_2 + x^3w_3 + \&c.$ (3'')

and assuming $y^\nu = x^\nu(\nu_0) + x^{\nu+2}(\nu_2) + \&c.$ (4)

Where (ν_0) obviously equals w_1^ν , and $(\nu_1), (\nu_2), \&c.,$ are functions of ξ, η to be determined, we have, from (4), $\nu y^{\nu-1} \frac{dy}{dx} = x^{\nu-1} \nu(\nu_0)$

$$+ x^\nu \cdot \nu + 1 \cdot (\nu_1) + x^{\nu+1} \cdot \nu + 2 \cdot (\nu_2) + \&c. \tag{5}$$

from (3''), $\frac{dy}{dx} = x^0 \cdot 1 w_1 + x^1 \cdot 2 w_2 + x^2 \cdot 3 w_3 + \&c.$ (6)

from (3'', 5), $\nu y^\nu \cdot \frac{dy}{dx} = x^\nu ((\nu_0)^\nu w_1) + x^{\nu+1} ((\nu_0)^\nu w_2 + (\nu_1) \cdot \nu + 1 \cdot w_1)$
 $+ x^{\nu+2} ((\nu_0)^\nu w_3 + (\nu_1) \cdot \nu + 1 \cdot w_2 + (\nu_2) \cdot \nu + 2 \cdot w_1) + \&c.$

from (4, 6), $\nu y^\nu \cdot \frac{dy}{dx} = x^\nu (\nu_0)^\nu w_1 + x^{\nu+1} ((\nu_0)^\nu \cdot 2w_2 + (\nu_1)^\nu \cdot 1w_1)$
 $+ x^{\nu+2} ((\nu_0)^\nu \cdot 3w_3 + (\nu_1)^\nu \cdot 2w_2 + (\nu_2)^\nu \cdot 1w_1) + \&c.$

$\therefore 0 = (\nu_0) \cdot \nu - 0 \cdot w^2 + (\nu_1) \cdot 0 - 1 \cdot w_1$
 $0 = (\nu_0) \cdot 2\nu - 0 \cdot w_3 + (\nu_1) \cdot \nu - 1 \cdot w_2 + (\nu_2) \cdot 0 - 2 \cdot w_1$
 $0 = (\nu_0) \cdot 3\nu - 0 \cdot w_4 + (\nu_1) \cdot 2\nu - 1 \cdot w_3 + (\nu_2) \cdot \nu - 2 \cdot w_2$
 $+ (\nu_3) \cdot 0 - 3 \cdot w_1$
 $\dots \dots \dots$
 $0 = (\nu_0) \cdot m\nu - 0 \cdot w_{m+1} + (\nu_1) \cdot (m-1)\nu - 1 \cdot w_m$
 $+ (\nu_2) \cdot (m-2)\nu - 2 \cdot w_{m-1} + (\nu_3) \cdot (m-3)\nu - 3 \cdot w_{m-2}$
 $+ \dots + (\nu_m) \cdot 0 - m \cdot w_1$

Whence we have—

$$(\nu_m) = \frac{(w_1)^{\nu-m}}{m!} \times$$

$$\begin{aligned} & \nu - 0 \cdot w_2 \quad , \quad 0 - 1 \cdot w_1 \quad , \quad 0 \quad , \quad \dots \quad 0 \quad , \quad 0 \\ & 2\nu - 0 \cdot w_3 \quad , \quad \nu - 1 \cdot w_2 \quad , \quad 0 - 2 \cdot w_1 \quad , \quad \dots \quad 0 \quad , \quad 0 \\ & 3\nu - 0 \cdot w_4 \quad , \quad 2\nu - 1 \cdot w_3 \quad , \quad \nu - 2 \cdot w_2 \quad , \quad \dots \quad 0 \quad , \quad 0 \end{aligned} \quad (7)$$

$$\begin{aligned} & \vdots \quad \quad \quad \vdots \quad \quad \quad \vdots \quad \quad \quad \vdots \quad \quad \quad \vdots \quad \quad \quad \vdots \quad \quad \quad \vdots \\ & (m-2)^\nu - 0 \cdot w_{m-1} \quad , \quad (m-3)^\nu - 1 \cdot w_{m-2} \quad , \quad (m-4)^\nu - 2 \cdot w_{m-3} \quad , \quad \dots \quad 0 - (m-2) \cdot w_1 \quad , \quad 0 \\ & (m-1)^\nu - 0 \cdot w_m \quad , \quad (m-2)^\nu - 1 \cdot w_{m-1} \quad , \quad (m-3)^\nu - 2 \cdot w_{m-2} \quad , \quad \dots \quad \nu - (m-2) \cdot w_2 \quad , \quad 0 - (m-1) \cdot w_1 \\ & m^\nu - 0 \quad \cdot w_{m+1} \quad , \quad (m-1)^\nu - 1 \cdot w_m \quad , \quad (m-2)^\nu - 2 \cdot w_{m-1} \quad , \quad \dots \quad 2\nu - (m-2) \cdot w_3 \quad , \quad \nu - (m-1) \cdot w_2 \end{aligned}$$

which determines the coefficients in (4). (*) Putting u_{rs} for

$$\frac{1}{r!, s!} \frac{\delta^r + s f}{\delta \xi^r \delta \eta^s}, \text{ we have } \frac{y^r}{r!} \frac{\delta^r}{\delta \eta^r} \sum_0^\infty (x^r u_r) = x^r ((\nu_0) u_{0\nu}) + x^{r+1} ((\nu_0) u_{1\nu})$$

+ $(\nu_1) u_{0\nu}) + x^{r+2} ((\nu_0) u_{2\nu} + (\nu_1) u_{1\nu} + (\nu_2) u_{0\nu}) + \&c.$, and this in (1') gives an equation of the form

$$0 = x^0 A_0 + x^1 A_1 + x^2 A_2 + x^3 A_3 + \&c. \quad (8)$$

$$\begin{aligned} \text{viz: } 0 = & x^0 [(0_0) u_{00}] + x^1 [(0_0) u_{10} + (0_1) u_{00} + (1_0) u_{01}] \\ & + x^2 [(0_0) u_{20} + (0_1) u_{10} + (0_2) u_{00} + (1_0) u_{11} + (1_1) u_{01} + (2_0) u_{02}] \\ & + x^3 [(0_0) u_{30} + (0_1) u_{20} + (0_2) u_{10} + (0_3) u_{00} + (1_0) u_{21} + (1_1) u_{11} \\ & + (1_2) u_{01} + (2_0) u_{12} + (2_1) u_{02} + (3_0) u_{03}] + \&c. \quad (8') \end{aligned}$$

for the abscissae of points common to (1) and (3). Similarly for the abscissae of points common to (2) and (3) we get an equation of the form

$$0 = x^0 B_0 + x^1 B_1 + x^2 B_2 + x^3 B_3 + \&c. \quad (9)$$

$$\text{viz: } 0 = x^0 [(0_0) v_{00}] + x^1 [(0_0) v_{10} + (0_1) v_{00} + (1_0) v_{01}] + \&c. \quad (9')$$

Let (2) contain at least p parameters, enabling us to pass (2) through p of the intersections of (1) with (3). When this is done we have the equation $0 = x^0 (A_0 - B_0) + x^1 (A_1 - B_1) + x^2 (A_2 - B_2) + \&c.$ (10) true for the p values of x corresponding to the p points common to (1), (2), (3). Let the p common points move to the origin, (10) must have p roots equal zero, that is, $0 = A_0 - B_0, 0 = A_1 - B_1, 0 = A_2 - B_2, \dots, 0 = A_{p-1} - B_{p-1}$ (11)

If we suppose (3) the parabolic representative of (1), x in (8) becomes indeterminate, and hence besides $0 = A_0$ we have also $0 = A_1, 0 = A_2, \&c.$

that is, $0 = f$, with

$$\left\{ \begin{aligned} 0 &= \frac{\delta f}{\delta \xi} + \frac{d\eta}{d\xi} \frac{\delta f}{\delta \eta} \\ 0 &= \frac{1}{2} \frac{\delta^2 f}{\delta \xi^2} + \frac{d\eta}{d\xi} \frac{\delta^2 f}{\delta \xi \delta \eta} + \frac{1}{2} \frac{d^2 \eta}{d\xi^2} \frac{\delta f}{\delta \eta} + \frac{1}{2} \left(\frac{d\eta}{d\xi} \right)^2 \frac{\delta^2 f}{\delta \eta^2} \\ 0 &= \frac{1}{3!} \frac{\delta^3 f}{\delta \xi^3} + \frac{1}{2!} \frac{d\eta}{d\xi} \frac{\delta^3 f}{\delta \xi^2 \delta \eta} + \frac{1}{2!} \frac{d^2 \eta}{d\xi^2} \frac{\delta^2 f}{\delta \xi \delta \eta} + \frac{1}{3!} \frac{d^3 \eta}{d\xi^3} \frac{\delta f}{\delta \eta} \\ &+ \frac{1}{2!} \left(\frac{d\eta}{d\xi} \right)^2 \frac{\delta^3 f}{\delta \xi \delta \eta^2} + \frac{1}{2!} \frac{d\eta}{d\xi} \frac{d^2 \eta}{d\xi^2} \frac{\delta^2 f}{\delta \eta^2} + \frac{1}{3!} \left(\frac{d\eta}{d\xi} \right)^3 \frac{\delta^3 f}{\delta \eta^3} \\ &\quad \&c. \qquad \qquad \qquad \&c. \qquad \qquad \qquad \&c. \end{aligned} \right. \quad (12)$$

* Putting $x = 1$ in (3'') and (4), we obtain the multinomial theorem in the form $(w_1 + w_2 + w_3 + \&c.)^\nu = (\nu_0) + (\nu_1) + (\nu_2) + \&c.$

equations fully determining $\frac{d\eta}{d\xi}$, $\frac{d^2\eta}{d\xi^2}$, $\frac{d^3\eta}{d\xi^3}$, &c., in terms of the partial derivatives of f .

Again, suppose (3) the parabolic representative of (2), then $0 = B_0$, with $0 = B_1$, $0 = B_2$, &c., and consequently by (11) $0 = A_0$, with $0 = A_1$, $0 = A_2$, . . . $0 = A_{p-1}$, or the first $p-1$ of the equations (12) are satisfied indifferently whether the $\frac{d\eta}{d\xi}$, $\frac{d^2\eta}{d\xi^2}$, . . . $\frac{d^{p-1}\eta}{d\xi^{p-1}}$ therein contained be derived from (1) or (2); that is, we have arrived at Lagrange's conditions for contact of the $(p-1)$ order, as a consequence of p -punctual contact; and it follows at once that the distance between two curves in the neighborhood of a p -tuple common point is of the p^{th} order when the distance along the curves from the p -tuple point is of the 1st order.*

NOTE.

The abstracts of communications to the Mathematical Section have each been examined by a special committee, consisting of the Chairman, the Secretary, and a third member appointed by the Chairman. These third members were as follows :

<i>Title.</i>	<i>Author.</i>	<i>Third Member.</i>
Alignment Curves on any Surface-----	C. H. KUMMELL.	A. S. CHRISTIE.
The Mass of a Planet from Observa- tions of two Satellites-----	A. HALL.	W. B. TAYLOR.
Infinites and Infinitesimals-----	M. H. DOOLITTLE.	G. W. HILL.
Planetary Perturbations of the Moon--	G. W. HILL.	E. B. ELLIOTT.
The Law of Error practically tested by Target-Shooting-----	C. H. KUMMELL.	A. S. CHRISTIE.
Form of Least-Square Computation--	H. FARQUHAR.	R. S. WOODWARD.
Rejection of Doubtful Observations--	M. H. DOOLITTLE.	W. C. WINLOCK.
Special Treatment of certain forms of Observation-Equations -----	R. S. WOODWARD.	W. C. WINLOCK.
Contact of Plane Curves -----	A. S. CHRISTIE.	C. H. KUMMELL.

* This paper will be continued.

CORRIGENDA.

Vol. V, p. 86, line 2. For "abused" read *absurd*.
" " " 7. For "east" read *earth*.

INDEX.

	Page.		Page.
Abbe, Cleveland: communication on Determining the temperature of the air.....	24	Announcement of new rules concerning papers read before sections.....	38
— —: report as Treasurer.....	xxii	— — organization of Mathematical Section..	23
Address of the Chairman of the Mathematical Section.....	117	— — summer vacation.....	39
— — — President.....	xxv	Anthropic evolution.....	xlvii
Action of the International Geodetic Association as to an initial meridian and universal time.....	106	Antisell, Thomas: inquiry concerning Hawaiian Islands.....	14
Activital evolution.....	xlvii	— —: remarks on meteorologic stations.....	47
Agricultural college grants.....	100	— —: report of Auditing Committee.....	5
Ague, The conservative function of.....	5	Aphapsis.....	133
Air, Determining the temperature of the, 24, 46, 47	33	Appalachian region, Geology of.....	31
Alaska, Glaciation in.....	36	Arithmetic, Binary.....	3, 38
—, Humidity of.....	36	Arkansas bonds.....	105
Alignment curves on any surface, with special application to the ellipsoid.....	123	Articulation by the congenitally deaf... 76, 78, 84	
Alvord, Benjamin: communication on a special case in maxima and minima.....	149	Astronomy (see <i>Mars</i> , <i>Perturbation</i> , <i>Saturn</i> , <i>Venus</i> .)	
— —: remarks on agricultural college grants	106	Attraction.....	xxviii, xxxii, xxxix
— — — glaciation in Alaska.....	35	Auditing Committee, Appointment of.....	111
— — — Smithsonian funds invested in Arkansas bonds.....	105	— —, Report of.....	5
Analogues in zoo-geography.....	41	Baker, Marcus: letter to Mathematical Section.....	122
Announcement of death of B. F. Sands.....	41	Balfour memorial fund.....	5
— — — C. H. Crane.....	41	Bates, H. H.: communication on the nature of matter.....	5
— — — Elisha Foote.....	48	Beaches, Ancient, of the Hawaiian Islands..	13
— — — Josiah Curtis.....	41	Bede, ———: cited on the miraculous cure of dumbness.....	54
— — — L. D. Gale.....	48	Bell, A. G.: communication on Fallacies concerning the deaf, and the influence of such fallacies in preventing the amelioration of their condition.....	48, 84
— — — R. D. Cutts.....	111	— — —: remarks on determining the temperature of the air.....	47
— — election to membership of Albert Williams, Jr.....	14	Bibliography of medallie medical history ...	40
— — — — C. D. Walcott.....	48	Billings, J. S.: remarks on the prevention of malarial diseases.....	10
— — — — D. E. Salmon.....	111	Binary arithmetic.....	3, 38
— — — — E. C. Morgan.....	87	Biotic evolution.....	xlv
— — — — E. S. Burgess.....	28	Black bulb thermometer.....	25
— — — — H. F. Walling.....	14	Black drop, The, a spurious phenomenon.....	23
— — — — J. H. Renshawe.....	14	Bodfish, S. H., Election to membership of... 28	
— — — — J. M. Browne.....	111	Brachisthode, The.....	124
— — — — J. O. Skinner.....	36	Browne, J. M., Election to membership of.....	111
— — — — R. S. Woodward.....	14	Bulletin of the General Meeting.....	1
— — — — S. F. Emmons.....	33	— — — Mathematical Section.....	113
— — — — S. H. Bodfish.....	28	—, Rules for the publication of the.....	xiii
— — — — T. C. Chamberlin.....	36	Bulwer, John: cited on the instruction of deaf-mutes.....	54
— — — — Thomas Russell.....	10	Burgess, E. S., Election to membership of..	28
— — — — W. C. Kerr.....	33		
— — — — W. T. Sampson.....	36		
— — filling of vacant offices.....	41		
— — invitation to Anthropological and Biological Societies.....	87, 98		

Page.	Page.		
Burnett, S. M.: communication on Refraction in the principal meridians of a triaxial ellipsoid; regular astigmatism and cylindrical lenses.....	4	as to an initial meridian and universal time	106
— — — — The character of the focal lines in astigmatism	45	— — —, Death of.....	111
Calendar, Perpetual	135	Dalgarno, George: cited on communication with mutes.....	71
Cambrian system, The, in the United States and Canada.....	98	Dall, W. H., Announcement by.....	5
Cape Hatteras, Geology of.....	28	— — —: communication on glaciation in Alaska.....	33
Certain possible abbreviations in the computation of the long-period perturbations of the moon's motion due to the direct action of the planets.....	136	— — —: remarks on glaciers and solar heat,	11
Chamberlin, T. C., Election to membership of,	36	Darwin's theory of the distribution of volcanoes.....	89, 91
Character of the focal lines in astigmatism..	45	Deaf, Fallacies concerning the.....	48
Chemistry (See <i>Explosive Eruption, Specific Gravity.</i>)		Donudation and volcanism.....	91
Chickering, J. W.: communication on The thermal belts of North Carolina.....	11	Deposition of ore by replacement	32
Christie, A. S.: communication on A quasi general differentiation.....	122	Determination of the mass of a planet from observations of two satellites	132
— — — — Contact of plane curves.....	157	— — — specific gravity of solids by the common hydrometer.....	26
— — —: remarks on infinitesimals.....	135	Determining the temperature of the air, 24, 46, 47	
Clarke, F. W.: remarks on volcanic explosions	93	Differentials defined	134
Climate, Response of, to variations in solar radiation	10	Differentiation, A quasi general.....	122
Coal, Origin of.....	28	Diorthode, The.....	123
Committee, Auditing, Appointment of.....	111	Dismal Swamp	28, 30
— —, Report of.....	5	Distribution of the surplus money of the United States among the States.....	103
—, General, Constitution and duties of the. vii		— — volcanoes.....	87
ix, x, xi		Doolittle, M. H.: communication on Infinite and infinitesimal quantities.	133
—, Members of the	xiv, xv	— — — — Substance, matter, motion, and force.....	14
— on Communications, Constitution and duties of the	xii	— — — — The rejection of doubtful observations	152
— — —, Members of the	xiv, xv	— — —: remarks on binary arithmetic.....	39
— — Publications, Constitution and duties of the.....	xii, xiii	Doubtful observations, Rejection of.....	152
— — —, Members of the.....	xiv, xv	Drainage, system, The, and the distribution of the loess in eastern Iowa	93
Committees on Mathematical Papers.....	135, 161	Dreams in their relation with psychology....	37
Computation, Least-square.....	150	Driftless region, Loess of the.....	96
— of lunar perturbations	136	Dumbness, Fallacies concerning.....	49, 78
Constitution	vii	Dunes of North Carolina	29
Contact of plane curves	157	Dutton, C. E.: communication entitled The volcanic problem stated.....	87
Correlation of Cambrian groups	98	— — — — on the Geology of the Hawaiian Islands.....	13
Corrigenda.....	162	— — —: exhibition of views of the Hawaiian Islands.....	10
Crane, C. H., Death of.....	xiv, 41	— — —: remarks on determining the temperature of the air.....	48
Criteria for the rejection of observations.....	155	— — — — Ennis' hypothesis.....	45
Crova's hygrometer	36	— — — — the separation of minerals by density	27
Cultivation of the encalyptus on the Roman Campagna.....	36	Dynamic hypothesis, The, controverted.....	xxx
Curtis, Josiah, Death of.....	41	Easter, Formulas for the computation of.....	15
Curves, Alignment.....	123	Eastman, J. R.: communication on The Florida expedition for observation of the transit of Venus.....	21
—, Contact of.....	157		
Cutts, R. D.: communication on The action of the International Geodetic Association			

	Page.		Page.
Education of deaf mutes.....	77, 82, 86	Gallaudet, E. M.: remarks on fallacies concerning the deaf.....	77
Elevation and subsidence.....	31, 92	Geikie, Archibald: cited on the division of Paleozoic time.....	93
— in Alaska.....	35	General committee (See <i>Committee</i>).	
— in the Hawaiian Islands.....	13	— Meeting, Bulletin of the.....	1
Elliott, E. B.: communication entitled Formulas for the computation of Easter.....	15	Geodesy (See <i>Alignment</i>).	
— — — — A financial problem.....	149	Geodetic line, The.....	124
— — — — on Units of force and energy, including electric units.....	137	Geology of Hatteras and the neighboring coast.....	28
— — — — exhibition of perpetual calendar.....	135	— — the Hawaiian Islands.....	13
— — — — remarks on infinitesimals.....	135	— (see also <i>Cambrian, Drainage, Fault, Glaciation, Ore, Volcanic</i>).	
— — — — the metric system.....	4	Gesture language of the deaf. 63, 66, 71, 75, 79, 84	
— — — — unification of time.....	110	Gilbert, G. K.: communication on Graphic tables for computing altitudes from barometric data.....	136
Ellipsoid, Alignment curves on the.....	123	— — — — The response of terrestrial climate to secular variations in solar radiation.....	10
Emmons, S. F.: communication on Ore deposition by replacement.....	32	— — — — remarks on the drainage system of eastern Iowa.....	97
— — — —, Election to membership of.....	33	Gill, T. N.: communication on Analogues in zoo-geography.....	41
Errors, Theory of.....	138	— — — — Ichthyological results of the voyage of the Albatross.....	48
Eruption of lava.....	87	Glaciation and solar heat.....	10
Evolution defined.....	xlii	— in Alaska.....	33
—, The three methods of.....	xxvii	Glaciers classified.....	33
Experiments in binary arithmetic.....	3, 38	Graphic tables for computing altitudes from barometric data.....	136
Explosive eruption discussed.....	93	Gravitation, Explanations of.....	xxxii
Exposure of thermometers.....	24, 46		
		Hall, Asaph: address as Chairman of the Mathematical Section.....	117
Fallacies concerning the deaf, and the influence of such fallacies in preventing the amelioration of their condition.....	48	— —: communication on The determination of the mass of a planet from observations of two satellites.....	132
Fan structure of mountains.....	31	— —: election as Chairman of the Mathematical Section.....	122
Farquhar, Edward: communication on Dreams in their relation with psychology.....	37	— —: remarks on criteria for the rejection of doubtful observations.....	155
—, Henry: communication on Experiments in binary arithmetic.....	3	Harkness, William: communication on The monochromatic aberration of the human eye in aphakia.....	4
— — — — A form of least-square computation.....	150	— —: remarks on accidental and constant errors.....	133
— — — — Further experiments in binary arithmetic.....	38	— — — — determining the temperature of the air.....	26
— — — — election as Secretary of Mathematical Section.....	122	— — — — hygrometric observations.....	36
— — — — remarks on infinitesimals.....	135	— — — — the postulation of continents to support hypotheses.....	
Fault near Harper's Ferry.....	30	Harper's Ferry, Fault near.....	30
Ferrel's temperature formula.....	25	Hatteras, Geology of Cape.....	28
Finance (See <i>Distribution</i>).		Hawaiian Islands, Geology of the.....	13
Financial problem, A.....	149	— —, Views of the.....	10
Fletcher, Robert: communication on Recent experiments on serpent venom.....	38	Hazen, H. A.: communication on Hygrometric observations.....	36
Florida expedition for observation of the transit of Venus.....	21		
Foote, Elisha, Death of.....	48		
Force.....	xxviii, xxxiii		
Form of least-square computation.....	150		
Formulas for the computation of Easter.....	15		
Fossil leaves, Method of preservation of.....	30		
Frozen soil of the arctic regions.....	34, 35		
Further experiments in binary arithmetic.....	38		
Gale, L. D., Death of.....	48		

Page.	Page
Hazen, H. A.: communication on Thermometer exposure.....	46, 47
Hilgard, J. E.: organization of the Mathematical Section.....	121
— — —: remarks on the unification of longitudes and time	109
Hill, G. W.: communication on Certain possible abbreviations in the computation of the long-period perturbations of the moon's motion due to the direct action of the planets.....	136
— — —: remarks on infinitesimals	135
—, Moritz: cited on natural language.....	80
— — — — the education of deaf mutes.....	78
— — — — value of sign language to the deaf	80, 85
Homophenes.....	57, 76
Hough, F. B.: communication on the cultivation of the Eucalyptus on the Roman Campagna	36
Hubbard, G. G.: remarks on fallacies concerning the deaf.....	82
Humidity observations.....	36
— of Alaska.....	36
Hydrometer determination of the specific gravity of solids.....	26
Hygrometer observations.....	36
Hypothesis, Utility of, in science	xxxiii
Ichthyological results of the voyage of the Albatross	
Idiots, Dumbness of.....	50, 83
Illinois, Loess hills of.....	97
Inaugural address of the Chairman of the Mathematical Section.....	117
Infinite and infinitesimal quantities	133
Initial meridian, Universal.....	106
Intermarriage of deaf mutes.....	74, 76, 83
Intermittence of volcanoes.....	91
International Geodetic Association	106
Invitation to Anthropological and Biological Societies.....	87
Iowa, Loess of eastern.....	92
Kerr, W. C.: communication On the geology of Hatteras and the neighboring coast ..	
— — —, Election to membership of.....	33
Kinematic hypothesis, The.....	xxviii
King, A. F. A.: communication on The prevention of malarial diseases, illustrating, <i>inter alia</i> , the conservative function of ague.....	5
Knox, J. J.: communication on The distribution of the surplus money of the United States among the States.....	103
Kotzebue Sound ice cliffs.....	34
Kummell, C. H.: communication on Alignment curves on any surface, with special application to the ellipsoid.....	123
— — — — The theory of errors practically tested by target shooting.....	138
— — —: remarks on consequences of the relation of the circle to the equilateral hyperbola.....	149
— — — — infinitesimals.....	135
— — — — refinement in the determination of the temperature of the air.....	26
Lavas of the Hawaiian Islands.....	13
Lee, William: communication entitled Sketches from medallie medical history	39
Leadville ore deposits.....	32
Least-square computation.....	150
Lefavour, E. B.: remarks on infinitesimals.....	135
Liagre's theory.....	139
List of members	xvi
Loess of eastern Iowa.....	93
Longitudes, Unification of	106
McCullough, Hugh: remarks on money deposited by the United States with the State of Indiana.....	
McDowell, Silas: cited on thermal belts of North Carolina.....	11, 12
McGee, W J: communication on The drainage system and the distribution of the loess of eastern Iowa.....	93
Malarial diseases, Prevention of.....	5
Mallery, Garrick: election as Vice-president	41
Mallet's theory of volcanism.....	90
Marriage of deaf mutes.....	74, 76, 83
Mass of planets, Determination of.....	132
Mathematical Section, Address by Chairman of the.....	117
—, Bulletin of the.....	113, 121
—, Committee of the.....	135, 161
—, Members of the.....	116
—, Officers of the.....	122
—, Organization of the.....	28, 121
—, Rules of.....	115, 135
Mathematics (see <i>Arithmetic, Formulas, Mathematical Section</i>).....	
Matter, Combination of.....	xxxv
Maxima and minima.....	149
Medallie medical history.....	39
Melanosis, Malarial.....	7
Members, List of.....	xvi
— of the Mathematical Section.....	116
Meridian, Universal initial.....	106
Metamorphic deposits.....	32
Metamorphism and subsidence	93
Meteorology (see <i>Climate, Humidity, Hygrometer, Temperature, Thermal, Thermometer</i> .)	

Page.	Page.		
Metric system discussed.....	4	Riley, C. V., Election of, as member of the General Committee.....	41
Minerals, Separation of, by density.....	26	Rings of Saturn.....	41
Modes of motion.....	xxxviii	Rules for the publication of the Bulletin.....	xiii
Moon's motion, Perturbations of the.....	136	—, New, on papers read before sections.....	33
Morgan, E. C., Election to membership of ...	87	—, Standing, of the General Committee.....	xii
Mosquito, Inoculation by the.....	7	— — — Mathematical Section.....	115
Motion, Modes of.....	xxxviii, xli	— — — Society.....	ix
Munroe, C. E.: communication on the De- termination of the specific gravity of solids by the common hydrometer.....	26	Russell, Thomas, Election to membership of,	10
Mutes, Fallacies concerning.....	49, 78	Salmon, D. E., Election to membership of....	111
Natural language	64, 70, 75, 79	Sampson, W. T., Election to membership of,	36
Nature, The, of matter.....	5	Sands, B. F., Death of.....	41
Nebular hypothesis and volcanic eruption... 87		Saturn's rings.....	41
— — not discredited by Saturnian and Mar- tial periods	45	"Science" to report the scientific proceed- ings of the Society.....	5, 122
North Carolina, Geology of.....	28	Seismographic record obtained in Japan.....	33
— —, Thermal belts of	11	Shelters for thermometers.....	46
Notation, New arithmetic.....	3, 38	Sibscota, George: cited on the cause of dumb- ness	49
Note on the rings of Saturn.....	41	Sign language of the deaf.....	63, 66, 71, 75, 79, 84
Observation-equations.....	156	Sketches from medallic medical history.....	39
Observations, Rejection of doubtful.....	132	Skinner, J. O., Election to membership of....	36
Officers of the Mathematical Section	28, 122	Smith, Edwin: communication on a Seismo- graphic record obtained in Japan.....	87
— — — Society.....	xiv, xv	Smithsonian investment	105
Ore deposition by replacement.....	32	Solar radiation in its relation to climate	10
Peat beds of North Carolina.....	28	Sound velocity as a measure of air tempera- ture.....	47
Periapsis.....	133	Speech and thought.....	53, 81
Periods, Saturnian.....	43	— reading by the eye.....	56, 60, 70, 76, 78, 84
Perpetual Calendar.....	135	Special case, A, in maxima and minima.....	149
Perturbations, Lunar.....	136	— treatment of certain forms of observa- tion-equations.....	156
Physical evolution.....	xliiii	Specific gravities, Determination of.....	26
Picture language	84	Standard time.....	106
Porter, Sarah: cited on the use of signs by deaf-mute children.....	81	Standing rules (See <i>Rules</i>).	
Powell, J. W.: address as President.....	xxv	Substance, matter, motion, and force.....	14
— — —: remarks on the drainage system of eastern Iowa.....	97	Surplus money, Distribution of.....	103
— — — — — loess of western Illinois.....	97	Survival of the fittest, not the law of an- thropic evolution	xlvii, lii
— — — — — volcanic eruption.....	92, 93	Taylor, W. B.: communication entitled Note on the rings of Saturn.....	41
President's annual address.....	xxv	— — —: remarks on binary arithmetic	4
Prevention of malarial disease.....	5	— — — — designation of apsides	133
Proöthode, The.....	123	— — — — — infinitesimals.....	135
Quasi general differentiation, A.....	122	— — — — — thermometric observation.....	47
Recent experiments on serpent venom.....	38	Target shooting	139
Rejection of doubtful observations.....	152	Temperature of the air.....	24, 46, 47
Renshawe, J. H., Election to membership of,	14	The theory of errors practically tested by target shooting.....	138
Replacement in ore deposition	32	The thermal belts of North Carolina.....	11
Report of the Treasurer.....	xxi	Thermometer exposure.....	24, 26
— of Auditing Committee.....	5	Thought and speech.....	53, 81
Response, The, of terrestrial climate to va- riations in solar radiation.....	10	Three methods, The, of evolution.....	xxvii
		Topographical indications of a fault near Harper's Ferry.....	30

	Page.		Page
Transit of Venus.....	21	Canada.....	98
Treasurer's annual report.....	xxij	— — —, Election to membership of.....	48
— accounts for 1882, Report of Auditing Committee on the.....	5	Walling, H. F.: communication on Topo- graphical indications of a fault near Har- per's Ferry.....	30
Unification of longitudes and time.....	106	— — —, Election to membership of.....	14
Units of force and energy, including electric units.....	137	Ward, L. F.: remarks on Dismal Swamp.....	30
Universal time.....	106	Water, a factor in volcanic eruption.....	87
Velocity of sound as a measure of air tem- perature	47	White, C. A.: remarks on the drainage sys- tems of Iowa.....	97
Venus, Transit of.....	21	— — — — — instability of continents....	93
Volcanic problem, The, stated.....	87	Williams, Albert, Jr., Election to mem- bership of.....	14
Walcott, C. D.: communication on The Cam- brian system in the United States and		Woodward, R. S.: communication on the Special treatment of certain forms of ob- servation-equations	156
		— — —, Election to membership of.....	111

BULLETIN
OF THE
PHILOSOPHICAL SOCIETY
OF
WASHINGTON.

VOL. VII.

Containing the Minutes of the Society and of the Mathematical
Section for the year 1884.

PUBLISHED BY THE CO-OPERATION OF THE SMITHSONIAN INSTITUTION.

WASHINGTON:
1885.



CONTENTS.

	Page.
Constitution	VII
Standing Rules of the Society.....	IX
Standing Rules of the General Committee.....	XII
Rules for the Publication of the Bulletin	XIII
Officers elected December, 1883	XIV
Officers elected December, 1884	XV
List of Members, corrected to December 31, 1884.....	XVI
Calendar	XXII
Annual Report of the Secretaries.....	XXIII
Annual Report of the Treasurer.....	XXIV
Annual Address of the President, J. C. Welling.....	XXIX
Bulletin of the General Meeting	1
The Rochester (Minnesota) tornado, J. R. Eastman	3
Recent advances in our knowledge of the limpets, W. H. Dall.....	4
The existing glaciers of the High Sierra of California, I. C. Russell	5
The mica mines of North Carolina, W. C. Kerr	9
Recent advances in economic entomology, C. V. Riley	10
Why the eyes of animals shine in the dark, S. M. Burnett	13
Some eccentricities of ocean currents, A. B. Johnson.....	14
The periodic law of chemical elements, F. W. Clarke.....	15
The sun-glows, H. A. Hazen	17
The application of physical methods to intellectual science, R. D. Mussey	18
Deposits of volcanic dust in the Great Basin, I. C. Russell....	18
Some physical and economic features of the upper Missouri sys- tem, Lester F. Ward	20
The diversion of water courses by the rotation of the earth, G. K. Gilbert	21
The relations between northers and magnetic disturbances at Havana, G. E. Curtis, (<i>Title only</i>)	25
Composite photography applied to craniology, J. S. Billings....	25
Fisheries exhibitions, G. B. Goode, (<i>Title only</i>)	26
Music and the chemical elements, M. H. Doolittle.....	26, 27
Review of the theoretical discussion in Prof. P. G. Tait's "En- cyclopædia Britannica" article on mechanics, H. Farquhar.....	29
A new meteorite, J. R. Eastman.....	32
Certain appendages of the mollusca, W. H. Dall, (<i>Title only</i>)....	32

The volcanic sand which fell at Unalashka, October 20, 1883, and some considerations concerning its composition, J. S. Diller	33
The methods of modern petrography, G. H. Williams	36
What is a glacier? (<i>Symposium</i>)	37
The physical basis of phenomena, H. H. Bates	40
The strata exposed in the east shaft of the water-works exten- sion, T. Robinson	69
Plan for the subject bibliography of North American geologic literature, G. K. Gilbert and J. W. Powell	71
Are there separate centres for light-form- and color-percep- tion? S. M. Burnett	72
Was the earthquake of September 19th felt in the District of Columbia? T. Robinson	73
Natural naturalists, Washington Matthews	73
Resolutions on the death of Dr. Woodward	75
The volcanoes and lava fields of New Mexico, C. E. Dutton ..	76
Electric lighting, E. B. Elliott, (<i>Title only</i>)	80
Thermometer exposure, H. A. Hazen	80
Presentation of the annual address	81
Annual Meeting	81
Bulletin of the Mathematical Section	83
Standing Rules of the Section	85
Officers of the Section	86
Curves similar to their evolutes, C. H. Kummell	87
The problem of the knight's tour, G. K. Gilbert	88
Empirical formulæ for the diminution of amplitude of a freely- oscillating pendulum, H. Farquhar	89
A concrete problem in hydrostatics, G. K. Gilbert	92
The formulæ for computing the position of a satellite, A. Hall- A formula for the length of a seconds-pendulum, G. W. Hill, (<i>Title only</i>)	101
A form of the multinomial theorem, A. S. Christie, (<i>Title only</i>) ..	101
Discussion of a concrete problem in hydrostatics proposed by Mr. G. K. Gilbert, R. S. Woodward, (<i>Title only</i>)	101
The quadric transformation of elliptic integrals, combined with the algorithm of the arithmetico-geometric mean, C. H. Kummell	101, 102
A case of discontinuity in elliptic orbits, W. B. Taylor	122
The verification of predictions, M. H. Doolittle	122
Memorial to Gen. Alvord	127
Committees on mathematical communications	129
Index	131

BULLETIN
OF THE
PHILOSOPHICAL SOCIETY OF WASHINGTON.

CONSTITUTION, RULES,
LIST OF
OFFICERS AND MEMBERS,
AND REPORTS OF
SECRETARIES AND TREASURER.



CONSTITUTION

OF

THE PHILOSOPHICAL SOCIETY OF WASHINGTON.

ARTICLE I. The name of this Society shall be THE PHILOSOPHICAL SOCIETY OF WASHINGTON.

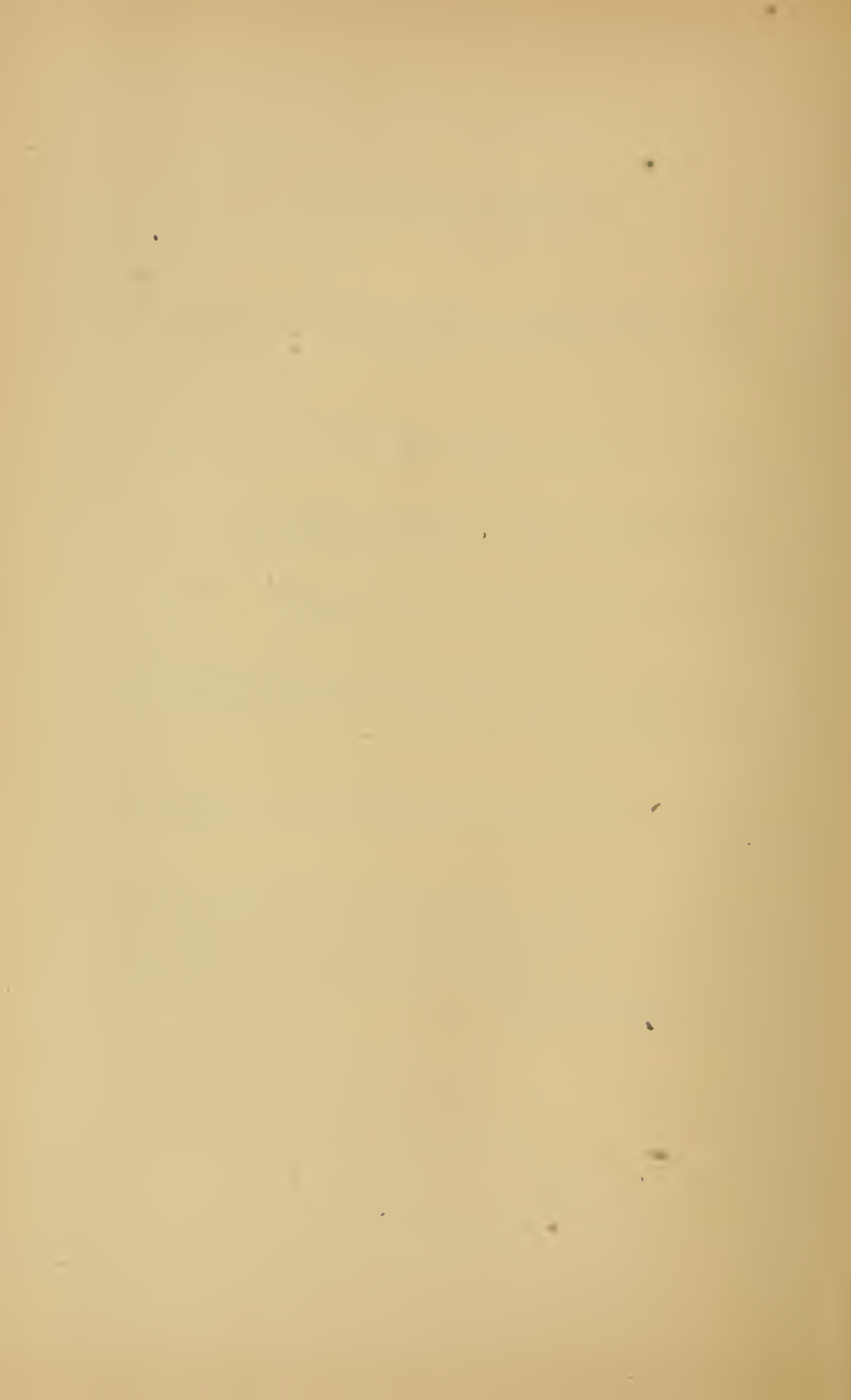
ARTICLE II. The officers of the Society shall be a President, four Vice-Presidents, a Treasurer, and two Secretaries.

ARTICLE III. There shall be a General Committee, consisting of the officers of the Society and nine other members.

ARTICLE IV. The officers of the Society and the other members of the General Committee shall be elected annually by ballot; they shall hold office until their successors are elected, and shall have power to fill vacancies.

ARTICLE V. It shall be the duty of the General Committee to make rules for the government of the Society, and to transact all its business.

ARTICLE VI. This constitution shall not be amended except by a three-fourths vote of those present at an annual meeting for the election of officers, and after notice of the proposed change shall have been given in writing at a stated meeting of the Society at least four weeks previously.



STANDING RULES

FOR THE GOVERNMENT OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON.

1. The Stated Meetings of the Society shall be held at 8 o'clock P. M. on every alternate Saturday; the place of meeting to be designated by the General Committee.

2. Notice of the time and place of meeting shall be sent to each member by one of the Secretaries.

When necessary, Special Meetings may be called by the President.

3. The Annual Meeting for the election of officers shall be the last stated meeting in the month of December.

The order of proceedings (which shall be announced by the Chair) shall be as follows:

First, the reading of the minutes of the last Annual Meeting.

Second, the presentation of the annual reports of the Secretaries, including the announcement of the names of members elected since the last annual meeting.

Third, the presentation of the annual report of the Treasurer.

Fourth, the announcement of the names of members who, having complied with Section 13 of the Standing Rules, are entitled to vote on the election of officers.

Fifth, the election of President.

Sixth, the election of four Vice-Presidents.

Seventh, the election of Treasurer.

Eighth, the election of two Secretaries.

Ninth, the election of nine members of the General Committee.

Tenth, the consideration of Amendments to the Constitution of the Society, if any such shall have been proposed in accordance with Article VI of the Constitution.

Eleventh, the reading of the rough minutes of the meeting.

4. Elections of officers are to be held as follows :

In each case nominations shall be made by means of an informal ballot, the result of which shall be announced by the Secretary ; after which the first formal ballot shall be taken.

In the ballot for Vice-Presidents, Secretaries, and Members of the General Committee, each voter shall write on one ballot as many names as there are officers to be elected, viz., four on the first ballot for Vice-Presidents, two on the first for Secretaries, and nine on the first for Members of the General Committee ; and on each subsequent ballot as many names as there are persons yet to be elected ; and those persons who receive a majority of the votes cast shall be declared elected.

If in any case the informal ballot result in giving a majority for any one, it may be declared formal by a majority vote.

5. The Stated Meetings, with the exception of the annual meeting, shall be devoted to the consideration and discussion of scientific subjects.

The Stated Meeting next preceding the Annual Meeting shall be set apart for the delivery of the President's Annual Address.

6. Sections representing special branches of science may be formed by the General Committee upon the written recommendation of twenty members of the Society.

7. Persons interested in science, who are not residents of the District of Columbia, may be present at any meeting of the Society, except the annual meeting, upon invitation of a member.

8. Similar invitations to residents of the District of Columbia, not members of the Society, must be submitted through one of the Secretaries to the General Committee for approval.

9. Invitations to attend during three months the meetings of the Society and participate in the discussion of papers, may, by a vote of nine members of the General Committee, be issued to persons nominated by two members.

10. Communications intended for publication under the auspices of the Society shall be submitted in writing to the General Committee for approval.

11. Any paper read before a Section may be repeated, either entire or by abstract, before a general meeting of the Society, if such repetition is recommended by the General Committee of the Society.

12. New members may be proposed in writing by three members of the Society for election by the General Committee; but no person shall be admitted to the privileges of membership unless he signifies his acceptance thereof in writing within two months after notification of his election.

13. Each member shall pay annually to the Treasurer the sum of five dollars, and no member whose dues are unpaid shall vote at the annual meeting for the election of officers, or be entitled to a copy of the Bulletin.

In the absence of the Treasurer, the Secretary is authorized to receive the dues of members.

The names of those two years in arrears shall be dropped from the list of members.

Notice of resignation of membership shall be given in writing to the General Committee through the President or one of the Secretaries.

14. The fiscal year shall terminate with the Annual Meeting.

15. Members who are absent from the District of Columbia for more than twelve months may be excused from payment of the annual assessments. They can, however, resume their membership by giving notice to the President of their wish to do so.

16. Any member not in arrears may, by the payment of one hundred dollars at any one time, become a life member, and be relieved from all further annual dues and other assessments.

All moneys received in payment of life membership shall be invested as portions of a permanent fund, which shall be directed solely to the furtherance of such special scientific work as may be ordered by the General Committee.

STANDING RULES
OF THE
GENERAL COMMITTEE OF THE PHILOSOPHICAL
SOCIETY OF WASHINGTON.

1. The President, Vice-Presidents, and Secretaries of the Society shall hold like offices in the General Committee.

2. The President shall have power to call special meetings of the Committee, and to appoint Sub-Committees.

3. The Sub-Committees shall prepare business for the General Committee, and perform such other duties as may be entrusted to them.

4. There shall be two Standing Sub-Committees; one on Communications for the Stated Meetings of the Society, and another on Publications.

5. The General Committee shall meet at half-past seven o'clock on the evening of each Stated Meeting, and by adjournment at other times.

6. For all purposes except for the amendment of the Standing Rules of the Committee or of the Society, and the election of members, six members of the Committee shall constitute a quorum.

7. The names of proposed new members recommended in conformity with Section 11 of the Standing Rules of the Society, may be presented at any meeting of the General Committee, but shall lie over for at least four weeks before final action, and the concurrence of twelve members of the Committee shall be necessary to election.

The Secretary of the General Committee shall keep a chronological register of the elections and acceptances of members.

8. These Standing Rules, and those for the government of the Society, shall be modified only with the consent of a majority of the members of the General Committee.

RULES
FOR THE
PUBLICATION OF THE BULLETIN
OF THE
PHILOSOPHICAL SOCIETY OF WASHINGTON.

1. The President's annual address shall be published in full.
2. The annual reports of the Secretaries and of the Treasurer shall be published in full.
3. When directed by the General Committee, any communication may be published in full.
4. Abstracts of papers and remarks on the same will be published, when presented to the Secretary by the author in writing within two weeks of the evening of their delivery, and approved by the Committee on Publications. Brief abstracts prepared by one of the Secretaries and approved by the Committee on Publications may also be published.
5. If the author of any paper read before a Section of the Society desires its publication, either in full or by abstract, it shall be referred to a committee to be appointed as the Section may determine.
The report of this committee shall be forwarded to the Publication Committee by the Secretary of the Section, together with any action of the Section taken thereon.
6. Communications which have been published elsewhere, so as to be generally accessible, will appear in the Bulletin by title only, but with a reference to the place of publication, if made known in season to the Committee on Publications.

OFFICERS

OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON

ELECTED DECEMBER 22, 1883.

President-----J. C. WELLING.
Vice-Presidents-----J. S. BILLINGS. GARRICK MALLERY.
 J. E. HILGARD. ASAPH HALL.
Treasurer----- CLEVELAND ABBE.
Secretaries ----- HENRY FARQUHAR. G. K. GILBERT.

MEMBERS AT LARGE OF THE GENERAL COMMITTEE.

H. H. BATES. E. B. ELLIOTT.
 W. H. DALL. ROBERT FLETCHER.
 C. E. DUTTON. WILLIAM HARKNESS.
 J. R. EASTMAN. J. J. KNOX. *
 C. V. RILEY.

STANDING COMMITTEES.

On Communications :

J. S. BILLINGS, *Chairman*. HENRY FARQUHAR. G. K. GILBERT.

On Publications :

G. K. GILBERT, *Chairman*. CLEVELAND ABBE. HENRY FARQUHAR.
 S. F BAIRD †

* Mr. Knox resigned May 10, 1884, and the General Committee elected Mr. F. W. Clark to the vacancy.

† As Secretary of the Smithsonian Institution.

OFFICERS

OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON

ELECTED DECEMBER 20, 1884.

President.....ASAPH HALL.
Vice-Presidents.....J. S. BILLINGS. GARRICK MALLERY.
 WILLIAM HARKNESS. J. E. HILGARD.
Treasurer.....ROBERT FLETCHER.
Secretaries.....G. K. GILBERT. HENRY FARQUHAR.

MEMBERS AT LARGE OF THE GENERAL COMMITTEE.

MARCUS BAKER.	H. H. BATES.
F. W. CLARKE.	W. H. DALL.
C. E. DUTTON.	J. R. EASTMAN.
E. B. ELLIOTT.	H. M. PAUL.
C. V. RILEY.	

STANDING COMMITTEES.

On Communications :

J. S. BILLINGS, *Chairman.* G. K. GILBERT. HENRY FARQUHAR.

On Publications :

G. K. GILBERT, *Chairman.* ROBERT FLETCHER. HENRY FARQUHAR.
 S. F. BAIRD.*

*As Secretary of the Smithsonian Institution.

LIST OF MEMBERS

OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON.

Corrected to December 20, 1884.

The names of founders are printed in SMALL CAPITALS.

(*d*) indicates *deceased*.

(*a*) indicates *absent* from the District of Columbia and excused from payment of dues until announcing his return.

(*r*) indicates *resigned*.

NAME.	P. O. ADDRESS AND RESIDENCE.	DATE OF ADMISSION.
Abbe, Cleveland.....	Army Signal Office. 2017 I St. N. W...	1871, Oct. 29
Abert, Sylvanus Thayer.....	1724 Penn. Ave. N. W.....	1875, Jan. 30
Adams, Henry.....	1607 H St. N. W.....	1881, Feb. 5
Aldis, Asa Owen.....	1765 Mass. Ave.....	1873, Mar. 1
Allen, James.....	Army Signal Office. 1907 I St. N. W.....	1882, Feb. 25
Alvord, Benjamin (<i>d</i>).....	1882, Mar. 23
ANTISELL, THOMAS.....	Patent Office. 1311 Q St. N. W.....	1871, Mar. 13
Avery, Robert Stanton.....	Coast and Geodetic Survey Office. 320 A St. S. E.	1879, Oct. 11
Babcock, Orville Elias (<i>d</i>).....	1871, June 9
Bailey, Theodorus (<i>d</i>).....	1873, Mar. 1
BAIRD, SPENCER FULLERTON.....	Smithsonian Institution. 1445 Mass. Ave. N. W.	1871, Mar. 13
Baker, Frank.....	326 C St. N. W.....	1881, May 14
Baker, Marcus.....	Coast and Geodetic Survey Office. 1205 Rhode Island Ave.	1876, Mar. 11
Bancroft, George.....	1623 H St. N. W., or Newport, R. I.....	1875, Jan. 16
Barnard, William Stebbins.....	Agricultural Department. 917 N. Y. Ave. N. W., or Canton, Ill.	1884, Mar. 1
BARNES, JOSEPH K. (<i>d</i>).....	1871, Mar. 13
Bates, Henry Hobart.....	Patent Office. The Portland.....	1871, Nov. 4
Bean, Tarleton Hoffman.....	National Museum. 1411 R. I. Ave.....	1884, Apr. 26
Beardslee, Lester Anthony (<i>a</i>).....	Captain U. S. N., Navy Department.....	1875, Feb. 27
Bell, Alexander Graham.....	Scott Circle. 1500 R. I. Ave.....	1879, Mar. 29
Bell, Chichester Alexander.....	1221 Conn. Ave.....	1881, Oct. 8
BENÉT, STEPHEN VINCENT.....	Ordnance Office, War Department. 1717 I St. N. W.	1871, Mar. 13
Bessels, Emil.....	Smithsonian Institution. 1444 N St. N. W.	1875, Jan. 16
BILLINGS, JOHN SHAW.....	Surg. Gen'l's Office, U. S. A. 3027 N St. N. W.	1871, Mar. 13
Birney, William.....	456 Louisiana Ave. 1901 Harewood Ave., Le Droit Park.	1879, Mar. 29
Birnie, Rogers (<i>a</i>).....	Cold Spring, Putnam Co., N. Y.....	1876, Mar. 11
Blair, Henry Wayne (<i>d</i>).....	1884, Feb. 2
Bodfish, Sumner Homer.....	Geological Survey. 605 F St. N. W.....	1883, Mar. 24
Boutelle, Charles Otis.....	Coast and Geodetic Survey Office. 1512 20th St. N. W.	1884, Feb. 16
Bowles, Francis Tiffany.....	1823 Jefferson Place.....	1884, Mar. 29
Brown, Stimson Joseph.....	Naval Observatory, 2133 K St. N. W.....	1884, Apr. 12
Browne, John Mills.....	Medical Director, U. S. N. The Port- land.	1883, Nov. 24
Burchard, Horatio Chapin.....	Director of the Mint. Riggs House.....	1879, May 10

LIST OF MEMBERS.

XVII

NAME.	P. O. ADDRESS AND RESIDENCE.	DATE OF ADMISSION.
Burgess, Edward Sandford.....	High School. 810 12th St. N. W.....	1883, Mar. 24
Burnett, Swan Moses.....	1215 I St. N. W.....	1879, Mar. 29
Busey, Samuel Clagett.....	1525 I St. N. W.....	1874, Jan. 17
CAPRON, HORACE.....	The Portland.....	1871, Mar. 13
Case, Augustus Ludlow (a).....	Bristol, R. I.....	1872, Nov. 16
CASEY, THOMAS LINCOLN.....	Col. Corps of Engineers. 1419 K St. N. W.....	1871, Mar. 13
Caziarc, Louis Vasmer (a).....	War Department.....	1882, Feb. 25
CHASE, SALMON PORTLAND (d).....	1871, Mar. 13
Chamberlin, Thomas Crowder.....	Geological Survey.....	1883, Mar. 24
Chickering, John White, Jr.....	Deaf Mute College, Kendall Green.....	1874, Apr. 11
Christie, Alexander Smyth.....	Coast and Geodetic Survey Office. 628 Mass. Ave. N. W.....	1880, Dec. 4
Clapp, William Henry (a).....	Ft. Davis, Tex. 1416 Corcoran St. Washington.....	1882, Feb. 25
Clark, Edward.....	Architect's Office, Capitol. 417 4th St. N. W.....	1877, Feb. 24
Clark, Ezra Westcote.....	Revenue Marine Bureau, Treasury Department. Woodley Road.....	1882, M.r. 25
Clarke, Frank Wigglesworth.....	Geological Survey. 1425 Q St. N. W.....	1874, Apr. 11
COFFIN, JOHN HUNTINGTON CRANE.....	1901 I St. N. W.....	1871, Mar. 13
Collins, Frederick (d).....	1879, Oct. 21
Comstock, John Henry (a).....	Cornell University, Ithaca, N. Y.....	1880, Feb. 14
Cones, Elliott.....	Smithsonian Inst. 1726 N. St. N. W.....	1874, Jan. 17
CRAIG, BENJAMIN FANEUIL (d).....	1871, Mar. 13
Craig, Robert.....	Army Signal Office. 1008 I St. N. W.....	1873, Jan. 4
Craig, Thomas (a).....	Johns Hopkins Univ., Baltimore, Md.....	1879, Nov. 22
CRANE, CHARLES HENRY (d).....	1871, Mar. 13
Curtis, George Edward.....	Army Signal Office. 1416 Corcoran St.....	1884, Jan. 5
Curtis, Josiah (d).....	1874, Mar. 28
Cutts, Richard Dominicus (d).....	1871, Apr. 29
DALL, WILLIAM HEALEY.....	Care Smithsonian Institution. 1119 12th St. N. W.....	1871, Mar. 13
Davis, Charles Henry (d).....	1874, Jan. 17
Davis, Charles Henry.....	Navy Department. 1705 Rhode Island Ave. N. W.....	1880, June 19
Dean, Richard Crain (a).....	Naval Hospital, New York.....	1872, Apr. 23
De Caidry, William Augustin.....	Commissary General's Office. 924 19th St. N. W.....	1881, Apr. 30
De Land, Theodore Louis.....	Treasury Dept. 126 7th St. N. E.....	1880, Dec. 18
Dewey, Frederick Perkins.....	National Museum. 1007 G St. N. W.....	1884, Apr. 25
Dewey, George (r).....	1879, Feb. 15
Diller, Joseph Silas.....	Geological Survey.....	1881, Mar. 1
Doolittle, Myrick Hasecall.....	Coast and Geodetic Survey Office. 1925 I St. N. W.....	1876, Feb. 12
Dorr, Frederic William (d).....	1874, Jan. 17
Dunwoody, Henry Harrison Chase (a).....	Army Signal Office. 3012 Dumbarton St., Georgetown.....	1873, Dec. 20
Dutton, Clarence Edward.....	Geological Survey.....	1872, Jan. 27
DYER, ALEXANDER B. (d).....	1871, Mar. 13
Earl, Robert Edward.....	National Museum.....	1884, Apr. 26
Eastman, John Robie.....	Naval Observatory. 1823 I St. N. W.....	1871, May 27
EATON, AMOS BEEBE (d).....	1871, Mar. 13
Eaton, John.....	Bureau of Education, Interior Dept. 712 East Capitol St.....	1874, May 8
Eimbeck, William.....	Coast and Geodetic Survey Office.....	1884, Feb. 2
Eldredge, Stewart (a).....	Yokohama, Japan.....	1871, June 9
ELLIOT, GEORGE HENRY (r).....	1871, Mar. 13
ELLIOT, EZEKIEL BROWN.....	Government Actuary, Treasury Department. 1210 G St. N. W.....	1871, Mar. 13
Emmons, Samuel Franklin.....	Geological Survey. 23 Lafayette Place.....	1883, Apr. 7
Endlich, Frederic Miller (a).....	Smithsonian Institution. Lake Valley, New Mexico.....	1873, Mar. 1
Ewing, Charles (d).....	1874, Jan. 17
Ewing, Hugh (a).....	Lancaster, Ohio.....	1874, Jan. 17
Farquhar, Edward.....	Patent Office Library. 1915 H St. N. W.....	1876, Feb. 12

NAME.	P. O. ADDRESS AND RESIDENCE.	DATE OF ADMISSION.
Farquhar, Henry.....	Coast and Geodetic Survey Office. Brooks Station, D. C.	1881, May 14
Ferrel, William.....	Army Signal Office. 471 C St. N. W....	1872, Nov. 16
Fletcher, Robert.....	Surgeon Gen's Office, U. S. A. 1326 L St. N. W.	1873, Apr. 10
Flint, Albert Stowell.....	Naval Observatory. 1450 Chapin St., College Hill.	1882, Mar. 25
Flint, James Milton.....	Navy Dept. U. S. S. Albatross.....	1881, Mar. 19
FOOTE, ELISHA (<i>d</i>).....	1871, Mar. 13
Foster, John Gray (<i>d</i>).....	1873, Jan. 18
French, Henry Flagg (<i>r</i>).....	1882, Mar. 25
Fristoe, Edward T.....	1434 N St. N. W.....	1873, Mar. 29
Gale, Leonard Dunnell (<i>d</i>).....	1874, Jan. 17
Gallaudet, Edward Miner.....	Deaf Mute College, Kendall Green....	1875, Feb. 27
Gannett, Henry.....	Geological Survey. 1881 Harewood Ave., Le Droit Park.	1874, Apr. 11
Gardiner, James Terry (<i>a</i>).....	State Survey, Albany, N. Y.....	1874, Jan. 17
Garnett, Alexander Young P. (<i>r</i>).....	1878, Mar. 16
Gihon, Albert Leary.....	Naval Hospital, 2019 Hillyer Place N. W.	1880, Dec. 18
Gilbert, Grove Karl.....	Geological Survey. 1424 Corcoran St....	1873, June 7
GILL, THEODORE NICHOLAS.....	Smithsonian Institution.....	1871, Mar. 13
Godding, William Whitney.....	Government Asylum for the Insane....	1879, Mar. 29
Goode, George Brown.....	National Museum. 1620 Mass. Ave. N. W.	1874, Jan. 31
Goodfellow, Edward.....	Coast and Geodetic Survey Office.....	1875, Dec. 18
Goodfellow, Henry (<i>r</i>).....	1871, Nov. 4
Gore, James Howard.....	Columbian Univ. 1305 Q St. N. W....	1880, Mar. 14
Graves, Edward Oziel (<i>a</i>).....	Asst. Treasurer U. S.....	1874, Apr. 11
Graves, Walter Hayden (<i>a</i>).....	Denver, Colorado.....	1878, May 25
Greely, Adolphus Washington.....	Army Signal Office. 1909 I St.....	1880, June 19
Green, Bernard Richardson.....	1738 N St. N. W.....	1879, Feb. 15
Green, Francis Mathews (<i>a</i>).....	Navy Department.....	1875, Nov. 9
GREENE, BENJAMIN FRANKLIN (<i>a</i>).....	West Lebanon, N. H.....	1871, Mar. 13
Greene, Francis Vinton.....	District Commissioners' Office, 1915 G St. N. W.	1875, Apr. 10
Gregory, John Milton.....	15 Grant Place.....	1884, Mar. 29
Gunnell, Francis M.....	Surgeon General, U. S. N. 600 20th St. N. W.	1879, Feb. 1
Hains, Peter Conover.....	1824 Jefferson Place.....	1879, Feb. 15
HALL, ASAPH.....	Naval Observatory. 2715 N St. N. W....	1871, Mar. 13
Hall, Asaph, jr.....	Naval Observatory. 2715 N St. N. W....	1880, Dec. 20
Hanscom, Isaiah (<i>d</i>).....	1873, Dec. 20
HARKNESS, WILLIAM.....	Naval Observatory. 1415 G St. N. W....	1871, Mar. 13
Hassler, Ferdinand Augustus (<i>a</i>).....	Santa Ana, Los Angeles Co., Cal.....	1880, May 8
HAYDEN, FERDINAND VANDEVEER (<i>a</i>).....	Geological Survey. 1803 Arch St., Phil- adelphia, Penn.	1871, Mar. 13
Hazen, Henry Allen.....	P. O. Box No. 427. 1416 Corcoran St....	1882, Mar. 25
Hazen, William Babcock.....	Army Signal Office. 1601 K. St. N. W....	1881, Feb. 5
Heap, David Porter.....	Light House Board, Treasury Depart- ment. 1618 Rhode Island Ave.	1884, Mar. 15
HENRY, JOSEPH (<i>d</i>).....	1871, Mar. 13
Henshaw, Henry Wetherbee.....	Bureau of Ethnology, P. O. Box 585....	1874, Apr. 11
HILGARD, JULIUS ERASMUS.....	Coast and Geodetic Survey Office. 1709 Rhode Island Ave. N. W.	1871, Mar. 13
Hill, George William.....	Nautical Almanac Office. 314 Ind. Ave. N. W.	1879, Feb. 1
Hitchcock, Romyn.....	P. O. Box 630.....	1884, Apr. 26
Holden, Edward Singleton (<i>a</i>).....	Madison, Wisconsin.....	1873, June 21
Holmes, William Henry.....	Geological Survey. 1100 O St. N. W....	1879, Mar. 29
Hough, Franklin Benjamin (<i>a</i>).....	Agricultural Dept. Lowville, N. Y....	1879, Mar. 29
Howell, Edwin Eugene (<i>a</i>).....	Rochester N. Y.....	1874, Jan. 31
HUMPHREYS, ANDREW ATKINSON (<i>d</i>).....	1871, Mar. 13
Jackson, Henry Arundel Lambe (<i>a</i>).....	War Department.....	1875, Jan. 30
James, Owen (<i>a</i>).....	Scranton, Pa.....	1880, Jan. 3
Jeffers, William Nicolson (<i>r</i>).....	1877, Feb. 24
JENKINS, THORNTON ALEXANDER.....	2115 Penn. Ave. N. W.....	1871, Mar. 13

NAME,	P. O. ADDRESS AND RESIDENCE.	DATE OF ADMISSION.
Johnson, Arnold Burges.....	Light House Board, Treasury Dept. 501 Maple Ave., Le Droit Park.	1878, Jan. 19
Johnson, Joseph Taber.....	926 17th St. N. W.....	1879, Mar. 29
Johnson, Willard Drake.....	Geological Survey. 501 Maple Ave., Le Droit Park.	1884, Feb. 16
Johnston, William Waring.....	1603 K St. N. W.....	1873, Jan. 21
Kampf, Ferdinand (<i>d</i>).....		1875, Dec. 18
Kauffmann, Samuel Hays.....	1000 M St. N. W.....	1884, Feb. 16
Keith, Reuel.....	2219 I St.....	1871, Oct. 29
Kerr, Mark Brickell.....	Geological Survey. 812 21st St. N. W.....	1884, Feb. 16
Kerr, Washington Caruthers (<i>a</i>).....	Raleigh, N. C.....	1883, Apr. 7
Kidder, Jerome Henry.....	Smithsonian Inst. 1816 N St., N. W.....	1880, May 8
Kilbourne, Charles Evans (<i>a</i>).....	War Department.....	1880, June 19
King, Albert Freeman Africanus.....	726 13th St. N. W.....	1875, Jan. 16
King, Clarence (<i>r</i>).....		1879, May 10
Knox, John Jay (<i>a</i>).....	Nat. Bk. Republic, New York City.....	1874, May 8
Kummell, Charles Hugo.....	Coast and Geodetic Survey Office. 608 Q St. N. W.	1882, Mar. 25
LANE, JONATHAN HOMER (<i>d</i>).....		1871, Mar. 13
Lawrence, William.....	First Comptroller's Office, Treasury Department. 1344 Vermont Ave.	1884, Feb. 16
Lawver, Winfield Peter.....	Mint Bureau, Treasury Department. 1912 I St. N. W.	1881, Feb. 19
Lee, William.....	2111 Penn. Ave. N. W.....	1874, Jan. 17
Lefavour, Edward Brown.....	Coast and Geodetic Survey Office. 905 O St. N. W.	1882, Dec. 16
Lincoln, Nathan Smith.....	1514 H St. N. W.....	1871, May 27
Lockwood, Henry H. (<i>r</i>).....		1871, Oct. 29
Loomis, Eben Jenks.....	Nautical Almanac Office. 1413 Col- lege Hill Terrace N. W.	1880, Feb. 14
Lull, Edward Phelps (<i>a</i>).....	74 Cedar St., Roxbury, Mass.....	1875, Dec. 4
Lyford, Stephen Carr (<i>r</i>).....		1873, Jan. 18
MacCauley, Henry Clay (<i>a</i>).....	P. O. Box 953, Minneapolis, Minn.....	1880, Jan. 3
McGee, W. J.....	Geological Survey. 1424 Coreoran St.	1883, Nov. 10
McGuire, Frederick Bauders.....	1306 F St. N. W. 614 E. St. N. W.....	1879, Feb. 15
Mack, Oscar A. (<i>d</i>).....		1872, Jan. 27
McMurtrie, William (<i>a</i>).....	Champaign, Ill.....	1876, Feb. 26
Maher, James Arran.....	Geological Survey. 21 E St. N. W.....	1884, Feb. 16
Mallery, Garrick.....	Bureau of Ethnology, P. O. Box 585. 1323 N St. N. W.	1875, Jan. 30
Marcou, John Belknap.....	Geological Survey.....	1884, Mar. 29
Marvin, Joseph Badger (<i>a</i>).....	Internal Revenue Bureau.....	1878, May 25
Marvin, Archibald Robertson (<i>d</i>).....		1874, Jan. 31
Mason, Otis Tufton.....	National Museum. 1305 Q St. N. W.....	1875, Jan. 30
Matthews, Washington.....	Surgeon General's Office, U. S. A.....	1884, June 7
MEEK, FIELDING BRADFORD (<i>d</i>).....		1871, Mar. 13
Meigs, Montgomery (<i>a</i>).....	U. S. Engineer Office, Keokuk, Iowa.....	1877, Mar. 24
MEIGS, MONTGOMERY CUNNINGHAM.....	1239 Vermont Ave. N. W.....	1871, Mar. 13
Merrill, George Perkins.....	National Museum.....	1884, Apr. 26
Milner, James William (<i>d</i>).....		1874, Jan. 31
Morgan, Ethelbert Carroll.....	918 E St. N. W.....	1883, Oct. 13
Morris, Martin Ferdinand (<i>r</i>).....		1877, Feb. 24
Murdoch, John.....	Smithsonian Institution. 1441 Chapin St., College Hill.	1884, Apr. 26
Mussey, Reuben Delavan.....	P. O. Box 618. 508 5th St. N. W.....	1881, Dec. 3
MYER, ALBERT J. (<i>d</i>).....		1871, Mar. 13
Myers, William (<i>a</i>).....	War Department.....	1871, June 23
NEWCOMB, SIMON.....	Navy Department.....	1871, Mar. 13
Nichols, Charles Henry (<i>a</i>).....	Bloomingdale, N. Y.....	1872, May 4
NICHOLSON, WALTER LAMB.....	1322 I St. N. W.....	1871, Mar. 13
Nordhoff, Charles.....	1731 K St.....	1879, May 10
Norris, Basil.....	1829 G St. N. W.....	1884, Mar. 1
Ogden, Herbert Gouverneur.....	Coast and Geodetic Survey Office. 1324 19th St. N. W.	1784, Feb. 2
Osborne, John Walter.....	212 Delaware Ave. N. E.....	1878, Dec. 7

NAME.	P. O. ADDRESS AND RESIDENCE.	DATE OF ADMISSION.
OTIS, GEORGE ALEXANDER (<i>d</i>).....	1871, Mar. 13
PARKE, JOHN GRUBB.....	Engineer Bureau, War Department. 16 Lafayette Square.	1871, Mar. 13
PARKER, PETER.....	2 Lafayette Square.....	1871, Mar. 13
Parry, Charles Christopher (<i>a</i>).....	Davenport, Iowa.....	1871, May 13
Patterson, Carlile Pollock (<i>d</i>).....	1871, Nov. 17
Paul, Henry Martyn.....	Naval Observatory. 109 1st St. N. E....	1877, May 19
Peale, Albert Charles.....	Geological Survey. 1010 Mass. Ave. N. W.	1874, Apr. 11
PEALE, TITIAN RAMSAY (<i>a</i>).....	Philadelphia, Penn.....	1871, Mar. 13
PEIRCE, BENJAMIN (<i>d</i>).....	1871, Mar. 13
Peirce, Charles Sanders (<i>a</i>).....	Coast and Geodetic Survey Office.....	1873, Mar. 1
Pilling, James Constantine.....	Geological Survey. 918 M St. N. W....	1881, Feb. 19
Poe, Orlando Metcalfe (<i>a</i>).....	34 Congress St. West, Detroit, Mich....	1873, Oct. 4
Poindexter, William Mundy.....	701 15th St. N. W. 806 17th St. N. W....	1884, Dec. 20
Pope, Benjamin Franklin.....	Surgeon General's Office, U. S. A. 1309 20th St. N. W.	1882, Dec. 16
Porter, David Dixon (<i>r</i>).....	1874, Apr. 11
Powell, John Wesley.....	Geological Survey. 910 M St. N. W....	1874, Jan. 17
Prentiss, Daniel Webster.....	1224 9th St. N. W.....	1880, Jan. 3
Pritchett, Henry Smith (<i>a</i>).....	Washington University, St. Louis, Mo.	1879, Mar. 29
Rathbone, Henry Reed (<i>a</i>).....	1874, Jan. 17
Rathbun, Richard.....	Smithsonian Institution 1622 Mass. Ave. N. W.	1882, Oct. 7
Ray, Patrick Henry.....	Army Signal Office.....	1884, Jan. 5
Renshaw, John Henry.....	Geological Survey. 1221 O St. N. W....	1883, Feb. 24
Richey, Stephen Olin.....	732 17th St.....	1882, Oct. 7
Ricksecker, Eugene.....	Geological Survey. 1505 Q St. N. W....	1884, Feb. 16
Ridgway, Robert (<i>a</i>).....	Smithsonian Inst. 1214 Va. Av. S. W....	1874, Jan. 31
Riley, Charles Valentine.....	Agricultural Department. 1700 13th St. N. W.	1878, Nov. 9
Riley, John Campbell (<i>d</i>).....	1877, May 19
Ritter, William Francis McKnight.....	Nautical Almanac Office. 16 Grant Place.	1879, Oct. 21
Robinson, Thomas.....	Howard University. 6th St. N. W., cor. Lincoln.	1884, Jan. 19
Rodgers, Christopher Raymond Perry (<i>a</i>).....	1723 I St. N. W.....	1872, Mar. 9
Rodgers, John (<i>d</i>).....	1872, Nov. 16
Rogers, Joseph Addison (<i>a</i>).....	Naval Observatory.....	1872, Mar. 9
Russell, Israel Cook.....	Geological Survey. 1424 Corcoran St.	1882, Jan. 25
Russell, Thomas.....	Army Signal Office. 1116 M. St. N. W.	1883, Feb. 10
Salmon, Daniel Elmer.....	Agricultural Dept. 1006 N St. N. W....	1883, Nov. 24
Sampson, William Thomas (<i>a</i>).....	Torpedo Station, Newport, R. I.....	1883, Mar. 24
SANDS, BENJAMIN FRANKLIN (<i>d</i>).....	1871, Mar. 13
Saville, James Hamilton.....	342 D St. N. W. 1315 M St. N. W....	1871, Apr. 29
SCHAEFFER, GEORGE CHRISTIAN (<i>d</i>).....	1871, Mar. 13
SCHOTT, CHARLES ANTHONY.....	Coast and Geodetic Survey Office. 212 1st St. S. E.	1871, Mar. 13
Searle, Henry Robinson (<i>d</i>).....	1877, Dec. 21
Seymour, George Dudley (<i>r</i>).....	1881, Dec. 3
Shellabarger, Samuel.....	Room 23 Corcoran Building. 812 17th St. N. W.	1875, Apr. 10
Sherman, John.....	1319 K St. N. W.....	1874, Jan. 17
SHERMAN, WILLIAM TECUMSEN (<i>r</i>).....	1871, Mar. 13
Shufeldt, Robert Wilson (<i>a</i>).....	Surgeon Gen'l's Office, U. S. A., or Box 144 Smithsonian Institution.	1881, Nov. 5
Siard, Montgomery (<i>a</i>).....	Ordnance Bureau, Navy Department.	1877, Feb. 24
Sigsbee, Charles Dwight.....	Naval Academy, Annapolis, Md.....	1879, Mar. 1
Skinner, John Oscar.....	1529 O St. N. W.....	1883, Mar. 24
Smiley, Charles Wesley.....	U. S. Fish Commission, 1443 Mass. Ave. 943 Mass. Ave.	1882, Oct. 7
Smith, David.....	1330 Corcoran St.....	1876, Dec. 2
Smith, Edwin.....	Coast and Geodetic Survey Office. 2024 Hillyer Place.	1880, Oct. 23
Spofford, Ainsworth Rand.....	Library of Congress. 1621 Mass. Ave. N. W.	1872, Jan. 27

LIST OF MEMBERS.

XXI

NAME.	P. O. ADDRESS AND RESIDENCE.	DATE OF ADMISSION.
Stearns, John (<i>a</i>).....	Boston, Mass.....	1874, Mar. 28
Stearns, Robert Edwards Carter.....	Smithsonian Institution. 1226 Mass. Ave. N. W.	1884, Nov. 22
Stone, Ormond (<i>a</i>).....	Leander McCormick Observatory, University of Virginia.	1874, Mar. 28
Taylor, Frederick William (<i>a</i>).....	Smithsonian Institution. Lake Valley, New Mex.	1881, Feb. 19
TAYLOR, WILLIAM BOWEN.....	Smithsonian Inst. 306 C St. N. W.....	1871, Mar. 13
Thompson, Almon Harris.....	Geological Survey.....	1875, Apr. 10
Thompson, Gilbert.....	Geological Survey. 1448 Q St. N. W.....	1884, Feb. 16
Tilden, William Calvin (<i>a</i>).....	New York City.....	1871, Apr. 29
Todd, David Peck (<i>a</i>).....	Lawrence Observ., Amherst, Mass.....	1878, Nov. 23
Toner, Joseph Meredith.....	615 Louisiana Ave.....	1873, June 7
True, Frederick William.....	National Museum.....	1882, Oct. 7
Twining, William J. (<i>d</i>).....	1878, Nov. 23
Upton, Jacob Kendrick (<i>r</i>).....	1878, Feb. 2
Upton, William Wirt.....	2d Comptroller's Office, Treasury Dept. 1746 M St. N. W.	1882, Mar. 25
Upton, Winslow (<i>a</i>).....	Brown University, Providence, R. I.....	1880, Dec. 4
Vasey, George (<i>r</i>).....	1875, June 5
Walcott, Charles Doolittle.....	Geological Survey, Nat. Museum.....	1883, Oct. 13
Waldo, Frank (<i>a</i>).....	Army Signal Office. Ft. Myer, Va.....	1881, Dec. 3
Walker, Francis Amasa (<i>a</i>).....	Mass. Inst. of Technology, Boston, Mass.	1872, Jan. 27
Walling, Henry Francis (<i>a</i>).....	Geological Survey, Cambridge, Mass.	1883, Feb. 24
Ward, Lester Frank.....	Geological Survey. 1464 R. I. Ave. N. W.	1876, Nov. 18
Webster, Albert Lowry (<i>a</i>).....	West New Brighton, Staten Island, N. Y.	1882, Mar. 25
Welling, James Clarke.....	1302 Connecticut Ave.....	1872, Nov. 16
Wheeler, George M. (<i>a</i>).....	Engineer Bureau, War Department.....	1873, June 7
WHEELER, JUNIUS B. (<i>a</i>).....	Lenoir, N. C.....	1871, Mar. 13
White, Charles Abiathar.....	Geological Survey. Le Droit Park.....	1876, Dec. 16
White, Charles Henry.....	1744 G St. N. W.....	1884, Mar. 1
White, Zebulon Lewis (<i>a</i>).....	Providence, Rhode Island.....	1880, June 19
Williams, Albert, Jr.....	Geological Survey. 23 Lafayette Square.	1883, Feb. 24
Wilson, Allen D. (<i>a</i>).....	1874, Apr. 11
Wilson, James Ormond.....	Franklin School Building. 1439 Mass. Ave. N. W.	1873, Mar. 1
Winlock, William Crawford.....	Naval Observatory. 723 20th St. N. W.	1880, Dec. 4
Wolecott, Christopher Columbus (<i>r</i>).....	1875, Feb. 27
Wood, Joseph (<i>a</i>).....	Supt. Motive Power, Penn. Co., Fort Wayne, Ind.	1875, Jan. 16
Wood, William Maxwell (<i>a</i>).....	Navy Department.....	1871, Dec. 2
Woodruff, Thomas Maher.....	Army Signal Office. 2020 Hillyer Place.	1884, Apr. 12
WOODWARD, JOSEPH JANVIER (<i>d</i>).....	1871, Mar. 13
Woodward, Robert Simpson.....	Geological Survey, 1125 17th St. N. W.	1883, Nov. 24
Woodworth, John Maynard (<i>d</i>).....	1874, Jan. 31
Yarnall, Mordecai (<i>d</i>).....	1871, Apr. 29
Yarrow, Harry Cr6ey.....	814 17th St. N. W.....	1874, Jan. 31
Yeates, William Smith.....	Smithsonian Institution. 401 G St. N. W.	1884, Apr. 29
Zumbrock, Auton.....	Coast and Geodetic Survey Office. 455 C St. N. W.	1875, Jan. 30

Number of <i>founders</i>	44
“ “ <i>members deceased</i>	41
“ “ <i>absent</i>	62
“ “ <i>resigned</i>	16
“ “ <i>active</i>	173
Total number enrolled.....	292

CALENDAR FOR THE USE OF THE PHILOSOPHICAL SOCIETY,

Showing the alternate SATURDAYS for holding Meetings during the several "Seasons" from 1884-'85 to 1907-'08, inclusive.

PREPARED BY MR. E. B. ELLIOTT.

Submitted to the General Committee June 7, 1884, and ordered published.

Years.	October.	November.	December.	Years.	January.	February.	March.	April.	May.	June.
1884.....	11, 25	8, 22	6, 20	1885.....	3, 17, 31	14, 28	14, 23	11, 25	9, 23	6, 20
1885.....	10, 24	7, 21	5, 19	1886.....	2, 16, 30	13, 27	13, 27	10, 24	8, 22	5, 19
1886.....	9, 23	6, 20	4, 18	1887.....	15, 29	12, 26	12, 26	9, 23	7, 21	4, 18
1887.....	15, 29	12, 26	10, 24	1888.....	7, 21	4, 18	3, 17, 31	14, 28	12, 26	9, 23
1888.....	13, 27	10, 24	8, 22	1889.....	5, 19	2, 16	2, 16, 30	13, 27	11, 25	8, 22
1889.....	12, 26	9, 23	7, 21	1890.....	4, 18	1, 15	1, 15, 29	12, 26	10, 24	7, 21
1890.....	11, 25	8, 22	6, 20	1891.....	3, 17, 31	14, 28	14, 28	11, 25	9, 23	6, 20
1891.....	10, 24	7, 21	5, 19	1892.....	2, 16, 30	13, 27	12, 26	9, 23	7, 21	4, 18
1892.....	15, 29	12, 26	10, 24	1893.....	7, 21	4, 18	4, 18	1, 15, 29	13, 27	10, 24
1893.....	14, 28	11, 25	9, 23	1894.....	6, 20	3, 17	3, 17, 31	14, 28	12, 26	9, 23
1894.....	13, 27	10, 24	8, 22	1895.....	5, 19	2, 16	2, 16, 30	13, 27	11, 25	8, 22
1895.....	12, 26	9, 23	7, 21	1896.....	4, 18	1, 15, 29	1, 14, 28	11, 25	9, 23	6, 20
1896.....	10, 24	7, 21	5, 19	1897.....	3, 17, 31	14, 28	13, 27	10, 24	8, 22	5, 19
1897.....	15, 29	12, 26	10, 24	1898.....	2, 16, 30	12, 26	12, 26	9, 23	7, 21	4, 18
1898.....	14, 28	11, 25	9, 23	1899.....	15, 29	4, 18	4, 18	1, 15, 29	13, 27	10, 24
1899.....	13, 27	10, 24	8, 22	1900.....	7, 21	4, 18	3, 17, 31	14, 28	12, 26	9, 23
1900.....	12, 26	9, 23	7, 21	1901.....	6, 20	3, 17	2, 16, 30	13, 27	11, 25	8, 22
1901.....	11, 25	8, 22	6, 20	1902.....	5, 19	2, 16	2, 16, 30	13, 27	11, 25	8, 22
1902.....	10, 24	7, 21	5, 19	1903.....	4, 18	1, 15	1, 15, 29	12, 26	10, 24	7, 21
1903.....	15, 29	12, 26	10, 24	1904.....	3, 17, 31	14, 28	14, 28	11, 25	9, 23	6, 20
1904.....	14, 28	11, 25	9, 23	1905.....	2, 16, 30	13, 27	12, 26	9, 23	7, 21	4, 18
1905.....	13, 27	10, 24	8, 22	1906.....	7, 21	4, 18	4, 18	1, 15, 29	13, 27	10, 24
1906.....	12, 26	9, 23	7, 21	1907.....	6, 20	3, 17	3, 17, 31	14, 28	12, 26	9, 23
1907.....	11, 25	8, 22	6, 20	1908.....	5, 19	2, 16	2, 16, 30	13, 27	11, 25	8, 22
1908.....	10, 24	7, 21	5, 19	1909.....	4, 18	1, 15, 29	1, 14, 28	11, 25	9, 23	6, 20

ANNUAL REPORT OF THE SECRETARIES.

WASHINGTON CITY, *December 20, 1884.**To the Philosophical Society of Washington :*

We have the honor to present the following statistical data for 1884.

At the beginning of the year the number of active members was 151

This number has been increased by the addition of 35 new members and by the return of 5 absent members. It has been diminished by the departure of 13 members and by the death of 5. There have been no resignations. The net increase of active members has thus been 22

And the active membership is now 173

The roll of new members is :

W. S. BARNARD.
T. H. BEAN.
H. W. BLAIR.
C. O. BOUTELLE.
F. T. BOWLES.
S. J. BROWN.
G. E. CURTIS.
F. P. DEWEY.
J. S. DILLER.
R. E. EARLL.
WILLIAM EIMBECK.
ASAPH HALL, Jr.
J. M. GREGORY.
D. P. HEAP.
ROMYN HITCHCOCK.
W. D. JOHNSON.
S. H. KAUFFMANN.
M. B. KERR.

WILLIAM LAWRENCE.
J. A. MAHER.
J. B. MARCOU.
WASHINGTON MATTHEWS.
G. P. MERRILL.
JOHN MURDOCH.
BASIL NORRIS.
H. G. OGDEN.
P. H. RAY.
W. M. POINDEXTER.
EUGENE RICKSECKER.
THOMAS ROBINSON.
R. E. C. STEARNS.
GILBERT THOMPSON.
C. H. WHITE.
T. M. WOODRUFF.
W. S. YEATES.

The names of deceased members are :

BENJAMIN ALVORD. O. E. BABCOCK. H. W. BLAIR.
CHARLES EWING. J. J. WOODWARD.

There have been 15 general meetings for the presentation and discussion of papers (not including the public meeting of Dec. 6); the average attendance has been 42. There have been six meetings of the Mathematical Section; average attendance 15.

In the general meeting 32 communications have been presented; in the mathematical section 11. Altogether 43 communications have been made by 32 members and one guest. The number of members who have participated in the discussions is 38. The total number who have contributed to the scientific proceedings is 50, or 29 per cent. of the present active membership.

Very Respectfully,

G. K. GILBERT,
H. FARQUHAR,

Secretaries.

ANNUAL REPORT OF THE TREASURER.

WASHINGTON CITY, December 31, 1884.

To the Philosophical Society of Washington :

I have the honor to present herewith my annual statement as Treasurer for the year ending December 20th, 1884.

The revenue of the Society has amounted to \$855.00 and the expenditures have been \$671.96, leaving a balance of \$183.04 on hand; the details of this account are given in the accompanying table.

The investments of the funds of the Society have not changed and consist, therefore, of \$1,000 in a U. S. Bond at $4\frac{1}{2}$ per cent. and \$1,500 in U. S. Bonds at 4 per cent.

The receipts during the past year may be classified as follows :

Interest on invested fund	\$95
5 Dues for 1882,	\$25
16 " " 1883,	80
126 " " 1884,	630
2 " " 1885,	10
	<hr/>	
149		745

The dues remaining unpaid are about as follows :

For 1882, 3	\$15
" 1883, 10	50
" 1884, 47	235
	<hr/>	
60		300

Early in February 500 copies of Volume VI of the Bulletin were received from the printer, and 148 copies have been distributed to active members, also 67 copies have been sent to domestic and 73 to foreign recipients; occasional copies of other volumes have also been sent to complete broken sets. The stock of publications now on hand is about as follows :

Bulletin, Volume I.	91 copies.
" " II.	82 "
" " III.	199 "
" " IV.	184 "
" " V.	201 "
" " VI.	215 "
W. B. Taylor, Memoir of Joseph Henry, 1st Ed.	64 copies.
" " " " 2d Ed.	30 "
J. C. Welling, Address on life of Joseph Henry	4 "
W. B. Taylor, Address as President	70 "

In return for the distribution of Bulletins the Society has received about seventy-five publications from other organizations or individuals and the Accessions Catalogue of the Library now includes 177 titles.

Very respectfully your obedient servant,

CLEVELAND ABBE, *Treasurer.*

TREASURER'S REPORT.

XXV

Dr. *The Philosophical Society of Washington in account with Cleveand Abbe, Treasurer, for the year ending Dec. 20, 1884.* Cr.

EXPENDITURES.				RECEIPTS.			
Date.	Vou'r.	Check.	To whom paid.	Amount.	From what source.	Amount.	Total.
1884.							
Feb. 1	1	80	H. Farquhar, expenses as Sec'y	\$27 00	Credit by receipts as follows:		
Feb. 1	2	81	G. K. Gilbert, " "	8 88	Balance carried over from Dec. 31, '83.		
Feb. 1	3	82	Judd & Detweiler, printers	39 55	(See over-draft, \$73.51, below.)	\$245 00	
Feb. 6	4	83	Cleveland Abbe, exp. as Treas.	20 75	Annual dues received:	155 00	
Feb. 18	5	85	A. H. Gawler, janitor	10 00	and deposited February 2, 1884	100 00	
Feb. 14	6	84	Judd & Detweiler, prs.	\$200 00	" " 9, " "	20 00	
April 2	6	86	" " " "	150 00	" " April 3, " "	5 00	
July 15	6	89	" " " "	28 00	" " June 11, " "	95 00	
Aug. 1	6	90	" " " "	41 07	" " July 15, " "	90 00	
May 15	7	87	G. K. Gilbert, exp. as Sec'y	5 37	" " August 1, " "		
June 12	8	88	H. Farquhar, " "	17 15	" " Dec'mb'r 16, " "		
Aug. 1	9	91	J. C. Welling, President	50	Cash in hand December 20, 1884	710 00	
Aug. 1	10	92	Judd & Detweiler, printers	31 60	Repayment for special printing,	35 00	
Aug. 1	11	93	A. H. Gawler, janitor	7 00	deposited February 2	15 00	
Dec. 6	12	94	G. K. Gilbert, exp. as Sec'y	10 68	Interest of \$1,000 at 4½%		
					" " 1,500 at 4-- 50 00	95 00	
			Total	598 45			\$855 00
			Balance on hand	183 04	Less over-draft of Dec., 1883		78 51
				781 49	Total		781 49



BULLETIN

OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON.

ANNUAL ADDRESS OF THE PRESIDENT.



ANNUAL ADDRESS OF THE PRESIDENT,

JAMES C. WELLING.

Delivered December 6, 1884.

THE ATOMIC PHILOSOPHY, PHYSICAL AND METAPHYSICAL.

Every nation under the sun has a philosophy of some kind, but the philosophy we profess draws the lines of its historic traditions, if not its "increasing purpose," from the home of our Aryan ancestors in Greece. It was here that the typical forms of our literature were invented, that the art of sculpture was carried to its climax, and that the architecture of the lintel came to a transfiguration in the Theseum and the Parthenon. And as if all these glories were not enough, it is the further good fortune of the Greeks to have at least opened up the great leading problems of human enquiry, in physics, in psychology, and in ethics; and to have so opened them up at the starting point of the world's Torch-race, that the light shed on these questions more than twenty-five centuries ago is still a matter of curious retrospection to this generation of ours on whom the ends of the world are come.

It is to one of the oldest of the formal physical philosophies ever framed by the mind of man for the explanation of the mechanical structure of the Universe that I purpose to call your attention to-night—a theory the most comprehensive in its scope, and, at the same time, the most searching in its subtlety, which has been handed down to us by all antiquity—a theory which in its ingenuity represents the synthetic power of the Greek mind at the highest stage of its physical speculation—a theory which the literature of Rome has preserved in the amber of Cicero's philosophical disquisition, and embalmed in the immortal verse of Lucretius—a theory, in fine, which has survived the old dialectic in which it was first conceived, because it has come to a new birth in the forms of modern science. I refer to what is known in history as the Atomic Philosophy of the Greeks.

The fundamental principle of the ancient physical philosophy—its point of departure and its ever re-entering point of return—is found in the famous well-worn maxim of metaphysics, that out of nothing nothing comes, and that what *is* can never be annihilated. It was in the name of this maxim and under the shadow of its authority that the Greek physical philosophers sought to shelter their whole right of free enquiry from the charge of impiety, and if to us the dictum seems the merest truism, it was not so regarded at the dawn of natural philosophy. Sometimes used as a logical club with which to brain a stolid and incurious indifferentism, and sometimes waved as a red flag in the face of polytheistic superstition, it meets us perpetually in all the oldest records of ancient philosophical speculation—in the formal elaborations of Aristotle,* in the lucubrations of Boëthius,† and in the verse of poets as remote from each other in style and creed as Lucretius, the lively Epicurean,‡ and Persius, the sternest of Stoic moralists.§ This maxim stirred the philosophical mind of antiquity to its lowest depth, because it was then the type and symbol of a whole method of philosophizing—a method regarded by many as not a little presumptuous, much as the Copernican theory of the Universe was regarded in the sixteenth century, or much as the Formula of Evolution is regarded to-day outside of scientific circles.

It was because the maxim seemed to so many the challenge of a vain wisdom and of a false philosophy that the early champions of physical philosophy sometimes felt themselves called to vindicate the truth of this truism by an appeal to formal argument. The necessity for such an appeal measures the scientific ineptitude of the average mind at that early age. “If what emerges into sensible perception,” argues Epicurus with the utmost gravity, “can be conceived as coming from nothing, then everything might come of anything, and that, too, without any need of germs; and if what disappears from sensible perception was really destroyed into nothing, then all things might perish without anything being left into which

* Aristotle: *De Generatione et Corruptione*, I, iii, 5, (Didot's ed., vol. 2, p. 437.)

† Boëthius: *De Consolatione Philosophiæ*, Lib. V, Prosa 1.

‡ Lucretius: *De Rerum Natura*, I, 151-227.

§ Persius: *Satira*, iii, 84.

they were resolved."* Such was the rude flint-flake with which, as their only weapon of logic, the early Nimrods of philosophy in Greece defended their right to philosophize in the palæolithic stage of natural enquiry.

As the next step in this metaphysical logic we find a distinction drawn by the ancient Greek philosophers between things as they are in substrate and things as they appear, disappear, and reappear in time—between the noumenal and the phenomenal world, as we would say to-day in the Kantian phraseology. It was the favorite doctrine of the Eleatic school of philosophers that we get a true conception of things only when, abstracting from their individuality, their partitiveness and their changing forms, we find the ultimate root and unity of all being in a simple, indivisible, and unchangeable substrate, which is the true object of knowledge, because it is the true basis of all reality. This concept increased in clearness as it passed through the minds of Xenophanes, Parmenides, and Empedocles, until, in the generalizations of the last-named philosopher, the ultimate substrate of things was resolved into four elementary substances—earth, air, fire, and water; each uncreated and imperishable, each equal in quantity, each composed, within itself, of parts that are qualitatively the same, and each forever incommutable with the others; yet each and all capable of every variety and degree of mixture in the manifold combinations of things as they appear in the sensible world.

On the other hand, it was held by Heraclitus that this fundamental substrate or unity of things is a mere figment of the philosophical imagination, and that it is only as things are conceived to be in perpetual flux that the forms of our knowledge can be brought into correspondence with the forms of actual being. That is, to the doctrine of the unchanging substrate of things Heraclitus opposed the doctrine of the perpetual flux of things.

It remained to effect a synthesis and reconciliation between these opposing views of the Eleatic and Heraclitic philosophies of nature, while at the same time saving the fundamental dogma of all natural philosophizing, that out of nothing nothing comes. Such a basis of pacification was found in the terms of the Atomic Philosophy, in the doctrine that the changing forms, positions, motions, and phases of

* Diog. Laërt.: Lives of the Philosophers, *sub voce* "Epicurus."

things are to be conceived as a perpetual flux, resulting from the changing permutations and combinations of the indestructible atoms composing the eternal substrate of nature. And thus it was that the doctrine of ultimate atoms, incessantly modified in the forms of their combination, but remaining forever the same in substance, became the legitimate deduction and the crowning corollary of the primal eldest maxim of physical philosophy. Aristotle expressly gives this genesis of the Atomic Philosophy of Greece in its reduction by Anaxagoras. After saying that Anaxagoras hypothesized an infinity of atoms, to explain the myriad varieties of nature, because he wished to avoid the reproach of getting something out of nothing, Aristotle adds: "From the fact that contraries are made out of each other, they must needs have previously existed in each other; for if everything that *becomes* must needs come either from something or from nothing, and if this latter alternative is impossible, (about which all who treat of nature are agreed in opinion,) then it only remains to infer that everything which becomes must have come from the things in which it pre-existed, though, on account of the smallness of their bulks, made out of things imperceptible to us."*

The Atomic Philosophy of the Greeks was, therefore, not a mere exhalation of the imagination, but a logical inference from the starting point and major premise of their natural metaphysics. The doctrine of ultimate atoms in nature was, indeed, the necessary complement and reconciliation of the conception that all things are in elemental stir, and that yet in this elemental stir there is no creation of anything out of nothing and no annihilation of anything, but only composition, decomposition, and recomposition.

It need not surprise us, therefore, to find that the doctrine of ultimate atoms in nature is a universal form of thought among thinking men of all the most advanced races in antiquity. Into the hidden historic springs of the Atomic Philosophy, as formulated by the Greeks, it is not here proposed to enquire. Whether its

* Aristotle: *Naturalis Auscultatio*, I, iv, 2, (Didot's ed., vol. 2, p. 252.)

Compare, also, Lucretius, *De Rer. Nat.*, I, 543-545:

— "Quoniam supra docui nil posse creari
De nilo, neque quod genitum est ad nil revocari,
Esse immortali primordia corpore *debent*."

germs were derived from Egypt, or from India, or from Phœnicia, or whether it was an original birth of the Hellenic mind, is a matter of curious historic interest which hardly admits, perhaps, of precise and positive determination, though certain it is that India had an Atomic Philosophy before the Greeks. However possible or probable it may be that the early Greek philosophers borrowed some of their lore under this head, as we know they did under others, from the Egyptian priests; or whatever truth there may be in the tradition, reported by Posidonius,* (Cicero's teacher in philosophy,) that one Moschus, a Phœnician, imparted the doctrine to Pythagoras, it is very certain that the Greek philosophers have made the doctrine their own by the logical development they gave to it, and by the hereditament in it which they have bequeathed to the subsequent generations of men moving along the lines of human progress. It has been more than suspected that the doctrine dates in Greece from the age of Pythagoras, by reason of certain specific ideas, which we can read in the spectrum analysis of the most distant times by the light of modern anthropological science. Certain definite lines of thought are to be found in the psychology of every epoch, and these lines betray the mental constitution of the epoch as surely as the vapors of the elements absorb rays of the same refrangibilities that they radiate. In the days of Pythagoras we discover certain psychical ideas which are seen to have been the natural reflex of the great fundamental dogma out of which the Atomic Philosophy sprang. I refer to the doctrine of metempsychosis and of its correlate, the pre-existence of souls. If it be assumed that the human soul is something generically different from the body, and is not generated by it, then it necessarily follows, according to the maxim *De nihilo nihil fit*, that the soul pre-existed somewhere before the atoms of the body were put together, and from the other branch of the maxim, that it must continue to exist somewhere after the body is dissolved. The doctrine of the transmigration of souls is not, therefore, a mere vagary of the ethnical imagination, but the natural offspring of that form of Pythagorean dualism which distinguished the soul, as not only generically, but genetically distinct from the body. Hence, the

*Strabo: *Geog.*, Lib. XVI. Cf. Sextus Empiricus: *Adversus Mathematicos*, Lib. 9,

doctrine reappears under one form or another in every dualistic conception of matter and mind—now in the purple light of Plato's imperial fancy, and now in the pallid shades of that metaphysical theology which, in the days of Origen and St. Augustine, arrayed the doctors of the Church into opposing schools on the great question of *Traducianism* or *Creationism*.

In whatever way the Atomic Philosophy was begotten in the Greek mind, we know that on its emergence it was subjected to the solvents of philosophical criticism, and underwent a variety of transformations. So soon as we come within the lines of definite history we find a bifurcation of ideas between such typical teachers as Anaxagoras on the one hand, and Leucippus and Democritus on the other. This dissidence of opinions had regard to the nature and the constitution of the ultimate atoms which compose the substance of matter. The doctrine of Anaxagoras was qualitative; the doctrine of Democritus was quantitative. Anaxagoras held that the atoms which compose the physical Universe in its fleeting forms, and at the same time in its enduring substance, are eternally differentiated in kinds, and that it was by the collocation and adhesion of like parts—of bony atoms to make bone, of fleshy atoms to make flesh, of stony atoms to make stones—that the actual varieties of body in the Universe were built up. This is the famous doctrine of *Homœomeria* which fares so ill in the spiritual philosophy of Plato, and which fares no better in the materialistic philosophy of Lucretius. Aristotle tells us that Anaxagoras was driven to adopt this hypothesis in order to relieve the doctrine of atoms at the points where the heaviest stress and tightest pinch seemed to be laid upon it by the dogma *De nihilo nihil fit*; for how else, said Anaxagoras, could we account for the existing varieties of matter unless there be an original and eternal variety in its constituent elements?

Democritus simplified the theory of atoms by giving to it a purely mechanical reduction. Conceiving atoms to be invisible by reason of their smallness, he at the same time conceived them to be indivisible, not as mathematically considered, but as physically considered; and while holding them to be infinite in number and infinite in their shapes, he at the same time held that they differed not at all in inherent quality, but simply in their shapes, sizes, situations, and motions, and that hence it was by the different combination of

atoms differing in these mechanical aspects that all the varieties of bodies and souls were integrated, disintegrated, and reintegrated.* The different impressions produced on the human senses by different bodies, according to their various mechanical constitutions, were regarded by him as purely subjective—the mechanical results of different concussions made on the senses by the different effluxes of things,† and, therefore, no more requiring any qualitative differences to explain the phenomena of sensation than to explain the phenomena of being. Weight and hardness were treated by Democritus as primary qualities of bodies resulting from the greater or less degrees in which their constituent atoms are compacted, as compared with the interstitial voids or vacua. The secondary qualities of bodies are simply the impressions they make on the human senses, depending, as has just been said, on the varying shapes, sizes, and arrangements of the atoms composing all the varieties of material substance.

Anaxagoras had made his theory of atoms a pendant to dualism, conceiving, as he did, that souls, both animal and rational, are eternally pre-existent before the birth, and post-existent after the dissolution, of the bodies in which they temporarily resided.‡ Democritus made the animal soul and the rational soul only two more distinct varieties in the mechanical collocation of atoms varying in shape, size, situation, and motion; and, therefore, he had no place in his theory for the transmigration of souls considered as entities distinct from bodies. Souls and bodies were equally the results of a concourse of atoms obeying in their movements the law of a mechanical necessity. That is, to the dualism which preceded him Democritus opposed a pure and simple monism. Yet between the materialism of Democritus and the dualism of Anaxagoras there is not much to choose; for the misty spiritualism of the latter did not

* Aristotle: *De Generat. et Corrup.*, I, i, 4, (Didot's ed., vol. 2, p. 432;) also Arist.: *Metaphysics*, VII, ii, 2, (Didot's ed., vol. 2, p. 559,) and the *Nat. Auscul.*, I, v, 1, (Didot's ed., vol. 2, p. 254.)

† Action from a distance, as of the magnet on iron, was also explained by Democritus on the hypothesis of "effluxes." Zeller: *Philosophie der Griechen*, Erster Theil, p. 704.

‡ Cudworth: *Intellectual System of the Universe*, vol. I, chap. 1, (Andover ed.) p. 95.

carry with it any clear conception of personal identity, and hence Lucretius justly argued that the doctrine of a future life, as held by many in his day, was stripped of all significance if the chain of personal consciousness is broken at death.*

And to this fundamental antithesis of ideas lying at the bottom of these two forms of the Greek Atomic Philosophy another antithesis must be added in the Stratonical Hylozoism, which, assuming in matter an atomic structure partly material and partly vital, proceeded to account for the genesis of animated bodies on the super-added assumption of a plastic energy working in nature to the production of every living thing. In a word, Strato's matter, instinct with life, and waiting only for the first chance to be stuck together in the composition of plants and animals, seems to have been the metaphysical anticipation of our modern protoplasm.†

It was in opposition alike to the physics of Anaxagoras, Democritus, and Strato, that Plato reared his splendid fabric of idealism, while Aristotle, for his part, rejected the philosophy of atoms altogether, and installed in its place for centuries the doctrine of Form and Quality, and Substance and Entelechy, whatever that may mean. "If," he says, "there be no other substance beyond the substances existing in nature, then Physics is the first science; but if there be a certain substance which is immovable, then this is before body, and Philosophy is the first science."‡ That single sentence recapitulates the whole verbal philosophy of the Middle Ages. Plato was so hostile to the hypothesis of Democritus that he never once names that philosopher in all his writings, though it is the Abderite physicist to whom he intends a disparaging allusion when in the *Timæus* he impales on the shafts of his irony "a certain philosopher of an indefinite and ignorant mind." Aristotle names him often enough, either separately or in conjunction with Leucippus, and treats the Atomic Philosophy with respect as an "invention framed to explain the transformation and birth of things—explaining birth and dissolution by the decomposition and recomposition of atoms,

* Lucret.: *De Rerum Natura*, Lib. iii, 851.

† Cicero aptly defines the antithesis of ideas between Democritus and Strato. See *Academ. Prior.*, Lib. II, xxxviii, 121. Also, *De Nat. Deor.*, Lib. I, xiii, 35.

‡ Arist.: *Met.*, Lib. V, i, 9; cf. Lib. X, vii, 9.

and explaining transformations by the arrangement and position of atoms."*

But it is in the physical philosophy of Epicurus, as that philosophy has been expounded and expanded by Lucretius, that we can discover the fullest and clearest exposition of the doctrine of atoms, considered as a key to the structure of the Universe. We here have the doctrine formulated into a theodicy of naturism, a theory of psychology, a cosmogony, and an anthropology. According to Epicurus, in his Lucretian rendering, atoms are minute material particles, indivisible, not by reason of their smallness, but of their solidity which makes them indestructible and unchangeable in their constitution; they have size, weight, and shape, yet are forever invisible to the eye; in shape, some of the atoms are different from the others, but, while the number of the different shapes is finite, the number of atoms of each shape is infinite; every atom must have at least three *cacumina* (*γωνίας*), that is, infinitesimally small bounding points which are incapable of existing apart from the atom, but must be conceived to coexist with it in order to give definition to it and to enclose its "solid singleness;" some of the atoms are hook-shaped, some only slightly jagged, some smooth, &c.; atoms are in incessant motion, racing through space in all directions under the stress of their weight,† according to the favoring conditions of a vacuum more or less complete, yet so that the sum of their motions results in the supreme repose of gross matter, except when a thing exhibits the motion of translation in space—a form of motion which is molar and not atomic; atoms move besides at an enormous uniform speed, in parallel lines, up and down, so far as there can be any up and down in a universe equally boundless in all directions, and except so far as some of the atoms have originally a shape which makes them capable of slight deflections from parallel straight lines—that *clinamen principiorum* which was invented by Epicurus to explain the phenomena of so-

* Arist.: *De Generat. et Corrup.*, I, ii, 4 (Didot's ed., vol. 2, p. 434.)

† Epicurus derived the motion of atoms from their weight, which gives movement *in vacuo*. Democritus derived the motion of atoms from an impulse given to them in the beginning. So says Cicero (*De Fato*, 20, 46), but for the contrary opinion, cf. Zeller: *Philos. der Griechen*, Erster Theil, 702, 714.

called voluntary motion in animals and free-will in men, while at the same time explaining how it is that this free-will is eternally encased in the rigid parallel lines of the other atoms. In this way Epicurus supposed himself to have added a useful supplementary hypothesis to the original hypothesis of Democritus, who binding nature fast in fate had not left free the human will, because he had omitted to provide for that third mode of motion in atoms which is required to explain the possibility and genesis of voluntary motion and self determination.

Such is a brief and imperfect exposition of the Atomic Philosophy of the Greeks—a form of physical speculation the most elaborate, the most ingenious, and, to use a Latinism of Dr. Johnson, the most concinnous which has come down to us from all antiquity. The Epicurean physics are as much superior to the Aristotelian and the Stoical physics as the ethics of the Lyceum and of the Porch are superior to the ethics of the Sty; and yet it now remains to be said that in all this operose system of metaphysico-physical atoms there is not an atom of scientific truth, in the modern sense of that word. The whole speculation is a mirage, caused by unequal refractions in the Greek intellect—by the volatility of the Greek fancy passing through a dense, practical ignorance with regard to everything but surface views in nature. Or, to borrow one of Plato's favorite figures, it was a "wind-egg," begotten of metaphysic conceit, and differing from the other "wind-eggs" of that time in the greater symmetry of its shell rather than in the greater fecundation of its contents. It had the form, but not the power of scientific truth. If there be such a thing as atoms they must needs be chemical conceptions, and the very word "chemistry" had not yet come into the Greek language, because the rationale of such a science had not even dawned on the horizon of the Greek intellect by the faintest reflection from below.

Much explanation, which does not explain, has been wasted to account for the incapacity of the Greek mind in physical philosophy. The learned historian of the Inductive Sciences, Dr. William Whewell, ascribes this incapacity to the alleged fact that though this sprightly race had in their possession an abundance of facts, and were acute observers and critics, their ideas "were not distinct and appropriate to the facts."* It would

* William Whewell: History of the Inductive Sciences, vol. I, p. 87.

hardly be possible to frame an explanation more pointless. If there has ever been a hypothesis framed with more "distinct ideas" than that of the Greek atomists, I am not acquainted with it, and it is precisely because it was so "appropriate" to the surface facts of the Greek observation that it was so illusory. It was fitted to these facts with a *concininitas* that is most admirable from a psychological point of view. It was *invented* to fit them, and its whole *raison d'être* was that it *did* fit them, so far as ideas and words could make it fit. For this purpose it was revised, modified, contracted, enlarged, supplemented, until it seemed to fit every sinuosity of the facts of nature, as far as the facts of nature were open to the apprehension of the Greeks in the 5th century before Christ. The hypothesis was strong just where it seems weak to Dr. Whewell, and it is precisely because it was so ideally strong that it was so physically weak, and it is precisely because it fitted the facts so well that it was a delusion and a snare. Men rested in it with a sense of satisfaction which simulated the rest of a mind turning on the poles of truth. It satisfied the highest cravings of Greek physical enquiry in the then contemporaneous stage of mental evolution in Greece. The Greek mind of that age had not reached a stage of development which required anything more than metaphysical hypotheses for the explanation of physical facts, because it had not reached a stage of evolution which capacitated it to frame hypotheses in physics capable of anything more than metaphysical verification. And hence it was in the ingenuity of a plausible hypothesis, and in the nicety with which it fitted the superficial facts that the subtle and artistic mind of the Greeks found the sole interest and zest which a physical hypothesis had for them or could have. "Ancient logic," says Prof. Jowett, "was always mistaking the truth of the form for the truth of the matter."* The conscious incapacity of the Greeks for physical science was so great that we find the best class of minds among them absolutely revolting at the very idea of such a science. Socrates, for instance, had no patience with it. Plato represents him in the *Phædo* as at the same time deploring misology—the hatred of formal ideas—and yet, in almost the same breath, confessing himself a misologist in the presence of mechanical conceptions of nature. He liked the doctrines of Anaxagoras well enough, so

* Jowett's Plato, vol. I, p. 376.

far as they moved in mind, but he detested them, to use the words put in his mouth by Plato, so far as they moved in "air, and ether, and water, and such like inconsequences;"* and, detesting them, he falls back upon a purely anthropomorphic conception of the Universe—anthropomorphic because it is avowedly anthropocentric, with Socrates for its centre. The whole passage is a most instructive page in comparative psychology, now that we can read it in the light of modern anthropological science.

It is no part of my present purpose to carry the history of the Atomic Philosophy into Roman speculation. The Romans took all their ideas in mental, moral, and physical philosophy at second-hand from the Greeks.† Strong in the practical arts of war and polity, they were content to be in literature imitators and in philosophy eclectics. Equally inept for the deft metaphysical analysis of the Greeks and for their fine artistic synthesis, the Romans none the less contributed, on the practical side of life, to the definite exposition of the contents of all the philosophical systems of the Greeks. Hence we could ill spare the ponderous banter of Cicero when he mocks at the weak points of the Atomic Philosophy,‡ and still less could we spare that reasoned elaboration of its strong points which has made the *De Rerum Natura* of Lucretius the most systematic, the most complete, the most earnest, and the most realistic of all the reductions which the Atomic Philosophy has ever received. But after allowing for all his skill in the episodic handling of the rival systems of Heraclitus, Empedocles, and Anaxagoras, for his power of description, for the vivacity of his narrative, for the force and often the beauty of his illustrations and analogies, it must still be conceded that there is much more of original poetry than of original philosophy in these glowing hexameters of the Epicurean philosopher-poet.

In a history of the Atomic Philosophy we can leap the chasm of the Middle Ages at a single bound. The physical philosophers of

* *Phædo*, § 47; Jowett's Plato, vol. I, p. 427.

† For evidence as to the imbecility of the Roman mind in physical philosophy, see the 2nd Book of Cicero's "*Prior Academics*," which is a long wail over the want of truth, or of tests of truth, in physical speculation.

‡ *De Natura Deorum*, I, 18, 54, 66, 69, 73, 120; cf. *De Fato*, I, x, xi, xx; *De Finibus*, I, vi--vii; *Tusc. Disput.* I, xi, 22; xviii, 42.

that time were not discussing the concourse of atoms, fortuitous or otherwise, but were carefully pondering, with Doctors Divine and Angelical, Subtile and Irrefragable, the difference between *Ens* and *Essentia*, between *materia quomodolibet accepta* and *materia signata*, between *quidditas per se* and *hæcceitas per se*, between *ultima entitas entis* and *ultima actualitas formæ*. As we plod our weary way through the *Quodlibeta* of these venerable doctors, we can but envy the angels one of the faculties ascribed to them by St. Thomas Aquinas—that of being able to pass from point to point without passing through intermediate spaces.

Bacon,* as he stood at the threshold of the new dispensation of physical science, had made a plea for the forgotten philosophy of Democritus, but when the metaphysical philosophy of Europe came to a new Avatar in the brain of Descartes, we find that thinker denying a discrete conception of matter, and arguing for the contrary conception of continuous extension, of the identification of extension with substance, and, hence, of the infinite divisibility of matter. He says: "It is easy to demonstrate that there cannot be atoms; that is, parts of bodies or of matter which are of an indivisible nature, as some philosophers have imagined, since, however small we may suppose these parts, inasmuch as they must needs have extension, we conceive that there is not one of them which cannot still be divided into two or more still smaller parts; whence it follows that it is divisible." † It will here be seen that Descartes falls into a confusion of ideas with regard to the atoms of the ancient philosophers. They did not conceive that the atom was indivisible because of its smallness, but because of the indestructible solidity which made it incapable of being cut, or broken, or bent, and which also made it impervious to heat or humidity. ‡

* See, especially, *Cogitationes de Natura Rerum*, and *De Principiis atque Originibus*, &c. Works, (Ellis & Spedding's ed., London,) vol. III, pp. 15, 82, *et seq.*; *cf.* Advancement of Learning, Book II, vii, 7, (Ellis & Spedding's ed.,) vol. III, p. 358.

† For a formal criticism on Democritus' theory of atoms see *Principes de la Philosophie*, *Œuvres de Descartes*, (Cousin,) tome III, p. 516, and *cf.* Aristotle: *De Generatione et Corruptione*, I, ii, 11–21, where this criticism is anticipated and surpassed.

‡ "Corpora individua propter soliditatem," Cic., *De Fin.*, I, vi, 17; *cf.* Lucret., I, lines 532–5.

And this supposed conflict between the infinite divisibility of matter, mathematically considered, and the actual indivisibility of atoms, physically considered, is a pure logomachy resulting from what the lawyers would call a misjoinder of parties and a misjoinder of issues. The mathematician, contending for the infinite divisibility of matter, proceeds from the idea of space to a fact in nature, while the atomist, contending for the actual indivisibility of the atom, proceeds from an assumed fact in nature to the idea of space, and so, as has been said, the duellists cross swords in the air over the head of a phantom standing between them, and never succeed in touching each other.*

From this time onward, for many years, the opinions of philosophers concerning the nature or reality of atoms seem to have floated in a state of uncertainty between the views of the ancients and the views of Descartes. For instance, we find Henry More, the platonizing metaphysician of England, in the 17th century, adventuring the following dogmatic definition of matter: "I have taken the boldness to assert that matter consists of indiscerptible parts, understanding by indiscerptible parts particles that have, indeed, real extension, but so little that they cannot have less and be anything at all, and, therefore, cannot be actually divided. The parts that constitute an indiscerptible part are real, but divisible only intellectually, it being of the very essence of whatever is to have parts or extension in some measure or other, for, to take away all extension is to reduce a thing only to a mathematical point."†

For the physical atom of Greek metaphysics, Leibnitz, it is known, substituted the monad or formal atom, considered as the continent and complex of an infinite number of essences. Leibnitz tells us that so soon as he had thrown off the yoke of Aristotle he plunged into the vacuum and atomic hurly-burly of Democritus, but that he could find no rest there, because he could not account for the genesis of mind in man on any mechanical theory of purely physical atoms. Hence the invention of the Leibnitzian Monadology and Pre-established Harmony—a form of metaphysical philosophizing which reflects the mental evolution and intellectual environment

*See Westminster Review, vol. 59, p. 178, *cf.* Samuel Brown: Lectures on the Atomic Theory, Edinburgh, 1858.

† Quoted in Munro's *Lucretius*, vol. 2, p. 158.

of the 17th century, as exactly as the metaphysical speculations of Anaxagoras and Democritus and Epicurus represent the mental evolution and intellectual environment of the Greeks two thousand years before. The atom of Leibnitz instead of being an indivisible and sempiternal "solid singleness" is a created monad, a "manufactured article," deriving its perpetuity and power from the immanent and perpetual "fulgurations of Divinity."* It is the curious destiny of the atomic philosophy, let me here say, in parenthesis, that it has subtended three very distinct orders of metaphysic—the polytheistic metaphysic of Greece and Rome, the theistic metaphysic of the Renaissance period, and the scientific metaphysic of our own day.

According to Leibnitz separate classes of monads have separate qualities. Different degrees of aggregation in monads, differing in kind, make the varieties of matter. The natural mutations of monads proceed from an intestine force which is the principle or change in matter. In all simple substance there is a plurality of relations and affections, so that a residuum of relations and affections remains after every transfer of affections and relations in the production of material changes. These material changes proceed according to the law of continuity, for all change of the created monad is only the modulus of its perdurancy.† The monad is inconceivable, except as a creation of Divinity. When created, it is destructible only by the decree of Omnipotence.‡ Monads work no changes in each other's inner constitution, and therefore act on each other according to a Divine Pre-established Harmony, which makes each monad the mirror of the Universe, and the continuous register of all physical changes, past, present, and future. Hence the order of the movement and the continuity of the process which have resulted in the formation of the only world possible and the best world possible. It will be seen that we are here

*"Dieu seul est l'unité primitive ou la substance simple originaire, dont toutes les monades créées ou dérivatives sont des productions, et naissent, pour ainsi dire, par des fulgurations continues de la Divinité, de moment à moment." (*Monadologie*, prin. 47). *Leib. : Opera Phil., Lat. Gal. Germ. omnia*. Berlin, 1840, p. 708.

† *Leibnitii Principia Philosophiæ, More Geometrico demonstrata*, p. 33.

‡ *Ibid.*, pp. 71, 74.

far enough away from the Epicurean atoms, but we are still working with the atoms of pure metaphysics.

It is equally in accordance with the chronological order of time, and the logical order of scientific ideas, that we should next turn to Newton. And of Newton, the greatest name in all physical philosophy, it need only be said that in his work on Optics he returned to a conception of atoms, which, except that it proceeds on the assumption of a Deity and of final cause, is substantially identical with that of Leucippus, Democritus, and Epicurus. He says: "All *these* things considered [that is, the chemical facts he had just recited], it seems probable to me that God in the beginning formed matter in solid, massy, hard, impenetrable, movable particles, of such sizes and figures, and with such other properties and in such proportion to space as most conduced to the end for which He formed them; and that these primitive particles, being solids, are incomparably harder than any porous bodies compounded of them, even so very hard as never to wear or break in pieces—no ordinary power being able to divide what God himself made one in the first creation." This definition reminds us of Lucretius.

In continuation Newton adds: "While the particles continue entire they may compose bodies of one and the same nature and texture in all ages; but should they wear away or break in pieces, the nature of things depending on them would be changed. Water and earth composed of old worn particles would not be of the same nature and texture now with water and earth composed of entire particles in the beginning. And, therefore, that nature may be lasting, the changes of corporeal things are to be placed only in the various separations and new associations, and motions of these permanent particles."

The very form of this last-cited statement carries us back to the cradle of the Atomic Philosophy.* But it is not so much the form of Newton's statement which excites our admiration as the connection of thought in which it stands. The whole of

* Δημόκριτος δὲ καὶ Λεόκιππος ποιήσαντες τὰ σχήματα, τὴν ἀλλοίωσιν καὶ τὴν γένεσιν ἐκ τούτων ποιῶσι, διακρίσει μὲν καὶ συγχρίσει γένεσιν καὶ φθοράν, τάξει δὲ καὶ θέσει ἀλλοίωσιν. Aristotle: *Περὶ Γενέσεως καὶ Φθορας*, I, 2, 4. (Didot's ed., vol. 2., p. 434.)

the "31st Query," under which this passage occurs in the book of "Opticks," is occupied with certain chemical analyses which Newton had made in his laboratory. Newton, we know, was an alchemist, and spent laborious days and nights in trying to discover the secret by which base metals might be rendered noble; but I can hardly concur with Prof. Jevons when he says that Newton's "lofty powers of deductive investigation were wholly useless" in the conduct of these experiments.* There is some gold at the bottom of even his alchemical crucible. He was the first to put the conception of atoms in their rightful logical connection with the phenomena of practical chemistry.†

It would here be in order to follow Joseph Boscovich in his profound theory of the constitution of matter, if in doing so we might not fall into the danger of drifting too far from the atom considered as a minim of corporeal singleness. With him the atom is a point of attractive and repulsive forces rather than an ultimate physical element; and as it was really the atom of chemical physics which Democritus posited in his mind without knowing it, thus setting up the altar of science to an "unknown god," it is time that we should hasten towards the epoch when Chemistry came to rend the veil from the face of this Isis whom the Greek atomists had so long and so ignorantly worshipped.

It is in the writings of the Hon. Robert Boyle, pleasantly described by his Irish biographer, with a somewhat Irish collocation of ideas, as "Father of Chemistry and brother of the Earl of Cork," that we find the period of transition, when the old order of metaphysical atoms is changing to give place to the new order of physical atoms as weighed and measured by modern chemistry. In his essay on "The Intestine Motions of the Particles of Quiescent Bodies," ‡ as also in his essays on Fluidity and Firmness, he threw out some positive ideas on the old atomic philosophy. He supposes it to be of Phœnician derivation, and even tries to effect a reconciliation between that philosophy and the Cartesian notion of continuous substance by drawing on the *materia subtilis* of the French philosopher (which was conceived to pass constantly, like a

* Jevons: Principles of Science, vol. II, p. 133.

† Opticks, Book III, Query 31.

‡ Robert Boyle's Works, vol. I, p. 444.

stream, through the pores of the solidest matter) as a very good analagon for the racing atoms of Epicurus.

It is, however, in his essay entitled an "Attempt to make chemical experiments useful to illustrate the notions of the corpuscular philosophy,"* that he approaches this discussion with a bold front. He there says: "The corpuscular doctrine, rejecting the substantial forms of the schools, and making bodies to differ but in magnitude, figure, motion, or rest, and situation of their component particles, which may be always infinitely varied, seems much more favorable to the chemical doctrine of the possibility of working wonderful changes and even transformations in mixed bodies. . . . As many chemical experiments may be happily explicated by the corpuscularian notions, so many of the corpuscularian notions may be commodiously either illustrated or confirmed by chemical experiments." †

It will be seen at once, in the very dialect and purport of such language, that we have reached, even in Boyle, a turning point of the whole Atomic Philosophy. His words import that we are to use "the corpuscularian notions" to explicate *chemical* experiments, and that, in turn, the corpuscularian notions may find a new and solid basis in chemical *experimentation*. Men have changed their whole *Welt-Anschauung*, as compared with that of the Greeks in the days of Epicurus, before such processes of thought and such instruments or methods of enquiry become possible. It is only as the thoughts of men are widened with the process of the suns that they take in, or can take in, those wider horizons and deeper vistas of truth which are opened to the human mind by the ascending hierarchies of the physical sciences. We have now passed the border-line which separates the metaphysico-physical atoms of Epicurus from the physico-metaphysical atoms of modern chemical science.

I can afford to pass over this part of my story *sicco pede*, for we shall henceforth have to deal only with the atoms required by the hypotheses of positive and experimental science to explain the actual facts and processes of nature, not as those facts and processes lie on the surface of things, but as extorted from the very bosom

* Robert Boyle's Works, vol. I, p. 354.

† *Ibid.*, pp. 358, 359.

of nature by the racks and thumbscrews of physical enquiry. Instead of taking our atoms as they were distilled and attenuated by the refining brains of an Anaxagoras, a Democritus, an Epicurus, or a Leibnitz, we can now take them as weighed and measured by the quantitative, qualitative, or volumetric analysis of modern chemistry, in ways that Anaxagoras or Democritus or Epicurus or Leibnitz never dreamed of in their philosophy. The distance between the 5th century before Christ and the year 1800 is measured as well by John Dalton as by John Howard. John Dalton and John Howard would have each been impossible in the days of Democritus—the one as much so as the other. John Howard plunged into the reek of European prisons at the impulse of a Christian philanthropy unknown to the Greek, with all his love of the Good, the Beautiful, and the True. John Dalton plunged into the reek of the Lancashire marshes,* at the impulse of an abstract science unknown to the Greek with all his love of dialectics, of art, and of æsthetic culture. John Howard, to use the fine phrase of Burke, taught men who love mercy to “take the gauge and dimension” of human misery. John Dalton taught men who love truth in disinterested studies to take the gauge and dimension of the elements which compose the physical Universe. Who was this John Dalton that stands in such typical relation with the scientific thought of our century?

Given, a man “meditative and ratiocinative;” a meteorologist, curious in all eudiometrical research, and, therefore, perpetually experimenting on the constitution of mixed gases; a teacher of arithmetic, so given to mental numeration that on his first visit to London he counts all the carriages he sees while wending his way to the Friends’ Meeting House on a Sunday; a chemist, who took the diffusion and absorption of elastic fluids as his special province of investigation; a theorist, who never theorized without an experiment, and an experimenter who never experimented without a theory, and you have John Dalton, the father and founder of the Modern Atomic Philosophy.

As early as the year 1802, in some experimental combinations of oxygen with nitrous gas, Dalton discovered that “the elements of oxygen combined with a certain portion of nitrous gas, or with twice that portion, but with no intermediate quantity.” Though he

* He obtained his inflammable gas from these marshes.

called attention at the time to "the theory of the process," he does not seem to have apprehended the generality of the principle of definite and multiple proportions till a few years later, when the doctrine dawned on him in the course of some investigations into the constitution of olefiant gas and carburetted hydrogen gas.*

Richter, before him, had ascertained the quantity of any base required to saturate one hundred measures of sulphuric acid, and had formed a table exhibiting the proportions of the acids and alkaline bases constituting neutral salts, but Dalton took this table and translated it into the relative weights of the ultimate atoms composing these saline compounds.†

The doctrine of atomic weights had thus already become a working hypothesis in chemistry, no longer an idle speculation, and we soon find Berzelius writing to Dalton that "multiple proportions are a mystery without it." ‡

From this time onward the history of chemistry has been studded with fresh confirmations of the new atomic logic, while ever and anon prophetic glints of truth, implicit in every true physical hypothesis, have leaped into the light of ocular demonstration with each advancing stage in chemical science. Time would fail to tell the beads of the atomic rosary. The doctrine of fixed, multiple, and volumetric combinations, as formulated by Avogadro in 1813; § the determination of the proportions in which bodies combine according to the number and disposition respectively of their molecules, as announced by Ampère in 1814, with special reference to the clear-cut distinction between molecules and their integrant atoms, (already presaged before Ampère by Laurent and Gerhardt); || the relation between the atomic weights of bodies and their specific heats, conjectured by Dalton and established by Dulong and Petit in 1819; ¶ the law of isomorphism, announced by Mitscherlich at the close of the same year, from which it appeared that "a similar atomic constitution determines not only

*Henry: *Memoirs of the Life and Scientific Researches of John Dalton*. p. 80.

† *Ibid.*, p. 85.

‡ *Ibid.*, p. 100.

§ Wurtz: *The Atomic Theory*, p. 36.

|| *Annales de Chimie*, vol. 90, p. 43.

¶ Wurtz: *The Atomic Theory*, p. 52.

the analogy of chemical properties, but also the similarity of physical forms;”* the discoveries in electrolysis, with their bearing on atomicity, as published by Faraday in 1834, in the Seventh Series or his Experimental Researches; † the labors of Berzelius in clarifying the atomic weights of the elements; the “law of Octaves,” announced by Newlands in 1865, according to which the elements were divided into groups, having numbers differing by seven, or some multiple of seven; ‡ the enlarged Periodic System of the elements, as published by Mendelejeff in 1869, with the prognostication of undiscovered metals required to make the system complete—among them a metal which the Russian chemist proceeded to name “ekalu-minium” in advance of its discovery; § the discovery of the missing metal in 1875, by Lecoq de Boisbaudran, who found it in a blende from the mines of Pierrefitte, in the Pyrenees, and gave to it the name of “Gallium,” without knowing that he had lighted on the “missing link” of Mendelejeff; || the extension of this periodic system by Lothar Meyer, with his Curve of the Elements, showing that the ductility, fusibility, and volatility of bodies are functions of their comparative atomic weights; the periodic system, as revised and extended during this very year, by Prof. Carnelley, in the light of the experimental boiling and melting points and heats of formation of the halogen compounds of the elements, ¶ (chlorides, bromides, and iodides;) Carnelley’s tables of color relations in chemical compounds as indicating the influence of atomic weights; ** and, lastly, Carnelley’s new reduction of the periodic system of the elements considered in the light of their occurrence in nature, with the helpful inferences to be drawn from it ***—these, and such like discoveries as these, following in the wake of the modern atomic

* Experimental Researches in Electricity, vol. I, pp. 230–258.

† Wurtz: The Atomic Theory, p. 58.

‡ Newlands: The Discovery of the Periodic Law, &c., p. 14.

§ *Annalen der Chemie und Pharmacie, Supplement Band 8*, p. 133 *et seq.*

|| *Comptes Rendus*, t. LXXXI, p. 493. How fully Mendelejeff recognized in gallium the characters wanted to fill the gap in his periodic system, see *Comptes Rendus*, same volume, p. 969.

¶ *Philosophical Magazine* for July, 1884.

** *Phil. Mag.* for August, 1884.

*** *Phil. Mag.* for September, 1884

theory, have abundantly vindicated its value as an instrument of chemical research, while conspiring to vindicate its truth by giving to its votaries that ability of prediction which is the crucial test of science. The theory, besides, has sometimes "snatched a grace beyond the reach of art" by working retroactively to the purification of chemical method from errors and defects incident to the most careful manipulations of the practical chemist.

Standing in the presence of chemical science, as now constituted, Baron Liebig has expressed the opinion that we can scarcely conceive how it could have been developed without the Daltonian hypothesis. And yet the atom of Dalton, considered in its relation to our natural senses, is just as incapable of visible and tangible demonstration as the atom of Democritus. For this reason it is known that Faraday could never fully reconcile himself to the modern doctrine of atoms.* But, in fact, there is a genetic and a generic difference between the ancient and the modern conception. The former is the offspring of the philosophical imagination toying with analogy. The latter is the offspring of the philosophical imagination gendering with the homologies of reason. The atom of Democritus sprang into thought under the plastic forms by which he figured to himself at will the invisible relations and constitution of matter. The atom of Dalton sprang into thought from a rigid mathematical mind figuring to itself certain determinate relations which had become visible in elastic fluids. The atom of Democritus was, by the terms of its genesis, incapable of verification. The atom of Dalton was, by the terms of its genesis, capable of verification, if true, in all the gases of nature. Metaphysic thought born of the analogical reason can never conclusively prove its legitimacy. Metaphysic thought born of the homological reason can always prove its legitimacy, and, until it does, has no rights of heirship in the kingdom of science. The essential quality of a metaphysico-physical hypothesis is that it should be plausible; the essential quality of a physico-metaphysical hypothesis is that it should be apodictic. The former is "magistral and peremptory;" the latter is "ingenuous and faithful." The former is contrived in such sort as to be "soonest believed," the

*Faraday: *Experimental Researches in Electricity*, vol. 2, p. 284. But cf. vol. I, p. 249.

latter is contrived in such sort as to be "easiest examined," to cite the words of Bacon.*

The Atomic Philosophy may, therefore, be said to offer a good type of all that is valid in physical metaphysics, and of all that is invalid in metaphysical physics. As the child in the infantile stage of his development dwells delightedly amid fays and talismans, because his metaphysic is stronger than his physics, so the savage man, artless child of nature, is easily pleased with the rattle of some lying legend, or tickled with the straw of some preposterous myth—the more preposterous the better. A cultivated race whose imagination is creative and artistic, but whose reason has not yet been developed by the processes of a rigorous logic, will demand, as has been already said, an artful and curious felicity in their physical theories—but they will demand nothing more, because when this demand is met, their highest intellectual demand has been met. It is not until "the heir of all the ages" has learned to change the organon and method of his physical enquiries, and to put his reason over his imagination, by making imagination the hand-maid of reason, that Science is born. Long before this stage has been reached the children of Science may come to the birth, but there is not strength to deliver, because the true *maieutic* of science—experimentation with rational hypothesis, and rational hypothesis with experimentation—has not yet come to the teeming mind of philosophy. The goddess Experimentation is the Lucina of Science. The free surrender of all metaphysical conceptions to the hands of this Lucina, with the distinct knowledge that she will strangle them if they are not well formed, is the birth-pang of the scientific spirit. Until this stage of mental evolution is reached we shall have as many theories of the Universe as we have stages of culture, for every stage of culture will have a physics of its own, because it has a metaphysic of its own. Hence, the endless varieties of cosmology—the Hottentot physics, the Indian physics, the Stoical physics, the Epicurean physics, the Leibnitzian physics, the Cartesian physics, and such like—all the coinage of the metaphysical imagination. Grote enumerates as many as twelve distinct physical philosophies which divided speculative opinion in Greece during the century and a half between Thales and the Peloponnesian war.

* The Advancement of Learning, Book I, v, 9.

It is the mission of science to bring the physics of the world into unity by reading the phenomena of the world in the dry light of reason, and by continuing to spell and parse the hieroglyphs of Nature until the rational processes of our logic are brought into demonstrated correspondence with the actual processes of Nature. Science still keeps metaphysic in her service. But instead of weaving whole fabrics from the metaphysical loom and devising ingenious tissues which only reveal the nakedness of reason, Science in passing from the known to the unknown employs metaphysic as the gossamer spider employs the single thread on which she sways and balances her movements between two solid points. The thread is tied to something solid as the condition of reaching something solid after her aerial flight. So the man of science, working in and under the limitations of physics, works on the lines of metaphysic thought when he frames the tentative hypotheses with which he returns again to the patient, practical study of nature.*

The scientific man reads the Universe backward by the inductive syllogism, because Nature has proceeded forward in her evolutions, according to an unbroken chain of antecedent causes. The physical Universe is indeed a fasciculus of natural syllogisms colligated into the compactest unity, and so holding all things, forces, and functions under the bonds of logic. The scientific man, at any given stage of his enquiry, has before him only the conclusions or at best only the minor premises and the conclusions of this world-process. And he knows that these conclusions of the natural syllogistic process have been reached through a perpetual flux in the universal complex of things, forces, and functions—a flux which dates from the beginning of star-mist and nebula, or from the beginning of that more elementary fluid out of which star-mist and nebula were generated, according to the scientific metaphysic of the present day. Is it any wonder, then, that many of the major premises of Nature's physical syllogisms should still be wrapt in impenetrable mystery to us, as many of the major premises which

* Bacon's oft-quoted contrast between metaphysicians, who, he says, spin "laborious cobwebs of learning," like spiders, and physical philosophers, who "work according to the stuff, and are limited thereby," seems hardly fair to the spider. *Advancement of Learning*, Book I, iv, 5.

we have spelled out were wrapt in an impenetrable mystery to the Greeks in the 5th century before Christ?

As there is a need that much of metaphysic thought must be blended with the psychological processes which lead to every passage from the known to the unknown; so every great discovery of the physical philosopher tends to widen the metaphysical horizon within which he works. The world was never so full of metaphysic as it is to-day, when physical science is transforming the minds of men not so much by the secular boons it is dropping in the lap of modern civilization as by its underlying doctrines; and these doctrines are often the mere metaphysical reflex or obverse of the physical truths they subtend. The psychological processes of every age are conditioned by its logical method, and its logical method is justified to itself by its metaphysic—by those necessary conceptions and fundamental relations which it takes to be architectonic of the Universe. What, for instance, can be more metaphysical than the latest conception of our highest physical science—the conception of vortex atoms moving in an imaginary frictionless fluid where the origin and the end of the motion are equally inconceivable? Or, take Mr. Darwin's doctrine of hypothetical gemmules "inheriting innumerable qualities from ancestral sources, circulating in the blood and propagating themselves, generation after generation, still in the state of gemmules, but failing to develop themselves into cells because other antagonistic gemmules are prepotent and overmaster them in the struggle for points of attachment"*—in what respect is this doctrine one whit less metaphysical than St. Augustine's doctrine of original and hereditary sin? Or, when the late Prof. Clifford tells us that "the Universe consists entirely of mind-stuff;" that "matter is a mental picture, in which mind-stuff is the thing represented," and that "reason, intelligence, and volition are properties of a complex which is made up of elements themselves not rational, not intelligent, not conscious"—how does his "mind-stuff" differ from the "mind-stuff" of Pythagoras, † except in the

* Galton: *Hereditary Genius*, p. 367; *cf.* Darwin: *Animals and Plants under Domestication*, (London,) vol. 2, p. 402. For a criticism on this physiological doctrine, see *Encyclopædia Britannica*, ("Atoms,") vol. 3, p. 42.

† For the "mind-stuff" of Pythagoras, see Cicero, *De Nat. Deorum*, I, xi, 27. For the "mind-stuff" of Clifford, see "Mind," January, 1878, p. 66.

greater ingenuity and method of the metaphysic art with which it is conceived?

If within the limits of this discussion I had the time, and if, under the limitations of my knowledge, I had the ability, to carry this enquiry into the realm of molecular physics and dynamics, where such star-eyed mystagogues as a Clausius or a Rankine, a Clerk-Maxwell or a Sir William Thompson have borne the thyrus of science before us, it would be easy to show that, under their guidance, we have escaped the pitiless parallel lines of the Epicurean atoms only to find ourselves inextricably implicated in the knottedness and linkedness of the vortex rings of atoms as they execute their infinite evolutions and involutions, vibrating now in one period and now in another behind that veil of matter where they can be descried only by the shadowy lines they reveal to the spectroscopic imagination. "It is the mode of motion," says Clerk-Maxwell, "which constitutes the vortex rings, and which furnishes us with examples of that permanence and continuity of existence which we are accustomed to attribute to matter itself. The primitive fluid, the only true matter, entirely eludes our perceptions when it is not endowed with the mode of motion which converts certain portions of it into vortex rings, and thus renders it molecular."*

Of these vortex rings we must say, in the dialect of the schools, *cognoscendo ignorantur, sed ignorando cognoscuntur*. Withheld from positive conception, yet necessitated to scientific thought and speculation by the exigencies of the knowledge we *can* conceive positively, they afford a good illustration of the physical metaphysic which has wafted the scientific mind of the present generation into an empyrean as much higher than the empyrean of Plato as the spectroscopic vision of modern science is more far-reaching than the highest flight of metaphysic wit among all the physical atomizers who ever lived or dreamed in Greece. Every chemical atom, says Sir John Herschel, is forever solving differential equations, which, if written out in full, might belt the earth. "An atom of pure iron," says Jevons, "is probably a vastly more complicated system than that of the planets and their satellites."

Between metaphysical physics and physical metaphysics there is a world-wide difference. The invisible ether posited behind the

* Encyclopædia Britannica, *sub voce* "Atom."

vail of matter by the East Indian philosophy of the Upanishads, or by the visionary dialectic of Cleanthes, was posited there by metaphysical physics. The invisible fluid posited by modern science behind the vail of matter is posited there by physical metaphysics. The vortices of Democritus as well as the vortices of Descartes are the creations of metaphysical physics. The vortices of Helmholtz and of Sir William Thompson are the creations of physical metaphysics. The fixed and crystalline sphere of the old Ptolemaic astronomers was an invention of metaphysical physics. The solid ether which transmits to us the light of the stellar Universe, and which, as Sir John Herschell remarks, is the modern "realization of the ancient idea of the crystalline orb," is the invention of physical metaphysics. When Lucretius finds in the iridescent hues of the peacock's tail, as it shimmers in the sun, a fresh type and instance of Nature's prodigality in the display of atoms, he does but yield another contingent to the barren store of his metaphysical physics. When Dr. John Tyndall finds in the iridescences of the common soap bubble a proof that stellar space is a plenum filled with a material substance that is capable of transmitting motion with a rapidity that would girdle the equatorial earth eight times in a second, he does but yield another contingent to the fertile store of his physical metaphysics. When Dr. George Cheyne, of Scotland, expressed the opinion in the last century, that "all animals, of what kind soever, were originally and actually created at once by the hand of Almighty God, it being impossible (he said) to account for their production by any laws of mechanism;" and when he further held that "every individual animal has, *in minimis*, actually included in its loins all those who shall descend from it, and every one of these again has all its offspring lodged in its loins, and so on *ad infinitum*," and that "all this infinite number of animalcules may be lodged in the bigness of a pin's head,"* he preached a biological doctrine which sounds in the terms of metaphysical physics. When Mr. Darwin in his provisional theory of Pangenesis assumes the existence of the gemmules which inherit innumerable qualities from ancestral sources, and which prelude as gemmules that struggle for existence which antedates and therefore conditions the terms of the human struggle witnessed in society, commerce, and national life, he expounds a biological doctrine which sounds just as clearly in the terms of physical metaphysics. When old

* J. Brown: Locke and Sydenham, p. 270.

Heraclitus proclaimed that the Universe with all it contains sprang into being from elemental heat, and was destined to be resolved again into the elemental heat from which it sprang, and thus in a ceaseless round to continue the cycle of being, he taught a doctrine of conservation and correlation of energy which had its root in metaphysical physics. When Dr. John Tyndall declares that "all our philosophy, all our poetry, all our science, all our art—Plato, Shakespeare, Newton, and Raphael—are potentially in the fires of the sun," and so tucks away the genius of a Darwin in the folds of a nebular blastema, he teaches a doctrine of equivalence which has its root in physical metaphysics.

It will thus be seen that under the dominion of Science the world has use for as much metaphysic as ever before, but only for a metaphysic radically different from the old metaphysic in its point of departure as also in the tests of its validity, and, therefore, radically different in the tenure by which it is held. The votaries of the old metaphysical physics proceeded from what was unknown to explicate and explain the known appearances of things, and rested content in explanations which seemed to consist with those appearances. The votaries of the modern physical metaphysics proceed from what is known to explicate and explain what is unknown in the deeper relations of things, and rest content in explanations only so long as, and so far as, they seem consistent with experimental proofs or with the broadest homologies of the deductive reason.

When the law of simple multiples in chemical combinations was given to the world by Dalton, and was expressed by him in atomic language, he had really made a great departure from the physical methods of Democritus, though it is curious to observe that there is a perfect identity between the metaphysical ideas underlying his logic and the metaphysical ideas of his Greek predecessor. The method of each proceeds on the assumption of the indestructibility of matter, and it is from this platform that the English chemist reaches out his hand to the Greek philosopher in token of a common metaphysic. "No new creation or destruction of matter," wrote Dalton, in his celebrated paper on "Chemical Synthesis," "is within the reach of chemical agency. We might as well attempt to introduce a new planet into the solar system, or to annihilate one already in existence, as to create or destroy a particle of hydro-

gen."* Democritus knew nothing of hydrogen, but he saw as clearly and said as plainly as Dalton that the antecedent premise of all physical philosophy must be found in the metaphysical maxim that "out of nothing nothing comes, and that nothing which is can ever be annihilated." †

And this maxim, with which the old Greek philosophy began, is about all of solid and sound that remains to us from the physical philosophizing of the ancients. It is true, as Mr. Balfour Stewart remarks, that the ancients had in some way grasped the idea of the essential unrest and energy of things; that they had the idea of small particles or atoms as the constituent elements of matter, and divined the existence of an ethereal medium extending through all space; but there is no evidence at all to support the statement that any one or all of these doctrines proceeded from even a rudimentary conception of "the most profound and deeply seated of the principles of the material universe."

There is, however, one respect in which it may be justly said that Democritus stands at the head of the long line of natural philosophers who since his day have been explicating for us the structure of the physical universe. He was the first who ever attempted a purely mechanical solution of the problem of physical being. It is the singular glory of the atomic philosophers that alone, among the jarring schools of Greece, they saw that a science of the Universe was possible only on the assumption that the phenomena of the physical universe are bound together by necessary law, and this law mechanical in the modes of its operation. They had no *science*, it is true, in the modern sense of the word, but it is no small distinction which they have won in standing at the head of an intellectual succession which embraces in its ranks a Copernicus and a Galileo, a Newton and a Laplace, a Dalton and a Faraday. ‡

* Henry: *Memoirs, &c.*, of Dalton, p. 88.

† Diog. Laert., *sub voce* "Democritus," where it is particularly recorded that he assumed as his point of departure the maxim "Out of nothing nothing comes," &c.

‡ "Was die Atomiker von ihren Vorgängern unterscheidet, ist nur die Strenge und Folgerichtigkeit mit der sie den Gedanken einer rein materialistischen und mechanischen Naturerklärung durchgeführt haben; diese kann ihnen aber um so weniger zum Nachtheil gedeutet werden, da sie damit nur die Schlüsse gezogen haben welche durch die ganze bisherige Entwicklung gefordert, und wozu in den Annahmen ihrer Vorgänger die Vordersätze gegeben waren." Zeller: *Philos. d. Griechen*, Erster Theil, 765.

With two short lessons cited to point the moral of this long story, and I have done. The first of these moralities shall be a warning against the folly of the old atomists in attempting to philosophize beyond the conditions of their knowledge. They reared imposing fabrics in astronomy, in physics, in psychology, and in anthropology, but they built without laying their foundation in any deep knowledge of nature, and laid the successive courses of their system-building in the untempered mortar of an incoherent logic. And the moral needs to be pointed as much for the admonition of modern scientific workers, with their cheap and easy cosmologies, as for the reproach of the old physiologists of Greece. One of our poets has sung:

From an old English parsonage
 Down by the sea,
 There came in the twilight
 A message to me.
 Its quaint Saxon legend,
 Deeply engraven,
 Hath, as it seems to me,
 Teaching from heaven;
 And all through the hours
 The quiet words ring,
 Like a low inspiration,
 "Doe the nexte thyng."

The message is as full of inspiration for guidance in physical philosophizing as for guidance in moral conduct. *Tantum series iuncturaque pollet.*

The only other morality which time permits to be pointed at the end of this review is a warning against intellectual impatience—not that intellectual impatience rebuked by the maxim just cited, and which seeks to leap at a single bound the limitations of knowledge in any given age—but the intellectual impatience which cavils at the short-comings of the men who dug the first ditches and planted the first hedges around the vineyards of science. They were humble pioneers, but they opened the way into that land of Beulah where the men of science sit to-day beneath their own vines and fig-trees, with none to make them afraid. Even after John Dalton had come to place the key of the new Atomic Philosophy in the hands of men, it was a saying of Mitscherlich that it took fourteen years to discover and establish a single fact in

chemistry. Let us not wonder, then, that it took more than two thousand years to perfect the doctrine of atoms as a clew to the "mystery of matter." Democritus invented a mechanical key of wonderful ingenuity, but it would not unlock anything that could not be unlocked without it. Newton divined that the key must be fitted to the two great wards of chemical attraction and chemical repulsion, but still the key would not turn in the adamantine lock of Nature. Dalton found that the secret of the combination must be sought in wards nicely graduated according to certain fixed, definite, and multiple numbers, and, since his day, door after door in the chemist's "chamber of imagery" has seemed to swing open at the touch of this talisman. And even, if in the next two thousand years, or in the next twenty years, the theory of John Dalton should be absorbed in some deeper truth, there will still be room in the pantheon of science for the memorial bust of the plain Manchester arithmetician, so long as men recall how far that little candle, which he lighted with inflammable gas obtained in the rudest way from the ponds of Lancashire, has thrown its quickening beams across the whole tract of modern chemistry.



BULLETIN

OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON.

GENERAL MEETING.



BULLETIN
OF THE
GENERAL MEETING.

244TH MEETING.

JANUARY 5, 1884.

The President in the Chair.

Twenty-eight members and guests present.

The Chair announced the death, since the last meeting, of General A. A. HUMPHREYS, one of the founders of the Society.

Mr. J. R. EASTMAN made a communication on

THE ROCHESTER (MINNESOTA) TORNADO,

describing the ground as it appeared a few days after the storm, and showing that the phenomena did not indicate cyclonic motion. All disturbed objects were thrown in essentially the same direction, and were pressed down rather than lifted.

Mr. ELLIOTT related that twenty-five years previous he had crossed a storm-track consisting of a double line of fallen timber, with an interval in which the timber was standing. Mr. EASTMAN thought this phenomenon should be referred to two separate cyclones, possibly moving as companions.

Mr. DALL described storm tracks in the Escanaba region in which the trunks of prostrate trees pointed uniformly in one direction, the path of destruction being definitely limited at the margins.

Mr. E. FARQUHAR suggested that a highly inclined storm axis might account for the uniformity in the direction of the wind in the zone of destruction.

Mr. W. H. DALL read a paper on

RECENT ADVANCES IN OUR KNOWLEDGE OF THE LIMPETS,

summarizing the researches of Spengel on the sensory organs or osphradia; Cunningham on the renal organ and renopericardial pore in *Patella* and *Patina*; Fraissé on the eye in *Patina*, *Fissurella* and *Haliotis*, and the speaker on the presence of an intromittent male organ in *Cocculina*. He stated that among the *Acmæidæ* and *Patellidæ* the type of eye differs, and while in *Patina* it is of a very rudimentary character, in other genera it might be well developed, as, for instance, in *Ancistromesus*, which has as well developed eyes as *Fissurella*. He also alluded to the gradual progress in classification afforded by anatomical investigation during the past few years, and observed that nearly all the known forms except *Propilidium* and *Scutellina* were amenable to classification; our ignorance of the branchiæ in the former, and the dentition in the latter, operating to prevent a final classification in these two cases, until more is known. Those authors who study the embryology and histology usually from a single species, generally ignore the wide differences of adult anatomy between the genera of Limpets, and sow their generalizations on a basis of classification which is little in advance of that of Lamarck and his immediate successors.

Professor C. H. HITCHCOCK being present was invited by the Chair to address the Society, and responded briefly.

The President of the Society then pronounced a brief eulogy on General Humphreys, characterizing him as a man who had left behind him an honorable name as well for his distinguished achievements in science and in war as for the virtues and graces which adorned his private life. Mingling among his fellow-men with the utmost unobtrusiveness, and as gentle in spirit as he was brave in conduct, he brought the highest intelligence as well as the highest conscientiousness to the discharge of all the duties—scientific, military, and administrative—with which he filled his long and useful life: a life fitly closed by the serenity and peace of his beautiful death.

245TH MEETING.

JANUARY 19, 1884.

The President in the Chair.

Forty-five members and guests present.

The Chair read a letter from the Biological Society of Washington inviting the members of the Philosophical Society to attend its meeting of January 25th, for the purpose of listening to the annual address of its President, Dr. C. A. White.

Announcement was made of the election to membership of Messrs. GEORGE EDWARD CURTIS and PATRICK HENRY RAY.

Mr. I. C. RUSSELL made a communication on

THE EXISTING GLACIERS OF THE HIGH SIERRA OF CALIFORNIA.

[Abstract.]

During the summer of 1883 I had an opportunity of tracing to their sources some of the ancient glaciers of the High Sierra in the region between Mono Lake and the Yosemite Valley.

From the glacial records seen during a number of excursions into the mountains it was evident that the High Sierra had formerly been so deeply covered with ice that only the culminating peaks and ridges escaped the general glaciation. From the vast névé of the mountain tops flowed long winding rivers of ice, both to the eastward and westward through the cañons and valleys. In nearly all cases the glaciers occupied drainage lines of pre-glacial date, which they modified and enlarged, but, with the exception of the cirques about the higher peaks and crests, they failed to originate any of the more prominent topographical features of the range. The glaciers of the Sierra Nevada were not connected with a northern ice-sheet, but were of local origin and of the same type as the Swiss glaciers of the present day, but of far greater magnitude. If the cañons and valleys of the Sierra are traced upward, it is almost invariably found that they head in cirques or amphitheaters, in some of which small glaciers still linger—perhaps remnants of the mighty ice-rivers that formerly flowed from the same fountains.

The first glacier visited by the writer was on the northern side of Mt. Dana, at an elevation of about 11,500 feet above the sea, and at the head of a deep cañon which drains into Leevining creek,

one of the tributaries of Mono Lake. The Mt. Dana glacier is approximately 2,500 feet long and of somewhat greater breadth. Although small, and in fact but a "pocket edition" of what may be seen on a far grander scale in many mountains, yet it is a veritable glacier, with nearly all the features that characterize such ice-bodies in other countries. The distinction between the snow-ice of the névé and the more solid blue or greenish-blue ice of the glacier proper is clearly marked—as was observed to be the case also in a number of neighboring glaciers. An irregular open fissure crosses the head of the névé, corresponding to the "bergschrand" of the Swiss glaciers, while a number of parallel fractures on the border of the glacier at the foot of the snow-field form marginal crevasses with walls of solid blue ice. Near the terminus of the glacier alternating sheets of porous, white ice, and of more compact bluish ice were observed, which produce a distinct laminated or ribboned structure. Dirt-bands were plainly visible, sweeping in undulating lines across the surface of the glacier; and similar bands are a conspicuous feature in nearly all the ice-bodies seen in the High Sierra. About the foot of the Mt. Dana glacier a true terminal moraine is now in process of formation. The fall of stones and dirt from the ice onto the moraine was noticed many times during our visits. Some of the rounded stones from beneath the ice are battered and scratched and have evidently received these markings within the past few years.

On the northern side of Mt. Lyell another glacier was visited, which is the source of the Tuolumne river. The Mt. Lyell glacier is somewhat larger than the one on Mt. Dana, and, like it, exhibits characteristic glacial phenomena. A protrusion of compact, banded ice from beneath a snow-field at the head of an amphitheatre was here again observed, as well as the presence of moraines, crevasses, dirt-bands, etc. On the lower portion of this glacier were observed "ice-pyramids" of the form represented in the figure on the following page.

At the northern base of a pyramid there invariably occurs a stone or a mass of dirt, that is depressed below the general surface of the glacier, as is indicated in the sketch. The pyramid invariably points toward the noon-day sun. Its mass is composed of porous and banded ice, like that forming the general surface of the glacier, but its northern face is sheeted with compact, bluish ice. The

northern face is also concave, as represented in the sketch, and usually conforms to some extent with the shape of the stone at its base.

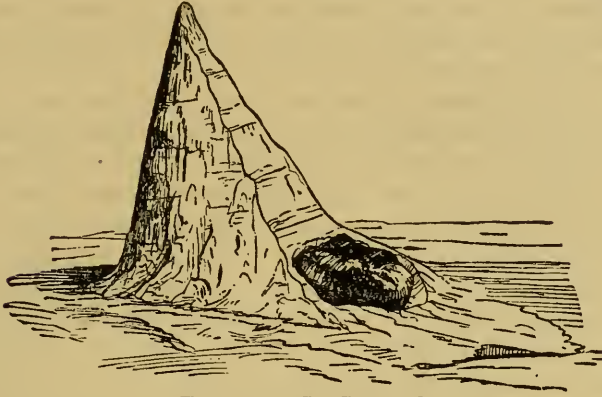


FIG. 1. An Ice-Pyramid.

On another glacier, discovered at the head of Parker creek, one of the tributaries of Mono Lake, all the glacial phenomena mentioned above are well displayed, and, in addition, "glacier-tables" were observed in considerable numbers. The following figure represents several of the glacier-tables of the Parker creek glacier, grouped for convenience of illustration :

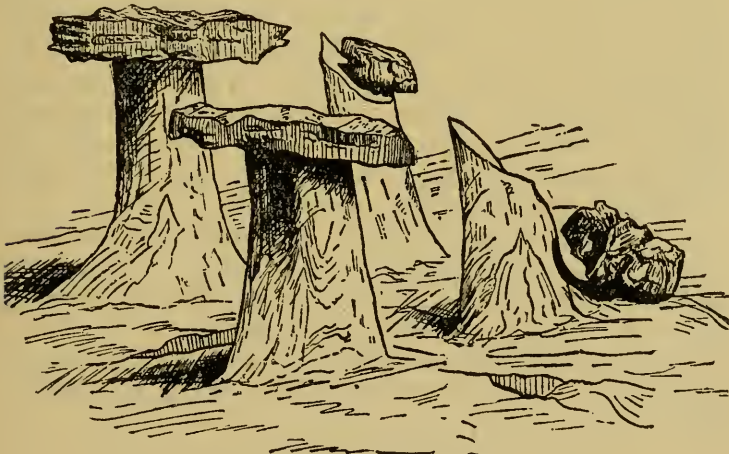


FIG. 2. Glacier-Tables.

The largest perched-block now being carried along by this glacier measures 34 by 28 by 10 feet, and is supported on a column of ice five or six feet thick, eight feet high on its northern side, and six feet high on its southern. Many masses of rock larger than the one measured were seen in the terminal moraine that circles about the foot of the glacier.

The motion of these glaciers was not observed, but that it exists is manifest from the nature of the crevasses and the curvature of the dirt-bands. The rate of flow of a glacier on Mt. McClure was measured several years since by Mr. Muir, who found it to be 47 inches in 46 days (from August 21st to October 6th, 1872).*

Six glaciers are known to the writer within the southern rim of the hydrographic basin of Mono Lake, and about twice this number were seen about Mt. Conness, Mt. McClure, Mt. Lyell, Mt. Ritter, and the Minarets.

Many of the glaciers mentioned above have been previously reported in popular articles by Mr. John Muir, but the fact that they are true glaciers having been denied by eminent geologists, it is desirable to have a more accurate description of them.

[The communication was illustrated by photographic lantern views. Its subject-matter will be more fully presented in the Fifth Annual Report of the United States Geological Survey.]

Mr. GILBERT THOMPSON described certain glaciers on Mount Shasta believed to be new to science. Their discovery increases the number of known glaciers on the flanks of Shasta to seven.

Mr. HOLMES described modern glaciers of the Rocky Mountains observed by himself. Those of the Wind River Mountains are from one-fourth mile to one mile in length. He illustrated by a sketch the position of three small glaciers in the gorges of Mount Moran, in the Teton Range, at an altitude of 10,000 feet.

Mr. POWELL remarked that the chief interest of these small modern glaciers lies in the fact that they illustrate the process by which the drift has been distributed, and aid in completing the theory of the ancient glaciation of the country.

Mr. MARK B. KERR mentioned the occurrence of a probable glacier in the Salmon Mountains, a division of the Coast Range.

* American Journal of Science, Vol. V, p. 69; 1873.

Mr. HARKNESS set forth the apparent difficulty of discriminating between a *névé* and a glacier proper, and requested that some geologist would define the term "glacier."

Mr. EMMONS said that a true glacier is an ice river, conforming in shape to the more or less restricted channel in which it flows, and this characteristic might form a base of distinction between the true glacier and the *névé*-field, the latter being comparable to the lake which forms the source of a mountain stream. Thus the *névé* would become a glacier only when from a broad and shallow ice-field it had become compressed into a narrower and deeper mass, between confining walls.

Other remarks were made by Messrs. E. FARQUHAR, GILBERT, DALL, and ELLIOTT.

Professor W. C. KERR made a communication on

THE MICA MINES OF NORTH CAROLINA.

[Abstract.]

The profitable mines are restricted to a plateau limited eastward by the Blue Ridge and westward by the Smoky Range. These were anciently worked on a very extensive scale. Few other modern mining operations have been so profitably conducted as those at the points occupied by the early miners. The ancient work was performed with blunt-pointed tools—doubtless of stone—and was confined to the partially decomposed portions of the granite veins, but large pits were nevertheless excavated. One of these measures 150 by 75 feet, and, despite a partial filling with *débris*, retains a depth of 35 feet. Facts connected with the arboreal vegetation show that some, and perhaps all of these openings were abandoned as much as five hundred years ago. The modern industry began in 1868, and, although it has assumed considerable importance, is not yet conducted in a systematic way.

The character of the mica and its associated minerals were discussed and illustrated by specimens.

246TH MEETING.

FEBRUARY 2, 1884.

The President in the Chair.

Forty-eight members and guests present.

The Chair announced the election to membership of Mr. THOMAS ROBINSON.

Mr. C. V. RILEY made a communication on

RECENT ADVANCES IN ECONOMIC ENTOMOLOGY.

The paper set forth the part which insects play in the economy of nature, and particularly their influence on American agriculture. The earlier writers on applied entomology in the United States, as Peck, Harris, Fitch, Walsh, LeBaron, Glover, did some excellent work in their studies of the habits and life-histories of injurious species, but the most important results followed when such studies were combined with field work and experiment by competent persons and upon scientific principles. A number of the remedies proposed in the agricultural press are foolish and based on misleading empiricism. Economic entomology as a science is of comparatively recent date. It implies full knowledge of the particular injurious species to be dealt with and of its enemies, of its relations to other animals and to wild and cultivated plants. In short, the whole environment of the species must be considered, especially from the standpoint of the farmer's wants. The habits of birds, more particularly, and the bearings of meteorology and of the development of minute parasitic organisms must be considered. Experiments with insecticides and appliances will then be intelligent and successful in proportion as the facts of chemistry, dynamics, and mechanics are utilized.

The complicated nature of the problem was illustrated by the life-history of *Phylloxera vastatrix* Planchon, and the difficulties often encountered in acquiring the facts were illustrated by the late work on *Aletia xyliana* (Say).

The chief insecticides considered for general use and applicable above ground were tobacco, white hellebore, soap, arsenical compounds, petroleum, and pyrethrum; those for use under ground, naphthaline, sulpho-carbonate of potassium, and bisulphide of car-

bon. The most advantageous and improved methods of utilizing each were indicated. Recent experiment showed that kerosene emulsions, such as had been recommended lately in the author's official reports, are superior to bisulphide of carbon when used under ground against the Grape *Phylloxera*, and the discovery is deemed of great importance, especially to the French people and those on our Pacific slope. Contrary to general belief, pyrethrum powder was shown to have a peculiar and toxic effect on higher animals as well as on the lower forms of life. Its deadly influence on lower organisms led the author to strongly recommend its use as a disinfectant, and to express the belief that it will yet come to be used in medicine. Dr. H. A. Hagen's recommendation of the use of yeast ferment was touched upon. It has proved of little or no practical avail, and some of the publications on the subject were characterized as unscientific. The use of malodorous substances as repellants, which was much relied on in the early days of economic entomology and strongly recommended by the two Downings, has lately been agitated as a new principle for the prevention of insect attack by Prof. J. A. Lintner. The principle can be applied in exceptional cases to advantage, but experiment gives little hope of its utility against most of our worst field insects. Prof. S. A. Forbes is engaged in interesting researches, having for object the utilization of micro-organisms, but with more promise for pure than applied science.

Of recent progress in mechanical appliances, the paper dealt with those lately perfected under the author's direction by Dr. W. S. Barnard, one of his assistants. This part of the subject was illustrated by models and by plates from the forthcoming fourth report of the United States Entomological Commission.

The paper concluded with the following plea for applied science: "Matters of fact do not tend to provoke thought and discussion; and I must confess to some misgivings in bringing these practical considerations before a body which reflects some of the highest and purest science and philosophy of the nation. From the days of Archimedes down to the present day there has existed a disposition to decry applied science and to sneer at the practical man. Yet I often think that science, no matter in what fine-sounding name we clothe her, or how high above the average understanding we stilt her, is, after all, but common sense employed in discovering the

hidden secrets of the universe and in turning them to man's wants, whether sensual or intellectual. Between the unbalanced vaporings of the pseudo-scientific theorizer and the uninformed empiric who stumbles upon a discovery, there is the firm middle ground of logical induction and deduction, and true science can neither be exalted by its inapplicability, nor degraded by its subserviency to man's material welfare. The best results follow when the pure and the applied go hand-in-hand—when theory and practice are wedded. Erstwhile the naturalist was honored in proportion as he dealt with the dry bones of his science. Pedantry and taxonomy overshadowed biologic research. To-day, largely through Charles Darwin's influence, we recognize the necessity of drawing our inspiration more directly from the vital manifestations of nature in our attempt to solve some of the many far-reaching problems which modern science presents. The fields of biology, morphology, physiology and psychology are more inviting than formerly. Nor is the lustre that glorifies the names of Stevenson, Watts, Faraday, Franklin, Morse, Henry, Siemens, and a host of yet living investigators dimmed because they made science useful. Goethe makes Wagner say :

“‘Ach wenn man so in sein Museum gebannt ist
Und sieht die Welt kaum einen Feiertag
Kaum durch ein Fernglas, nur von Weiten
Wie soll man sie durch Ueberredung leiten?’”

“If to-day, right here in Washington, there is great activity in the field of original research; if the nation is encouraging it in a manner we may well be proud of, the fact is due in no small degree to the efforts of those, many of them members of this Society, who have made practical ends a means, rather than to those who would make science more exclusive, and who are indifferent to practical ends or popular sympathy. Such, at least, is my apology for the nature of this paper.”

In response to an inquiry by Mr. White, Mr. RILEY said that the ox-eye daisy had been subjected to a thorough test under his supervision and the result had shown that it has none of the insecticide qualities of pyrethrum.

Mr. S. M. BURNETT made a communication entitled

WHY THE EYES OF ANIMALS SHINE IN THE DARK.*

[Abstract.]

Erroneous opinions have been held and expressed, not only by the non-scientific, but also by some persons holding high positions in the scientific world, in regard to the phenomena of luminosity of the eyes of animals, and particularly of cats, when they are in obscurity. It is not due, as has been commonly supposed, to phosphorescence, but to light reflected from the bottom of the eye, which light is diffused on account of the hypermetropic condition that is the rule in the lower animals.

In response to a question by Mr. White, Mr. BURNETT said that human eyes affected by hypermetropia do not yield similar results, partly because the human pupil is too small and partly because the bottom of the human eye is not so strongly reflecting a surface as that of most animals.

Mr. HARKNESS remarked that in determining the degree of divergence of rays emitted by an eye, from an image situated upon its retina, it is necessary to consider the magnitude of that image as well as its distance from the focal plane of the lens. The divergence of the rays coming from any *one* point of the image is determined by the interval which separates the retina from the focal plane of the lens, while the divergence of the rays coming from any *two* points of the image depends principally upon the size of the image itself. The total divergence is the sum of the divergences produced by these two causes, and the neglect of that due to the size of the image will probably account for the discrepancy between the observed angle of divergence and that computed by Dr. Burnett.

It also seems desirable to bear in mind the distinction between fluorescent and phosphorescent light; the former disappears as soon as the incident waves are cut off; the latter does not.

* This paper is published in full in the Pop. Sci. Monthly for April, 1884; Vol. XXIV, pp. 813-818.

Mr. A. B. JOHNSON made a communication on

SOME ECCENTRICITIES OF OCEAN CURRENTS.

[Abstract.]

The records of the Light House Board show that no less than eleven buoys of various patterns have gone adrift from the waters of the United States and been found at distant points where ocean currents have carried them. Many of these were not so fully identified that their precise original station could be indicated. In the case of a few, it has been determined that they were swept from the harbor and bay of New York by the outgoing ice in the winter of 1880-81 when nineteen buoys were carried to sea.

1. In the spring of 1871, a buoy was picked up on the west coast of Ireland.

2. In March, 1871, the Norwegian vessel Vance picked up a buoy in lat. $42^{\circ} 22'$, long. $26^{\circ} 38'$.

3. In February, 1881, a buoy went ashore on one of the cays near Turk's island. This was recognized as a New York buoy.

4. May 17, 1881, the steamer William Dickinson passed a whistling buoy in lat. $29^{\circ} 46'$, long. $77^{\circ} 38'$.

5. In March, 1881, a buoy of the largest size, likewise referred to New York, was found near Bermuda.

6. In February, 1882, a Sandy Hook buoy was found near Bermuda.

7. In February or March, 1882, a buoy was washed ashore at Pendeen Cove, Penzance Bay, England.

8. In the spring of 1882, the Swedish bark Abraham Lincoln picked up a buoy in lat. $32^{\circ} 30'$, long. $28^{\circ} 40'$.

9. October 22, 1883, a buoy was picked up on the east side of Teneriffe in lat. $28^{\circ} 21'$, long. $16^{\circ} 15'$.

10. October, 1883, a second buoy was picked up fifteen miles from the east coast of Teneriffe.

11. August 20, 1883, the British bark Jane Richardson picked up a buoy in lat. $24^{\circ} 11'$, long. $32^{\circ} 43'$.

All were identified as the property of the United States by letters cast in the plates.

The charted currents of the ocean readily explain the courses and account for the positions of many of these buoys, but others appear anomalous.

Mr. JENKINS cited an instance of a bell-buoy, carried away from the coast of the United States in 1850, which was seen and heard while adrift and finally stranded on the southwest coast of Ireland.

Mr. WELLING suggested that the phenomena might not be referable to ocean currents exclusively, but in part to wind currents. Mr. JOHNSON judged from the forms of the buoys that their movements would be controlled more by currents than by winds.

Mr. H. FARQUHAR and Mr. JENKINS were of opinion that the buoy picked up off Florida might have been carried there by the southward coast-current. Mr. DALL concurred, but thought it also possible that it had made the entire circuit of the Sargasso sea.

Mr. DALL, referring to Mr. WELLING's suggestion, said that wind and current worked together, and their effects could not be discriminated. The wind does not blow prevailingly in any direction without coercing currents to correspondence.

247TH MEETING.

FEBRUARY 16, 1884.

The President in the Chair.

Fifty-four members and guests present.

The Auditing Committee reported through its Chairman, Mr. C. A. WHITE, that it had examined the accounts of the Treasurer for 1883, finding the same properly vouched in respect to expenditures and receipts. On motion of Mr. DUTTON, the report was accepted.

The Chair announced the election to membership of Mr. HENRY WAYNE BLAIR and Mr. HERBERT GOUVERNEUR OGDEN.

Mr. F. W. CLARKE made a communication on

THE PERIODIC LAW OF CHEMICAL ELEMENTS.

After giving an account of the law as worked out by Newlands, Mendelejeff, and Lothar Meyer, he exhibited an enlarged copy of

Meyer's atomic volume curve, drawn with the latest values for both atomic weight and specific gravity. On the same sheet was also drawn a similar curve, illustrating the connection between atomic weight and melting point, and it was shown that in the latter the highest portions correspond to the lowest depressions in the atomic volume curve. The opinion was expressed, in view of the regularities exhibited by these curves, that the elements had originated by some method of evolution, and that a future transmutation of one element into another was not improbable.

In reply to a question by Mr. Farquhar, Mr. CLARKE said that search was being made for similar evidence of system in the spectra of the elements, but that the subject was rendered difficult by reason of the fact that not all the lines of the spectra fall within the range of visibility.

Mr. ANTISELL remarked that while the determination of the atomic weights of the elements was one of the most important labors which the modern chemist could be occupied with until a final constant numerical result should be arrived at, and until the other properties of matter which appear to have some definite relation with the atomic weight were rigidly investigated, there was necessity for continued effort to search into those hidden relations; but if by such investigation it was believed that we could arrive at any certainty about atoms, their form and structure, or about matter itself, we should be much disappointed. Situated as we are on a cold planet, we are precluded from ever arriving, by the study of matter from a standpoint merely terrestrial, at any ideas of the ultimate nature of atom or molecule, or whether there be really any such thing as "elements" or one form of matter wholly distinct from another. To arrive at a knowledge of matter, pure and simple, we must have ready means for dissociating all compound matter, and we have at our command at present no such methods or apparatus on this globe. Subjection to intense heat is required, and our most glowing furnaces and the arc light itself is insufficient for the purpose. It calls for the exhibition of such heat as is produced in the sun and its atmosphere to reduce our elements, as we term them, to the more simple condition of matter as it exists under solar temperature, and the present spectroscope and its future improvements by which such dissociation is to be studied. The

investigations of Huggins and Lockyer and other spectroscopists have revealed to us the presence of several of our so-called elements in the solar atmosphere; but constant observation has raised in the minds of these observers grave doubts whether the spectral lines of the elements, as obtained by observation of them in our atmosphere, are universally of such or whether only conditionally so, that is true only in our cold atmosphere. Doubts have arisen as to the spectral lines of elements being permanent characters of their essential nature, seeing that the spectral lines of an element, which at one time resemble those of copper, are found to be interchangeable and attached to a different element, as calcium, and that there are elements which possess the character of giving multiple spectra, as carbon, for example, which, under these solar temperatures, yields no less than three distinct and characteristic spectra.

In view of these apparently contradictory and confusing results, obtained by the examination of matter found in the solar atmosphere, which are so different from those obtained from matter in our own atmosphere, it behoves us to be very cautious in asserting the existence of any distinct elements so called, or whether there be only one matter under various cosmical conditions.

Other remarks were made by Messrs. DOOLITTLE and WHITE.

Mr. H. A. HAZEN made a communication on

THE SUN-GLOWS,

opposing the theory that they are due to dust, either cosmic or volcanic, and advocating a theory involving electrical action in connection with frost particles.*

A general discussion followed, in which Messrs. ELLIOTT, PAUL, ROBINSON, HALL, DUTTON, GILBERT, and E. FARQUHAR, participated.

Mr. ELLIOTT advocated the electrical origin of the glows, basing his argument on the simultaneousness of the phenomena throughout the planet, on the transparency of the glow as shown by observations on Lyra, and on the extraordinary abundance of sun spots for the past few weeks.

* This paper is published in full in the American Journal of Science for March, 1884; Vol. XXVII, pp. 201-212.

248TH MEETING.

MARCH 1, 1884.

The President in the Chair.

Forty-two members present.

The Chair announced that MESSRS. CHARLES OTIS BOUTELLE, GILBERT THOMPSON, WILLARD DRAKE JOHNSON, and EUGENE RICKSECKER had been elected to membership.

It was announced from the General Committee that standard time would hereafter be recognized in the opening and closing of the meetings.

Mr. R. D. MUSSEY read a paper entitled

THE APPLICATION OF PHYSICAL METHODS TO INTELLECTUAL
SCIENCE.

The aim of the paper was to show in how far those methods which had been successfully employed in the investigation of the phenomena of nature, and which were denominated the Physical Sciences, were applicable to those sciences, the subject-matter of which were mental operations and their results, and which, for distinction, might be named the Intellectual Sciences. Some illustrations were given of the application of these methods to the study of the law; and the paper concluded with the remark that its writer desired it to be regarded as a suggestion rather than a solution of the problem stated: "How far and in what way physical methods and physical sciences help thinkers to say *Therefore.*"

Remarks were made by Mr. ROBINSON.

Mr. I. C. RUSSELL made a communication on

DEPOSITS OF VOLCANIC DUST IN THE GREAT BASIN.

[Abstract.]

In contrast with the aridity of the Great Basin at the present time, geologists have shown that during the Quaternary it was crowded with lakes. In studying the sedimentary deposits of one of these fossil lakes, named Lahontan by Mr. King, I found strata

of white, unconsolidated, dust-like material, which is undistinguishable in general appearance from pure diatomaceous earth. Beds of this material, varying in thickness from a fraction of an inch to four or five feet, were observed at a number of localities in the sides of the cañons that have been carved in lacustrine strata of Lahontan age by the Humboldt, Truckee, Carson, and Walker rivers. Deposits identical with those of the Lahontan sections were observed at a number of localities among the mountains of Nevada and California at an elevation of several hundred feet above the former level of Lake Lahontan and at a distance of forty or fifty miles from its borders, thus showing that the deposits were both sub-aerial and sub-aqueous in their mode of accumulation. Further exploration revealed the fact that similar beds occur abundantly in Mono Lake Valley, where they may be seen to pass into well-characterized fragmental deposits of pumice and obsidian, thus suggesting that the finer material was also of volcanic origin. Experiment confirmed this hypothesis. Under the microscope the dust from a number of widely separated localities was found to consist almost wholly of angular flakes of transparent glass, with scarcely a trace of crystallized matter. When a sample of pumice from near Mono Lake was reduced to a fine powder, it was found to present the same physical and optical properties as the dust in question, with which it also agreed closely in chemical composition, as shown by analyses made by Dr. Chatard, of the Geological Survey.

The Mono Craters, from which this dust is supposed to have been erupted, form a group of cones about fifteen miles in length, situated in the southeastern part of the Mono Lake Valley, California. These extinct volcanoes are composed almost entirely of pumice and obsidian, in the condition both of coulées and lapilli, the latter constituting cones of great symmetry and beauty, the grandest of which have an elevation of nearly three thousand feet above Mono Lake. Some of these craters were in eruption during Quaternary times, while others were active after the ancient lakes and glaciers of the region had passed away. Many times during their history vast quantities of lapilli and dust were thrown out. As the volcanic dust interstratified with the sediments of Lake Lahontan is undistinguishable from that deposited in the Mono Basin, there is little room for doubting that they had a common origin. The

greatest distance from the Mono Craters at which the dust was observed, was in the Humboldt Cañon, about two hundred miles northward of the point of eruption.

At three localities in the Lahontan Basin the bones of extinct mammals were found closely associated with the deposits described above, thus furnishing the suggestion that the showers of fine volcanic dust were, at least to some extent, fatal to animal life.

Mr. ANTISELL said it was useless to look for the source of volcanic dust in existing volcanoes on the land. Pumice in the character of fine particles, as exhibited, is exclusively the product of submarine eruption. Other remarks were made by Mr. HARKNESS.

Mr. LESTER F. WARD read a paper entitled

SOME PHYSICAL AND ECONOMIC FEATURES OF THE UPPER MISSOURI SYSTEM,

in which he described the process by which the valleys of the Lower Yellowstone and Upper Missouri are formed, and pointed out the importance and the feasibility of utilizing the water of these rivers for purposes of irrigation.*

Mr. GILBERT said that Mr. Ward's description of the process by which the Missouri constructs its flood plain was verified by a nearly identical group of phenomena observed by himself on the lower course of the Colorado. Mr. ELLIOTT concurred with the speaker's view that the system of irrigation should be inaugurated by national action rather than local. Mr. RILEY was of opinion that the proposed plan of irrigation was entirely feasible, and said that the final solution of the grasshopper problem lay in the cultivation of the northern plains.

Mr. BURCHARD said that while the political advantage of a continuous belt of settlement uniting the Atlantic and Pacific States was undeniable, he questioned the advisability of increasing at present our agricultural production.

* This paper was subsequently separated into its two natural divisions, and the part relating to the "physical features" was published with illustrations in the "Popular Science Monthly" for September, 1884 (Vol. XXV, pp. 594-605), while that relating to the "economic features" appeared in "Science" for August 29, 1884 (Vol. IV, pp. 166-168).

249TH MEETING.

MARCH 15, 1884.

The President in the Chair.

Fifty members present.

The Chair announced the election to membership of Messrs. MARK BRICKELL KERR, SAMUEL HAYS KAUFMANN, JOSEPH SILAS DILLER, CHARLES HENRY WHITE, and WILLIAM LAWRENCE.

Mr. G. K. GILBERT made a communication on

THE DIVERSION OF WATER COURSES BY THE ROTATION OF THE EARTH.

[Abstract.]

It being admitted that the rivers of the northern hemisphere are, by the rotation of the earth, pressed against their right banks, and those of the southern hemisphere against their left banks, it remains to determine whether this pressure is quantitatively sufficient to appreciably modify the courses of rivers. Opinion is divided, and the results of observation have been largely negative. Those who regard the cause as insufficient to produce observable results have approached the subject from two points of view, which are illustrated by the discussions of Messrs. Bertrand and Buff. The former computes that a river flowing in N. lat. 45° with a velocity of three metres per second exerts a pressure on its right bank of $\frac{1}{33\frac{1}{3}}$ of its weight, and regards this pressure as too small for consideration. The latter points out that the deflecting force, by combining with gravitation, gives the stream's surface a slight inclination toward the left bank, thereby increasing the depth of water near the right bank, and consequently increasing the velocity of the current at the right. This increment of velocity has a certain erosive effect, but it is regarded as less than that assignable to wind waves on the same water surface, so that the prevailing winds have a more important influence than the rotation of the earth.

The object of the paper is to consider the theoretical effect from a new point of view. The form of cross-section of a stream flowing in a straight channel depends on the loading and unloading of detritus, and is essentially stable, its character being naturally

restored if accidentally or artificially modified. The distribution of velocities within this cross-section is symmetric, the swiftest threads of the current being in the center and the slowest adjacent to the banks. If now curvature be introduced in the course of the channel, centrifugal force is developed. This centrifugal force is measured by the square of the velocity, and is therefore much greater for the swift central threads of the current than for the slow lateral threads. The central threads, tending the more strongly toward the outer bank, displace the slower threads at that bank, and the symmetry of the distribution of velocities is thus destroyed. As pointed out by Thomson and others, this redistribution of velocities determines the erosion of the outer bank and the simultaneous deposition of detritus along the inner bank.

It has been shown by Ferrel that the deflecting power of the rotation of the earth upon a body moving on the surface is equivalent to the centrifugal force which would be developed if the body followed a circular course with radius of curvature (ρ) equal to $\frac{v}{2n \cos. \vartheta}$. In this expression v is the velocity of the body, n the angular velocity of the earth's rotation, and ϑ the polar distance of the locality.

The effect of rotation on a stream being equivalent to a centrifugal force is identical in kind with the effect of curvature of channel,* and this identity renders a quasi-quantitative comparison possible. Humphreys and Abbott found during flood a mean velocity of the Mississippi river at Columbus of 8.4 feet per second. The value of ρ corresponding to this velocity and the polar distance of the locality is about 20 miles. The actual bends of the channel in the same region, which depend for their features on the velocity and volume of the river at flood stage, have a radius of

* The author has since seen reason to modify this statement. The two effects are not strictly identical in kind, because the effect of rotation varies with the first power of the velocity, while the effect of curvature of channel varies with the second power. For this reason the selective power of curvature is, for the same deflective force, double the selective power of rotation. The introduction of this consideration would modify the numerical results derived from the Mississippi river, but would not impair the qualitative conclusion. A modified treatment of the subject will be found in the American Journal of Science for June, 1884; Vol. XXVII, pp. 427-432.

curvature of about $1\frac{1}{2}$ miles. Centrifugal force being a simple inverse function of radius of curvature, it follows that the deflective force by which the river is impelled toward its right bank by virtue of rotation is proportioned to the force by which it is impelled toward its outer bank on acute bends in the ratio of $1\frac{1}{2}$ to 20. That is to say, in this particular instance the rotational deflective force is $7\frac{1}{2}$ per cent. of the deflective force from curvature of channel.

The process of lateral corrasion is so complex that it is impossible to convert this result into terms of erosion and consequent deflection of stream channel, but a consideration of the manner in which the two deflective forces are combined sufficiently indicates that that due to rotation cannot be ignored. Wherever the stream bends toward the left the centrifugal force developed by the curvature is augmented by the rotational force; wherever the stream turns toward the right the centrifugal force is diminished by the amount of the rotational force; so that the tendency of the swiftest threads of current to approach the outer bank must be notably greater in one set of bends than in the other.

If this analysis of the subject is legitimate, the rotation of the earth ought surely to modify the courses of rivers to such extent that the modifications are observable phenomena. Exception should however be made of two important cases: first, rivers which are rapidly deepening their channels are by that fact held rigidly to their original courses, and are not deflected either by rotation or by any other cause; second, those parts of rivers whose function is deposition instead of erosion, should theoretically, under the influence of rotation, built their alluvial plains higher on the right hand side than on the left, and having established an inclination of the alluvial plain toward the left, should thereafter meander over the plain with equal facility in all directions. It is only in the middle courses of streams, where the work performed by the water is chiefly that of transportation, that the discovery of the effects of rotation should be expected.

Mr. WARD remarked that in the regions especially discussed the river courses are, in general, southerly, while the prevailing winds are westerly, so that the influence of the winds is opposed to whatever influence may be exerted by rotation. Mr. ABBE said that the tendency of driftwood toward certain river banks, cited by

von Baer, had been plausibly explained as due to prevailing winds, but such action is purely or chiefly superficial, and a less important factor in erosion than the behavior of the main current, which is comparatively little influenced by winds. Nevertheless, he was surprised that the rotational influence admitted of so large a quantitative expression.

Mr. DALL said that the northward-flowing rivers entering the Arctic ocean afforded at their mouths no evidence of the effect of rotation. The summer winds of Arctic regions are from the northeast and east, and these produce on the north coast of America a shore-current, which drifts the beach sand and shingle westward, and deflects the river-mouths in the same direction. All the rivers from the Mackenzie to Point Barrow illustrate this tendency. On the coast of Siberia the fresh water discharged by the large rivers has been observed to turn eastward, although the winds would tend to throw it the opposite way. The Arctic ocean is there deeper; and it is believed that its principal currents are controlled by the northeasterly set of the general currents of the North Atlantic.

Mr. ROBINSON spoke of the indirect influence of wind on river channels, through drifting sand. Mr. HAZEN pointed out that the influence of wind might be eliminated from the problem by studying the streams running east or west. Mr. BOUTELLE suggested that the course of the Mississippi did not indicate any result of rotational influence. Mr. E. FARQUHAR inquired whether the behavior of the Gulf Stream and other ocean currents was in accordance with the theory of rotational influence; and Mr. DALL responded that in the discussion of ocean currents this cause had lately dropped out of sight, the determination of courses being ascribed to the winds.

Mr. MUSSEY inquired whether the acuteness of continental masses toward the south admitted of an explanation based on the effect of terrestrial rotation; and Mr. DUTTON responded by saying that the mass of speculation in regard to the recurrence of certain forms of continental outline had never really accomplished more than the statement of the fact. The fact itself is an accident, dependent on the volume of the ocean and the general laws governing the formation of mountain chains. If the ocean were five hundred feet deeper, or five hundred feet shallower, the forms of

continents would be so far different that all the existing resemblances would disappear. The pointed extremities of some continents are merely expressions of the fact that mountain chains are more or less linear, and do not hold the same height throughout their whole extent.

Mr. G. E. CURTIS read a paper on

THE RELATIONS BETWEEN NORTHERS AND MAGNETIC DISTURBANCES AT HAVANA,

upon which remarks were made by Messrs. ABBE and COFFIN. [It will be published by the Army Signal Office as *Signal Service Note No. XIII.*]

Mr. GILBERT recurred to the subject of Mr. Russell's paper of the preceding meeting, and dissented from the view advanced by Mr. Antisell in regard to the origin of pumice. Mr. ANTISELL announced that he would discuss the matter more fully at some future meeting.

250TH MEETING.

MARCH 29, 1884.

Vice-President MALLERY in the Chair.

Forty-two members present.

The Chair announced the election to membership of Messrs. BASIL NORRIS and WILLIAM STEBBINS BARNARD.

Mr. J. S. BILLINGS spoke briefly on

COMPOSITE PHOTOGRAPHY APPLIED TO CRANIOLOGY,

exhibiting several composite photographs of skulls. Adult male skulls of the same race were selected for composition and were photographed in sets of from 7 to 18—front, side, and back views being separately taken. The composition was directly from the skulls and not from the photographs.

Incidental mention was made of the uncertainty of measurements of cranial capacity by means of shot. Not only did differ-

ent observers obtain widely different determinations from the same skull, but the same observer was not able to obtain closely approximate results in successive determinations.

Mr. G. BROWN GOODE made a communication on

FISHERIES EXHIBITIONS,

giving a list of all international exhibitions and describing especially those of Berlin (1880) and London (1883). The administrative systems of these two national exhibits were contrasted, and the social and economic results of the London exhibit were explained. [The substance of the paper will be published in the executive report on the London and Berlin exhibitions.]

Mr. M. H. DOOLITTLE began a communication on

MUSIC AND THE CHEMICAL ELEMENTS,

but was unable to complete it before the hour for adjournment. The remaining portion was postponed until the next meeting.

By unanimous consent adjournment was deferred for a few minutes in order to afford Mr. Antisell an opportunity to reply to a criticism made at the previous meeting in regard to his views on the origin of pumice.

251ST MEETING.

APRIL 12, 1884.

The President in the Chair.

Forty-one members and guests present.

Announcement was made of the election to membership of JAMES ARRAN MAHER, JOHN BELKNAP MARCOU, JOHN MILTON GREGORY, FRANCIS TIFFANY BOWLES, and WILLIAM EIMBECK.

Mr. M. H. DOOLITTLE made a communication on

MUSIC AND THE CHEMICAL ELEMENTS.

[Abstract.]

The mathematical theory of music requires the satisfaction of the equation $2^x = \left(\frac{3}{2}\right)^y$ *nearly*; in which, for equal temperament, x = the number of equal intervals in the octave, and y = the number of these intervals that correspond to a nearly perfect fifth; and, for untempered music, x = the number of approximately equal intervals in the octave, and y = the number corresponding to a perfect fifth.

The above equation gives

$$\frac{x}{y} = \frac{\log \frac{3}{2}}{\log 2} \text{ nearly} = \frac{176091}{301030} \text{ nearly};$$

and by the method of continued fractions we obtain the succession of approximations $\frac{3}{5}$, $\frac{7}{12}$, $\frac{24}{41}$, $\frac{31}{53}$, &c.

For scales appropriate to major thirds, but disregarding fifths, we may substitute $\frac{5}{4}$ for $\frac{3}{2}$ in the above equations, and obtain the approximations $\frac{1}{3}$, $\frac{9}{28}$, $\frac{19}{59}$, &c. For the chord having the vibration ratio 7 : 4 (called by Ellis the subminor seventh), we may obtain in like manner the approximations $\frac{4}{5}$, $\frac{21}{26}$, &c.

Since $\frac{1}{3} = \frac{4}{12}$, the first two series of approximate fractions include a common scale of twelve intervals to the octave, of which seven intervals give the fifth, and four give the major third. The first and the third of these series include a scale of five intervals to the octave, of which three constitute the major third, and four constitute the subminor seventh. There is some reason to believe that this is the scale of Japanese music, with the intervals $\frac{7}{6}$, $\frac{8}{7}$, $\frac{9}{8}$, $\frac{7}{6}$, $\frac{8}{7}$. Five-tone scales have universally prevailed in early music; but it is questionable whether the vibration ratios

have in any case involved the prime number seven. It would be interesting to know what scale best represents the songs of wild birds.

There is much reason to believe that simple mathematical principles underlie the phenomena of chemistry. It is not, *à priori*, absurd to suppose that matter in some way conforms to the properties of the primes 2, 3, and 5; in which case such derivative numbers might be expected prominently to appear as prominently occur in the science of music. The fraction $\frac{7}{12}$ might reasonably be expected.

If all the keys of a piano should be arranged seven consecutive keys in a line, the next seven in the next line, and so on, the columns give successions of fifths. It has been shown that if the chemical elements are arranged in the order of their atomic weights in lines of seven, the columns contain elements remarkably similar to each other. We seem to have a chemical scale remarkably analogous to the ordinary musical scale. If the piano keys be arranged in lines of twelve, the columns give octaves; but nothing is developed from a similar arrangement of the chemical elements, whence it may be inferred that the observed analogies are accidental, and have no true logical basis.

If the intervals of the chemical scale could be supposed to correspond to the seven intervals of the diatonic scale, the non-appearance of the twelve-fold relation would be accounted for; but, while the diatonic scale may have some claim to be called natural, it is not directly established by algebraic investigation of the relations of prime numbers. Until the discovery of chemical flats and sharps, there will be insufficient reason to regard the present chemical scale as diatonic.

Mr. LEFAVOUR illustrated the connection between tone and wave-length by means of a logarithmic spiral of base 2, the harmonic notes having *radii vectores* equal to multiples of the principal note.

Mr. ELLIOTT said he had learned from Mr. Poole that he had endeavored, in his euharmonic organ, to produce perfect chords in all keys without temperament.

Mr. KUMMELL remarked that in modern music the intervals of the major and minor thirds are the most important, because with-

out them there is no harmony. This is also apparent from the well-known rule in thorough-bass that a third with its fundamental note is to be treated as a complete chord. Now it happens, in dividing the octave by equal temperament into 12 equal parts, that a major third is nearly 4 and the minor third nearly 3 of these, and thus we obtain not only tolerable fifths, but also tolerable thirds, and the requirement of thirds for harmony is approximately fulfilled. They are still better fulfilled, of course, if we divide the octave into 41 or 53 parts, as Mr. Doolittle has shown. As to the seventh harmonic, Poole and Helmholtz rightly hold that it should be and is used by instruments which can temper. It is obviously the fourth element of the chord of the dominant G, B, D, F, the F being the seventh harmonic to the G two octaves below (nearly so in equal temperament and exactly in natural harmony), and this chord in modern music forms the opposing harmony to the tonic chord C, E, G, in major, and C, E flat, G, in minor. Instruments with fixed tones like the piano-forte have to use equal temperament, and thus virtually reject all natural harmony except the octave. This defect is generally inappreciable in very slow movements, but may be noticed by a very cultivated ear.

Other remarks were made by Messrs. CLARKE, MUSSEY, and HARKNESS.

Mr. H. FARQUHAR read a

REVIEW OF THE THEORETICAL DISCUSSION IN PROF. P. G. TAIT'S
"ENCYCLOPÆDIA BRITANNICA" ARTICLE ON MECHANICS.

[Abstract.]

This article covers seventy-four quarto pages in the last edition of the Encyclopædia, and gives a thorough mathematical treatment of the subject. No innovations calling for comment—unless an extended use of the "fluxional" notation for derivative functions be so regarded—appear until near the end, where two and a half pages are devoted to a disproof of the objective reality of force, and an advocacy of the disuse of the term in scientific writing. The character of the publication, and the eminence of the author in mathematics and physics, entitle his arguments to a careful examination.

In the first place, Prof. Tait infers that force can have no such reality as matter has, because it is to be reckoned positively and negatively—an action being opposed by reaction—while matter or mass is signless. This suggests two comments: (1), the author never questions the objective reality of space and time, of which realities it is an essential feature that to every direction or interval $A-B$, an equal direction or interval $B-A$, of opposite sign, corresponds; (2), the idea of a negative mass is not a self-contradictory one, and was once generally accepted. The element phlogiston was given up not because of any absurdity in ascribing levity to material substance, but because a form of matter with positive mass (oxygen), capable of explaining all the phenomena, had been actually separated and identified.

Prof. Tait's next criterion of objective reality is quantitative indestructibility, an attribute shared by time, space and matter, to which he adds energy. But the evidence of the indestructibility of energy is not of the same nature as that of the indestructibility of matter; for the latter in all its forms may be localized, and its density or elasticity measured; while the former, when stored up or "potential," cannot be shown to possess any of the properties of energy kinetic, or any existence in space, or any objective character whatever. Prof. Tait admits this difficulty virtually, and awaits for its solution the discovery of some evidence "as yet unexplained, or rather unimagined." All strains and other actions of a clock-weight on its supports are obviously precisely the same—or impalpably somewhat stronger—with the weight wound up an inch, as with it wound up a yard; and the existence of a greater "potential energy" in the latter case is to be found not in the clock, but in the mind, which requires this expression as a form in which to put its conviction that a certain greater amount of work can be obtained. Even though it be admitted that there are no other intelligible terms in which this conviction can be stated, it is clear that the indestructibility of energy is an ideal and subjective truth, and cannot, therefore, be relied on as evidence of a reality distinctively "objective."

A third point made by Prof. Tait against force is that its numerical expression is that of two ratios: "the space-rate of the transformation of energy" and "the time-rate of the generation of momentum." These results are obtained by simple division, in an

equation which expresses the fact that the work done by a body in falling the distance h is just that required to lift it through h against gravity. The fallacy involved in treating the numerical expression for force as force itself, has been well exposed by Mr. W. R. Browne (in a criticism of the same article, *L. E. D. Phil. Mag.* for November, 1883); and the assumption that ratios are necessarily non-existent is even more fallacious. Were it trustworthy, Prof. Tait's deductions would not be the only ones admissible. His equations would lead quite as conclusively to proofs of the non-objectivity of space and time (the former becoming the rate of work-units, the latter of motion-units, per unit of force), and so to a confirmation of the celebrated German view, that that which is universal and necessary in thought, belongs to the Subject; or they might even give mass in the form of a ratio, and hence suggest the non-objectivity of matter.

Not the least of the Professor's objections against force, it would appear, is that it is "sense-suggested." It is a mere truism to say that no other suggestor is possible, within the domain of science. It is, perhaps, better worth while to call attention to the indubitable fact that the real, if not the avowed, ground of the objection against "action at a distance," entertained by many physicists, is that such action is not directly suggested by sense-impressions. This is what they must mean by calling it "occult;" actions as our consciousness knows them, and as we can produce them, being generally characterized by proximity undistinguishable from actual contact. Further, if there is any reproach in this epithet, energy is quite as open to it as any function of energy can be. In fact, our senses directly report work, in the form of nerve-disturbance, and nothing else. Force is no more truly an inference from nerve-reports testifying of energy exerted, than is matter. In fact, the inference of the independent existence of matter is the less direct and more questionable of the two. The view advocated by Mr. Browne, following Boscovich, that matter is but "an assemblage of central forces, which vary with distance and not with time" or with direction, is one of great simplicity as well as suitability to analytic treatment, and one of which no disproof is possible.

The paper was discussed by Messrs. DOOLITTLE and ELLIOTT.

252D MEETING.

APRIL 26, 1884.

Mr. HARKNESS in the Chair.

Thirty-eight members and guests present.

Announcement was made of the election to membership of Messrs. DAVID PORTER HEAP and THOMAS MAYHEW WOODRUFF.

Mr. J. R. EASTMAN made a communication on

A NEW METEORITE.

[Abstract.]

A mass of meteoric iron weighing 113 pounds was accidentally discovered in the making of an excavation at Grand Rapids, Michigan, and was examined by the speaker in 1883. One face shows evidence of fracture, and the greater part of the remaining surface, of fusion. A very small sample submitted to Mr. F. W. Taylor for chemical examination had a specific gravity of 7.53 and a composition :

Iron	94.54
Nickel	3.81
Cobalt40
Insoluble (about)12

The stone is supposed by its holders to consist of gold and silver, and to be the buried treasure of a miser. This delusion has caused it to form the subject of a lawsuit.

The communication was discussed by Messrs. BATES and F. W. CLARKE.

Mr. W. H. DALL read a paper on

CERTAIN APPENDAGES OF THE MOLLUSCA.*

* Published in the American Naturalist, Vol. XVIII, pp. 776-778.

Mr. J. S. DILLER made a communication on

THE VOLCANIC SAND WHICH FELL AT UNALASHKA OCTOBER 20,
1883, AND SOME CONSIDERATIONS CONCERNING ITS
COMPOSITION.

[Abstract.]

The sand is composed chiefly of crystal fragments of feldspar, augite, hornblende, and magnetite, with a considerable proportion of microlitic groundmass and a very few splinters of volcanic glass. Its mineralogical composition is that of a hornblende andesite; but the chemical analysis by Mr. Chatard shows it to contain only 52.48 per cent. of silica,—which is much more basic than the average for that group. The character of the minerals, as well as the general composition of the sand, indicated so clearly that the crater from which it must have issued was erupting hornblende-andesite, that I was led to seek an explanation for its paucity in silica.

With this purpose in view, a number of volcanic sands and dusts from various parts of the world were examined and compared with the lavas to which they belong. First and most important among these is a sand from Shastina, a crater named by Captain Dutton, upon the northwestern flank of Mt. Shasta, in northern California. This sand, like that from Unalashka, is composed chiefly of crystal fragments of feldspar, augite, hornblende, and magnetite, with fragments of microlitic groundmass. Besides these, there are many pieces of hypersthene crystals and pumiceous glass. The sand contains 60.92 per cent. of silica, while the hornblende-andesite lava (rich in hypersthene) of Shastina, to which the sand belongs, contains 64.10 per cent. of silica.

From these and other examples it may be stated as generally true that volcanic sand is composed essentially of crystalline fragments, and contains less silica than the lava to which it belongs.

With volcanic dust, however, the case is different. Microscopical examination shows that it is composed chiefly of volcanic glass particles; and as far as chemical analyses have been made, they indicate that volcanic dust is more silicious than the lava to which it belongs.

That volcanic sand should be crystalline and basic, and the accompanying dust vitreous and acidic, as compared with the lava

to which they belong, is not merely determined by accidental circumstances, but has its inception in the magma before the eruption takes place. By the process of crystallization magmas are frequently divided into a crystalline solid portion, and an amorphous more or less fluent portion. Basic minerals are the first to crystallize, so that as the process advances the amorphous remnant of the magma becomes more and more silicious. The crystals are generally thoroughly intermingled with the amorphous magma, and in the latter are accumulated nearly all of the absorbed gases under great tension, so that when the pressure is relieved it may be blown to fine silicious dust, which may be carried by the wind many miles from its source, while the solid crystalline portion will contribute chiefly to the formation of sand, and be precipitated comparatively near the crater from which it issued.

In cases where no previous crystallization has taken place in the magma before it comes to violent eruption, the volcanic dust then formed will have about the same chemical composition as the lava to which it belongs. Mr. Russell has recently described an interesting case of this kind in the western part of the Great Basin. It appears to be generally true that if other conditions are favorable the difference in chemical composition between volcanic sand and dust is directly proportional to the amount of crystallization in the magma before its ejection.

The basic character of the Unalashka sand may be explained by supposing that the silicious portion of the magma was carried away in the form of dust.

The source of this sand is supposed by the collector, Mr. Applegate, the Signal Service Observer at Unalashka, to have been the new crater formed last autumn, near the Island of Bogosloff, about sixty miles away.

Mr. DUTTON spoke in commendation and amplification of Mr. Diller's contribution to geologic philosophy. Mr. DALL described the geographic relations of the volcano from which the Unalashkan dust was presumably derived, showing the improbability of the eruption having been directly observed. He spoke also of the distribution of the Aleutian volcanoes and the lithologic characters of their *ejectamenta*.

There ensued a general discussion of the nature and properties

of volcanic dust and of the theory which ascribes recent meteorologic phenomena to the dust ejected by Krakatoa. In this Messrs. DUTTON, PAUL, W. B. TAYLOR, DILLER, ROBINSON, and WARD participated. Mr. DUTTON pointed out that their process of formation tends to give volcanic dust particles a quasi-definite size, and probably does not produce a large amount of dust fine enough for indefinite suspension. The greatest distance to which volcanic dust has been definitely ascertained to travel is eight hundred miles.

Mr. PAUL argued from the violence of the Krakatoan explosion its competence to charge the atmosphere at very great altitudes, and considered the fineness of the dust a sufficient explanation of its indefinite suspension.

Mr. TAYLOR said the phenomenon to be accounted for was specially remarkable, first, for the unusual elevation of the finely-divided smoke or dust extending far above the highest cirrus clouds, or probably to twenty or thirty miles above the earth's surface (as shown by its twilight duration); secondly, for its wide diffusion (covering a large fraction of the terrestrial atmosphere); and thirdly, for the long continuance of its suspension in the air (extending over many months). Mr. Lockyer and Mr. Preece had suggested an electrical condition of the matter as favoring both its extraordinary diffusion and its equally extraordinary suspension. This hypothesis seemed to the speaker very plausible. Electricity is a phenomenon of volcanic eruption, and dust particles charged with electricity in the same sense with the earth would be repelled not only by one another, but by the earth. At thirty miles above the ground the air is not only very rare, but is practically anhydrous, and the discharge of electricity is impossible.

Mr. DILLER, in response to a question by Mr. Paul, said that the microscope reveals no limit to the fineness of Krakatoan dust. The higher the magnifying power applied, the greater the number of particles visible; and this relation extends to the limits afforded by the capacity of the instrument. To more powerful microscopes, yet finer particles would presumably be visible.

253D MEETING.

MAY 10, 1884.

The President in the Chair.

Fifty-four members and guests present.

Announcement was made of the election to membership of Messrs. JOHN MURDOCH, ROMYN HITCHCOCK, WILLIAM SMITH YEATES, GEORGE PERKINS MERRILL, and FREDERIC PERKINS DEWEY.

It was announced that a vacancy in the General Committee, occasioned by the resignation of Mr. J. J. KNOX, had been filled by the election of Mr. F. W. CLARKE.

By invitation, Mr. G. H. WILLIAMS, of Baltimore, Maryland, addressed the Society on

THE METHODS OF MODERN PETROGRAPHY,

first, defining the field of petrography, and second, discussing the methods of petrographic investigation. These methods are: (1), chemical; (2), mechanical; (3), optical; (4), thermal. The chemical methods are quantitative and qualitative. The mechanical methods include the separation of the constituent minerals of rocks by precipitation in heavy solutions and by the use of electro-magnets. The optical methods include the preparation of thin sections, their examination by transmitted ordinary light, and their examination by polarized light, for the determination of crystallographic system, pleochroism, and angles of extinction. The thermal methods are chiefly synthetic, consisting in the artificial production of mineral aggregates for the purpose of determining the processes of their natural production. By the regulation of temperatures in fusion and refrigeration all varieties and all structures of basic rocks are reproduced. Acidic rocks have not been thus reproduced, and it is believed that great pressure is a condition of their genesis.

Mr. DUTTON spoke of the bearing of modern petrographic investigations on some of the greater problems of geology.

There followed a symposium on the question

WHAT IS A GLACIER?

[Abstract.]

Mr. I. C. RUSSELL: In framing a definition of a glacier it is evident that we must include both alpine and continental types, and also take account of the secondary phenomena that are commonly present. With this preamble we may define a glacier as an ice-body, originating from the consolidation of snow in regions where the secular accumulation exceeds the loss by melting and evaporation, *i. e.*, above the snow-line, and flowing to regions where loss exceeds supply, *i. e.*, below the snow-line.

Accompanying these primary conditions, many secondary phenomena dependent upon environment, as crevasses, moraines, lamination, dirt-bands, glacier-tables, ice-pyramids, etc., may or may not be present.

Mr. S. F. EMMONS: The glacier is a river of ice, possessed, like the aqueous river, of movement and of plasticity. In virtue of the latter quality it adapts itself, though more slowly, to the form of the bed in which it flows. The névé field is the reservoir, from which it derives not only its supply of ice, but the impulse which gives it its first movement. The névé is formed by the snows which accumulate in relatively wide basins above the snow-line from year to year, living through the heat of summer. Its mass may be more or less compact, according as it is thicker or thinner, and it may have a certain movement, which will be greater or less, according to the greater or less inclination of the basin; but until it moves from its wide and shallow bed into a narrower and deeper one, and thus gives outward proof of the plasticity of the ice of which it is composed, it does not become a glacier. It may be crevassed. Often a long crevasse at its upper edge gives definite proof of its movement; and this movement may cause a cracking or crevassing in other points, resulting from the unevenness of its bed. It may or may not carry blocks of rock on its surface, but these would be rare, and never in the well-defined moraine ridges that are formed upon the glacier proper. Not, however, until its form had essentially changed to fit the bed in which it flows should it be considered to constitute a glacier proper.

Mr. W J MCGEE: The phenomena of glacier ice and névé ice appear to belong to a graduating series; and in consequence the two phases can only be arbitrarily discriminated. Any classification depending upon coincidence of the *loci* of apparent transition from the first phase to the second with *loci* of sudden constriction or abrupt acclivity in the valley is artificial and incompetent, since such coincidence is fortuitous; the classification depending upon the ability of the second phase to sustain bowlders upon its surface is superficial and incompetent (provided such ability be due to density of the ice), since the sub-surface density of the névé, being determined by its age and the pressure of the superincumbent mass, must, in some portions, equal the surface density of the glacier; and the classification depending upon rate of motion is equally incompetent, since motion is common to the entire ice-mass, and abruptly varies only where conditions of glacier-bed are suddenly variant. Arbitrary diagnostic characters may and should be, however, agreed upon by consense among glacialists. Perhaps the most satisfactory line of demarkation detectable is the *snow-line*, above which superficial débris is buried by precipitation, and below which it is exposed by ablation.

Mr. W. H. DALL: It is proper to discriminate masses of ice moving in a definite direction from the immense fields of ice which are practically stationary. The term "glacier" should be restricted to the former. A glacier is a mass of ice with definite lateral limits, with motion in a definite direction, and originating from the compacting of snow by pressure. Moraines are not diagnostic; and the definition should not include those masses of arctic ice which, by reason of their low temperature, are fixed in position.

Mr. T. C. CHAMBERLIN: Nomenclature is a matter of convenience. When subjects rise into familiar thought and frequent reference brevity of expression calls for specific names. But terms arising thus from a natural demand are not closely discriminative. Hard and fast lines of demarcation do not prevail in nature, but rather gradations of character. Were it otherwise names of sharply-defined application could be more freely used. The terms *névé* and *glacier* doubtless originated to satisfy the convenience of guides and travelers, and were without strict scientific application. In attempting to give them scientific definition, I think we shall fail of satisfaction by making them structural terms. The better distinction

is genetic. There is an area of growth and an area of waste to every glacier, and the distinct recognition of the two in quaternary glaciers is likely to rise to some importance. Superficially the area of growth coincides with the névé; the area of waste is that of the glacier proper. From every annual snow-fall there remains, at the time of maximum summer melting, a remnant that feeds the glacier. This is the névé for that year. The area may be greater or less in different seasons. The névé-field is accurately shown only on the day of maximum waste.

A contribution of much value, bearing upon the property of ice which permits glacier motion, has recently been made by Petterson, who has demonstrated, by refined experimentation, that ice, especially if impure, *shrinks* as it approaches the melting point and becomes plastic.

Mr. C. E. DUTTON desired to reiterate the remarks of Mr. Chamberlin to the effect that definitions can rarely or never be made rigorous. Glaciers, no doubt, vary in their characteristics like almost all other groups of phenomena. There is little difficulty in recognizing a glacier when all those features which characterize it are present, and when the conditions are of the ordinary nature. But exceptional cases arise. The lower parts are sometimes wanting and the névé alone remains, or the portion where the névé passes into the glacial stream may constitute the termination. In the latter case those who desire to be extremely precise in their phraseology might hesitate. It should seem best, whenever an occurrence is modified or defective, to use the term "glacier," with a qualification which shall express the particular circumstances.

Remarks were also made by Messrs. GILBERT and ELLIOTT.

254TH MEETING.

MAY 24, 1884.

The President in the Chair.

Twenty-six members and guests present.

It was announced from the General Committee that after the 255th meeting, June 7, the Society would take a vacation until October 11.

A request on behalf of the coming Electrical Exhibition at Philadelphia for instruments and books was communicated to the Society.

Mr. H. H. BATES read the following paper on

THE PHYSICAL BASIS OF PHENOMENA.

If there is anything entirely disheartening, it is to see the few landmarks of human achievement disappear before the shifting current of opinion, as headlands disappear under the ceaseless buffeting of the ocean. It is no doubt a matter of poignant regret to the cherisher of ardent theological convictions to see the bulwarks of faith slowly undermined by controversy. So, also, to him who has built his convictions on supposed demonstrable and irrefragable fact, to find nothing unassailable, not even the axioms and postulates conceded for ages as first principles, on which the fabric of science was reared, nor the sublime inductions of Galileo and Newton, on which the modern philosophy called natural—the only fruitful philosophy which man has produced—has been founded.

But the course of criticism shows that there are no first principles. Nothing is unquestionable. Even the mathematic joins hands with the metaphysic. I propose briefly to examine the fundamental grounds of mechanical philosophy, in view of the wide divergence of basal hypotheses in recent years, and especially on account of the importance conferred upon certain speculations by their admission into works of standard reference and authority.*

To do this aright it is necessary to go behind the mere sub-science of mechanics to the essence and substance of things, as did the eighteenth-century philosophers succeeding Newton. The observational data which have accumulated since that time by the splendid efforts of the molecular physicists enable us to review and recast, with some promise, the primary dogmas regarding the physical basis of phenomena. It is legitimate to frame hypotheses on subjects which are still unfathomed, but which confessedly do not belong to the domain of the unknowable. The distinguished example of the authors of the vortex atom would alone justify such a conclusion.

No entirely satisfactory hypothesis of the atom has yet been

* Encyclopædia Britannica, 9th Ed., Articles "Mechanics," "Measurement," etc.

found. I do not design to discuss the vortex atom here at length; for, although it is the most successful form of the Cartesian doctrine of vortical substance, it has not been perfected, and is generally regarded rather as an example of remarkable speculative and mathematical ingenuity, than as a discovery, corresponding with any facts of objective physics. It has insuperable difficulties, some of which have been pointed out by Clifford, and others by Clerk-Maxwell. Moreover, unparticled or continuous substance, the necessary postulate in this hypothesis, is something we not only have no experience of, but find full of inconsistencies with experience, when we gain a clear conception of what it implies. Such a conception fulfills Hegel's paradox that being and non-being are the same, since it forbids all mobility, all differentiation, as was perceived by the followers of Democritus. It simply affords an inviting basis for analytical discussion, on account of the elimination of the very conditions of objective existence which make the mathematical difficulty.

There are some postulates regarding substance which we may probably be permitted to assume at the outset. We may postulate its objectivity, and also its discontinuity. I have no space to review here the time-worn controversy between continuous and discontinuous substance. The arguments, which are exhaustive from the metaphysical side, are as old at least as Democritus and Anaxagoras. Suffice it to say that modern experiential philosophy has decided the battle experimentally in favor of the discontinuity of matter. The dispute only lingers in the region of the atom, where observation cannot penetrate or has not penetrated. The inability to conceive which attaches to all non-experiential affairs is encountered here, coupled with the too great facility of conceiving what is superficially observed, but will not bear analysis. Thus our first impressions of substance are in favor of its continuity. It is only after much reflection that we get the idea of necessary discontinuity, as bound up with the exhibition of existing phenomena. But the wonderful development of the Cartesian mathematics, in conjunction with the infinitesimal calculus, and its great facility in dealing with geometrical continuities, has tacitly revived the Cartesian idea regarding the nature of matter, as synonymous with space relations, which never reached intelligible development at the hands of its author, and wholly declined and disappeared after the

establishment of the Newtonian philosophy, and the discovery of the discrete character of substance.

In point of fact, experience would point to extreme porosity or discreteness as characteristic of substance, rather than to its opposite—perfect continuity. The infinite divisibility of space has nothing in the world to do with the question, though this is a confusion often fallen into. On the contrary, there is an infinite distinction between the infinitesimal discrete units of substance, occupying extension by their interactivity, and the passive infinitesimal resolvability of space continuity. This is the antipodean difference between the Epicurean and the Cartesian conceptions; the former admitting of the operations of force, the free exhibition of motion, the organization of material phenomena, which are phenomena of mobility; the latter constituting a plenum, with only ideal divisions, and phenomenally as necessarily barren a negation as space itself.

Substance is purely experiential. In its essence it is still incomprehensible, because experience has not yet reached down to those recesses. We know nothing of substance except by its manifestations. These manifestations are cognized by us through sense impressions, weighed, compared, adjusted, and analyzed in the mysterious alembic of the mind. First impressions have enormous predominance, and are intensified by heredity of cerebral predisposition and function.

We cognize substance only in bulk by direct perception, and these vast aggregations stand in thought for matter. A drop of water contains incomparably more molecules than the ocean contains drops; a grain of sand more particles than the earth contains grains; and it is this vast mesh of complicated forces that forms the integrated concept of matter to our apprehension. The child, before he can walk, encounters obstacles to movement, reaction to his every muscular effort, of equal measure to his own; and thus his first and profoundest convictions of objective existence are associated with resistance, opposition, repulsion. This impression of matter is so early that it remains with us as its most natural and obvious characteristic.

The idea of weight is also one of the earliest experiences. This idea would not be conceivable to a denizen of the deep sea, for our first ancestor who emerged from the water gained the experience at the cost of great struggle and enterprise. By the natural devel-

opment of muscle and function the child rears itself very early against the constant pull of our pedestal, triumphs over it with new-found energies, dances on tiptoe, and spurns the ground, but is soon content to draw the battle, to wander around a few weary years on equal terms, at length to call in the aid of a stick or crutch, and, finally, to resign the unequal contest, and sink, vanquished and satisfied, to rest in its bosom. Weight thus seemed a natural characteristic of matter until identified and generalized by Newton as a universal and especially a reciprocal property. This generalization transferred the property, in conception, from the naturally heavy body to a cause outside thereof, namely, the earth itself. Here the human mind relucted, for, unlike repulsion, attraction is not an observational fact. All forms of tension, stress, constraint—by whatever name called—are attended in the child's experience with an intermediary connection. The string is necessary to pull the cart, and the action of the magnet upon the iron particles is viewed with astonishment and awe. The sense of mystery does not proceed so far in his case as to contemplate the equally mysterious power which makes his string differ from a rope of sand. The most profound attention of the human mind has not yet fathomed this mystery.

Inertia or mass is a less obvious property, being in early observation and in common apprehension bound up with weight. It was not recognized in philosophy till Galileo's time, nor is it now by the common perception, except after training. A lady makes no scruple of asking to have a loaded car or train or vessel stopped at a given point on the instant, and reinvested with motion any number of times; and would-be inventors often contrive theoretical machines having numerous heavy reciprocating parts timed to velocities impossible of execution. With beings under other conditions it is wholly different. The sword-fish, *e. g.*, can have no conception of gravity, as he has no perception of it, but his apprehension of inertia is finely cultivated, through the muscular sense, in setting up and modifying the rapid movements in which his existence delights, as well as through his vivid realization of momentum, in the piercing of a whale or a vessel, by which his function is so powerfully exhibited. When once realized by human perception, however, inertia becomes identified with substance as its most primary characteristic.

The old scholastic property of impenetrability, also, is one of the superficial notions of experience, gained in the same way as that of repulsion. It seems to pertain to solids—the typical matter—with approximate accuracy, though calcined plaster of Paris and water, *e. g.*, will occupy a good share of each other's volume, and still form a highly porous solid. But a quart receiver full of hydrogen can have a quart of carbonic acid gas deftly introduced into it as into a void space; and so can a quart of water, at ordinary temperature and pressure, according to Gmelin, without increase of volume, although water is the type of material continuity. As to impenetrability in the molecule we can predicate nothing. The evolution of heat in chemical combinations indicates penetration of volume, with reorganization of the molecule in less space; and there is no reason, except a scholastic one, why two or more molecules, or even atoms, should not occupy the same place, as admitted by the highest authority—James Clerk-Maxwell.

Dimension is also a common notion, derived similarly from superficial and early experience. Solids alone have figure and assignable dimension, though liquids have fixed volume, and gases variable volume, in inverse ratio to constraint; but even solids are of varying and fluctuating dimensions, according to temperature, density, etc. Solidity and liquidity are, it is well known, but mere transitory conditions of material aggregation, for all matter is capable, by sufficient accession of molecular motion, of assuming that hyperbolic or expansive condition which we call gaseous, and in this state dimension and impenetrability are meaningless terms. Concerning dimension as a necessary attribute of the unit of mass, Clerk-Maxwell says (*Encyclopædia Britannica*, 9th Ed., Vol. 3, p. 37): "Many persons cannot get rid of the opinion that all matter is extended in length, breadth, and depth. This is a prejudice * * * arising from our experience of bodies consisting of immense multitudes of atoms." That there is no necessary relation between mass and volume as there is, *e. g.*, between mass and weight is shown to common experience by the notably different masses of a buck-shot and a pith-ball of the same dimensions, or of a cannon-ball and a child's hydrogen balloon. A pellet of iridium equivalent in mass to the pith-ball might be microscopic, and, by extreme supposition, infinitesimal. We are not forced, however, to deny to

the unit of mass finite magnitude, as this would be an experiential fact when ascertained.

The remaining so-called properties of matter are too obviously transitory, accidental, or derivative to require attention. Color, luminosity, opacity, transparency, sapidity, sonority, odor, texture, temperature, diathermancy, plasticity, hardness, brittleness, density, compressibility, conductivity, malleability, fusibility, solubility, and many others, are too clearly but conditions of aggregation, or else mere subjective states due to the way the complicated interactions of the primary qualities affect our senses. What are the primary qualities?

Here is where the modern method of philosophy flags, by the disappearance one by one of the experimental means of approach, as we eliminate the non-essentials. But though the substance is thus elusory, we cannot yet believe it to be illusory.

Chemical and molecular physics have already gone marvellously beyond the ordinary range of sense-perception, by strictly scientific methods. Not only is the discrete character of matter established, but many data of the differentia and organization of the molecule are discovered. Here is a vast field of science in itself. From the ideal molecule, or simple couple, up through the 70 actual organized molecules of our provisional elements, then the chemical molecules of their combinations in vast numbers, discovered and undiscovered, and, lastly, the enormously complex organic molecule in infinite variety, the domain transcends in area for classification that of biologic science. The simple molecule has not yet been discovered, much less the molecular constituent, the atom, or the *indivisible*. It is evident, however, that the properties of matter which are essential, not differential, must reside in the atom. The philosophers succeeding Newton treated the atom and the elementary molecule as one, from lack of sufficient chemical knowledge. We are on a higher plane of information, but their method is not necessarily vitiated by such lack of distinction.

We cannot, as before said, attribute *à priori* to the atom dimension or figure, though we postulate it to aid conception. As the atom is an absolute unit, there is incongruity in finally assigning to it such relative attributes, which are but matters of comparison and degree. There are properties, however, which are inseparable from an absolute essence. These are the properties by which the

essence is manifested to us. We know them provisionally as forces, in the Newtonian nomenclature. Had gaseous matter neither weight nor mass, we could not know of its existence. But these attributes are so constant in matter that we estimate its quantity in terms of them and have no other exact terms. Weight is the statical measure; mass the dynamical measure. And since weight and mass correspond for all substances, under all transformations, we judge that the correspondence identifies them alike with the essence. They cannot be the mere result of organization. They must belong to the ultimate atom.

At this point it would seem proper to attend to a question of definition. Definitions are essential to clearness, on the one hand, and a source of entanglement on the other, if we fall into the scholastic error of regarding a mere word as the coextensive symbol of an idea. Words are evolved during the imperfection of ideas, and language is still a most imperfect medium of expression. Hence, logic is not a science in the sense that mathematics is. I have used the term *force*. This is a word of much ambiguity of meaning. We may use it as a convenient mathematical expression for a mere rate of change of momentum, or we may go farther and *define* it, as that which changes a body's state of rest or of uniform motion in a straight line; either of which uses restricts it to only a portion of phenomena, and ignores the whole science of statics, dealing with forces in equilibrium and the phenomena of balanced stress. If we give it a more general signification, as that which changes or tends to change, or conserve, the state of motion of particles, or systems of such, either in quantity or direction, we embrace statics as well as kinematics, and get a measurably philosophical definition, if we bear in mind the proviso that we do not thereby postulate force as an entity apart from substance.

And since the compound variable space and time condition which we call motion (of which rest is but a phase) is the sensible resultant of the interaction of such discrete substance by constant rearrangement where readjustment is free, or the potential resultant where confined, we may admit that the observed tension and persistence, of whatever form, is that which effects the phenomenon (though masked by infinite variety and composition), and always across the discontinuity: not as separate entities, but as modes of manifestation of the interacting and pervasive substance itself and

its only manifestations. This we call *force*—the inscrutable agent of phenomena—and this I take to be the true Newtonian conception, as evinced by his maturest conclusions, expressed in query 31 appended to his *Optics*. (B. 3, 2d Ed., 1717.)

So far as weight goes, it was generalized by Newton to be a reciprocal force or stress, operative without limit on the law which inheres in radial space relations—the inverse square of the distance. The term operative means effective upon mass, namely, bridging the discontinuity. Gravity is the typical attractive force—*vis centripeta*. The relation is mutual by the law of action and reaction, and amounts to a universal tension among particles, controlling all matter everywhere into orderly movements and relations. This is what we postulate from observation, on the Newtonian plan of naming simply what we see. The notion, however, of action at a distance has encountered a metaphysical difficulty in many minds, from the preconception derived from ordinary experience that all affections or stresses must proceed through an intermediary connection, deemed continuous. Even Newton made concession to this prejudice in his oft-quoted letter to Bentley. That there is really no such continuity in any mode of connection known is demonstrable, and the notion itself that the fancied continuity of some rare effluvium could in any way aid the mechanics of the problem is chimerical. Clerk-Maxwell, moreover, has shown (*Nature*, Vol. 7, p. 324; *Encyclopædia Britannica*, Vol. 3, p. 63) that action at a distance is as necessarily implied in repulsion as in attraction, so that theories of repulsion do not aid conception. Ability or inability to conceive, furthermore, is not held even by the metaphysicians to be a criterion of objective truth. Such truths exist independent of the conceiving mind. The conceiving organ was evolved by experience, and conception develops with attention. The first law of motion was wholly inconceivable to the contemporaries of Galileo, and we find such instances even now. Thus, while plain truths are inconceivable until established, some utter absurdities have been deemed conceivable, as, for instance, vacuity of two dimensions. State of mind, then, is no measure of external truth.*

* In this connection, to illustrate how entirely a matter of opinion or prejudice or culture is this notion of conceivability, I quote from a letter

The second force or manifestation of the atom, inertia,—or mass,—unlike gravity, is not unlimited in range of action. As to this property matter is discrete. Mass has both a *locus* and a limit (being apparently dependent for dimension on multiplicity), and amounts to that incomprehensible property by which conservation of motion is maintained. Under gravity, quantity of motion varies according to relations of contiguity, but under inertia motion is conserved in direction and quantity, is modified in direction and quantity by interaction of mass with gravity, and is redistributed by interaction with repulsive force upon an indefinitely near approach of particles, upon conservative principles. Its discreteness gives matter its numerical and finite character, and admits of that interplay which constitutes phenomena.* Its reality and primary

written by Faraday to Dr. Playfair, in response to some inquiries of the latter about his atomic opinions:

* * * "I believe in matter and its atoms as freely as most people—at least, I think so. As to the little solid particles which are by some supposed to exist independent of the forces of matter, and which in different substances are imagined to have different amounts of these forces associated with or conferred upon them, * * * as I cannot form any idea of them apart from the forces, so I neither admit nor deny them. They do not afford me the least help in my endeavor to form an idea of a particle of matter. On the contrary, they greatly embarrass me; for, after taking an account of all the properties of matter, and allowing in my consideration for them, then these nuclei remain on the mind, and I cannot tell what to do with them. The notion of a solid nucleus without properties is a natural figure or stepping-stone to the mind at its first entrance on the consideration of natural phenomena; but when it has become instructed, the like notion of a solid nucleus apart from the repulsion, which gives our only notion of solidity, or the gravity, which gives our notion of weight, is to me too difficult for comprehension; and so the notion becomes to me hypothetical, and, what is more, a very clumsy hypothesis." (Playfair's works, Vol. 4, p. 84.)

Here we see a difficulty opposite to that usually encountered, for, while many people profess an infirmity of conception of the forces apart from the imaginary vehicle, Faraday finds the vehicle of no use as a carrier of the properties, but a positive impediment.

* This property has a multiplicity of names in the Newtonian nomenclature, according to the varying aspect of its function. Thus, in the aspect of persistence of mass in state of rest or of motion uniform in direction

character, when once apprehended, have proved more acceptable to the imagination than has the conception of central force, and under appulsion hypotheses (with the aid of that other readily accepted property, repulsion, and certain highly artificial hypothetical media), it has been made to do duty in providing so-called explanations of gravity, under its form of *vis viva*.

It has always seemed to me that the mode of approach adopted by Boscovich was the most philosophical and rigorous of any. He viewed matter for the purposes of mathematical treatment and for investigation of its essentials, as divested of accidental and fugitive properties; and as the analytical calculus had not then become so developed as to wholly fascinate the attention of geometers with abstract and ideal relations, he proceeded from prime physical data. He thus identified matter by those apparently general and characteristic properties recognized by Newton as the basis of mechanical philosophy in conjunction with the laws of motion. These properties are, as before said, gravity, inertia, and repulsion; or, as characterized by function, attraction, conservation, distribution. In this view matter consists of certain *loci* of central forces, mutually attractive by the first property according to a variable law in the duplicate inverse ratio of distance without limit, but restricted in manifestation as to the second property to the infinitesimal *locus*, thereby excluding unitary dimension. Contemplating matter under this aspect alone, a dilemma arose. For gravity waxing by the law of inverse squares of the distance up to the focus or origin involves the consideration of infinite force and apparently of infinite velocity in the limit, in the supposable case of rectilinear ap-

and quantity, *i. e.*, of resistance to change of state except in conformity with motion impressed, the property is called *vis insita*, which may be *vis insita activa* (momentum), or *vis insita passiva* (*vis inertiae* of mass.) In its aspect of acquirement of a new state of motion by interaction with other forces or masses, Newton called the new state thus superposed *vis impressa*; which, when the operation of acquirement has ceased, becomes again *vis insita*. In its aspect of persistence of mass towards uniform direction of motion under the constant deflective stress of vector central force, it is called *vis centrifuga*. And in its active form, conditioned by motion acquired, its capacity for furnishing motion from its store, either for impressing motion upon other mass, with consequent loss, or for supplying the potential fund under the drain of adverse central force, is called *vis viva* (energy.)

proach, at which point the equations become unexplainable. While Euler and La Place differ in their interpretations of the result, Boscovich sought to solve the apparent absurdity and inconceivability by the invention of his ingenious and complex system of alternate spheres of attraction and repulsion, or change of sign, on a very near approach, with infinite repulsion at the focus, which so loaded down and vitiated his hypothesis as to cause its rejection. This result was similar to that of Le Sage's speculations and those of the Ptolemaic astronomers, each thus working out the falsity of his respective scheme by superadded complications to readjust the theory to the progress of criticism or of observed fact.

By attributing finite magnitude to the atomic mass, however, Boscovich's difficulty disappears, as I had the honor of pointing out before this Society some ten years ago. This may be deemed a violent hypothesis in regard to a positive discrete simple absolute, as the atom is presumed to be, but parallel difficulties inhere in any other finite supposition, as, *e. g.*, a sphere of repulsion. Under my provisional assumption, the way out follows from an elementary proposition of Newton's, and it does not demand the gratuitous change of law or of continuity involved in the resort of Boscovich. The movement of a gravitating particle under stress of a center of gravitative force would be in all respects as the great 18th century mathematicians have demonstrated, until the margin of the particle reached the attracting center, where, if we suppose the attractive virtue to prevade the particle equally throughout a certain finite volume of mass, however minute, as gravity does the mass of a sphere, the maximum of attractive force would be attained; for, as Newton has shown, homogeneous spheres are controlled under gravity by a law of force varying directly as the mass and inversely as the squares of the distance between their center of mass and the attracting center, at all points *beyond* the surface, and directly as the distance between the said centers *within* the surface; so that, after passing the surface, the attractive center must proceed onwards to the gravitating center of mass (relatively), not by a force increasing to infinity, but by a force decreasing to zero, after passing the maximum, since it is balanced at the center by opposing stresses.*

* Let M be an exaggerated particle of mass and C a fixed center of gravitation external thereto. Newton proved that for all positions outside of a

A similar law of attraction prevails between two gravitative particles when both are similarly endowed with finite spherical volume and mass, excluding the idea of impenetrability (which is not a necessary attribute of mass), the Newtonian law being the product of the masses divided by the product of the distances $\left(\frac{Mm}{dd}\right)^*$ for outside positions.

gravitating homogeneous spherical mass the stress is precisely as though the whole mass thereof were concentrated at the center of said sphere, and varies directly as the mass and inversely as the square of the distance between the said center and the fixed center of gravitation; *i. e.*, $G \rightsquigarrow \frac{M}{d^2}$.

The maximum of gravitating force will here be at the surface, where d is minimum. He also proved that at all points within a homogeneous gravitating spherical concentric shell a gravitating particle is uniformly affected by balanced attractions. Hence, the stress for any smaller concentric sphere is $g \rightsquigarrow \frac{m}{r^2}$, m being the smaller spherical mass and r the reduced radius.

But since homogeneous and similar masses are as the volumes, and similar volumes are as the cubes of the homologous dimensions,

$$m \rightsquigarrow r^3. \therefore g \rightsquigarrow \frac{r^3}{r^3} \rightsquigarrow r.$$

The maximum of gravitating force is here also at the surface, where r is maximum.

* I write the formula this way because it is possible that we have been in error all along in regarding the denominator as a radial space relation, as implied when we write it $\frac{Mm}{d^2}$. In discussing the deflection of the particle under gravity, Newton, for mathematical simplicity, treated it as governed by a fixed attracting central force, and in testing various relations found that the radial space relation gave the true path of the planetary bodies under the immense preponderating influence of the sun's mass. The fixed center of attraction is, however, a mathematical, not a physical, condition, and can only be realized by making $M = \infty$, when we get a form of expression which does not give a law of force. I think it possible that the relation is a mere reciprocal distance relation, since the stress is mutual for the masses and each is equally distant from the other. The inverse form of the relation, moreover, may arise from our subjective way of viewing distance, as measured outwardly from ourselves, since we have to go from here to yonder. It is possible to look upon the relation as really one of contiguity or nearness, and by placing $\frac{1}{d} = c$ we get the cosmical law of gravitation as $Mcmc$. This, however, would not be a useful formula, since we are not accustomed to expressions which attain maximum value with minimum magnitude.

For positions of encroachment the law is more complicated, and forms an interesting field for mathematical discussion. Where three or more atoms are superimposed the problem becomes too complex for discussion. It is noted, however, that such compound atom, if quiescent from extreme abstraction of heat, would be in a condition of elastic equilibrium, ready to respond like a bell to the slightest disturbances. In all these cases of interpenetration the law of stress would be finite and diminishing, and if the line of encounter should chance to be a right line through their centers (a condition infinitely rare in actual occurrence), they would continue on or repeat according to energy of approach; while upon any other lines of approach orbital relations would supervene, in modified curves of the second order, either hyperbolic, parabolic, or elliptic, according to velocity, and with or without partial penetration, according to nearness of approach.

Boscovich, however, did not adopt this solution, although within his reach. The problem of the action of a gravitative particle as controlled by an attractive center has several aspects of statement, which may be confined to four, for practical investigation. In the first, where the particle is assumed to be without mass, no discussion is possible, for the two suppositious points instantly assume the same locality, and end the relation. In the second, where the particle is endowed with inertia but not magnitude (and the attractive *locus* fixed by postulate), the element of motion enters, but infinite terms appear in the equations in the limit, forbidding interpretation. Thirdly, when we attribute finite magnitude to the gravitative particle for gravitative pervasion, as in actual spherical masses, no infinite terms appear, and we get an intelligible mathematical discussion, with planetary results for exterior positions, and pendulum results for interior positions, as I have heretofore demonstrated; and lastly, when both the gravitating *loci* are invested with similar attributes of volume and of mass (excluding extraneous notions of ordinary collision and repulsion from the problem), the results are similar to those of the third hypothesis. I do not introduce any of the mathematical discussions here, as the dynamics of the particle have been fully treated by mathematicians, though I am not aware that any of them have pursued it to physical conclusions.

It is not likely, however, that there is any matter so simple as this modified Boscovichian atom; that is, which can be identified.

All the matter we know of is already compounded and highly organized. The ideal simple molecule would consist of a single pair of such atoms, bound to each other in orbital relations of more or less eccentricity, including the extreme rectilineal form of simple pendulum-like oscillation through one another's centers; and it is a most significant fact that spectroscopic observation of all incandescent matter shows atomic matter to be in this state of transverse or orbital oscillation with inconceivable but synchronous rapidity without regard to range, according to the pendulum law of stress varying directly as the range of oscillation, discovered by Galileo. Any theory of the simple molecule must take cognizance of this observed fact. Another cognate fact is that the law of elastic cohesion manifest in all elastic tensile action—"ut tensio sic vis"—is a parallel law of stress, as illustrated in the spring balance weighing scale, the spring dynamometer, the isochronous spring governor, etc., and is a function of molecular and ultimately of atomic force and distance.

If the atom is really thus characterized, the repulsion or resistant property experienced in matter becomes worthy of investigation, since it drops out as the primitive affection or disaffection postulated by Boscovich. I have shown that it is not necessary to oscillatory motion. We must admit that the notion of rebound or recoil, in the ordinary sense, between simple atoms possesses difficulties. No less does the idea of plasticity or destruction of momenta. Consider what is involved in the hypothesis of two absolutely hard, rigid, unparticled, homogeneous spherical bodies of any magnitude at all, if possessed of mass, meeting on a rectilineal central line of motion. We know what would happen in case of ordinary spherical elastic masses or aggregations of molecules. Such merely undergo, first, apparent contact, then compression, deformation, strain, accumulation of stress, retardation of velocity, momentary arrest, acceleration on new lines of departure, relief of strain, recovery of form, redistribution of momenta, and final resumption of uniform velocities, with relative motion inverted and aggregate energy of motion unimpaired, unless permanent distortion and heat have absorbed a portion. All this complex action is involved in the term elasticity. None of this could take place with simple undifferentiated particles, unless we invent for them a mystic atmosphere or cushion of repulsive capacity surrounding the *locus*, as Boscovich was forced to do

by logical conclusions. Without this, contact would be absolute and instantaneous at first impact. As hardness involves impenetrability, absolute destruction of motion on the instant must ensue; that is, motion and no motion at consecutive instants of time; a discontinuity unknown to experience, and known to be inconsistent with the nature of motion and of time. This argument from breach of continuity is due to Leibnitz. Conversion into heat motion is excluded, heat being a mode of motion of the entire atom. Moreover, the destroyed motion has to be recreated instantaneously in new directions, for destruction of energy cannot be postulated. This geometrically angular motion is also unknown to experience, for all deflected bodies pass by continuity from motion in one direction into a new direction, and, so far as we can see, must do so. These discontinuities in translatory relations are therefore put aside, not because they are inconceivable, but as illogical and non-experiential. Simple repulsion by contact without occult intervention is a false suggestion, and we find that we get the pseudo-conception from our false observation of what occurs in the collision of sensible masses, somewhat as we make a false observation and generalization about material continuity, or about tension, from a superficial perception of matter; thus creating concepts from supposed experience which can have no true objective counterparts. I shall recur later to a possible derivative basis for repulsion.

It is remarkable that to Newton we owe the final establishment of the majority of those fundamental and universal truths which by simplicity and generality seem to touch the absolute; that is, more than to any and all other philosophers combined. Thus, of the six ultimate generalizations, four were formulated and placed on an impregnable basis by Newton: the three laws of motion and the law of gravitation. All of these were inconceivable when first promulgated, were hotly controverted on the metaphysical plan, were finally established experientially, and are now generally accepted as axiomatic by the modern mind, except for sporadic reversions which appear now and then to deny their actuality and reassert their inconceivability. The remaining two universal inductions are the collective group of axioms formulating the relations of extension—the only enduring remnant of the Greek philosophy—and the law of the conservation and unity of energy, unperceived in Newton's time in its generality, though taught as a dogma by the

Cartesians. These also are still held to be inconceivable by certain disciples of metaphysical methods and axiomatic by others. Such mental attitudes should lead us to believe that simplicity has been arrived at in all these cases and the boundaries of explainable knowledge reached, where inconceivability necessarily begins.

It has been said that paradox is born either of confusion of thought, or of knowledge, or confusion of statement arising out of the imperfection or subtlety of the verbal vehicle of thought. Thus, as Clerk-Maxwell points out, the celebrated arguments of Zeno of Elea, establishing the inconceivability of motion, represented in the paradox of Achilles and the tortoise, were unanswerable and unanswered until Aristotle showed, some half century later, that duration is continuous and incommensurable by numerical methods in the same sense that extension is. The old logical dilemma of the irresistible force encountering the immovable body was insoluble to the Greek mind, both from lack of physical knowledge and lack of verbal clearness of statement. The acute sophist knew not the nature of force, the constitution of bodies, the conservation, transformation, and dissipation of energy, and consequently knew not the refuge and escape from the dilemma contained in the perception of the conversion of molar energy into heat energy, expansion, and dissipation. The resources of verbal subtlety and of inner consciousness failed, as they always do. Something of the same difficulty remains in modern problems, where observation and strict verification are, from the nature of the problem, inapplicable, or where the confusion arises from the still-existing imperfection of language, or, again, where generalizations, both clearly made out and clearly formulated, have not passed into the instinctive popular apprehension. The modern dilemma of the inconceivability of infinite or finite space is, I take it, due to the metaphysical form of the statement. For when we reflect that the ideas of immensity and of infinitesimal resolvability are but abstract generalizations of the merely relative continuities, extension, distance, and dimension, which are in their turn but abstractions of the sense-perceptions, form, translation, and volume, the statement becomes intelligible and entirely conceivable, and I think, though with deference, saves geometry; that is, the universality of that system of inductive postulates regarding the relations of extension and inferences therefrom, known as geometry to the Greek philosophy,

but now named Euclidean by certain analysts whose so-called geometry is symbolic. Geometry is therefore able to deal with all aspects of extension, without regard to limit, in spite of some infirmity in the Greek method, for scale cannot affect the generality of extension relations, and abstract unconditioned space is not an entity but a mere negation, concerning which relative propositions are unintelligible. A false philosophy regarding space is at the root of all modern heresies concerning geometry and mensuration, founded in misapprehension of the Euclidean inductions or generalizations.*

The first law of motion is but the formulated recognition of inertia, which is only manifest in conjunction with motion, actively or passively. It was known to Galileo, and laid down by Descartes as a law in his *Principia*. It is a cosmical truth, bound up with the absolute nature of mass and the true relations of extension, which correlates the whole fabric of dynamical knowledge with rectilinear geometry, curvilinear motion being demonstrably not a simple state of conservation under inertia, but a resultant of multiple forces. The simple action of mass under the first law of motion, if undisturbed, furnishes the absolute unreturning rectilinear path which overthrows all speculation about possible ideal spaces. I here recall a book written by a learned American of Philadelphia—learned, that is, according to the mediaeval standard of the colleges—and published only during the past year, en-

* There are two opposite though similar forms of error in the assumptions regarding space. The first is that space is a specific or perhaps generic entity or objectivity *per se*, possessed of conditions and attributes, like substance, such as dimension (in several), differentia in locality, figure, as curvature, etc. (hence necessarily finite), and only uncognizable by us simply for lack of perceptive faculties to correspond. This is the fundamental error, as it seems to me, of Riemann and Lobatschewsky. The second is that of the older Cartesians, who viewed space as but the mere attribute or synonym of substance, and inconceivable apart from it, so that bodies separated by void space would be absolutely in contact without regard to distance. Both of these speculations are purely metaphysical, and non-experiential, the latter resulting from the old scholastic method of syllogistic deduction from primary postulates of verbal definition, and the former from similar inferences from the forms of the analytical logic of symbols, the use of which is still in the scholastic stage. Like Zeno's paradox, these merely intellectual difficulties should be removable by intellectual processes.

titled "An Examination of the Philosophy of the Unknowable, as expounded by Herbert Spencer," wherein he naively lays down the first law of motion as unintelligible except by appulsion. Motion, he says, in the absence of propulsion is inconceivable. I have no space here to reproduce the explanation evolved out of consciousness by this reasoner to account for the action of a ball struck by a bat after leaving the bat. It resembles in ingenuity and gratuity some of the inventions devised to explain gravity. The notable thing about it is that here, at this date, is a mind of good caliber, informed in the higher schools of learning, which is still of the mental period of Aristotle; a mind which has evidently never apprehended inertia, nor heard of the great contributions to knowledge made by Galileo and Newton, by which philosophy was entirely revolutionized.

The second law of motion, regarding the independence and co-existence of motions, on which we occasionally see comments in the metaphysical vein controverting its possibility, has long been established experientially. Its early experimental proof is attributed to Galileo. Yet I recall a pamphlet written and published only during the last year by a learned German at Leipzig, the theme of which was that "the sun changes its position in space, therefore it cannot be regarded as being in a condition of rest." This, he concludes, overthrows the entire fabric of Copernicus, because the planetary orbits in such case cannot be closed.

The third law of motion is but formulated reciprocal stress, in its modes of compulsion and repulsion, through which mass acts on mass to redistribute motion by what appears to be necessary law. The stress is necessarily reciprocal, since there is no *point d'appui*, or fixed fulcrum, in the universe.

We have thus been brought to the boundary of the absolute, where all is inconceivable until found out, and where the simple data are unexplainable. All examination seems to continue to point to mass and weight as the ineffable simple insignia of substance standing on this limit. We must accept something as elementary fact; what shall we find more elementary? Repulsion is still debatable; for, if we make an issue between repulsion and compulsion as contradictory primary attributes of the same essence, or untenable in conjunction for artificiality, by far the greater difficulties attach to the former, some of which I have already alluded

to. The profound mind of Boscovich was forced to accept repulsion as a primal quality, but in deference to the physical hypotheses of his time, he overloaded it with complication. This has been weighed in the balance of philosophical judgment and found wanting. I have intimated that there are possible grounds for surmising that it may not be a simple property of the atom, but a mere mode of distribution of energy dependent on composition of motion of atomic mass after change of sign, *i. e.*, a mode of *vis impressa* after exhaustion of the space relation; for, mathematically, the hyperbolic lines of approach and recession of two atoms under the high proper motion characteristic of the atom, and on lines not directly central, would be similar, at sensible distances, in their asymptotes (which would be the practical paths), whether the deflection were due to attractive or repulsive stress, though acceleration and retardation at the passage of the infinitesimal focus would be inverted.*

* It is well known that for any finite system of two particles controlled by gravity the lines of movement are closed curves of the second order, of more or less eccentricity, about the common center of gravity, which, for equal masses, would be midway. For an infinite system under the same conditions the orbits are parabolic, but for a system to which the particles enter by extraneous motion the lines of movement are hyperbolic, thus :



FIG. 1.

Now, under repulsion, the lines of motion are seen to be similar, A B, D E, Fig. 2, being asymptotes of the hyperbolas representing the two paths at sensible distances :

It therefore seems to me immaterial to result which of the two modes of passing the infinitesimal focus is the true one. In either case the distance at passage is infinitesimal, and the force may be as near infinity as the facts require it to be assigned. The normal or rectilinear encounter is here excluded from supposition. In that case, under repulsive stress, as postulated by Boscovich, the recoil would be rectilinear and opposite, without breach of continuity. Under attractive stress, with finite volume of the atomic mass, penetration would ensue as before shown; but without dimension or repulsion we have an insoluble condition, although the occurrence would be infinitely rare. Only one pair of elements is here considered. In all real encounters, whether of masses or molecules, the effect is a vast resultant, but should not be different in kind from that of the elements; that is, hyperbolic or expansive between alien systems under motion. As the number of elements ordinarily engaged could not be represented by any numerical places of arabic notation for which we have names, we see the hopelessness of stating the problem mathematically. I therefore do not presume to

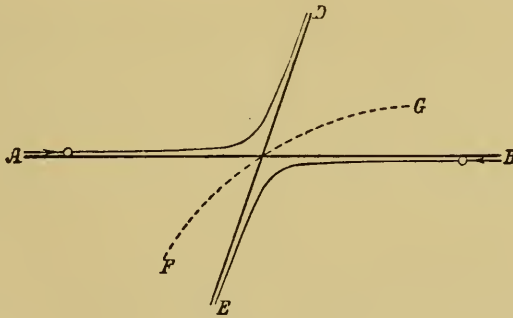


FIG. 2.

This encounter represents only one element of the molecule, of which myriads are engaged at every recoil of molecules, not to speak of solids. It is thus seen that the mesh constituting the molecule is ordinarily impenetrable to other meshes. If the curve F G be allowed to represent the outline of the molecule, the limb of the solid to which it belongs, say a buck-shot, will be represented by the Sierra Nevada, or the Andes, and its diameter would be measurably represented by that of the earth, as approximately shown by Sir Wm. Thompson in the case of a drop of water.

offer this as an explanation of repulsion, and I confess that to me repulsion is in its mechanism incomprehensible. We know the result experimentally, and that is resistance to penetration, and reaction at insensible distances on an undefined boundary which begins prior to contact and increases in a high exponential ratio as approximation progresses. The contact boundary of any solid—even the smoothest and hardest—resembles the astronomical limb of Jupiter in geometrical indefiniteness. The contact transmitter in the telephone, the whole range of whose phenomena occurs under pressure and so-called contact of varying degrees, illustrates how relative a thing is contact. Under high velocities the distinction between solids, liquids, and even æriform bodies entirely disappears in respect to repulsive reaction, though this is the most sensible distinction between them under low velocities.

We may, therefore, adopt the conclusion that if any of the apparently simple properties of the atom are to be thrown out as derivative and secondary, presumption points to repulsion as the complex one. We could possibly account for phenomena in a universe bound together by purely tensile stress, but most of the sensible phenomena of solids—cohesion, affinity, tenacity, etc., including nearly all of statics—remain hopelessly unattackable problems under a hypothesis of pure repulsion, like that of Le Sage, or Preston. It is to be noted that the kinetists who freely postulate repulsion and appulsion, without analysis, as a primordial fact, but reluctant against compulsion or tension, are forced to the invention of the most complicated and gratuitous mechanism and media to explain the phenomenon of gravity, and then without attainment of result. Le Sage's atom is too complicated, even without his suppositious or extra-mundane operative machinery; and the vortex atom is but a mere analytical expression for an unproducibile condition in a figmentary mathematical plenum.

The thesis that conservation is the characteristic by which we identify objective existence will not bear the test of examination. It is only in the most recent times that such a quality has been known or imagined, and its establishment, both as to matter and energy, is justly viewed as the triumph of modern philosophy. The evocation of matter from nothing and its relegation to nothing, even by the finite will of a wizard, was ever a common and universal notion, which did not at all impair the belief in its present reality

and substantiality. We have only to go to Apuleius for this, and it is doubtful if even now the notion of the indestructibility of matter is anything but a scientific conviction, for do we not see numbers of our contemporary fellow-citizens meeting together frequently in our midst to witness feats of materialization out of nonentity by powers akin to those of the sorcerer, without an idea of incongruity? Nor has the essentially modern doctrine of the conservation of energy anything to do with the belief in its reality. Few people apprehend it even now. No philosopher understood it a hundred years ago. Its verity rests on a sufficiently general inductive basis, from the refined and exhaustive experiments of Joule, and the theoretical conclusions of Mayer and Clausius, and it is accepted in the same sense that the law of gravitation is accepted. But the duality of matter and energy to the exclusion of force is a verbal shift, the assumption of which removes no difficulty. Matter, the object, remains unexplained; and energy, the phenomenon, becomes segregated and unintelligible. Energy, in fact, is but mass in phenomenal manifestation, being a product of triple factors, two of which—translation and speed—are not things, but variable and evanescent conditions, and, taken together, constitute motion. Mass is the absolute or persistent factor, but the evanescent character of the variable component—motion—would render the entire phenomenon—energy—apparitional, were it not for the distance relation involved in motion, which, under the same inscrutable agency which modifies and saps the motion renders it potential upon change of sign. This agency, the dynamical source of the manifestation, being central to mass and likewise persistent and constant, renders the positive and negative potentialities of movement constantly equal, and the actual and potential energies consequently complementary, from which energy gets its character of conservation.

Energy cannot therefore be that other reality of existence (besides matter), since force is clearly the one reality at the bottom of the manifestation of both, to whose persistence and resistance to change, except through transformation, the conservation of both is due. This one reality is, in its triple aspect of causation, (1) attraction—the source and modifier of motion; (2) inertia—the conserver of motion; and (3) repulsion—the distributor of motion; or, more correctly, in its aspect of quality: (1) *vis centripeta*—the power of mutual control across distance; (2) *vis insita*—the power

of persistence in state of motion impressed; and (3) the distributive power of imparting and acquiring motion by transfer, at minimum distance, which may be called *vis partitiva*, the result of which is Newton's *vis impressa*. Matter thus comes into the world of phenomena by the simple presence of other matter, permitting the exhibition of these comparisons and interactions, involving the conditions of contiguity, distance, position, translation, direction, succession or sequence, and time-rate for the continuous increments, decrements, successions, and uniformities, all bound up in the compound variable continuity—motion. With motion and distance comes the dependent phenomenon—energy—active and potential, which should be a constant, the numerical units of mass being constant throughout immensity, provided the sum of the motions, potential and actual, be constant. This the dynamical theory deduces from the fact of central force (for without force potential motion is ridiculous), and the thesis of the conservation of energy is a dynamical truth or nothing. It is therefore all the more extraordinary that certain kinetists, who reluct against central force, should have selected, out of all the manifestations of the universe, the variable and conditional product—energy—to be the one reality or objectivity, aside from the undefined hypostasis—matter—as a primordial simple fact at the basis of phenomena. It has been mathematically demonstrated by Mr. Walter R. Browne (London Edinburgh and Dublin Philosophical Magazine, January, 1883, p. 35) that the conservation of energy is true if the material system is a system of central forces, and is not true if the system is anything but a system of central forces. In fact, the ordinary theoretical proof of the principle of the conservation of energy assumes the forces acting to be central forces, *i. e.*, reciprocal stresses between units of mass, as recognized by Clausius in his Mechanical Theory of Heat. Moreover, the entire body of kinetists, who have aimed to supersede gravity or central force, have freely assumed an extramundane supply of motion and energy without regard to conservation, and it is notable that every hypothesis for this purpose yet broached involves the constant expenditure of work without recovery, and postulates the accession of energy in infinite influx from some occult source, of which only a small portion relatively is available or manifest in observable phenomena, thus violating all three of the canons of philosophical ascription—true cause, sufficient

cause, and least cause. Such is the power of conception of the unknown in endeavor to explain the inconceivable known.

If the dynamic hypothesis of perpetual transformation of energy could be established as a universal induction, with as much generality, *e. g.*, as the statement of the law of gravitation, it would establish and confirm that law, by Mr. Browne's demonstration, as something more than a law, to wit, the necessary constitution of matter as a system of central forces and nothing more, substantially as conceived by Newton and elaborated by Boscovich. At present it is but a dynamic induction, but the theory of gravity is no more. Our appliances are material, and we can deal with molar forces, but only indirectly and inferentially with those which are atomic. Conservation is indubitably true of energy in the mechanical and molar sense, under the laws of dynamics and the persistence of force. It is, also, experimentally true, so far as we can trace it, of those less understood forms of energy which are molecular or atomic, the establishment of which was the great glory of Benjamin Thompson, Clausius, and Joule as to heat, and of a multitude of observers as to electrical energy. We infer it as a general truth of these energies (formerly known as imponderables, since they are not manifestations of matter in the concrete), from the fact of their convertibility with other modes of energy which are undoubtedly dynamical, and also from the intimate connection of electrical energy with one of the specific exhibitions of central atomic force—magnetism. Such clues create a warrantable presumption that the phenomena in question will all ultimately be classified among the modes of atomic mass and motion, inductively as well as hypothetically. Possibly in the investigation of these evanescent modes of energy the missing simple particle may come to light. Provisionally, we are entitled to rank them among the mechanical modes of energy, as products of the same material forces, assuming, until the contrary is proved, that some form of matter is concerned in manifestations so correlated by conservation with undoubted material activities.

In including the imponderables within the general dynamical law of conservation, we have to take account of the phenomenon of dissipation, first pointed out by Sir William Thompson. It is true that heat (as well as electrical energy) is strictly correlated with and interconvertible with energy of mass motion, as before

stated, but in its final form energy seems to take leave of matter altogether, so far as our perceptions can follow it, and disappear as a material phenomenon (though liable to reappear wherever matter is encountered whose particles are deficient in a like species of atomic motion with that which disappeared; which fact indicates that atomic mass is still a factor, with its inherent property of persistence and transference). The earth and all upon it is radiating heat energy away into space at the constant rate of 500° F. of absolute temperature, more or less; the sun and the visible stars at the rate of many millions of degrees. Much energy also passes off in the luminous form. Of electrical and actinic energies we know less, and of some we doubtless know nothing. This amounts to a constant drain of the dynamical supply of energy. These final forms, the radiant energies, have a remarkable specific high cosmical velocity of their own, which is a function of something not material, or at least not molar. It is supposable that, in addition to the dynamical source of motion from central forces, and the contraction of systems in dimension which supplies dissipation, there may be an inherent and primordial store of atomic motion. The high proper motion of some of the stars, beyond what can be accounted for on dynamical principles, and the inexhaustible and enormous supply of radiant energy from the visible stars, have afforded grounds for such a surmise, but these speculations do not belong to the domain of mechanics.

And here we must bear in mind that the dynamical theory, in placing these assumed agencies and modes of interaction in causal relation to phenomenal motion, by no means predicates or can predicate anything concerning absolute motion or its cause. The lack of this distinction may have proved a stumbling block to some in comprehending the idea of force. Were it not for the observed dissipation of energy no system could become contracted in dimensions a particle by the interactions of material forces, nor is there now any known way by which the material system can be expanded in dimensions except by the accession of motion from extra-mundane sources, which there is no scientific mode of ascertaining. The sum of motions under the action of forces remains the same, and any change would imply creation or annihilation, which is not ascribable to a material agency. Primordial dimension remains as inscrutable a fact as ever, and primordial motion an unsolved problem.

In conclusion, I know nothing of force except as a manifestation of matter, and nothing of matter except through its manifestations. It is substance that interacts with substance, so far as we know, always reciprocally, and force is but the convenient translation of the terminology invented by Newton to designate these several species or modes of action, in the word *vis*, with its appropriate adjective. He was arraigned by the Cartesians (and virtually is by their modern representatives) as the reintroducer of occult qualities into philosophy, but his statement was "*hypotheses non fingo*," and to a similar charge brought against him by Leibnitz he pertinently replied that it was a misuse of words to call those things occult qualities whose *causes* are occult though the qualities themselves be manifest.

I have adopted gravity as the type of central inherent force—*vis centripeta*—but I would not thereby be understood as excluding from the category of material forces any and all other modes of tensile or constraining force which may be hereafter made out as specific, by the elucidation of such phenomena as affinity, cohesion, tenacity, elasticity, ductility, viscosity, capillarity, polarity, magnetism, etc., now so little understood, any more than I would exclude any form or mode of energy which may be observed, from the category of material phenomena. The Newtonian doctrine of force would not be impaired by such discovery, and its strength lies in the fact that it as readily includes static phenomena—that despair of the kinetist, who has no imaginable hypothesis by which to range them under a form of motion—as it does kinematical phenomena. Statical force (Newton's *vis mortua*) cannot be ignored in a theory of force. The straw that breaks the camel's back—the very lightning that crashes through the sky—are familiar examples of its power made manifest. Its reality may be exemplified by suspending two heavy balls of equal weight at equal heights—one by an elastic cord, and the other by a tense string. The difference of effort required to displace the two vertically upwards, which can be measured, makes sensible the difference between the two forms of balanced statical forces. In the one case the antagonizing force is suddenly withdrawn, and in the other gradually. Wherever strain exists—and it is everywhere—there force is as certainly present as when it becomes manifested in a stress relieved by motion and measurable in terms of energy.

Let us, then, give up the standard of *a priori* conceivability, in view of its many historical failures, and adopt as possible that which is provisionally ascertained. The "ego" and the "cogito"—Cartesian starting points—have proved barren and irrelevant in Philosophy. True Philosophy is concerned with objectivity. The data of consciousness, mainly acquired in infancy or in the womb, are blind guides. Many an ego, whose brain was his cosmos, has run through his brief subjectivity, but the order of nature endures. The same facts are continually observed, verified, recorded, and rectified, but the observers change. Their intelligent observations add to the sum of knowledge. This is all the proof we need of objectivity, and all we will get. The insoluble difficulties of Philosophy have disappeared one by one since the happy thought of eliminating them by observation entered. The immortals are those who have successfully applied this method. It is only where observation fails that the insolubility lingers. Beyond the sphere of the knowable it will continue, in spite of introspection. How masterful is fact in the presence of the most intricate mental subtleties. The ball leaves the bat, in spite of the inconceivability. Galileo's plummet dropped from the moving mast strikes the deck and not the water, in spite of the inconceivability. The Earth returns in its orbit, to the second, in spite of the sun's rapid fall through space, and of the inconceivability. Two opposed horses can pull no more than one, in spite of the inconceivability. The guinea and the feather dropped in the exhausted receiver strike the plate together, in spite of the inconceivability. The isochronous pendulum swings through the widest arc in the same time as through the smallest, in spite of the inconceivability. The minute hand overtakes the hour hand, in spite of the inconceivability. The magnet draws the iron with undiminished force through all possible interpositions, in spite of the inconceivability. Could an exception be found, the perpetual-motion "crank" would work a greater inconceivability, by the instant contrivance of a power-generating machine.

We need not aspire, therefore, to remove any of the inconceivabilities of the external world. We must accept them as natural to the finite comprehension, as necessary to faculties which act by comparison, and above all as evidences of objectivity. On the other hand we should avoid that opposite error of the introspective

school, of deeming that probable, or in any way connected with fact, which merely seems conceivable. I have shown that while the simplest truths have generally proved inconceivable until found out and established by genius, the greatest absurdities have had ready currency without a doubt of their conceivability. This all mythology shows. Such rubbish as "a thing cannot act where it is not," and "a body cannot move where it is not," or "a cause cannot precede its effect"—mere metaphysical assertions or subtleties in face of everyday fact—were stumbling blocks for ages. Such assumptions formed the basis of deduction in lieu of observation, and blocked the possibility of advance. And even yet, rigid deduction from the most hare-brained premiss, if the chain of deduction is sufficiently intricate, seems to possess fascinations over a verifiable induction, with many minds.

And now, if any ask, "*cui bono*" to the scientist, these philosophical inquiries and intricacies when he has the vast field of unexplored data still before him to occupy him, I answer, the queries of Philosophy are not only the main-spring and final cause of science (her first fruitful daughter and handmaid), but they, consciously or unconsciously, dominate the methods and results of science herself. Each investigator, even though in the domain of the most abstract of the sciences, postulates more philosophy than he is aware of; and with so much the more danger to final accomplishment if he assumes his philosophical basis without examination. It is the errors of giant minds that are dangerous, by their ponderosity. The infallibility of the master, Aristotle, seemed to make investigation useless, until the rise of parallel giants, like Galileo and Copernicus, stimulated a new conflict of opinion. And Descartes, though harmless from all his productions within the metaphysical domain, is dangerous by his very eminence and originality in science, which gives vogue and currency to his monumental errors. Although acquainted with the true law of motion, his scheme of matter evolved from consciousness would forbid all exhibition thereof. A grand geometer, he erected a scaffold for scaling immensity, and with unparalleled penetration perceived how a purely ideal logic, if general, would represent truth in a wholly dissimilar realm of deduction, if equally general. Strange to say, this grand and useful discovery has become the engine, in nihilistic hands, for overthrowing all the positive knowledge we

possess—the achievements of two thousand years of human effort. Not only geometry—all that has survived to us of philosophical value from the antique world—but the basis of positive dynamics, as handed down from Galileo and Newton and Boscovich and Dalton, are apparently undermined, for all that gives them intellectual value—their certainty—unless an effort be made in the neglected field of philosophy. With strange inconsistency these advocates *par excellence* of the experiential origin of knowledge are found in the same breath promulgating as possible truth matters not only non-experiential, but not representable in ideas derived from or verifiable by experience, and avowedly originating not from inductive generalizations—the only source of knowledge—but in purely deductive processes in the old scholastic way, from logical premises of bald assumption. In a similar way, in the hands of the Greek sophist, language, a good servant, became a vicious master, and made a chaos of all ethical achievement. A remnant of knowledge, fortunately expressed, not in verbal, but diagrammatic logic—geometry—was left, but only to fall now by the hands of similar iconoclasts, armed with more potent destructiveness, in its full flower and fruit of twenty centuries of unmo-lested growth.

It is time, therefore, to get back to Baconian ground, and while using for its legitimate purposes the magnificent modern machinery of analytical investigation in the field of abstract continuity—extension, motion, duration—not attempt to conjure with it as a source of objective revelation, which no mere machinery can be. A scaffold of n dimensions is as useless to the geometer as to the architect. To assume matter as continuous, simply because of the possession of a potent engine for the investigation of continuities, is to repeat the practice of certain quack specialists, who are prone to diagnose nearly every form of disease as a variety of their own peculiar speciality. And to interview the symbols of a mathematical logic for the prime definition of a fundamental objectivity, like force, is to revert to a barren source of knowledge, by an obsolete process in philosophy, and bar all progress in anything but abstract technique.

The paper was discussed by Mr. W. B. TAYLOR and Mr. KUM-MELL.

Mr. T. ROBINSON made a communication on

THE STRATA EXPOSED IN THE EAST SHAFT OF THE WATER-WORKS
EXTENSION.

[Abstract.]

The shaft (23' square in the clear) was begun in the bottom of an old sand-pit at a level of 131.5' above tide. This sand-pit was excavated in the side of a hill; and recent cuttings have exposed the strata from the hill-top to the level of the top of the shaft. Thus we have a vertical section of 188.5', extending from 171.5' above tide (or 40' above the top of the shaft) to 17' below tide.

1. About 6" of surface soil.
2. A layer of gravel in red clay, about 4' thick, containing isolated boulders from a foot to two feet in their longest diameters.
3. About 24' of a mixed material, consisting mainly of sand and kaolin. The two are sometimes uniformly mixed; at other times they lie in separate masses of two or three feet in thickness at one point, and run down to as many inches at another. In short, the whole bed is a sort of "pell-mell" of sand and clay.
4. A bed of sand, about 10' thick, generally sharp and clean, but varying from coarse to fine grains, and streaked with iron oxides, with pebbles near bottom of stratum.
5. A thin stratum of clay, about 2' thick, varying in color from blue to red, and containing in spots fragments of lignite.
6. 2.5' of sharp, coarse, clean sand.
7. 32.5' of red clay, mottled with blue and gray, showing no lamination.
8. 5' of sandy clay, mottled as above. Between this stratum and the clay above, there was no dividing line; the two beds blended gradually along their line of union.
9. A bed of gray, clayey sand, 6' thick. In this bed occurred, on one side of the shaft, some masses of sandstone, somewhat more ferruginous than the surrounding sand, and on the other side a *tongue* of clean, red clay.

10. A bed of sand with its upper surface horizontal, having a thickness of about 1' at one side of the shaft and 4' on the other.
11. A stratum, about 2' thick, of sandy mud, containing lignite. The laminae of this bed were horizontal, while its upper surface fell from north to south at the rate of about one in eight.
12. 6' of sand containing nodules of iron pyrites, isolated masses of lignite, and pockets of red clay.
13. A bed of fine, clean sand, containing here and there a little clay. This bed was 9' thick, and gradually gave way to the succeeding bed.
14. A bed of sandy kaolin, 6' thick, very wet and difficult to work. It was a regular mortar-bed in consistence.
15. A layer, 2" to 4" thick, of hard, ferruginous conglomerate.
16. 9' of blue-grey clay, hard, compact, and possessing a very unctuous feel. This bed contained a bunch of rootlets, the first trace of organic remains below the lignite of No. 11.
17. A bed of clayey sand, streaked with red, blue, and grey, 7' thick, and gradually running into the subjacent stratum.

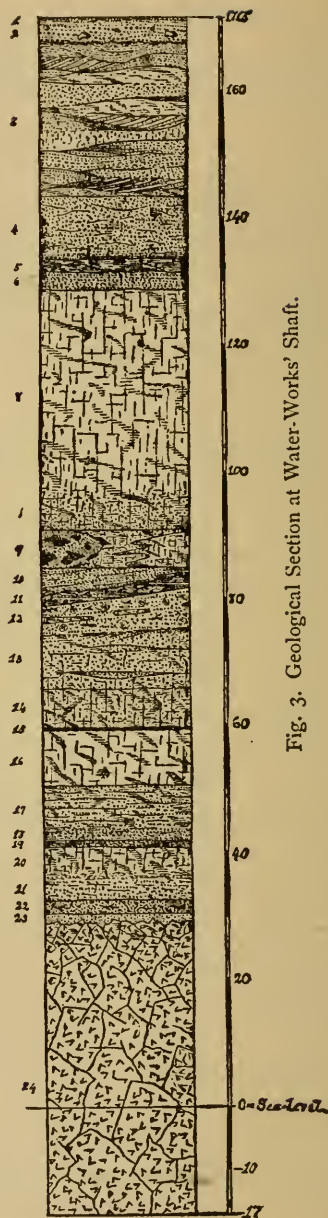


Fig. 3. Geological Section at Water-Works' Shaft.

18. A bed of clean, white, sharp sand, about 2' thick. (These last nine feet were difficult to work. The material could not be shovelled, and was too sandy to pump.)
 19. A layer of red sand about 1' thick, containing on one side of the shaft a clayey sediment with lignite, and on the other a ferruginous conglomerate.
 20. 5' of blue-black, hard clay, running into a sandy sediment, and this, in turn, into the next stratum.
 21. 3.5' of clean, white sand.
 22. 2' of dark green, compacted sand, containing pebbles and lignite.
 23. 1.5' of fine, sharp sand, almost apple-green in color. Beneath this lay the irregular surface of No. 24.
 24. Dark, coarse-grained, soft, chloritic rock. This rock could be easily removed by the pick to a depth of three feet, where blasting was begun at about twenty-six feet above mean tide. The rock grew harder as the depth increased for about ten feet, when it became a chloritic gneiss, and in general remained of that nature through about thirty feet to the bottom of the tunnel grade, or seventeen feet below mean tide.
-

255TH MEETING.

JUNE 7, 1884.

Vice-President BILLINGS in the Chair.

Thirty-five members and guests present.

Mr. G. K. GILBERT presented a

PLAN FOR THE SUBJECT BIBLIOGRAPHY OF NORTH AMERICAN
GEOLOGIC LITERATURE.

Mr. J. W. POWELL presented a slightly different plan for the same purpose.

These plans proposed to establish at the outset a limited number of divisions of the subject-matter of the literature and to simultaneously prepare a bibliography of each.

Mr. J. S. BILLINGS criticised the plans at length and advocated that which has been adopted for the indexing of the Library of the Army Medical Museum.

Other remarks were made by Messrs. ANTISELL, NORRIS, GOODE, E. FARQUHAR, F. W. CLARKE, HARKNESS, TONER and WARD.

The meeting announced for October 11 was informally adjourned, to enable members to attend a meeting of the Anthropological Society, and listen to an address by Dr. E. B. Tylor, of Oxford, England.

256TH MEETING.

OCTOBER 25, 1884.

The President in the Chair.

Forty members and guests present.

The Chair announced the death, since the last meeting, of Dr. JOSEPH JANVIER WOODWARD, a former President of the Society, Gen. ORVILLE ELIAS BABCOCK, and Gen. BENJAMIN ALVORD.

Announcement was also made of the election to membership of Messrs. WASHINGTON MATTHEWS, STIMSON JOSEPH BROWN, TARLETON HOFFMAN BEAN, and ROBERT EDWARD EARLL.

Mr. S. M. BURNETT read a paper entitled—

ARE THERE SEPARATE CENTRES FOR LIGHT-, FORM-, AND
COLOR-PERCEPTION?

controversing the theory which gives an affirmative answer to the question, and maintaining, first, that there is no white-light sensation that cannot be resolved into its constituent elements of color sensation; and, second, that the sense of form is an expression of the idea of extension as represented by the dimensions of the area of the retina impressed. The idea of form is not a purely visual sensation, but is based also on information derived from other sources.

[The paper is published in the *Archives of Medicine*, Vol. XII, No. 2, October, 1884.]

Mr. T. ROBINSON read a paper entitled—

WAS THE EARTHQUAKE OF SEPTEMBER 19TH FELT IN THE
DISTRICT OF COLUMBIA?

[Abstract.]

At 3.20 p. m. of September 19 I noticed a peculiar vibration of the floor, table, and chair. I saw my ink shaking and heard the door of the room rattling. The table and chair rocked in a north and south direction. The sounds made by the door were at regular intervals of something less than a second each. My room is on the second floor of the Howard University building.

Immediately after the occurrence I inquired if other persons had noticed anything unusual at that time. One had heard a rumbling, another had felt the shock, and a third had both felt and heard it. The miners in the water-works' tunnel also heard a rumbling noise at about the same hour.

From the motion of my table and chair and the continued thumpings of the door I judge that the shock passed in the direction of the meridian, and continued from ten to fifteen seconds.

There was no local cause for the phenomenon, and I concluded that it was in some way connected with the earthquake that occurred in the West at about the same time.

Mr. PAUL remarked that the direction of the motion communicated to buildings by a slight earthquake shock is not a reliable index of the direction of the earth tremor. The azimuth, amplitude, and period of vibration of the buildings are functions of their structure rather than of the azimuth, amplitude, and period of the earth vibration.

Other remarks were made by Mr. H. A. HAZEN and Mr. ELLIOTT.

Mr. J. S. BILLINGS exhibited a collection of microscopes illustrating the evolution of the mechanical stage. The collection will be sent by the Army Medical Museum to the New Orleans Exhibition.

Mr. BILLINGS read a paper by Mr. WASHINGTON MATTHEWS on
NATURAL NATURALISTS.

[Abstract.]

It is easy to understand that a savage may be well versed in the knowledge of animals and plants which contribute to his wants,

but it is a matter of surprise that with equal care he acquires and disseminates information about creatures which he does not use. I have never yet failed to get from an Indian a good and satisfactory name for any species of mammal, bird or reptile inhabiting his country; and I have found their knowledge of plants equally comprehensive. It is true that not all Indians are equally well informed in this respect, but, as a class, they are incomparably superior to the average white man or to the white man who has not made zoology or botany a subject of study.

There is a prevalent impression that Indians are unable to generalize; and a paragraph goes the rounds of ethnological treatises to the effect that the Chetas have no general term for oak tree, but only specific names for the white oak, the black oak, the red oak, etc. This impression is entirely erroneous. The Indian is as good a generalizer and classifier as his Caucasian brother. His system of classification does not fully coincide with that of the white naturalist, because his system of philosophy leads him to base his groups upon a different series of resemblances, but his arrangement is nevertheless the result of a process of generalization.

Mr. WARD remarked that his own experience fully sustained the statements of the paper in regard to the botanical ignorance of white men, but less fully in regard to the accuracy of Indian observations. When collecting plants in Utah, he had found that Piute boys and girls gave names to nearly all his specimens, discriminating allied species; but in collating the Indian botanical names recorded by others, he had been led to suspect that certain discrepancies arose from failure to recognize the same species in different stages of development.

Mr. MASON said it is a canon of anthropology that things seem marvellous to us only when we do not understand them, every human phenomenon being governed by law. Our ignorance in regard to wild animals and plants is to be explained by the fact that our activities do not bring us into close relation with them, whereas the savage is dependent on them for sustenance. The market-women who bring herbs to Washington have names for them all, and ignorant mechanics handle technical terms of their craft with great familiarity.

Mr. DUTTON said that his own acquaintance with the Navajos

made him prone to believe that they diagnose species of plants, but he questioned their powers of generalization.

In illustration of Mr. Mason's remark that familiarity is conditioned by contact, he related that rural rambles had made him when a boy so familiar with the fauna and flora of his district that he knew a name for every prominent species. As a man, he had been occupied with other and different matters, and had lost this familiarity.

Mr. WELLING admitted that the Indian was an acute observer, but questioned the propriety of calling him a naturalist. As illustrated by the paper, his methods of interpretation are metaphysical, not scientific.

Other remarks were made by Mr. HILGARD.

257TH MEETING.

NOVEMBER 8, 1884.

Vice-President BILLINGS in the Chair.

Forty-eight members and guests present.

Mr. BILLINGS, on behalf of the General Committee, reported the following resolutions:

Resolved, That this Society receives with deep regret the announcement of the the death, on the 17th of August last, of Dr. JOSEPH JANVIER WOODWARD, an ex-president of this Society and one of its original founders.

Resolved, That this untimely death has deprived science of one of its most energetic, patient, and skilful workers and this Society of one of its most efficient and distinguished members.

Resolved, That in our sorrow for this affliction we have some consolation in the knowledge that his long and great suffering is at last ended and that the fruits of his unceasing labors for the last twenty-five years remain for the benefit of the world and as an enduring monument to his memory.

Resolved, That a copy of these resolutions, duly authenticated, be forwarded to his bereaved family.

In presenting these resolutions, Mr. BILLINGS spoke briefly of Dr. Woodward's work and his characteristics as a scientific man,

eulogizing his accuracy of observation, his delicacy of manipulation, his conservatism as a theorist and as a critic of new ideas, and alluding to his delight in teaching and his interest in, and affection for, the Philosophical Society.

Mr. POWELL spoke of his remarkable acumen and his conspicuous mental integrity. Mr. GIBON spoke of his boyhood; Mr. TONER of his ability as a practitioner; and Mr. E. FARQUHAR of the impression of great force conveyed by his presence and conversation.

The resolutions were unanimously adopted.

Mr. C. E. DUTTON made a communication on

THE VOLCANOES AND LAVA FIELDS OF NEW MEXICO,

his remarks being illustrated by photographic lantern views, and by a map exhibiting the boundaries of the region usually termed the Plateau country.

[Abstract.]

Beginning at the north, the boundary of the Plateau country runs along the southern base of the Uinta Range to the junction of the latter with the Wasatch; following the eastern base of the Wasatch southward it strikes off towards the southwestern corner of Utah; thence turning due south it crosses the Colorado river, and gradually shifts its course to the southeastward, preserving this direction for nearly 400 miles and far into New Mexico; here it rapidly turns north northeastward, reaching into the Valley of the Rio Grande, and follows the western bank of that river nearly or quite into Southern Colorado; here the course of the boundary is somewhat indeterminate, but is, in a general way, first northwestward, then northward to the place of beginning. The western and southern border of the Plateau province is usually sharply defined; the plateaus end generally in great cliffs suddenly terminating the horizontal strata, and the profiles drop down upon the rough, irregular topography of a type peculiar to the Great Basin. The eastern border of the Plateau province is by no means so definite; the features peculiar to it pass rather by gradual transition into those characterizing the Rocky Mountains of Colorado.

Among the many geological features of this wonderful region, the volcanic masses are not the least interesting. Volcanic action has prevailed there upon a grand scale, and it may be first noted

that volcanic rocks predominate around the borders of the province. The interior spaces, while not wholly devoid of them, show but a very small amount. The region of the High Plateaus of Utah, which lies upon the western or northwestern border, discloses a very large mass of lavas, erupted chiefly during tertiary time, and representing almost continuous activity from the eocene to the quaternary. Proceeding southward, we are never out of sight of eruptive masses, and in the Unkarets, on the border of the Grand Cañon, we find many scores of old and young cinder-cones and some considerable lava-fields. In the San Francisco Mountains we also have a vast field of volcanic rocks, and thence southeastward they augment in volume and area until at the southernmost extension of the Plateau country they become indeed immense. Still following the boundary northward into the Valley of the Rio Grande they are found abundant, and a singularly interesting field is presented in the neighborhood of Mt. Taylor. The speaker was engaged during the past summer in the geological examination of the Mt. Taylor district, and it is of the striking features there presented that he designs especially to speak.

Mt. Taylor is an old volcano long since extinct. Its altitude is about 11,400 feet above the sea. It stands upon a high *mesa*, from the summit of which it rises as an ordinary volcanic cone of considerable magnitude—much larger than Vesuvius, much smaller than Ætna. Its lavas are rather monotonous in type, so far as external appearances are concerned, consisting probably of basalts and andesites. The *mesa* upon which it stands is of great extent, being 40 miles long and 25 miles wide. It is composed of nearly horizontal cretaceous strata, capped everywhere with basalt or andesite, ranging from 200 to 400 feet in thickness. To the north-east and to the south of it are similar high *mesas*, also capped by basalt and andesite, but presenting no great volcanic pile like Mt. Taylor. The only features which indicate volcanic vents are barely noticeable hillocks, which scarcely affect the evenness of the horizontal surfaces and which are wholly incommensurate, apparently, with the vast lava caps upon which they occur.

These lavas are all of tertiary age. It would be difficult to say to what divisions of tertiary time their activity should be assigned, but it cannot have been very late tertiary and it is reasonably certain that it cannot have been very old tertiary. In a general

way their activity is inferred to have prevailed in a period not far from middle tertiary time—possibly in the miocene. The large amount of erosion which has occurred since their eruptions ceased forbids a much later period, and the still larger amount of tertiary erosion which preceded this activity equally forbids a much earlier one.

Upon the summits of the *mesas* no recent eruptive rocks occur. But in the broad valleys which lie between them and around them are lavas of quite another age. These valley lavas are all recent. Indeed the most superficial observer is at once impressed with the freshness of their aspect, and critical examination confirms the view that none of them have any geologic antiquity, while some of them are so modern that it seems as if half a dozen centuries were a large estimate of the time which separates us from their outflow.

These recent eruptions are basalts of normal type. The external aspects of the fields of young lava resemble those of the Hawaiian Islands. The two forms of solidified lava are well presented, viz: the viscous or ropy, and the rough clinker fields.

A striking characteristic of both old and young lavas—those upon the *mesa* summits and those in the valleys below—is the usual though not universal absence of cinder cones or piles of fragmental matter built up around the orifices from which the lavas were extruded. The eruptions, with the exception of those of Mt. Taylor, belonged to the quiet order which are typified among volcanoes now active, by Mauna Loa and Kilauea.

But the volcanic remnants which appeal most strongly to the imagination of the observer, remain to be described. In the broad valleys which separate the lava-capped *mesas* are seen many conspicuous objects rising as sharp peaks or aiguilles of rock to great altitudes. They are very black in color, and contrast powerfully with the bright tints of the sedimentary beds around them. These peaks, which range in altitude above the valley plains from 700 or 800 feet to 2,000 feet, consist of columnar basalt. They are, in fact, the ancient lavas which congealed in the volcanic pipes, while the sedimentary strata which formerly inclosed them have been swept away in the great erosion of the country. In that long-continued and great denudation these "necks," by their more adamantine character, have resisted the general decay, and remain to attest the former extension of the strata over the valleys and the

existence, prior to their denudation, of volcanic extravasations which probably covered them wholly or in part. In the *mesa* walls and on their slopes may be seen numerous instances of partially excavated necks, while in others the necks are just beginning to be exhumed. In the latter cases remnants of the old cinder-cones which were piled up over their summits are still preserved, so that natural sections of the whole apparatus are exhibited. There are many scores of these necks, and the effects of erosion in unearthing them are exhibited in all stages. Wherever the true neck or core is disclosed the basalt is seen to be columnar, and the columns are often arranged in beautiful fashions.

No more striking illustration and proof of a great erosion could be mentioned than is here disclosed, and the region must become a classic one, to be referred to by future geologists as an excellent example of some of the grandest laws and processes with which their science deals.

Mr. POWELL spoke of the distribution of eruptions. They are apt to occur on the faces of acclivities undergoing erosion, but not on acclivities due to displacement. Near a fault they break through the uplifted block rather than the thrown. They do not occur in the bottoms of cañons.

In mapping the Plateaus he had thrown the boundary farther north than Captain Dutton, so as to include a large area north of the Uinta Mountains.

The peculiarly favorable conditions under which geology is studied in the plateau region enable its features to be comprehended without the doubts and the laborious compilation of details elsewhere necessary. It results that while the structure of the Plateau country is as well known as that of any equal area in the world, the literature of its geology is exceedingly small.

Other remarks were made by Messrs. WHITE and GILBERT.

258TH MEETING.

NOVEMBER 22, 1884.

The President in the Chair.

Forty-nine members and guests present.

Mr. E. B. ELLIOTT made a communication on

ELECTRIC LIGHTING,

which was discussed by Messrs. HILGARD, WELLING, MUSSEY, PAUL, and POWELL.

Mr. H. ALLEN HAZEN made a communication on

THERMOMETER EXPOSURE.

[Abstract.]

In recent experiments for determining the relative values of temperatures in city and country, it has been found that ordinarily, on clear days, in the early morning, at 6 feet above ground, in the country, temperatures are 4 to 5 degrees lower than in the city, and also that the air is always nearly saturated in the country, but not as nearly in the city. This is due more to intense radiation from grass in the country, this cooling the air to the dew point, than to the heating and drying from pavements and walls or chimneys of houses.

To obtain a standard air temperature it is proposed to use bright and black bulb thermometers joined together and swung over grass ground under an umbrella, with no shade from trees or buildings, in the day time. Under such circumstances the two thermometers can be brought within 0.5° of each other, and the true air temperature may be taken as about as much lower than the bright-bulb as that is lower than the black.

Recent experiments with six different thermometer shelters indicate a general agreement, except in the case of the Wild shelter. The peculiar condition effected by the Wild shelter is inferior ventilation, and the experiments indicate the practical sufficiency of the single-louvred shelter. To determine the humidity with the psychrometer in still air, the employment of artificial ventilation is recommended.

Remarks were made by Mr. PAUL.

259TH MEETING.

DECEMBER 6, 1884.

By courtesy of the officers of the Columbian University, the meeting was held in the lecture hall of the University building.

Members of the Anthropological, Biological, and Chemical Societies and their friends were present by invitation.

Mr. J. W. POWELL, by request of the President, occupied the Chair.

Present, one hundred and four members and guests.

The business of the evening was the presentation of the Annual Address of the President, Mr. J. C. WELLING. In introducing him to the audience, the Chairman sketched the history of the Society, describing the socio-scientific club of which it was the offspring, and referring to the younger scientific societies of Washington, of which it might be regarded as the parent.

The President then read an address on

THE ATOMIC PHILOSOPHY, PHYSICAL AND METAPHYSICAL.

[Printed in full on pp. XXIX-LIX.]

On motion of Mr. GREGORY, the Society tendered its President a vote of thanks for his efficient administration and instructive address.

260TH MEETING.

DECEMBER 20, 1884.

THE FOURTEENTH ANNUAL MEETING.

The President in the chair.

The Chair announced the death, since the last meeting, of Mr. HENRY WAYNE BLAIR.

The Chair announced the election to membership of Mr. ROBERT EDWARDS CARTER STEARNS.

It was announced that the Mathematical Section would, in the future, hold its meetings in the mathematical class room of the Columbian University, the use of that room having been tendered by the officers of the University.

The order of business was then read, and afterward the minutes of the last annual meeting.

The report of the Secretaries were read and accepted. (Printed on page XXIII.)

The report of the Treasurer was read, received, and referred to an Auditing Committee, consisting of Messrs. H. C. Yarrow, Marcus Baker, and W. C. Winlock. (The report is printed on pages XXIV and XXV.)

The minutes of the 258th and 259th meetings were read and approved.

The officers of the ensuing year were then elected. (The list is printed on page xv.)

The rough minutes of the meeting were read, and the meeting adjourned.

BULLETIN

OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON

MATHEMATICAL SECTION.



STANDING RULES

OF THE

MATHEMATICAL SECTION.

1. The object of this Section is the consideration and discussion of papers relating to pure or applied mathematics.

2. The special officers of the Section shall be a Chairman and a Secretary, who shall be elected at the first meeting of the Section in each year, and discharge the duties usually attaching to those offices.

3. To bring a paper regularly before the Section it must be submitted to the Standing Committee on Communications for the stated meetings of the Society, with the statement that it is for the Mathematical Section.

4. Meetings shall be called by the Standing Committee on Communications whenever the extent or importance of the papers submitted and approved appear to justify it.

5. All members of the Philosophical Society who wish to do so may take part in the meetings of this Section.

6. To every member who shall have notified the Secretary of the General Committee of his desire to receive them, announcements of the meetings of the Section shall be sent by mail.

7. The Section shall have power to adopt such rules of procedure as it may find expedient.

OFFICERS
OF THE
MATHEMATICAL SECTION FOR 1884.

Chairman, ASAPH HALL.

Secretary, HENRY FARQUHAR.

LIST OF MEMBERS WHO RECEIVE ANNOUNCEMENT OF THE
MEETINGS.

ABBE, C.	HALL A.
AVERY, R. S.	HARKNESS, W.
BAKER, M.	HAZEN, H. A.
BATES, H. H.	HILGARD, J. E.
BILLINGS, J. S.	HILL, G. W.
BURGESS, E. S.	KING, A. F. A.
CHRISTIE, A. S.	KUMMELL, C. H.
COFFIN, J. H. C.	McGEE, W J
CURTIS, G. E.	NEWCOMB, S.
DELAND, T. L.	PAUL, H. M.
DOOLITTLE, M. H.	LEFAVOUR, E. B.
EASTMAN, J. R.	PEIRCE, C. S.
EIMBECK, W.	RITTER, W. F. M'K.
ELLIOTT, E. B.	SMILEY, C. W.
FARQUHAR, H.	TAYLOR, W. B.
FLINT, A. S.	UPTON, W. W.
GILBERT, G. K.	WALLING, H. F.
GORE, J. H.	WINLOCK, W. C.
GREEN, B. R.	WOODWARD, R. S.

BULLETIN

OF THE

MATHEMATICAL SECTION.

10TH MEETING.

JANUARY 30, 1884.

The Chairman presided.

Seventeen members and guests present.

The Section proceeded, under Rule 2, to the election of a Chairman and a Secretary for the year 1884. On motion of Mr. ELLIOTT, the rules governing the elections of the Society were adopted. The officers for 1883—Mr. HALL, as Chairman, and Mr. H. FARQUHAR, as Secretary—were re-elected, after each had briefly expressed a desire that the choice might fall on some one else.

Mr. KUMMELL read an extract from a letter lately received from Mr. Artemas Martin, of Erie, Pennsylvania, in which the formation of an American Mathematical Society was recommended. After some informal discussion, Mr. WINLOCK moved the appointment of a special committee, with instructions to report on the advisability of taking steps for the formation of such a society. On motion of Mr. ELLIOTT, the matter was postponed.

Mr. KUMMELL then made a communication on

CURVES SIMILAR TO THEIR EVOLUTES,

in which he made use of the intrinsic equation, and showed this property to belong to a whole class, of which the logarithmic spiral is at one extreme and the cycloids are at the other.*

* Prof. Benjamin Peirce solved a problem almost identical with this one, in *Gill's Mathematical Miscellany* for May, 1839, by essentially the same methods. This solution, which had not been seen by Mr. Kummell at the time of reading his paper, is believed to contain the first use of what has since become known as the "intrinsic equation."

Remarks on this communication were made by Messrs. CHRISTIE and HILL.

Mr. G. K. GILBERT made a communication on

THE PROBLEM OF THE KNIGHT'S TOUR.

[Abstract.]

The ordinary problem, requiring the knight to traverse the chess-board and return to his original position in sixty-four moves, is susceptible of very numerous solutions, and is not difficult. Its interest is increased by extending it so as to include fields of other form and size.

It is readily shown that a perfect tour is impossible on any field containing an odd number of squares.

A *symmetric* tour is one divisible into two or more similar parts. A tour has *bilateral symmetry* when one-half, being turned face downward upon the other, coincides with it. A tour has *biradial symmetry* when one-half, being rotated through 180° about the center of figure, coincides with the other half. A tour has *quadriradial symmetry* when its fourth part, being rotated through 90° about the center of figure, coincides with the adjacent quarter.

A tour having bilateral symmetry cannot be devised on a field containing a number of squares divisible by four.

A tour having biradial symmetry cannot be devised on a field whose number of squares is divisible by two and not by four.

A tour having quadriradial symmetry cannot be devised on a field whose number of squares is divisible by eight.

It follows that *on square fields* the tour is impossible if the number of spots on a side is odd; bilateral symmetry is never possible; quadri-radial symmetry is possible only when the number of squares on a side is the double of an odd number. The only symmetry possible on a chess-board is biradial.

The above conclusions are deductive. It is determined empirically that the smallest square field on which the tour can be executed is that with 36 spots. Upon this field the number of possible tours with biradial symmetry is twenty-one, of which five have also quadriradial symmetry.

Remarks on this communication were made by Messrs. ELLIOTT and HALL, who called attention to previous work on the subject.

11TH MEETING.

FEBRUARY 20, 1884.

The Chairman presided.

Eighteen members and guests present.

Mr. H. FARQUHAR made a communication on

EMPIRICAL FORMULÆ FOR THE DIMINUTION OF AMPLITUDE OF
A FREELY-OSCILLATING PENDULUM.

[Abstract.]

The theoretical formulæ usually employed are obtained by integration from an expression for the diminution of the amplitude in terms of the amplitude itself. The most important term in this expression is one involving the first power of the amplitude, indicating a resistance proportional to the velocity of the pendulum's motion. A term containing the square of the velocity (or amplitude) also enters; and, to allow for the friction of the pendulum knife-edge on its support, a term independent of the velocity would have to be added. Atmospheric resistance to very high velocities is found, moreover, to be proportional to a higher power than the square of the velocity. There are thus more than three terms theoretically required to express the resistance, and these must be calculated, such is the uncertainty of the subject and the complexity of the conditions on which the different resistances depend, from the observations themselves. Since these observations must also be depended on for an additional constant (the amplitude at some initial time or the time of some standard amplitude), and since they are not complete or exact enough to furnish more than three constants, or four in a few exceptional cases, it is obvious that a good approximation to theory must content us in practice.

Two convenient methods of representing amplitude in terms of time are suggested by imposing arbitrary conditions. First, taking three terms to express the diminution (the amplitude being φ), thus:

$$a + b\varphi + c\varphi^2,$$

suppose the square of half the middle co-efficient equal to the product of the other two. This expression has then the form:

$$\frac{1}{a}(\varphi + b)^2.$$

Integrating this value of $-D_t\varphi$, and supplying a constant, we have:

$$(\varphi + b)(t - e) = a,$$

in which the constants $a + be$, e and $-b$, are easy to calculate by least squares.

To show the agreement of this formula with observation, take Mr. Pierce's "mean swing" at three European stations (U. S. Coast Survey Report for 1876, appendix 15, pages 232, 271) and apply $b = 29'.2$, $e = -7632''$, $a = 756847$, in calculating φ from t . Hence the following table:

t .	φ , obs'd.	φ , calc'd.	Residuals (1st).	Residuals (2d).
-2880°	130'	130'.07	-0'.07	-0'.16
-2187	110	109.80	+0.20	+0.13
-1779	100	100.11	-0.11	-0.04
-706	80	80.08	-0.08	+0.24
0	70	69.97	+0.03	+0.40
+1927	50	49.98	+0.02	0.00
+3304	40	40.01	-0.01	-0.66

The agreement (in column "residuals, 1st") is as close as could be desired. The equation is that of the equilateral hyperbola, with asymptotes parallel to the axes of φ and t . This agreement can be made still closer by inclining one of the asymptotes, a term $-c(t - e)^2$ being added. There are thus four constants to compute; but this form of equation has the advantage of having its constants directly deducible by least square reduction. With the additional term, a perfect agreement between theory and the most precise observations hitherto made can be attained. As an instance, the thirty-five observations of amplitude, from over 2° down to $10'$, given by Prof. Oppolzer in the Proceedings of the Vienna Academy for October, 1882, were compared with the formula

$$(\varphi + 60'.6)(t + 10.8) - 0.5(t + 10.8)^2 = 2178.1$$

(the unit of t being an interval of about $5^m.7$) and of the residuals, which need not be given in detail, the largest was $0'.8$. A similar accordance was found in a set of observations extending over six hours, the pendulum swinging under less than half an inch of atmospheric pressure. (See Mr. Pierce's report, page 248, last two columns combined.) In this formula,

$$D_t \varphi = -\frac{1}{2a} \{ (\varphi + b)^2 - 4ac + (\varphi + b) \sqrt{(\varphi + b)^2 - 4ac} \}$$

$$= -\frac{1}{a} (\varphi + b)^2 + 3c + \frac{ac^2}{(\varphi + b)^2} + \text{etc.}$$

The correction to the time of oscillation $\left(\frac{1}{16} D_t^{-1} \varphi^2 \right)$ involves the logarithm of $t - e$, and is not very simple in practical application.

The second convenient method is the one by which the residuals in the last column of the table above given were calculated. In this the rate of diminution is supposed proportional to φ^{1+n} , n being a proper fraction. Hence,

$$\varphi^n (t - e) = a, \text{ and } D_t^{-1} \varphi^2 = -\frac{na^{\frac{2}{n}}}{(2-n)(t-e)^{\frac{2}{n}-1}} = -\frac{na\varphi^{2-n}}{2-n}$$

This formula is very simple, and the table shows its agreement with observation to be fair for the larger amplitudes—those of chief importance. In this calculation $n = \frac{1}{2}$, $e = -10716^s$, and $a = 89400$. Better results would have been obtained by using a slightly smaller value of n , say 0.44; but in practice the nearest tenth or reciprocal of a whole number is sufficient. In reducing the observations given by Prof. Oppolzer, n was taken equal to 0.28; but one of the residuals exceeded 1', though two others were as high as 0'.9. The observations at low pressures, above referred to, indicated a much smaller n . By using the value 0.04, however, the agreement of formula and observation was perfect. n thus appears to be nearly proportional to the square root of the atmospheric pressure; but when very small, it may be supposed to vanish, and φ^n replaced by the logarithm of φ . In this case e will of course be the time of unit-amplitude, instead of that of infinite amplitude as in former cases.

No two observations of the diminution of amplitude of the same pendulum will in general be found to be copies of each other, for differences in atmospheric conditions and in friction on the support, imperceptible otherwise, will manifest themselves in a changed rate of diminution. Even in calculating the correction for different parts of one extended swing, it is advisable to adopt different values of one or other of the constants found. By so varying the quan-

tity e , in the formula last given, all disadvantages from its want of exact accordance with observation disappear, and the results are brought far within the needful limits of accuracy.

Mr. GILBERT then stated

A CONCRETE PROBLEM IN HYDROSTATICS,

suggested by the fact that the shore-line of a quaternary lake in the Great Basin is shown by levels to be more than a hundred feet higher on elevated land, that once formed islands near its middle part, than on the margin of the lake. This inland sea, known as Lake Bonneville, was one hundred and twenty miles across. Among the possible explanations of the present difference of level, the effect of the removal of a large body of water in changing the form of level surfaces in its basin had been suggested, and the problem was to find how great an effect was due to this cause.

In the discussion that followed, Mr. PAUL called attention to the complexity of the calculation of equipotential surfaces.

Mr. WOODWARD had formerly made a somewhat similar computation to ascertain the deflection of the plumb-line caused by unequal local attraction to eastward and to westward at the eastern end of Lake Ontario; from which it appeared to result that the effect due to this cause was insignificant in comparison with that required by the problem.

Other remarks were made by Messrs. DOOLITTLE, HILL, H. FARQUHAR, and S. J. BROWN.

At the request of the Chairman, a communication promised by him was postponed until next meeting.

12TH MEETING.

MARCH 5, 1884.

The Chairman presided.

Fifteen members present.

Mr. A. HALL read the following paper on

THE FORMULÆ FOR COMPUTING THE POSITION OF A SATELLITE.

The method of rectangular co-ordinates in space furnishes a very simple and at the same time a general method of treating many questions in astronomy. This method was introduced into practical astronomy by Lagrange in his memoir on the Transit of Venus, June 3, 1769 (Berlin Academy Memoirs, 1766). Whenever we have to consider the relations of three points in space, we may take the origin of co-ordinates at one of the points, and then forming the values of the rectangular co-ordinates of the other points in terms of the polar co-ordinates, the sum or difference of two of the x co-ordinates being equal to the third x co-ordinate, we have an equation between the three polar co-ordinates. Similar relations hold for the axes of y and z , and hence result three equations between the two angles and the distance that are required to be found. This method is extremely useful, and can be applied to a great number of questions in parallax, aberration, eclipses, and to those that occur in nearly every part of spherical astronomy. A great recommendation of this method is its simplicity, and the fact that it is so closely connected with first principles that it can be applied with the greatest ease. After the equations are formed they have only to be transformed by known rules, and the whole work is thus reduced to algebraic and trigonometric transformations which can be safely made. These advantages are so great that it is not surprising that this method of treating astronomical questions has come so largely into use, and the generality and elegance of the process are in marked contrast with the old methods which proceed by spherical trigonometry. Perhaps a disadvantage of the new method is that it is too mechanical, and one is apt to forget or never know the meaning of the quantities that are employed. The old geometrical methods have therefore their value in calling to mind a more exact knowledge of the quantities that are used in the solution of a problem.

In the method which Bessel has employed for computing the position of a satellite, he has derived his formulæ by Lagrange's method. Thus if a and δ be the apparent right ascension and declination of the planet at any instant, a' , δ' the same quantities for the satellite, and if ρ and ρ' be their distances from the earth, and if r be the radius vector of the satellite, and a and d its right ascension and declination seen from the planet, we have, by the method of rectangular co-ordinates,

$$\begin{aligned}\rho' \cos \delta' \cos a' &= \rho \cos \delta \cos a + r \cos d \cos a \\ \rho' \cos \delta' \sin a' &= \rho \cos \delta \sin a + r \cos d \sin a \\ \rho' \sin \delta' &= \rho \sin \delta + r \sin d\end{aligned}\quad (1)$$

If p and s are the angle of position and distance of the satellite with respect to the center of the planet, the spherical triangle formed by the pole of the equator, the planet, and the satellite gives us the following equations:

$$\begin{aligned}\cos s &= \sin \delta \sin \delta' + \cos \delta \cos \delta' \cos (a' - a) \\ \sin s \cos p &= \cos \delta \sin \delta' - \sin \delta \cos \delta' \cos (a' - a) \\ \sin s \sin p &= \cos \delta' \sin (a' - a)\end{aligned}\quad (2)$$

If N and J be the longitude of the node of the orbit of the satellite on the equator, and its inclination to the equator, and u the distance of the satellite from the node counted on its orbit, we have

$$\begin{aligned}\cos d \sin (a - N) &= \sin u \cos J \\ \cos d \cos (a - N) &= \cos u \\ \sin d &= \sin u \sin J\end{aligned}\quad (3)$$

These three sets of equations are fundamental, and are sufficient for the complete solution of the problem—Given the orbit of a satellite to determine its apparent angle of position and distance. We have only to transform these equations, and, in order to ease the computation, to introduce, as Bessel has done, certain auxiliary quantities which depend on the position of the planet in the heavens, and the position of the orbit of the satellite with respect to the equator. These auxiliary quantities will of course vary with the position of the planet, and also from the slow changes that the node and inclination of the orbit undergo, but they can be tabulated easily. So far, therefore, as the practical solution of this question is concerned there is not much more to be desired, but it is interest-

ing to look at the problem from another point of view, and one that will lead us to consider more closely its geometry.

Imagine a set of rectangular axes in space, the origin being at the center of the planet, and denote by X, Y, Z the points on the celestial sphere made by the intersections of these axes. Let S be the point where the prolongation of the radius vector of the satellite strikes the sphere; then we have for the co-ordinates of the satellite

$$\begin{aligned} x &= r. \cos SX \\ y &= r. \cos SY \\ z &= r. \cos SZ \end{aligned}$$

We can express these cosines by means of six auxiliary quantities similar to those that Gauss has used for computing the position of a planet. Take the prolongation of the right line drawn from the earth to the planet as the axis of Z , the axis of Y in the plane of the declination circle that passes through Z , and the axis of X at right angles to this plane and in the direction of increasing right ascensions. Let O be the pole of the equator and T the positive pole of the orbit of the satellite. Introduce the following notation, which is the same as Bessel's :

$$\begin{aligned} \text{arc } TX &= f, & \text{angle } OTX &= F \\ \text{“ } TY &= g, & \text{“ } OTY &= G \\ \text{“ } TZ &= h, & \text{“ } OTZ &= H \end{aligned}$$

Since the arc $TS = 90^\circ$, the spherical triangles STX, STY , and STZ give

$$\begin{aligned} \cos SX &= \sin f \cos STX \\ \cos SY &= \sin g \cos STY \\ \cos SZ &= \sin h \cos STZ \end{aligned}$$

The distance of the satellite in its orbit from the node being u , and the angle OTN being 90° , we have

$$\begin{aligned} STX &= 90^\circ - (F + u) \\ STY &= 90^\circ - (G + u) \\ STZ &= 90^\circ - (H + u) \end{aligned}$$

And the values of the co-ordinates are therefore:

$$\begin{aligned} x &= r. \sin f \sin (F + u) \\ y &= r. \sin g \sin (G + u) \\ z &= r. \sin h \sin (H + u) \end{aligned} \tag{4}$$

These are the values at which Bessel arrives by the analytical method. The arcs f, g, h are always less than 180° , and the only difficulty is in counting the angles F, G, H . In the purely analytical process we merely substitute so as to satisfy the equations, and the result is right if we pay attention to the algebraic signs; but in the preceding quasi-geometrical method we must be careful to count the angles F, G, H in the direction of increasing right ascensions from 0° to 360° . The formulæ for computing the six auxiliary quantities can be found from the spherical triangles TOX, TOY, TOZ . In these triangles the angles at O are

$$TOX = 180^\circ - (a - N)$$

$$TOY = 90 - (a - N)$$

$$TOZ = 90 + (a - N)$$

Hence, we have

$$\begin{aligned} \cos f &= -\sin J \cos (a - N) \\ \sin f \sin F &= -\sin (a - N) \\ \sin f \cos F &= \cos J \cos (a - N) \\ \cos g &= \cos \delta \cos J + \sin \delta \sin J \sin (a - N) \\ \sin g \sin G &= -\sin \delta \cos (a - N) \\ \sin g \cos G &= \cos \delta \sin J - \sin \delta \cos J \sin (a - N) \\ \cos h &= \sin \delta \cos J - \cos \delta \sin J \sin (a - N) \\ \sin h \sin H &= \cos \delta \cos (a - N) \\ \sin h \cos H &= \sin \delta \sin J + \cos \delta \cos J \sin (a - N) \end{aligned} \quad (5)$$

The computation of these formulæ may be changed by introducing other auxiliary quantities, as is commonly done, but nothing is gained by such a change if the computer is accustomed to the use of addition and subtraction logarithms.

By means of the spherical triangles we can find a number of elegant relations among the quantities f, g, h, F, G, H . But we have first

$$\cos f^2 + \cos g^2 + \cos h^2 = 1,$$

or these are the direction cosines of the line drawn from the planet to the pole of the orbit of the satellite.

The triangle XTY gives

$$\cos XY = \cos XT \cos YT + \sin XT \sin YT \cos XTY,$$

and we have $XY = 90^\circ, XTY = F - G,$

hence the values of $\cos XY$, $\cos YZ$, $\cos ZX$ furnish the equations

$$\begin{aligned}\cos (F - G) &= -\cotg f \cotg g \\ \cos (G - H) &= -\cotg g \cotg h \\ \cos (H - F) &= -\cotg h \cotg f\end{aligned}\tag{6}$$

Again the triangle XTY gives

$$\cos f = \sin g \cos T Y X,$$

and from the triangle TYX

$$\sin h \sin Y T Z = \sin T Y Z,$$

but $T Y X - T Y Z = 90^\circ$,

and $Y T Z = -(G - H)$,

hence these equations and similar ones give

$$\begin{aligned}\sin (F - G) &= \frac{\cos h}{\sin f \sin g} \\ \sin (G - H) &= \frac{\cos f}{\sin g \sin h} \\ \sin (H - F) &= \frac{\cos g}{\sin h \sin f}\end{aligned}\tag{7}$$

By combining equations (6) and (7), we have

$$\cotang (F - G) = -\frac{\cos f \cos g}{\cos h}$$

$$\cotang (G - H) = -\frac{\cos g \cos h}{\cos f}$$

$$\cotang (H - F) = -\frac{\cos h \cos f}{\cos g}$$

$$\cos f^2 = \cotg (F - G) \cotg (H - F)$$

$$\cos g^2 = \cotg (G - H) \cotg (F - G)$$

$$\cos h^2 = \cotg (H - F) \cotg (G - H)$$

$$\sin f^2 = -\frac{\cos (G - H)}{\sin (F - G) \sin (H - F)}$$

$$\sin g^2 = -\frac{\cos (H - F)}{\sin (G - H) \sin (F - G)}$$

$$\sin h^2 = -\frac{\cos (F - G)}{\sin (H - F) \sin (G - H)}$$

These six auxiliary quantities are therefore strictly analogous to those which Gauss introduced for computing the position of a planet. For controlling the computation, we have

$$\text{tang } J = \frac{\sin g \sin h \sin (H - G)}{\sin f \cos F},$$

an equation in which each of the six auxiliaries enters into the value of J .

If we introduce another auxiliary quantity, and put the angle

$$TZO = 180^\circ - k,$$

it follows, from the manner adopted for counting an angle of position, that

$$TZO = 180^\circ - (p - k).$$

Denoting the angle between the radius vector and the axis of Z by σ , the spherical triangle TZS gives

$$\begin{aligned} \sin \sigma \sin (p - k) &= \cos (H + u) \\ \sin \sigma \cos (p - k) &= \sin (H + u) \cos h \\ \cos \sigma &= \sin (H + u) \sin h \end{aligned} \quad (8)$$

But we have also

$$\begin{aligned} \rho' \sin s &= r \sin \sigma \\ \rho' \cos s &= r \cos \sigma + \rho, \end{aligned}$$

and by uniting these equations with (8), we can find s and p . This method of finding the distance and the angle of position is due to Marth, and as it is in constant use by him for the very convenient ephemerides of satellites which he publishes, it may be well to consider it further. If we multiply equations (8) by r , and then substitute the values of $r \sin \sigma$ and $r \cos \sigma$ from the last equations, we have

$$\begin{aligned} \rho' \sin s \sin (p - k) &= r \cos (H + u) \\ \rho' \sin s \cos (p - k) &= r \sin (H + u) \cos h \\ \rho' \cos s &= r \sin (H + u) \sin h + \rho \end{aligned} \quad (9)$$

Instead of these exact equations we may use in nearly all known cases of satellites the first two equations and put ρ for ρ' and s for $\sin s$. The equations for use are then

$$\begin{aligned} s \sin (p - k) &= \frac{r}{\rho} \cos (H + u) \\ s \cos (p - k) &= \frac{r}{\rho} \sin (H + u) \cos h \end{aligned} \quad (10)$$

If we express s and r in seconds of arc, and assume that the orbit is circular, $\frac{r}{\rho}$ will be the semi-major axis of the apparent ellipse described by the satellite, and $\frac{r}{\rho} \cos h$ will be the semi-minor axis.

The quantities $\frac{r}{\rho}$, $\frac{r}{\rho} \cos h$, H and k can be tabulated, and equations (10) furnish the easy method of computing s and p which is employed by Marth (Monthly Notices, Royal Astronomical Society.)

For computing k we have from the triangle TZO

$$\sin h \sin k = \cos (a - N) \sin J$$

$$\sin h \cos k = -\sin (a - N) \sin J \sin \delta - \cos J \cos \delta \quad (11)$$

and, also, $\sin h \sin k = -\cos f$

$$\sin h \cos k = -\cos g$$

In what precedes it is assumed that the orbit of the satellite is known. If this orbit is not known the easiest method of proceeding seems to be the following: First, we assume the orbit of the satellite to be a circle, and from the observed angles of position and the observed distances determine the major and minor axes of the apparent ellipse described by the satellite around the planet, and the angle of position of the minor axis. Generally these quantities can be found by a graphical method. The preceding angle k is the angle of position of the minor axis, and $\cos h$ is found from the ratio of the two axes. Then from the triangle TOZ we have the equations

$$\sin J \cos (N - a) = \sin h \sin k$$

$$\sin J \sin (N - a) = \cos h \cos \delta + \sin h \sin \delta \cos k \quad (12)$$

$$\cos J = \cos h \sin \delta - \sin h \cos \delta \cos k$$

With the approximate values of J and N found from these equations we can compute the auxiliary quantities depending on the position of the plane of the orbit and the position of the planet, and can determine the elements belonging to the plane of the orbit. These approximate elements can afterwards be corrected by equations of condition or by other methods.

In work of this kind it is more convenient to have the inclination and node of the orbit referred to the equator, and since these elements are commonly given with respect to the ecliptic we have to transfer them to the equator. If n and i are the node and inclina-

tion referred to the ecliptic, ε the obliquity of the equator, and w the distance from the ecliptic to the equator counted on the orbit, we have the following equations for finding J , N , and w . These equations come from the triangle between the equator, the ecliptic, and the orbit of the satellite. They are similar to those given in the *Theoria Mot.*, Art. 55,

$$\sin \frac{1}{2} J \cos \frac{w - N}{2} = \cos \frac{n}{2} \sin \frac{\varepsilon + i}{2}$$

$$\sin \frac{1}{2} J \sin \frac{w - N}{2} = \sin \frac{n}{2} \sin \frac{\varepsilon - i}{2}$$

$$\cos \frac{1}{2} J \cos \frac{w + N}{2} = \cos \frac{n}{2} \cos \frac{\varepsilon + i}{2}$$

$$\cos \frac{1}{2} J \sin \frac{w + N}{2} = \sin \frac{n}{2} \cos \frac{\varepsilon - i}{2}$$

For the inverse problem of finding i , N , and w from J , N , and ε , we have from the same triangle

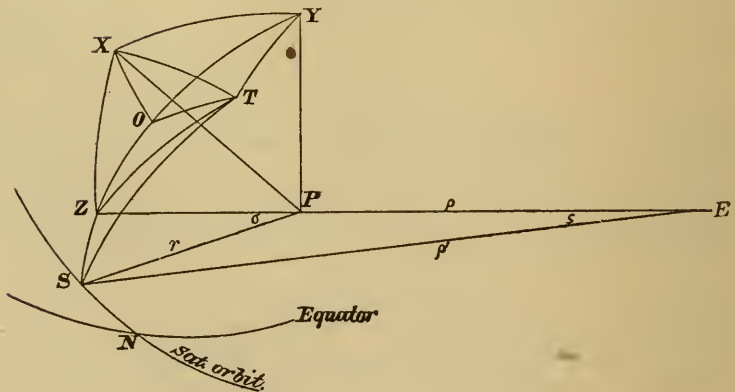
$$\cos \frac{1}{2} i \cos \frac{n - w}{2} = \cos \frac{N}{2} \cos \frac{J - \varepsilon}{2}$$

$$\cos \frac{1}{2} i \sin \frac{n - w}{2} = \sin \frac{N}{2} \cos \frac{J + \varepsilon}{2}$$

$$\sin \frac{1}{2} i \cos \frac{n + w}{2} = \cos \frac{N}{2} \sin \frac{J - \varepsilon}{2}$$

$$\sin \frac{1}{2} i \sin \frac{n + w}{2} = \sin \frac{N}{2} \sin \frac{J + \varepsilon}{2}$$

POSITION OF A SATELLITE.



$$\begin{aligned}
 TX = f, \quad OTX = F, \quad OT = J, \quad STZ = 90^\circ - (H + u) \\
 TY = g, \quad OTY = G, \quad OY = \delta, \quad TZO = 180^\circ - k \\
 TZ = h, \quad OTZ = H, \quad OZ = 90^\circ - \delta, \quad TZS = 180^\circ - (p - k) \\
 NS = u, \quad NOZ = a - N, \quad TOZ = 90^\circ + (a - N), \quad SZO = 360^\circ - p \\
 TOX = TOY + 90 = 180^\circ - (a - N)
 \end{aligned}$$

N is the pole of OT , $\therefore NOT = NTO = 90^\circ$

In response to a question, Mr. HALL said that in computations of orbits of double stars, as little reliance should be placed upon measures of distance as possible. Variations of angular velocity are far safer.

Mr. G. W. HILL made a communication on

A FORMULA FOR THE LENGTH OF A SECONDS-PENDULUM,

which is published in full in the Astronomical Papers of the American Ephemeris, Vol. III, Part 2, Chapter V.

13TH MEETING.

MARCH 26, 1884.

The Chairman presided.

Fourteen members present.

Mr. ALEX. S. CHRISTIE made a communication on

A FORM OF THE MULTINOMIAL THEOREM.

This communication is reserved by the author. Remarks were made by Mr. HILL.

Mr. R. S. WOODWARD gave a

DISCUSSION OF A CONCRETE PROBLEM IN HYDROSTATICS
PROPOSED BY MR. G. K. GILBERT.

Remarks on this communication were made by Mr. GILBERT.

Mr. C. H. KUMMELL gave the first part of a communication on

THE QUADRIC TRANSFORMATION OF ELLIPTIC INTEGRALS,

which was unfinished when the hour of adjournment arrived.

14TH MEETING.

MAY 7, 1884.

The Chairman presided.

Nine members present.

In the absence of the Secretary, the minutes were read by Mr. CHRISTIE.

Mr. KUMMEL finished the paper begun by him at last meeting on

THE QUADRIC TRANSFORMATION OF ELLIPTIC INTEGRALS,
COMBINED WITH THE ALGORITHM OF THE
ARITHMETICO-GEOMETRIC MEAN.

[Abstract.]

The algorithm of the arithmetico-geometric mean, so remarkable for its symmetry and convenience, was first used by Gauss many years before the brilliant era of Abel and Jacobi. The form which the theory of elliptic functions assumed under the hands of these eminent geometers, though extremely beautiful, might be improved from a practical point of view by a combination with the Gaussian algorithm. In the attempt to do this, the defects of the usual notation became very annoying, and gradually the new, simple, and consistent system of notations, as used in the following, resulted:

I assume for the type of an integral of the first species,

$$u = \int_0^{\varphi} \frac{ad\varphi}{\sqrt{a^2 - c^2 \sin^2 \varphi}} = \int_0^{\varphi} \frac{ad\varphi}{\sqrt{a^2 \cos^2 \varphi + b^2 \sin^2 \varphi}}$$

$$= \int_0^{\varphi} \frac{d\varphi}{\sqrt{1 - \gamma^2 \sin^2 \varphi}} = \int_0^{\varphi} \frac{d\varphi}{\sqrt{\cos^2 \varphi + \beta^2 \sin^2 \varphi}} = \varphi\gamma \quad (1)$$

For the inverse of this I write $u - \gamma = \varphi$. (2)

By (1) we have the modulus $\gamma = \frac{c}{a}$ and the complementary modulus $\beta = \frac{b}{a}$. The letters γ and β are used throughout as symbols for $\frac{c}{a}$ and $\frac{b}{a}$, respectively, and are expressed in a , b , and c whenever required.

In the theory of elliptic functions, $\sin amu$, $\cos amu$, Δamu (Jacobi's notation) or snu , cnu , dnu (Gudermann's notation), the elliptic quadrant K (Jacobi) is the numerical unit of their period. Consistency requires the use of the quadrant as a unit for trigonometric functions also. Let \int denote a circular quadrant (ordinarily denoted $\frac{\pi}{2}$); then we have, by the notation just explained,

$$\int_0^{\int} \frac{d\varphi}{\sqrt{1 - \gamma^2 \sin^2 \varphi}} = \int \gamma (= K \text{ of Jacobi}). \quad (3)$$

The complementary integral then

$$\int_0^{\int} \frac{d\varphi}{\sqrt{1 - \gamma^2 \sin^2 \varphi}} = \int \beta (= K' \text{ of Jacobi}). \quad (4)$$

If n is an integer, then, and only then, $(n \int) \gamma = n \int \gamma$. (5)

Thus we should be careful in distinguishing between integrals such as

$$\left(\frac{1}{2} \int\right) \gamma = \int_0^{\frac{1}{2} \int} \frac{d\varphi}{\sqrt{1 - \gamma^2 \sin^2 \varphi}} \text{ and } \frac{1}{2} \int \gamma = \frac{1}{2} \int_0^{\int} \frac{d\varphi}{\sqrt{1 - \gamma^2 \sin^2 \varphi}}$$

According to the system of notation just explained, it is unnecessary to use the Jacobian am or the Gudermannian n , neither of which define the functional relation completely, and we write simply

$$\sin \varphi = \sin u_{-\gamma} (= \sin amu \text{ of Jacobi or } \operatorname{snu} \text{ of Gudermann})$$

$$\cos \varphi = \cos u_{-\gamma} (= \cos amu \text{ of Jacobi or } \operatorname{cnu} \text{ of Gudermann})$$

$$\sqrt{1 - \gamma^2 \sin^2 \varphi} = \Delta \varphi = \Delta u_{-\gamma} (= \Delta amu \text{ of Jacobi or } \operatorname{dnu} \text{ of Gudermann}) \quad (6)$$

I remark that none of the usual notations indicate the modulus, and a grave objection to Gudermann's is that it is apt to give the impression that snu and cnu are not an ordinary sine and cosine. I shall now give in this notation a number of well-known relations, of which use will be made hereafter. The theorem of addition is, if u and v are two integrals to the modulus γ ,

$$\begin{aligned}\sin(u \pm v)_{-\gamma} &= \sin u_{-\gamma} \cos v_{-\gamma} \Delta v_{-\gamma} \pm \sin v_{-\gamma} \cos u_{-\gamma} \Delta u_{-\gamma} \\ &\quad \div 1 - \gamma^2 \sin^2 u_{-\gamma} \sin v_{-\gamma} \\ \cos(u \pm v)_{-\gamma} &= \cos u_{-\gamma} \cos v_{-\gamma} \mp \sin u_{-\gamma} \Delta u_{-\gamma} \sin v_{-\gamma} \Delta v_{-\gamma} \\ &\quad \div 1 - \gamma^2 \sin^2 u_{-\gamma} \sin v_{-\gamma} \\ \Delta(u \pm v)_{-\gamma} &= \Delta u_{-\gamma} \Delta v_{-\gamma} \mp \gamma^2 \sin u_{-\gamma} \cos u_{-\gamma} \sin v_{-\gamma} \cos v_{-\gamma} \\ &\quad \div 1 - \gamma^2 \sin^2 u_{-\gamma} \sin v_{-\gamma}\end{aligned}\quad (7)$$

We have

$$\begin{aligned}\sin(\pm _)\gamma &= \pm 1 \\ \cos(\pm _)\gamma &= 0 \\ \Delta(\pm _)\gamma &= \beta\end{aligned}\quad (8)$$

therefore, replacing v by $_ \gamma$, we have

$$\begin{aligned}\sin(u \pm _)\gamma &= \pm \frac{\cos u_{-\gamma}}{\Delta u_{-\gamma}} \\ \cos(u \pm _)\gamma &= \pm \beta \frac{\sin u_{-\gamma}}{\Delta u_{-\gamma}} \\ \Delta(u \pm _)\gamma &= \frac{\beta}{\Delta u_{-\gamma}}\end{aligned}\quad (9)$$

Replacing in these u by $u \pm _ \gamma$, we have

$$\begin{aligned}\sin(u \pm 2 _)\gamma &= -\sin u_{-\gamma} \\ \cos(u \pm 2 _)\gamma &= -\cos u_{-\gamma} \\ \Delta(u \pm 2 _)\gamma &= \Delta u_{-\gamma}\end{aligned}\quad (10)$$

It follows, replacing in these u by $u + 2 _ \gamma$, that $4 _ \gamma$ is the complete period of the elliptic sine and cosine and $2 _ \gamma$ that of the delta.

Placing $u = v$, we have the duplication formulæ:

$$\begin{aligned}\sin(2u)_{-\gamma} &= 2 \sin u_{-\gamma} \cos u_{-\gamma} \Delta u_{-\gamma} \div 1 - \gamma^2 \sin^4 u_{-\gamma} \\ \cos(2u)_{-\gamma} &= \cos^2 u_{-\gamma} - \sin^2 u_{-\gamma} \Delta^2 u_{-\gamma} \div 1 - \gamma^2 \sin^4 u_{-\gamma} \\ \Delta(2u)_{-\gamma} &= \Delta^2 u_{-\gamma} - \gamma^2 \sin^2 u_{-\gamma} \cos^2 u_{-\gamma} \div 1 - \gamma^2 \sin^4 u_{-\gamma}\end{aligned}\quad (11)$$

Replacing in these u by $\frac{1}{2} u$ and solving, we have the dimidia-tion formulæ:

$$\begin{aligned}\sin^2\left(\frac{u}{2}\right)_{-\gamma} &= 1 - \cos u_{-\gamma} \quad \div 1 + \Delta u_{-\gamma} \\ \cos^2\left(\frac{u}{2}\right)_{-\gamma} &= \Delta u_{-\gamma} + \cos u_{-\gamma} \quad \div 1 + \Delta u_{-\gamma} \\ \Delta^2\left(\frac{u}{2}\right)_{-\gamma} &= \beta^2 + \Delta u_{-\gamma} + \gamma^2 \cos u_{-\gamma} \div 1 + \Delta u_{-\gamma}\end{aligned}\quad (12)$$

Jacobi's imaginary transformation consists in assuming

$$\sin \varphi = i \tan \psi$$

or
$$\cos \varphi = \frac{1}{\cos \psi}$$

or
$$\Delta \varphi = \frac{1}{\cos \psi} \sqrt{1 - \beta^2 \sin^2 \psi} = \frac{1}{\cos \psi} \Delta (\psi \beta)_{-\gamma} \quad (13)$$

then
$$u = \int_0^\varphi \frac{d\varphi}{\Delta \varphi} = i \int_0^\psi \frac{d\psi}{\sqrt{1 - \beta^2 \sin^2 \psi}}$$

or
$$u = \varphi \gamma = i \psi \beta \quad (14)$$

therefore, by (13),

$$\sin u_{-\gamma} = i \tan \left(\frac{u}{i} \right)_{-\beta} = \frac{1}{i} \tan (ui)_{-\beta}$$

$$\cos u_{-\gamma} = \frac{1}{\cos \left(\frac{u}{i} \right)_{-\beta}} = \frac{1}{\cos (ui)_{-\beta}}$$

$$\Delta u_{-\gamma} = \frac{1}{\cos \left(\frac{u}{i} \right)_{-\beta}} \Delta \left(\frac{u}{i} \right)_{-\beta} = \frac{1}{\cos (ui)_{-\beta}} \Delta (ui)_{-\beta} \quad (15)$$

Using these relations in (7), we obtain the following formulæ for elliptic functions, with complex arguments and complementary moduli:

$$\sin (u \pm vi)_{-\gamma} = \sin u_{-\gamma} \Delta v_{-\beta} \pm i \cos u_{-\gamma} \Delta u_{-\gamma} \sin v_{-\beta} \cos v_{-\beta} \\ \div 1 - \Delta^2 u_{-\gamma} \sin^2 v_{-\beta}$$

$$\cos (u \pm vi)_{-\gamma} = \cos u_{-\gamma} \cos v_{-\beta} \mp i \sin u_{-\gamma} \Delta u_{-\gamma} \sin v_{-\beta} \Delta v_{-\beta} \\ \div 1 - \Delta^2 u_{-\gamma} \sin^2 v_{-\beta}$$

$$\Delta (u \pm vi)_{-\gamma} = \Delta u_{-\gamma} \cos v_{-\beta} \Delta v_{-\beta} \mp \gamma^2 i \sin u_{-\gamma} \cos u_{-\gamma} \sin v_{-\beta} \\ \div 1 - \Delta^2 u_{-\gamma} \sin^2 v_{-\beta} \quad (16)$$

We have

$$\sin (_ \beta)_{-\beta} = 1$$

$$\cos (_ \beta)_{-\beta} = 0$$

$$\Delta (_ \beta)_{-\beta} = \gamma \quad (17)$$

therefore, replacing in (16) v by $_|\beta$, we have

$$\begin{aligned}\sin (u \pm _|\beta i)_{-\beta} &= \frac{1}{\gamma \sin u_{-\gamma}} \\ \cos (u \pm _|\beta i)_{-\beta} &= \mp i \frac{\Delta u_{-\gamma}}{\gamma \sin u_{-\gamma}} \\ \Delta (u \pm _|\beta i)_{-\beta} &= \mp i \cot u_{-\gamma}\end{aligned}\quad (18)$$

Placing in these $u \pm _|\beta i$ for u , we have

$$\begin{aligned}\sin (u \pm 2 _|\beta i)_{-\gamma} &= \sin u_{-\gamma} \\ \cos (u \pm 2 _|\beta i)_{-\gamma} &= -\cos u_{-\gamma} \\ \Delta (u \pm 2 _|\beta i)_{-\gamma} &= -\Delta u_{-\gamma}\end{aligned}\quad (19)$$

It follows, replacing in these u by $u \pm 2 _|\beta i$, that $4 _|\beta i$ is the imaginary period of the elliptic cosine and delta and $2 _|\beta i$ that of the sine. We have then, if m and μ are integers,

$$\begin{aligned}\sin (u + 4 m _|\gamma + 2 \mu _|\beta i)_{-\gamma} &= \sin u_{-\gamma} \\ \cos (u + 4 m _|\gamma + 4 \mu _|\beta i)_{-\gamma} &= \cos u_{-\gamma} \\ \Delta (u + 2 m _|\gamma + 4 \mu _|\beta i)_{-\gamma} &= \Delta u_{-\gamma}\end{aligned}\quad (20)$$

The general problem of transformation may be stated thus: Assuming

$$\int_0^{\varphi} \frac{d\varphi}{\sqrt{a^2 - c^2 \sin^2 \varphi}} = \int_0^{\varphi'} \frac{d\varphi'}{\sqrt{a'^2 - c'^2 \sin^2 \varphi'}} \text{ or } \frac{1}{a} \varphi_{\gamma} = \frac{1}{a'} \varphi'_{\gamma'} \quad (21)$$

then it is required to discover the relations between the given quantities φ , a , γ and φ' , a' , γ' .

Before treating of the special subject of this paper (the quadric transformation), a short exposition of some important points of the general problem of transformation, slightly modified from Abel (see Enneper's *Elliptische Functionen*, page 239-246), will be given.

We have, by (21),

$$\sin \varphi = \sin \left(\frac{a}{a'} \varphi'_{\gamma'} \right)_{-\gamma} = f(\sin \varphi') = f \left\{ \sin \left(\frac{a'}{a} \varphi_{\gamma} \right)_{-\gamma'} \right\} \quad (22)$$

where f denotes the unknown relation between $\sin \varphi$ and $\sin \varphi'$.

But we have, by (20),

$$\begin{aligned} & \sin (\varphi' \gamma' + 4 m' _ \gamma' + 2 \mu' _ \beta' i) _ \gamma' \\ &= \sin \left\{ \frac{\alpha'}{\alpha} (\varphi \gamma + 4 m _ \gamma + 2 \mu _ \beta i) \right\} _ \gamma' \end{aligned} \quad (23)$$

therefore,
$$m' _ \gamma' = \frac{\alpha'}{\alpha} m _ \gamma \quad (24)$$

$$\mu' _ \beta' = \frac{\alpha'}{\alpha} \mu _ \beta \quad (25)$$

$$\therefore \frac{\alpha'}{\alpha} = \frac{m'}{m} \cdot \frac{_ \gamma'}{_ \gamma} = \frac{\mu'}{\mu} \cdot \frac{_ \beta'}{_ \beta}$$

and
$$\frac{m'}{\mu'} \cdot \frac{_ \gamma'}{_ \beta'} = \frac{m}{\mu} \cdot \frac{_ \gamma}{_ \beta}$$

Anticipating here the definition of the highly important constant, the nome q , which is such a prominent feature in the brilliant researches of Jacobi and Abel, we have

$$q = e^{-2 \frac{_ \beta}{_ \gamma}} \quad (26)$$

and the nome q' of the transformed integral is

$$q' = e^{-2 \frac{_ \beta'}{_ \gamma'}} _ \beta' = e^{-2 \frac{m' \mu _ \beta}{\mu' m _ \gamma}} _ \beta' = q \frac{m' \mu}{\mu' m} \quad (27)$$

Thus it appears that the nomes of the given and transformed integrals are in a relation

$$q^n = q'^{n'}$$

where n and n' are integers, and, if $n = 1$ and $n' = 2$, we have the quadric transformation.

Landen's transformation consists in assuming

$$\sin (2\varphi' - \varphi) = \frac{c}{a} \sin \varphi \quad (28)$$

which is Legendre's convenient form for computing the amplitude φ' . Differentiating, we have

$$(2d\varphi' - d\varphi) \cos (2\varphi' - \varphi) = \frac{c}{a} \cos \varphi d\varphi$$

or
$$\frac{d\varphi}{a \Delta \varphi} = \frac{d\varphi'}{\frac{1}{2} (a \Delta \varphi' + c \cos \varphi')} \quad (29)$$

Solving for φ , we have

$$\tan \varphi = \frac{a \sin 2\varphi'}{c + a \cos 2\varphi'} = \frac{a \tan \varphi'}{a' - b' \tan^2 \varphi'} \quad (30)$$

$$\sin \varphi = \frac{2a \sin \varphi' \cos \varphi'}{\sqrt{a^2 + 2ac \cos 2\varphi' + c^2}} = \frac{a \sin \varphi' \cos \varphi'}{a' \Delta \varphi'} \quad (31)$$

$$\cos \varphi = \frac{c + a \cos 2\varphi'}{2a' \Delta \varphi'} = \frac{1}{c} \left(a' \Delta \varphi' - \frac{b'}{\Delta \varphi'} \right) \quad (32)$$

$$\Delta \varphi = \frac{1}{a} \left(a' \Delta \varphi' + \frac{b'}{\Delta \varphi'} \right) \quad (33)$$

where we have placed

$$\begin{aligned} \frac{1}{2}(a+c) &= a'; \quad \frac{1}{2}(a-c) = b'; \\ \sqrt{ac} &= c'; \quad \sqrt{a^2 - c^2 \sin^2 \varphi'} = a' \Delta \varphi' \end{aligned} \quad (34)$$

From (32) and (33) follows

$$a' \Delta \varphi' = \frac{1}{2} (a \Delta \varphi + c \cos \varphi) \quad (35)$$

$$\frac{b'}{\Delta \varphi'} = \frac{1}{2} (a \Delta \varphi - c \cos \varphi) \quad (36)$$

and (29) becomes
$$\frac{d\varphi}{a \Delta \varphi} = \frac{d\varphi'}{a' \Delta \varphi'} \quad (37)$$

the integral is
$$\frac{1}{a} \varphi \gamma = \frac{1}{a'} \varphi' \gamma' \quad (38)$$

The first and third formula of (34) give the first step in the algorithm of the arithmetico-geometric mean, and the first two follow from (35) and (36) by placing $\varphi = 0 = \varphi'$, *i. e.*, they are relations at the lower limit of the integrals, corresponding to (35) and (36).

Assuming
$$\sin(2\varphi'' - \varphi') = \frac{c'}{a'} \sin \varphi' \quad (28')$$

$$a'' = \frac{1}{2}(a' + c'); \quad b'' = \frac{1}{2}(a' - c'); \quad c'' = \sqrt{a' c'} \quad (34')$$

then we have
$$\frac{1}{a} \varphi \gamma = \frac{1}{a'} \varphi' \gamma' = \frac{1}{a''} \varphi'' \gamma'' \quad (38')$$

Proceeding in this manner the amplitudes will very rapidly reach a limit $\varphi^{(\infty)}$, while simultaneously a and c tend to become equal to their common limit, the arithmetico-geometric mean of a and c . Gauss, when investigating its functional properties, denotes

this by $M(a, c)$; elsewhere he uses the notation $a^{(\infty)}$ or $c^{(\infty)}$, which is sufficiently distinct for our purpose.

At the limit we have $a^{(\infty)} \Delta \varphi^{(\infty)} = c^{(\infty)} \cos \varphi^{(\infty)}$, therefore,

$$\frac{1}{a} \varphi \gamma = \frac{1}{a'} \varphi' \gamma' = \frac{1}{a''} \varphi'' \gamma'' = \dots \dots \frac{1}{a^{(\infty)}} \varphi^{(\infty)}$$

$$\left(= \int_0^{\varphi^{(\infty)}} \frac{d\varphi^{(\infty)}}{c^{(\infty)} \cos \varphi^{(\infty)}} = \frac{1}{c^{(\infty)}} \tan \frac{1}{2} (_ _ + \varphi^{(\infty)}) \right) \quad (38^{(\infty)})$$

Let $\varphi = _ _$ then $\varphi' = _ _'$; $\varphi'' = _ _'' \dots \dots \varphi^{(\infty)} = _ _^{(\infty)}$ and

$$\frac{1}{a} _ _ \gamma = \frac{1}{a'} _ _ \gamma' = \frac{1}{a''} _ _ \gamma'' = \dots \dots \frac{1}{a^{(\infty)}} _ _ \gamma^{(\infty)}$$

$$\left(= \frac{1}{c^{(\infty)}} \tan \frac{1}{2} (_ _ + _ _^{(\infty)}) \right) \quad (39^{(\infty)})$$

This transformation can be applied also to the more general form:

$$I = \int_0^{\varphi} \frac{d\varphi}{a \Delta \varphi} f(\sin \varphi, \cos \varphi, \Delta \varphi) \quad (40)$$

for if, simultaneously to the above algorithm, we express $\sin \varphi, \cos \varphi, \Delta \varphi$ in terms of $\sin \varphi', \cos \varphi', \Delta \varphi'$, and these again in terms of $\sin \varphi'', \cos \varphi'', \Delta \varphi''$, etc., by means of (31), (32), (33), we arrive, after a few transformations, at the form

$$I = \int_0^{\varphi^{(\infty)}} \frac{d\varphi^{(\infty)}}{c^{(\infty)} \cos \varphi^{(\infty)}} f^{(\infty)}(\sin \varphi^{(\infty)}, \cos \varphi^{(\infty)}) \quad (41)$$

which is an elementary form if $f(\sin \varphi, \cos \varphi, \Delta \varphi)$ is rational with respect to $\sin \varphi, \cos \varphi, \Delta \varphi$.

In tracing this process backwards, the quantities may be distinguished at the several steps by subprimes, so that we have, at the first backward step,

$$\sin(2\varphi - \varphi_i) = \frac{c_i}{a_i} \sin \varphi_i = \frac{a - b}{a + b} \sin \varphi_i \quad (28_i)$$

$$a = \frac{1}{2} (a_i + c_i); \quad b = \frac{1}{2} (a_i - c_i); \quad c = \sqrt{a_i c_i} \quad (34_i)$$

Adding, and then also subtracting, $\sin \varphi_i$ from (28_i) and dividing the difference by the sum, we have the following convenient formula, also given by Legendre:

$$\tan(\varphi_i - \varphi) = \frac{b}{a} \tan \varphi \quad (42)$$

Solving (34) for a, b, c , we have

$$a = a + b; \quad b = 2\sqrt{ab}; \quad c = a - b$$

In order to have again the convenient algorithm of the arithmetico-geometric mean, it is preferable to assume

$$a_1 = \frac{1}{2} a, \quad b_1 = \frac{1}{2} (a + b); \quad b_1 = \frac{1}{2} b, \quad c_1 = \sqrt{ab}; \quad c_1 = \frac{1}{2} c, \quad c_1 = \frac{1}{2} (a - b) \quad (43)$$

For the second step assume

$$\tan(\varphi_{II} - \varphi_I) = \frac{b_1}{a_1} \tan \varphi_I \quad (42)$$

$$a_2 = \frac{1}{2} (a_1 + b_1); \quad b_2 = \sqrt{a_1 b_1}; \quad c_2 = \frac{1}{2} (a_1 - b_1) \quad (43)$$

$$\text{We have then} \quad \frac{1}{a} \varphi_\gamma = \frac{1}{2a_1} (\varphi_I)_{\gamma_1} = \frac{1}{2^2 a_2} (\varphi_{II})_{\gamma_2} \quad (44)$$

Continuing this process, which diminishes the modulus, and is therefore called descending the scale of moduli, while the above is called ascending, the a and b will rapidly approach their arithmetico-geometric mean, $a_\infty = b_\infty$, while $\frac{1}{2^n} \varphi^{(n)}$ tends towards a limit which I shall denote ψ_∞ . The limiting form of the integral is

$$\int_0^{\varphi^{(\infty)}} \frac{d\varphi^{(\infty)}}{2^\infty b_\infty} = \frac{\psi_\infty}{b_\infty}$$

and we have

$$\frac{1}{a} \varphi_\gamma = \frac{1}{2a_1} (\varphi_I)_{\gamma_1} = \frac{1}{2^2 a_2} (\varphi_{II})_{\gamma_2} = \dots = \frac{1}{2^\infty a_\infty} (\varphi_\infty)_\infty \quad \left(= \frac{\psi_\infty}{b_\infty} \right) \quad (44^{(\infty)})$$

$$\text{If } \varphi = \perp \text{ then } \frac{1}{2} \varphi_I = \frac{1}{2^2} \varphi_{II} = \dots = \frac{1}{2^n} \varphi^{(n)} = \dots = \perp$$

and we have

$$\frac{1}{a} \perp_\gamma = \frac{1}{a_1} \perp_{\gamma_1} = \frac{1}{a_2} \perp_{\gamma_2} = \dots = \frac{1}{a_\infty} \perp_\infty \quad \left(= \frac{1}{b_\infty} \perp \right) \quad (45^{(\infty)})$$

This remarkable value for the complete integral was discovered by Gauss by means of a different transformation, known as Gauss'. This may be deduced as follows: Assume in place of (44^(∞)) the following series of relations

$$\frac{1}{a} \varphi_\gamma = \frac{1}{a_1} (\psi_1)_{\gamma_1} = \frac{1}{a_2} (\psi_2)_{\gamma_2} = \dots = \frac{1}{a_\infty} (\psi_\infty)_\infty \quad \left(= \frac{1}{b_\infty} \psi_\infty \right) \quad (44_\infty)$$

To discover the relations for the first step we have to determine ψ_1 from the equations

$$(\psi_1)_{\gamma_1} = \frac{1}{2}(\varphi)_{\gamma_1} = \frac{a_1}{a} \varphi_{\gamma} \quad (46)$$

Place in (12) $u = (\varphi)_{\gamma_1}$, then $\frac{1}{2} u = (\psi_1)_{\gamma_1}$ and $u_{-\gamma_1} = \varphi; \left(\frac{u}{2}\right)_{-\gamma_1} = \psi_1$, and consequently

$$\begin{aligned} \sin^2 \psi_1 &= 1 - \cos \varphi, & \div 1 + \Delta \varphi, \\ \cos^2 \psi_1 &= \Delta \varphi + \cos \varphi, & \div 1 + \Delta \varphi, \\ \Delta^2 \psi_1 &= \beta_1^2 + \Delta \varphi + \gamma_1^2 \cos \varphi, & \div 1 + \Delta \varphi, \end{aligned} \quad (47)$$

From (32) and (33) we derive with due regard to (43)

$$\begin{aligned} a_1 \Delta \varphi &= \frac{1}{2} \left(a \Delta \varphi + \frac{b}{\Delta \varphi} \right) \\ c_1 \Delta \varphi &= \frac{1}{2} \left(a \Delta \varphi - \frac{b}{\Delta \varphi} \right) \end{aligned} \quad (48)$$

and eliminating φ , from (47) by means of (48) there result the relations

$$\begin{aligned} \sin^2 \psi_1 &= \frac{a_1}{c_1} \cdot \frac{1 - \Delta \varphi}{1 + \Delta \varphi} \\ \cos^2 \psi_1 &= \frac{a \Delta \varphi - b}{c_1 (1 + \Delta \varphi)} \\ \Delta^2 \psi_1 &= \frac{a \Delta \varphi + b}{a_1 (1 + \Delta \varphi)} \end{aligned} \quad (49)$$

whence also

$$\begin{aligned} \sin \varphi &= \frac{a \sin \psi_1}{a_1 + c_1 \sin^2 \psi_1} \\ \cos \varphi &= \frac{a_1 \cos \psi_1 \Delta \psi_1}{a_1 + c_1 \sin^2 \psi_1} \\ \Delta \varphi &= \frac{a_1 - c_1 \sin^2 \psi_1}{a_1 + c_1 \sin^2 \psi_1} \end{aligned} \quad (50)$$

This is Gauss' transformation. For practical use it is far less convenient than that given above.

Instead of (46) we might have assumed -

$$m(\theta_1)_{\gamma_1} = n(\varphi)_{\gamma_1} = 2n \frac{a_1}{a} \varphi_{\gamma} \quad (m \text{ and } n \text{ integers}) \quad (51)$$

For any special values of m and n we can express, by means of

the addition theorem, the elliptic functions of $\{m(\theta_1)\gamma_1\}_{-\gamma_1}$ in terms of those of θ_1 , and in the same manner those of $\{n(\varphi)\gamma_1\}_{-\gamma_1}$ in terms of those of φ . Since we know φ in terms of θ_1 , we can eliminate φ , and obtain a relation between θ_1 and φ , which would be a new transformation. However, we need not expect to discover in this manner any substitution sufficiently simple for practical use.

The substitutions given above may of course be applied also to the complementary integral, and, since interesting relations will be thus discovered, I place the different series of forms together for comparison.

$$\begin{aligned} \frac{1}{a} \varphi\gamma &= \frac{1}{a'} \varphi'\gamma' = \frac{1}{a''} \varphi''\gamma'' = \dots = \frac{1}{a^{(\infty)}} \varphi_1^{(\infty)} \\ &\left(= \frac{1}{c^{(\infty)}} l \tan \frac{1}{2} (_ _ + \varphi^{(\infty)}) \right) \\ &= \frac{1}{2a_1} (\varphi_1)\gamma_1 = \frac{1}{2^2 a_2} (\varphi_2)\gamma_2 = \dots = \frac{1}{a_\infty} \lim \frac{\varphi^{(n)}}{2^n} \\ &\left(= \frac{1}{b_\infty} \psi_\infty \right) \\ &= \frac{1}{a_1} (\psi_1)\gamma_1 = \frac{1}{a_2} (\psi_2)\gamma_2 = \dots = \frac{1}{a_\infty} (\psi_\infty)_0 \\ &\left(= \frac{1}{b_\infty} \psi_\infty \right) \tag{52\gamma} \end{aligned}$$

$$\begin{aligned} \frac{1}{a} \varphi\beta &= \frac{1}{a_1} (\varphi_1)\beta_1 = \frac{1}{a_2} (\varphi_2)\beta_2 = \dots = \frac{1}{a_\infty} (\varphi_\infty)_1 \\ &\left(= \frac{1}{b_\infty} l \tan \frac{1}{2} (_ _ + \varphi_\infty) \right) \\ &= \frac{1}{2a_1} (\varphi_{-1})\beta' = \frac{1}{2^2 a''} (\varphi_{-2})\beta'' = \dots = \frac{1}{a^{(\infty)}} \lim \frac{\varphi_{-n}}{2^n} \\ &\left(= \frac{1}{c^{(\infty)}} \psi^{(\infty)} \right) \\ &= \frac{1}{a'} \psi'\beta' = \frac{1}{a''} \psi''\beta'' = \dots = \frac{1}{a^{(\infty)}} \psi_0^{(\infty)} \\ &\left(= \frac{1}{c^{(\infty)}} \psi^{(\infty)} \right) \tag{52\beta} \end{aligned}$$

$$\frac{1}{a} _ _ \gamma = \frac{1}{a'} _ _ \gamma' = \frac{1}{a''} _ _ \gamma'' = \dots = \frac{1}{a^{(\infty)}} _ _ 1^{(\infty)}$$

$$\begin{aligned} & \left(= \frac{1}{c^{(\infty)}} l \tan \frac{1}{2} (_ _ + _ _^{(\infty)}) \right. \\ & = \frac{1}{a_1} _ _ \gamma_1 = \frac{1}{a_2} _ _ \gamma_2 = \dots = \frac{1}{b_\infty} _ _ \quad (53\gamma) \\ \frac{1}{a} _ _ \beta & = \frac{1}{a_1} (_ _)_1 \beta_1 = \frac{1}{a_2} (_ _)_2 \beta_2 = \dots = \frac{1}{b_\infty} (_ _^{(\infty)})_1 \\ & \left(= \frac{1}{b_\infty} l \tan \frac{1}{2} (_ _ + _ _^\infty) \right. \\ & = \frac{1}{a'} _ _ \beta' = \frac{1}{a''} _ _ \beta'' = \dots = \frac{1}{c^{(\infty)}} _ _ \quad (53\beta) \end{aligned}$$

We easily deduce the symmetrical relations

$$\varphi_1^{(\infty)} (\varphi_\infty)_1 = \psi_\infty \psi^{(\infty)} \quad (54)$$

$$_ _ 1^{(\infty)} (_ _^\infty)_1 = _ _ ^2 \quad (55)$$

This last equation is well known ; it appears here, however, as a particular case of a more general relation. The quantity ψ_∞ is the argument of the θ functions and then usually denoted x ; $\varphi_1^{(\infty)}$ is then denoted by x' ; Schellbach has $\frac{\nu}{2}$ for $(_ _)_1$ and $\frac{\nu'}{2}$ for $(_ _^{(\infty)})_1$, while Hoüel, in his Recueil de Tables, has ρ and ρ' , respectively.

Other relations are

$$\frac{\varphi_1^{(\infty)}}{_ _ 1^{(\infty)}} = \frac{\psi_\infty}{_ _}; \frac{\varphi_1^{(\infty)}}{_ _} = \frac{\psi_\infty}{(_ _^\infty)_1}; \frac{\varphi_1^{(\infty)^2}}{_ _ 1^{(\infty)}} = \frac{\varphi_1^{(\infty)} \psi_\infty}{_ _} = \frac{\psi_\infty^2}{(_ _^\infty)_1} \quad (56)$$

$$\frac{(\varphi_\infty)_1}{(_ _^\infty)_1} = \frac{\psi^{(\infty)}}{_ _}; \frac{(\varphi_\infty)_1}{_ _} = \frac{\psi^{(\infty)}}{_ _ 1^{(\infty)}}; \frac{(\varphi_\infty)_1^2}{(_ _^\infty)_1} = \frac{(\varphi_\infty)_1 \psi^{(\infty)}}{_ _} = \frac{\psi^{(\infty)^2}}{_ _ 1^{(\infty)}} \quad (57)$$

The following expressions for the nome q can now be given :

$$\begin{aligned} q & = e^{-2 \frac{_ _ \beta}{_ _ \gamma} _ _} = e^{-2 (_ _^\infty)_1} \\ & = e^{-2 \frac{b_\infty}{c^{(\infty)}} _ _} = e^{-2 \frac{b_\infty}{a} _ _ \beta} \quad (58) \end{aligned}$$

The first form is simply Jacobi's definition ; the second gives, since

$$(_ _^\infty)_1 = l \tan \frac{1}{2} (_ _ + _ _^\infty) \quad (59)$$

$$q = \cot^2 \frac{1}{2} (_ _ + _ _^\infty) \quad (60)$$

This is one of the best formulæ for computing q , especially if the modulus does not differ much from unity. The third form may be

used if b and c are not very different, for in that case the algorithm of the arithmetico-geometric mean converges equally fast in both directions. If either b or c is very near to a , the process may converge in one direction so slowly that the formula becomes nearly inapplicable.

The fourth form may be transformed to a new formula, which is more convenient than any given. In (52β) place $\varphi = 2^n _$, then, since

$$\begin{aligned}\varphi_1 &= 2^{n-1} _ ; \varphi_2 = 2^{n-2} _ ; \varphi_3 = 2^{n-3} _ \dots \\ \varphi_n &= _ ; \varphi_{n+1} = (2^n _)_{n+1} \dots\end{aligned}$$

we have

$$\begin{aligned}\frac{2^n}{a} _ \beta &= \frac{2^{n-1}}{a_2} _ \beta_1 = \frac{2^{n-2}}{a_2} _ \beta_2 = \dots \\ &= \frac{1}{a_n} _ \beta_n = \frac{1}{a_{n+1}} \left\{ (2^n _)_{n+1} \right\} \beta_{n+1} \quad (61)\end{aligned}$$

$$\text{But we have by (28)} \quad \sin (2(2^n _)_{n+1} - _) = \frac{b_n}{a_n} \sin _$$

$$\text{or} \quad 2 \sin^2 (2^n _)_{n+1} - 1 = \frac{b_n}{a_n}$$

$$\therefore \sin (2^n _)_{n+1} = \sqrt{\frac{1}{2} \left(1 + \frac{b_n}{a_n} \right)}$$

If we suppose $a_n = b_n = b_\infty$ within the precision of the computation, c_n will be very small, yet not zero. We have then

$$\begin{aligned}\frac{1}{a^\infty} _ \beta_n &= \frac{1}{a_{n+1}} \left\{ (2^n _)_{n+1} \right\} \beta_{n+1} \\ &= \frac{1}{a_{n+1}} l \tan \frac{1}{2} (_ + (2^n _)_{n+1}) \\ &= \frac{1}{a_{n+1}} l \sqrt{\frac{1 + \sin (2^n _)_{n+1}}{1 - \sin (2^n _)_{n+1}}} \\ &= \frac{1}{a_{n+1}} l \sqrt{\frac{1 + \sqrt{\frac{1}{2} \left(1 + \frac{b_n}{a_n} \right)}}{1 + \sqrt{\frac{1}{2} \left(1 + \frac{b_n}{a_n} \right)}}}\end{aligned}$$

$$\begin{aligned}
 &= \frac{1}{a_{n+1}} l \frac{1 + \sqrt{\frac{1}{2} \left(1 + \frac{b_n}{a_n}\right)}}{\sqrt{\frac{1}{2} \left(1 - \frac{b_n}{a_n}\right)}} \\
 &= \frac{1}{b_\infty} l \frac{2 \sqrt{a_n}}{\sqrt{\frac{1}{2} (a_n - b_n)}} \quad (\text{sufficiently near}) \\
 &= \frac{1}{b_\infty} l \frac{2^2 \sqrt{a_n a_{n+1}}}{c_n} \quad (\text{sufficiently near}) \\
 &= \frac{1}{b_\infty} l \frac{2^2 a_n}{c_n} \quad (\text{sufficiently near}) \quad (62)
 \end{aligned}$$

therefore we have by (61)

$$\frac{1}{a} \lrcorner \beta = \frac{2^{-n}}{b_\infty} l \frac{2^2 a_n}{c_n}$$

or $\frac{b_\infty}{a} \lrcorner \beta = l \left(\frac{2^2 a_n}{c_n}\right) 2^{-n}$

$$l \left(2^2 a_n \cdot \frac{2^2 a_n}{c_{n-1}^2}\right) 2^{-n} = l \left(\frac{2^2 a_n}{c_{n-1}}\right) 2^{-n+1}$$

since $c_n = \frac{1}{2} (a_{n-1} - b_{n-1}) = \frac{c_{n-1}^2}{2^2 a_n}$

$$= l \left(2^2 a_n \cdot \frac{2^2 a_{n-1}}{c_{n-2}^2}\right) 2^{-n+1} = l \left(\frac{2^2 a_{n-1}}{c_{n-2}}\right) 2^{-n+2}$$

if $a_{n-1} = \sqrt{a_n a_{n-1}}$

$$= l \left(2^2 a_{n-1} \cdot \frac{2^2 a_{n-2}}{c_{n-3}^2}\right) 2^{-n+2} = l \left(\frac{2^2 a_{n-2}}{c_{n-3}}\right) 2^{-n+3}$$

if $a_{n-2} = \sqrt{a_{n-1} a_{n-2}}$

$$= l \left(2^2 a_3 \cdot \frac{2^2 a_2}{c_1^2}\right) 2^{-2} = l \left(\frac{2^2 a_2}{c_1}\right) 2^{-1}$$

if $a_2 = \sqrt{a_3 a_2}$ (63)

$$= l \left(2^2 a_2 \cdot \frac{2^2 a_1}{c^2}\right) 2^{-1} = l \left(\frac{2^2 a_1}{c}\right)$$

if $a_1 = \sqrt{a_2 a_1}$ (64)

Using (63) in the fourth form of (58) we have

$$q = \frac{c_1}{2^2 a_2} = \frac{a-b}{2^3 a_2} \tag{65}$$

and using (64) we have

$$q = \left(\frac{c}{2^2 a_1} \right)^2 \tag{66}$$

The nome of the complementary integral is denoted by Jacobi and writers that follow him by q' . In our system this would be the notation for the nome of the integral $\varphi'\gamma'$; q'' that for $\varphi''\gamma''$, etc; also q_1 that of $(\psi_1)\gamma_1$; q_2 of $(\psi_2)\gamma_2$, etc. It is therefore better to follow the example of Broch, who denotes the nome of the complementary integral by p . We have then

$$\begin{aligned} p &= e^{-2 \frac{\lfloor \gamma \rfloor}{\lfloor \beta \rfloor}} = e^{-2 \lfloor 1 \rfloor^{(\infty)}} = e^{-2 \frac{c^{(\infty)}}{b_{\infty}}} \lfloor \rfloor \\ &= \cot^2 \frac{1}{2} (\lfloor \rfloor + \lfloor \rfloor^{(\infty)}) = \frac{a-c}{2^2 a''} = \left(\frac{b}{2^2 a'} \right)^2 \end{aligned} \tag{67}$$

where

$$\begin{aligned} a^{(n-1)} &= \sqrt{a^{(n)} a^{(n-1)}} \\ a^{(n-2)} &= \sqrt{a^{(n-1)} a^{(n-2)}} \\ a^{(n-3)} &= \sqrt{a^{(n-2)} a^{(n-3)}} \\ &\dots \dots \dots \\ a'' &= \sqrt{a''' a''} \\ a' &= \sqrt{a'' a'} \end{aligned} \tag{68}$$

By (55) and the second forms of (58) and (67) we have the following relation between p and q

$$lp^{-\frac{1}{2}} lq^{-\frac{1}{2}} = \lfloor \rfloor^2 \tag{69}$$

or in Briggsian logarithms

$$\log \{ \log p^{-\frac{1}{2}} \log q^{-\frac{1}{2}} \} = \log (\lfloor \rfloor \log e)^2 = 9.6678034 \tag{69'}$$

or $\log \{ \log p^{-1} \log q^{-1} \} = 0.2698684 \tag{70}$

By means of this relation we can always choose the shortest route to either p or q . It is easy to see that the nomes and com-

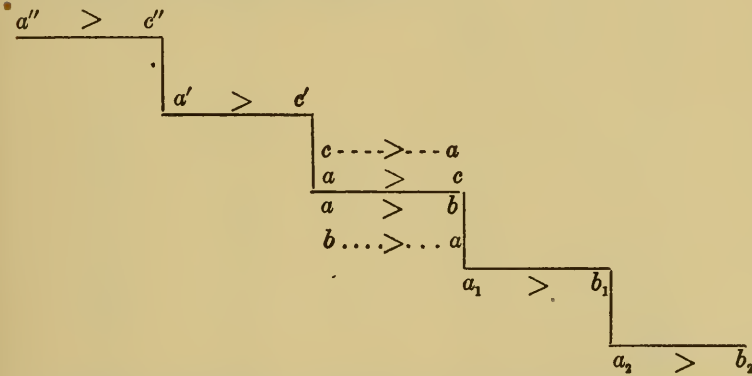
plementary nomes at the several steps of the modular scale are as follows

$$q_n = q^{2^{-n}} \dots q_2 = q^{2^{-2}} ; q_1 = q^{2^{-1}} \quad q = q ; q' = q^2 ; q'' = q^{2^2} \dots q^{(n)} = q^{2^n} \tag{71}$$

$$p_n = p^{2^n} \dots p_2 = p^{2^2} ; p_1 = p^2 ; p = p ; p' = p^2 ; p'' = p^{2^2} \dots p^{(n)} = p^{2^n} \tag{72}$$

We have then in this transformation the simplest possible case of Abel's theorem (27); and because in ascending we pass to the square of the nome, it is called the quadric transformation.

The ascending transformation is possible in real quantities if $c > a$, for we have $M(c, a) = M(a, c)$. Also if $b > a$ we can use the descending transformation; and in either case we can, after one transformation, proceed in either direction. This may be symbolized by the following diagram



In order to exhibit the practical nature of the formulæ given, I shall make the necessary computations for the integral

$$u = \int_0^\varphi \frac{dy}{\sqrt{1 - \sin^2 75^\circ \sin^2 \varphi}}$$

if $\varphi = 70^\circ$ and also for the complete integral.

Because $\gamma = \sin 75^\circ$ is $> \sqrt{\frac{1}{2}}$ we must use the ascending transformation. The computation for $70^\circ_{\sin 75^\circ}$ may be conveniently arranged as follows:

$\alpha = 1$	$\log c = 9.9849438$	$\varphi = 70^{\circ}00'00''.00$	$\log \sin \varphi = 9.9729858$
$c = 0.9659258$	$\log a = 0.0000000$	$2\varphi' - \varphi = 65\ 11\ 08.84$	$\log \sin (2\varphi' - \varphi) = 9.9579296$
$a' = 0.9829629$	$\log e' = 9.9924719$	$\varphi' = 67\ 35\ 34.42$	$\log \sin \varphi' = 9.9659063$
	$\log a' = 9.9925371$	$2\varphi'' - \varphi' = 67\ 34\ 19.33$	$\log \sin (2\varphi'' - \varphi') = 9.9658411$
$\log e^{(\infty)} = \log e'' = 9.9925045$		$\varphi^{(z)} = \varphi'' = 67\ 34\ 56.88$	$\log \tan \frac{1}{2} (_) + \varphi^{(z)} = 0.7029746$
		$\frac{1}{2} (_) + \varphi^{(\infty)} = 78\ 47\ 28.44$	$\log \log \tan \frac{1}{2} (_) + \varphi^{(\infty)} = 9.8469397$
			$-\log \log e = -9.6377843$
			$-\log e^{(\infty)} = -9.9925045$
			$\log 70^{\circ} \sin 75^{\circ} = 0.2166509$

The computation of $_ \sin 75^{\circ}$ by this process requires exactly the same amount of computation.

(By 53 γ) and (67), we have

$$\frac{1}{a} _ y = \frac{1}{e^{(\infty)}} _ _ 1^{(\infty)} = \frac{1}{e^{(\infty)}} l p^{-1/2} = \frac{1}{e^{(\infty)}} l \sqrt{\frac{2^3 a''}{a-c}} l \frac{2^3 a'}{e^{(\infty)}} l \frac{2^3 a'}{b} \quad (73)$$

We compute then the complementary nome and from that the complete integral is found easily.

$$\begin{array}{r}
 -\log a'' = -9.9925045 \\
 -\log 2^2 = -0.9030900 \\
 a - c = 0.0340742 \qquad \log(a - c) = 8.5324257
 \end{array}$$

$$\begin{array}{r}
 \log p = 7.6368312 \\
 \log p^{-1/2} = 1.1815844
 \end{array}$$

Computation of $\int_{\sin 75^\circ}$

$$\begin{array}{r}
 \log \log p^{-1/2} = 0.0724648 \\
 -\log \log e = -9.6377843 \\
 -\log e^{(\infty)} = -9.9925045
 \end{array}$$

$$\log \int_{\sin 75^\circ} = 0.4421760$$

This method is far more simple than by amplitudes.

The computation of the same integral by the descending scale will now be shown, though it is longer in this case, and therefore less accurate.

$a = 1$ $b = 0.2588190$	$\log b = 9.4129962$ $\log a = 0.0000000$	$\varphi = 70^{\circ}00'00.00$ $\varphi - \varphi = 35\ 24\ 59.80$	$\log \tan \varphi = 0.4389341$ $\log \tan (\varphi - \varphi) = 9.8519303$
$a_1 = 0.6294095$ $b_1 = 0.5087425$	$\log b_1 = 9.7064981$ $\log a_1 = 9.7989333$	$\varphi' = 105\ 24\ 59.80$ $\varphi' - \varphi' = 108\ 50\ 16.04$	$\log \tan \varphi' = 0.5594721_n$ $\log \tan (\varphi' - \varphi') = 0.4670369_n$
$a_2 = 0.5690760$ $b_2 = 0.5658687$	$\log b_2 = 9.7527157$ $\log a_2 = 9.7551704$	$\varphi'' = 214\ 15\ 15.84$ $\varphi'' - \varphi'' = 214\ 06\ 14.04$	$\log \tan \varphi'' = 9.8331396$ $\log \tan (\varphi'' - \varphi'') = 9.8306850$
$a_3 = 0.5674724$	$\log b_3 = 9.7539430$ $\log a_3 = 9.7539447$	$\varphi''' = 428\ 21\ 29.88$ $\varphi''' - \varphi''' = 428\ 21\ 29.60$	$\log \tan \varphi''' = 0.4014610$ $\log \tan (\varphi''' - \varphi''') = 0.4014593$
$\log b_{\infty} = \log b_4 = 9.7539439$	$\varphi^{(\infty)} = \varphi_{iv} = 856\ 42\ 59.48$ $\varphi_{\infty} = 53\ 32\ 41.22$ $= 192761.22$		$\log \psi_{\infty} = 5.2850197$ $\log \arcsin 1'' = 4.6855749$ $-\log b_{\infty} = -9.7539439$
			$\log 70^{\circ} \sin 75^{\circ} = -0.2166507$ $\log \sphericalangle = 0.1961199$ $-\log b_{\infty} = -9.7539439$
			$\log \sphericalangle \sin 75^{\circ} = 0.4421760$

Computation of $\sphericalangle \sin 75^{\circ}$

The computation of the nome q stands thus :

$$\begin{array}{r} \log a_3 = 9.7539441 \\ \hline - \log a_3 = - 9.7545572 \\ - \log 2^3 = - 0.9030900 \\ a - b = 0.7411810 \quad \log a - b = 9.8699243 \\ \hline \log q = 9.2122771 \end{array}$$

To check by (70), we have

$$\begin{array}{r} \log p^{-1} = 2.3631688 \quad \log \log p^{-1} = 0.3734948 \\ \log q^{-1} = 0.7877229 \quad \log \log q^{-1} = 9.8963735 \end{array}$$

$$0.2698683$$

The above incomplete sketch is, I hope, sufficient to show the practical advantages from the introduction of the algorithm of the arithmetico-geometric mean into the theory of elliptic functions.

Mr. HALL spoke of the importance of the arithmetico-geometric mean in astronomy.

Mr. W. B. TAYLOR made a communication on

A CASE OF DISCONTINUITY IN ELLIPTIC ORBITS

around an empty center of gravitative force. Diminution of the minor axis of the attracted body's path (the major axis being constant) increases the ratio of distance at the two apses without limit, the "periapsis" continually approaching the attractive center, as long as the minor axis has a value, however small. But when this axis is made to vanish, and the motion is directly to the center of force, the body, instead of rebounding from it, as continuity would require, will pass through it, and describe an equal path on the opposite side, the orbit being at once doubled.

This paper was discussed by Messrs. BATES, CHRISTIE, HALL and others, and brought out a wide diversity of view as to the demeanor of a heavy point when coincident with an empty attracting center.

15TH MEETING.

DECEMBER 3, 1884.

The Chairman presided.

Nineteen members and guests present.

Mr. M. H. DOOLITTLE made a communication on

THE VERIFICATION OF PREDICTIONS.

[Abstract.]

Mr. G. K. Gilbert has published (*American Meteorological Journal*, 8°, *Detroit*; September, 1884, pp. 166-172) a method of estimating the ratio of skill in predictions of occurrences and non-occurrences of a simple event. Adopting his notation, we have

s = the sum or total number of cases,

o = the number of occurrences,

p = the number of predictions of occurrences,

c = the number of coincidences or verifications,
 i = the inference-ratio, or that part of the success which is due to skill and not to chance, and which may be called the *degree of logical connection* between event and prediction.

Since success is proportional to each of the two fractions

$$\frac{c}{o} \text{ and } \frac{c}{p},$$

it may be represented by their product

$$\frac{c^2}{op}.$$

The fraction $\frac{o}{s}$ represents the ratio of random success, and therefore $\frac{op}{s}$ verifications out of p predictions are to be ascribed to chance and must be subtracted throughout. The remainders,

$$o - \frac{op}{s} \text{ and } p - \frac{op}{s},$$

represent fields which chance leaves for science to conquer; and

$$c - \frac{op}{s}$$

represents the portion of each which science does conquer. Hence

$$i = \frac{c - \frac{op}{s}}{o - \frac{op}{s}} \times \frac{c - \frac{op}{s}}{p - \frac{op}{s}} = \frac{(cs - op)^2}{op(s - o)(s - p)}.$$

By another method,

$\frac{c}{o}$ = the probability that any single occurrence will be predicted in some manner.

$\frac{p - c}{s - o}$ = the probability that any single date of non-occurrence will correspond to an unsuccessful prediction = the general probability of unskillful prediction in any case.

Subtract from the probability that any single occurrence will be predicted in some manner the general probability of unskillful prediction, and we have

$\frac{c}{o} - \frac{p - c}{s - o}$ = the probability that any given occurrence will be skillfully predicted.

In like manner

$\frac{c}{p}$ = the probability that any single prediction will be fulfilled in some manner.

$\frac{o-c}{s-p}$ = the general probability of unpredicted occurrence; which, in case of prediction, becomes probability of fortuitous fulfillment.

$\frac{c}{p} - \frac{o-c}{s-p}$ = the probability that any single prediction will be fulfilled by reason of a logical connection.

Since the skillful predictions are mingled indistinguishably with all the unskillful ones, and are vitiated accordingly, the value of the *vitiated* probability of the skillful prediction of any single occurrence may be represented by the product

$$i = \left(\frac{c}{o} - \frac{p-c}{s-o} \right) \times \left(\frac{c}{p} - \frac{o-c}{s-p} \right) = \frac{(cs - op)^2}{op(s-o)(s-p)},$$

as before.

Prof. C. S. Peirce (in *Science*, 1884, Nov. 14, Vol. IV, page 453) deduces the first of these factors as the unqualified value of *i*, making no allowance for the vitiation, and tacitly assuming that an assortment of predictions is the logical equivalent of a jumble of the same predictions. He obtains his result by the aid of the supposition that part of the predictions are made by an infallible prophet, and the others by a man ignorant of the future. If Prof. Peirce had called on omnipotence instead of omniscience, and supposed the predictions to have been obtained from a Djinn careful to fulfill a portion of them corresponding to the data, the remainder of the occurrences being produced by an unknown Djinn at random, he would have obtained by parallel reasoning the second factor, $\left(\frac{c}{p} - \frac{o-c}{s-p} \right)$. These Djinns represent, respectively, the known and unknown forces of nature, and gauge the prophet's knowledge with principal reference to the proportion of predictions fulfilled. Prof. Peirce's test refers principally to the proportion of occurrences predicted. His test eliminates sins of omission; the other, sins of commission; and both are necessary to a proper estimate of the prophet's comparative rectitude.

In the data cited by Mr. Gilbert from Finley's tornado predictions, $s = 2803$, $o = 51$, $p = 100$, and $c = 28$. By Mr. Gilbert's formula,

$$i = \frac{cs - op}{s(o + p - c) - op}$$

he obtains

$$i = .216.$$

Prof. Peirce obtains

$$i = .523.$$

I obtain

$$i = .142.$$

By making s , o , and i constant, and imposing conditions on p and c , we may obtain hypothetical data involving equal skill. Putting $c = p$, I infer that Mr. Finley would have manifested equal skill if he had made no false predictions of tornadoes, and, out of the 51, had predicted 7.35. Mr. Gilbert's formula gives 11.18, and Prof Peirce's 26.67. Putting $c = o$, I infer that he would also have manifested equal skill if he had included all the 51 tornadoes by making 323.7 predictions. Mr. Gilbert's formula gives 221.5, and Prof. Peirce's 1364.

Mr. Finley's entire success in predicting tornadoes is

$$\frac{c^2}{op} = .154;$$

and since the portion due to skill = .142, we may infer that .923 of this success is due to skill, and only .077 to chance. On the other hand, of his success in predicting the non-occurrence of tornadoes, only .147 is due to skill, and .853 is due to chance.

Prophecy and fulfillment are effects of a common cause. Neither causes the other. The problem, broadly stated, requires a numerical expression for the causal relation between two classes of phenomena either in co-existence or in sequence, when the presence of one corresponds sometimes to the presence and sometimes to the absence of the other, and sometimes both are absent. In case of sequence it is immaterial which is antecedent. The quantities denoted by o and p should therefore be interchangeable.

My formula responds properly to every test proposed by Mr. Gilbert. The value of i increases rapidly with that of c , and

slowly with that of s , diminishes with increase of o or p , and varies between the limits 0 and 1. Skill in making false predictions is indicated by a negative value of $es - op$; but the same degree of causal relation exists as when equal skill is employed in making true predictions; and a negative value of i can never occur. When

$s =$ either p or o , $i = \frac{0}{0}$; but the apparent indeterminateness van-

ishes when we consider that i is the product of two factors, of which one = 0 and the other is indeterminate within limits. And the value of i is unaltered when predictions of non-occurrences are substituted for those of occurrences, and *vice versa*. In the latter case, write $s - o$ for o , $s - p$ for p , and $s - o - p + c$ for c ; and the formula reduces to its original form.

In addition to Mr. Gilbert's tests, two others may be considered. In the case of predictions all falsely reported, we may write $s - p$ for p and $o - c$ for c ; and the formula becomes

$$i = \frac{(op - cs)^2}{op(s - o)(s - p)},$$

with a proper reversal of signs in the quantity under the exponent and no change in the value of i .

If occurrences always appear whenever they are not predicted, and never appear when they are predicted, we put $c = 0$ and $p = s - o$, with the result

$$i = 1;$$

or the logical connection is perfect.

In order that the general formula shall be properly applicable, care must be taken that the predictions are fairly homogeneous in definiteness of time and space. For illustration: if predictions that phenomena will occur in given months are examined indiscriminately with those that they will occur on given days, the result will be manifestly worthless.

It has been proposed to extend the problem so as to include three or more classes of events of which one must happen and only one can happen in any case. It seems clear to me that no single numerical expression can be a proper solution of such a problem. Suppose the three classes of events, A, B, and C. By the method above given A and Not A may be examined; and all instances

involving either the prediction or occurrence of A may be excluded and B and C separately investigated. Suppose it thus ascertained that great skill has been shown in discriminating between A and Not A, and little or none in discriminating between B and C. No single numerical expression can properly comprehend these heterogeneous results.

Mr. CURTIS showed that some of the results given by Mr. Doolittle could be independently deduced by another method.

Mr. GILBERT noted as a defect in the formula proposed by Prof. Peirce, that it did not duly discourage positive predictions of rare events; and, while gratified with Mr. Doolittle's discussion of the subject, he expressed a disappointment that no satisfactory decision as to the treatment of cases of three or more alternatives had been reached by him.

After some further discussion, a communication by Mr. M. BAKER was called, but postponed, on motion of Mr. H. FARQUHAR, to allow time for the consideration of a testimonial to a late associate, Mr. ALVORD.

Mr. E. B. ELLIOTT read the following tribute, prepared by Mr. BAKER and himself:

MEMORIAL.

The Mathematical Section of the Philosophical Society of Washington, having suffered the loss by death, on October 16th, 1884, of General BENJAMIN ALVORD, one of its founders and active workers, desires to place on record this testimonial to his worth and to the loss to this Section and to science by his death.

Of his worth, one of America's greatest mathematicians has said that he was a scientist of "real originality who had actually extended the boundaries of science."

The bent of General Alvord's mind and studies was early directed towards a purely geometrical solution of the general problem of tangencies, and his reward, which it is our pleasure to chronicle, was success.

Of his mathematical publications, the following is submitted as a provisionally complete list:

LIST OF MATHEMATICAL PUBLICATIONS BY GENERAL BENJAMIN ALVORD.

1. The tangencies of circles and of spheres.
[*In* Smithsonian Contributions to Knowledge. 4°. Washington, 1856, Vol. 8, Article 4, 16 pp., 9 plates.]
Also issued separately.
2. On the interpretation of imaginary roots in questions of maxima and minima.
[*In* The Mathematical Monthly. 4°. New York, 1860, April, Vol. 2, No. 7, pp. 237-240.]
3. Tangencies.
[*In* Johnson's New Universal Cyclopædia. 8°. New York, 1878, Vol. 4, pp. 723-4.]
4. Mortality in each year among the officers of the army for fifty years, from 1824 to 1873, as derived from the army registers.
[*In* Proceedings of the American Association for the Advancement of Science, 23d Meeting, Hartford, August, 1874. 8°. Salem, 1875, pp. 57-59.]
5. The intersection of circles and the intersection of spheres.
[*In* American Journal of Mathematics. 4°. Baltimore, 1882, March, Vol. 5, No. 1, pp. 25-44; 4 plates.]
6. Curious fallacy as to the theory of gravitation.
[*In* Bulletin of the Philosophical Society of Washington. 8°. Washington, 1883, Vol. 5, pp. 85-88.]
7. A special case in maxima and minima.
[*In* Bulletin of the Philosophical Society of Washington. 8°. Washington, 1884, Vol. 6, p. 149.]

Mr. M. BAKER, in moving the adoption of this memorial by the Section, said :

General Alvord's entire life was that of the soldier, and his routine of life work did not call him in the direction of mathematical study. Hence whatever he accomplished in mathematics or literature was accomplished in military surroundings and with only such facilities as barrack and camp life afford. If under these

conditions the total of his contributions to science appears small, we should bear in mind that any contribution under such circumstances is exceptional. And to have been able, therefore, to make even a single contribution to human knowledge is to have done that which few men in any generation do and that of which any one of us might well be proud.

General Alvord early became interested in the problem of tangencies and intersections of circles, and his chief mathematical work and fame rests on his complete and purely geometrical solution of the various problems relating to this subject. His chief writings on this subject consist of the paper on Tangencies, in the Smithsonian Contributions in 1856; the article on Tangencies, in Johnson's New Universal Cyclopædia; and the paper on intersections, in the American Journal of Mathematics, March, 1882.

The memorial was adopted, and the Secretary was instructed to send a copy of it to the family of the deceased.

NOTE.

The following members have assisted the Chairman and Secretary in the examination of abstracts of communications to the Mathematical Section :

<i>Title.</i>	<i>Author.</i>	<i>Third Member.</i>
The Problem of the Knight's Tour	G. K. GILBERT.	E. B. ELLIOTT.
Formulæ for Diminution of Amplitude of a Pendulum -----	H. FARQUHAR.	A. S. CHRISTIE.
The Formulæ for Computing the Position of a Satellite -----	A. HALL.	C. H. KUMMELL.
The Quadric Transformation of Elliptic Integrals -----	C. H. KUMMELL.	G. W. HILL.
The Verification of Predictions ----	M. H. DOOLITTLE.	M. BAKER.



INDEX.

	Page.
Abbe, Cleveland: remarks on deflection of rivers.....	23
— report as Treasurer.....	xxiv
Address of the President.....	xxix, 81
Alaska river mouths.....	24
Alvord, Gen. Benjamin, Death of.....	72
— Memorial to.....	127
Antisell, Thomas: remarks on the chemical elements.....	16
— — — pumice.....	20, 26
Annual address.....	xxix, 81
— meeting.....	81
Application of physical methods to intellectual science.....	18
Are there separate centres for light-form and color-perception?.....	72
Aristotle, cited on atoms.....	xxxii
Atomic philosophy.....	40
— — The, physical and metaphysical.....	xxix, 81
Auditing committee, Appointment of.....	82
— — Report of.....	15
Babcock, Gen. O. E., Death of.....	72
Bacon, cited on atoms.....	xli
Baker, Marcus: memorial to General Alvord.....	127
Barnard, W. S., Election to membership of.....	25
Bates, H. H.: communication on the physical basis of phenomena.....	40
Bean, T. H., Election to membership of.....	72
Bibliography of North American geology.....	71
— — mathematical papers by Benjamin Alvord.....	128
Billings, J. S.: communication on composite photography applied to craniology... ..	25
— exhibition of microscopes.....	73
— remarks on bibliography.....	72
— resolutions on the death of Dr. Woodward.....	75
Blair, H. W., Death of.....	81
— Election to membership of.....	15
Bogosloff, Volcanic dust from.....	34
Boutelle, C. E., Election to membership of... ..	18
— remarks on the deflection of rivers.....	24
Bowles, F. T., Election to membership of.....	26
Boyle, Robert, cited on atoms.....	xlvi
Brown, S. J., Election to membership of.....	72
Brown, W. R., cited on matter.....	31
Bulletin of the General Meeting.....	1, 3
— — — Mathematical Section.....	83, 87
— Rules for publication of.....	xiii

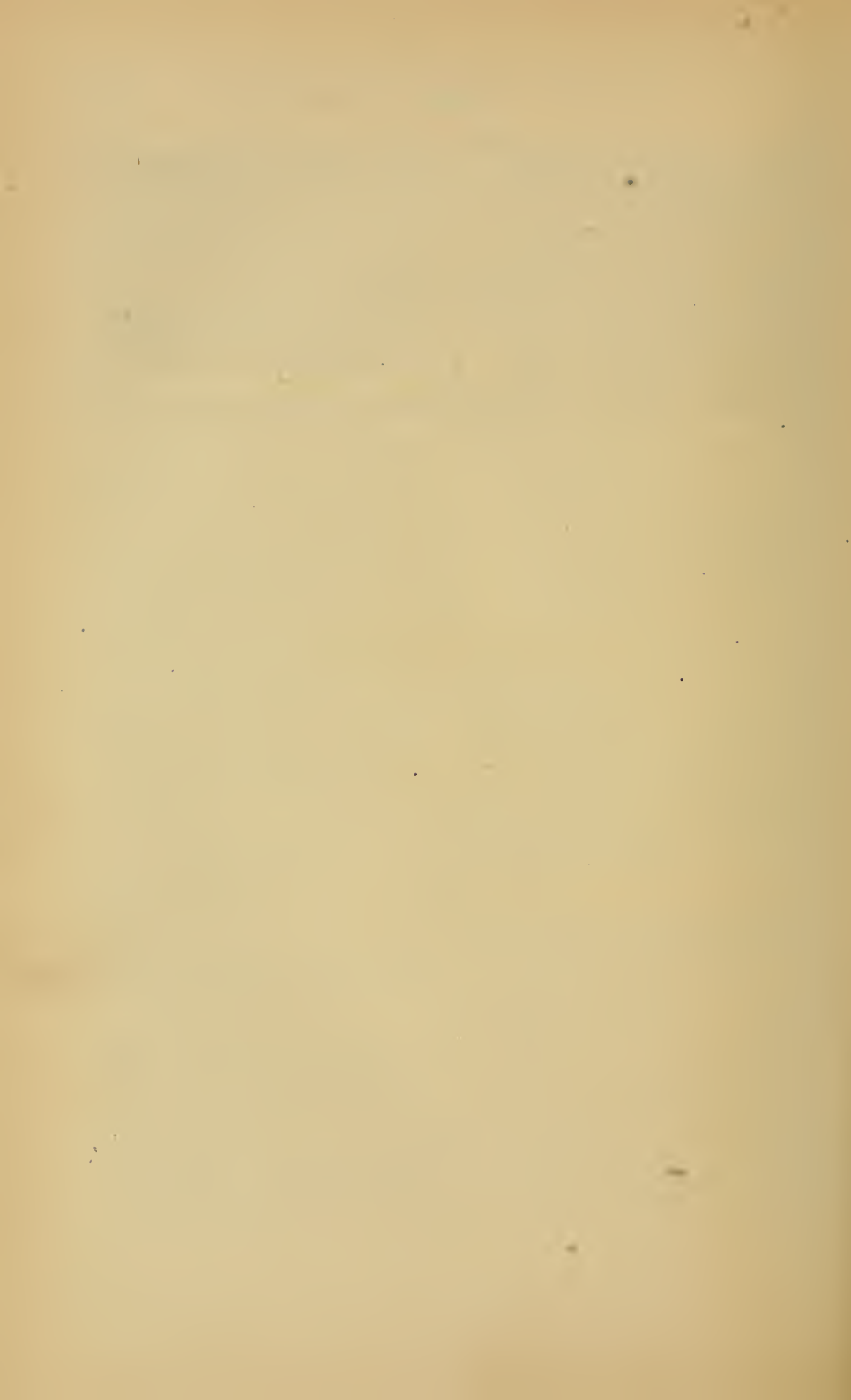
	Page.
Buoys drifted by ocean currents.....	14
Burchard, H. C.: remarks on the irrigation of the upper Missouri valley.....	20
Burnet, S. M.: communication on separate centres for light-form and color-perception.....	72
— — — Why the eyes of animals shine in the dark.....	13
Calendar.....	xxii
Case of discontinuity in elliptic orbits.....	122
Chamberlin, T. C.: communication on What is a glacier?.....	38
Chatard, T. M.: analysis of andesite.....	33
Chemical elements and music.....	27
— — Periodic law of.....	15
Cheyne, Dr. George, cited on heredity.....	lv
Christie, A. S.: communication on a form of the multinomial theorem.....	101
Clarke, F. W.: communication on the periodic law of chemical elements.....	15
— election to General Committee.....	36
Clerk-Maxwell, James, cited on properties of matter.....	44, 47
— — — vortex rings.....	liv
Clifford, Prof., cited on mind-stuff.....	liii
Columbian University affords the Society facilities.....	80, 81
Committee, Auditing.....	15, 82
— on communications, Duties of.....	xii, 85
— — — Membership of.....	xiv, xv
— — — publications, Duties of.....	xiii
— — — Membership of.....	xiv, xv
Committees, Standing.....	xii, xiv, xv
Composite photography applied to craniology.....	25
Concrete problem in hydrostatics.....	92, 101
Constitution.....	vii
Continents, Forms of.....	24
Craniology.....	25
Curtis, G. E.: communication on the relations between northerners and magnetic disturbances at Havana.....	25
— election to membership.....	5
— remarks on the verification of predictions.....	127
Curves similar to their evolutes.....	87
Dall, W. H.: communication on certain appendages of the mollusca.....	32

	Page.		Page.
Dall, W. H.: recent advances in our knowledge of the limpets.....	4	Elliott, E. B.: communication on electric lighting.....	80
— — — What is a glacier?.....	38	— memorial to General Alvord.....	127
— remarks on Alaskan volcanoes.....	34	— remarks on the euharmonic organ.....	28
— — — deflection of rivers.....	24	— — — irrigation of the upper Missouri valley.....	20
— — — drifting of buoys.....	15	— — — sun-glows.....	17
— — — tornadoes.....	3	— — — tornadoes.....	3
Dalton, John, contribution to atomic theory.....	xlvii, 1, lvi	Emmons, S. F.: communication on What is a glacier?.....	37
Darwin, cited on gemmules.....	liii	— remarks on glaciers.....	9
Death of Gen. Benjamin Alvord.....	72, 127	Empirical formulæ for the diminution of amplitude of a freely-oscillating pendulum.....	89
— Gen. O. E. Babcock.....	72	Entomology, Economic.....	10
— — H. W. Blair.....	81	Euharmonic organ.....	28
— — Gen. Chas. Ewing.....	xxviii	Ewing, Charles, Death of.....	xxiii
— — Gen. A. A. Humphreys.....	3, 4	Existing glaciers of the High Sierra of California.....	5
— — Dr. J. J. Woodward.....	72	Eyes of animals, why they shine in the dark.....	13
— — — Resolutions concerning.....	75	Faraday cited on the nature of matter.....	47
Deceased members, List of.....	xxiii	Farquhar, Edward: remarks on ocean currents.....	24
Deflection of rivers.....	21	— — — tornadoes.....	3
Deposits of volcanic dust in the Great Basin.....	18	— — — the late Dr. Woodward.....	76
Dewey, F. P., Election to membership of.....	36	Farquhar, Henry: communication on empirical formulæ for the diminution of amplitude of a freely-oscillating pendulum.....	89
Diller, J. S.: communication on the volcanic sand which fell at Unalashka Oct. 20, 1883, and some considerations concerning its composition.....	33, 35	— — — the theoretical discussion in Prof. P. G. Tait's Encyclopædia Britannica article on mechanics.....	29
— Election to membership of.....	21	— election as Secretary of the Mathematical Section.....	87
Discontinuity in elliptic orbits.....	122	— remarks on drifting of buoys.....	15
Discussion of a concrete problem in hydrostatics proposed by Mr. G. K. Gilbert.....	101	— report as Secretary.....	xxiii
Diversion of water-courses by the rotation of the earth.....	21	Ferrel, William, cited on rotational deflection.....	22
Doollittle, M. H.: communication on the verification of predictions.....	122	Finley's tornado predictions.....	125
— — — music and the chemical elements.....	27	Fisheries exhibitions.....	26
Dust, Volcanic.....	18, 33	Force, Reality of.....	30
Dutton, C. E.: communication on the volcanoes and lava fields of New Mexico.....	76	Form of the multinomial theorem.....	101
— — — What is a glacier?.....	39	Formula for the length of a seconds-pendulum.....	101
— remarks on the forms of continents.....	24	Formulæ for computing the position of a satellite.....	93
— — — Navajos as scientific observers.....	74	General Meeting, Bulletin of.....	1, 3
— — — petrography.....	36	Geological section of water-works shaft.....	69, 70
— — — sun-glows.....	35	Gihon, A. L.: remarks on the late Dr. J. J. Woodward.....	76
Earl, R. E., Election to membership of.....	72	Gilbert, G. K.: communication on a concrete problem in hydrostatics.....	92
Earthquake of Sept. 19.....	73	— — — the diversion of water-courses by the rotation of the earth.....	21
Eastman, J. R.: communication on a new meteorite.....	32		
— — — the Rochester (Minn.) tornado.....	3		
Eimbeck, William, Election to membership of.....	26		
Election of officers.....	82, 87		
— — new members.....	xi, 5, 10, 15, 18, 21, 25, 26, 32, 36, 72, 81		
Electric lighting.....	80		
Elements, Periodic law of.....	15		
Elliott, E. B.: calendar for the use of the society.....	xxii		

	Page.		Page.
Gilbert, G. K.: a plan for the subject bibliography of North American geologic literature.....	71	Kerr, M. B., Election to membership of.....	21
— — — the problem of the knight's tour.....	88	— remarks on glaciers.....	8
— remarks on the origin of pumice.....	25	Knight's tour.....	88
— — — upper Missouri valley.....	20	Knox, J. J.: resignation from General Committee.....	36
— — — — verification of predictions.....	127	Kummell, C. H.: communication on curves similar to their evolutes	87
— report as secretary.....	xxiii	— — — the quadric transformation of elliptic integrals, combined with the algorithm of the arithmetico-geometrical mean	102
Glacier tables.....	7	-- remarks on musical intervals.....	28
Glacier, What is a.....	37	Lake Bonneville.....	92
Glaciers of the Coast Range.....	8	Lawrence, William, Election to membership of.....	21
— — — High Sierra.....	5	Lefavour, E. B.: remarks on musical scales.	28
— — — Rocky Mountains.....	8	Leibnitz, cited on atoms.....	xliii
Goode, G. Brown: communication on fisheries exhibitions.....	26	Limpets.....	4
Gregory, J. M., Election to membership of...	26	McGee, W. J.: communication on What is a glacier?.....	38
Hall, Asaph: communication on the formula for computing the position of a satellite.....	93	Maher, J. A.: Election to membership of.....	26
— election as chairman of the Mathematical Section.....	87	Marcou, J. B., Election to membership of...	26
— remarks on the arithmetico-geometric mean	122	Martin, Artemas: letter to Mathematical Section.....	87
Harkness, William: remarks on glaciers.....	9	Mason, O. T.: remarks on the conditions of observation.....	74
— — — the shining of eyes in the dark.....	13	Mathematical Section, Bulletin of.....	83, 87
Hazen, H. A.: communication on the sun-glow.....	17	— — Members of.....	86
— — — thermometer exposure.....	80	— — Officers of.....	86, 87
— remarks on the deflection of rivers.....	24	— society proposed.....	87
Heap, D. P., Election to membership of.....	32	Matthews, Washington: communication on natural naturalists.....	73
High Sierra, Glaciers of	5	— election to membership.....	72
Hill, G. W.: communication on a formula for the length of a seconds-pendulum...	101	Members, List of.....	xvi
Hitchcock, Prof. C. H.....	4	— — — deceased.....	xxiii
Hitchcock, Romy, Election to membership of.....	36	— — — new.....	xxiii
Holmes, W. H.: remarks on glaciers.....	8	— of Mathematical Section.....	86
Humphreys, A. A., Death of.....	3, 4	Memorial to General Alvord.....	127
Ice pyramid.....	6, 7	Merrill, G. P., Election to membership of...	36
Indians, Observation and generalization by.	73	Meteorite	32
Insecticides.....	10	Methods of modern petrography.....	36
Integrals, Transformation of elliptic.....	102	Mica mines of North Carolina	9
Intrinsic equation.....	87	More, Henry, cited on nature of matter.....	xlii
Irrigation of the upper Missouri valley.....	20	Mount Taylor, Geology of.....	77
Jenkins, T. A.: remarks on drifting of buoys.....	15	Muir, John, cited on glaciers.....	8
Johnson, A. B.: communication on some eccentricities of ocean currents.....	14	Murdoch, John, Election to membership of.	36
Johnson, W. D., Election to membership of...	18	Music and the chemical elements.	27
Kauffmann, S. H., Election to membership of.....	21	Mussey, R. D.: communication on the application of physical methods to intellectual science.....	18
Kerr, W. C.: communication on the mica mines of North Carolina.....	9	— remarks on the forms of continents.....	24
	27	Natural naturalists.....	73
		Necks, Volcanic	78
		Névé defined.....	37

	Page.		Page.
New members.....	xxiii	Ricksecker, Eugene, Election to membership of.....	18
— meteorite.....	32	Riley, C. V.: communication on recent advances in economic entomology.....	10
— Mexico, Volcanoes of.....	76	— remarks on the irrigation of the upper Missouri valley.....	20
Newton, cited on atoms.....	xliv	Rivers, deflection of.....	21
Norris, Basil, Election to membership of.....	25	Robinson, Thomas: communication entitled Was the earthquake of Sept. 19 felt in the District of Columbia?.....	73
North Carolina, Mica mines of.....	9	— on the strata exposed in the east shaft of the water-works extension.....	69
Ocean currents.....	14	— election to membership.....	10
Officers, Election of.....	82, 87	— remarks on the deflection of rivers.....	24
— List of.....	xiv, xv	Rochester (Minn.) tornado.....	3
— of the Mathematical Section.....	85, 86, 87	Rotation and rivers.....	21
Ogden, H. G., Election to membership of.....	15	Rules for the publication of the Bulletin... xiii	
Paul, H. M.: remarks on earthquakes.....	73	— of the General Committee.....	xii
— — — equipotential surfaces.....	92	— — — Mathematical Section.....	85
— — — sun-glows.....	35	— — — Society.....	ix
Peirce, Prof. Benjamin, cited on the intrinsic equation.....	87	Russell, I. C.: communication on deposits of volcanic dust in the Great Basin.....	18
Peirce, C. S., cited on pendulum observations.....	90	— — — the existing glaciers of the High Sierra of California.....	5
— — — the verification of predictions.....	124	— — — What is a glacier?.....	37
Pendulum, Formula for diminution of amplitude of oscillation of.....	89	Sand, Volcanic.....	33
Periodic law of chemical elements.....	15	Satellite, Computation of position of a.....	93
Petrographic methods.....	36	Scales, Musical.....	27
Physical basis of phenomena.....	40	Secretaries' report.....	xxiii, 82
— and economic features of the upper Missouri system.....	20	Sierra Nevada glaciers.....	5
Plan for the subject bibliography of North American geologic literature.....	71	Some eccentricities of ocean currents.....	14
Plateau country.....	76, 79	Standing rules of the General Committee.....	xii
Powell, J. W.: communication on a plan for the subject bibliography of North American geologic literature.....	71	— — — Mathematical Section.....	85
— remarks on the distribution of eruptions.....	79	— — — Society.....	ix
— — — glaciers.....	8	Stearns, R. E. C., Election to membership of.....	81
— — — the history of the society.....	81	Strata exposed in the east shaft of the water-works extension.....	69
— — — late Dr. Woodward.....	76	Sun-glows.....	17, 35
Predictions, Verification of.....	122	Tait, Prof. P. G., on mechanics; reviewed... 29	
Presidential address.....	xxix	Taylor, F. W.: analysis of meteorite.....	32
Problem of the knight's tour.....	88	Taylor, W. B.: communication on a case of discontinuity in elliptic orbits.....	122
Pumice, Formation of.....	20, 25, 26	— remarks on sun-glows.....	35
Quadric transformation of elliptic integrals, combined with the algorithm of the arithmetico-geometric mean.....	102	Thermometer exposure.....	80
Ray, P. H., Election to membership of.....	5	Thompson, Gilbert, Election to membership of.....	18
Recent advances in economic entomology... 10		— remarks on glaciers.....	8
— — — our knowledge of the limpets.....	4	Toner, J. M.: remarks on the late Dr. Woodward.....	76
Relation between northers and magnetic disturbances at Havana.....	25	Tornado at Rochester (Minn.).....	3
Report of secretaries.....	xxiii, 82	Treasurer's report.....	xxiv, 15, 82
— — — treasurer.....	xxiv, 15, 82	Verification of predictions.....	122
Review of the theoretical discussion of Prof. P. G. Tait's Encyclopædia Britannica article on mechanics.....	29	Volcanic dust.....	18, 33

	Page.		Page.
Ward, L. F. : communication on some physical and economic features of the upper Missouri system.....	20	White, C. H., Election to membership of....	21
— remarks on the deflection of rivers.....	23	White, C. A. : report of auditing committee.	15
— — — Indians as botanic observers.....	74	Why the eyes of animals shined in the dark.....	13
Was the earthquake of Sept. 19 felt in the District of Columbia?.....	73	Woodruff, T. M., Election to membership of.....	32
Welling, J. C. : eulogy on Gen. Humphreys..	4	Woodward, Dr. J. J., Death of.....	72
— presidential address.....	xxix, 81	— Resolutions on death of.....	75
— remarks on drifting of buoys.....	15	Woodward, R. S. : discussion of a concrete problem in hydrostatics proposed by Mr. G. K. Gilbert.....	101
— — — the Indian as a scientific observer...	75	— remarks on deflection of plumb-line.....	92
Williams, G. H. : communication on methods of modern petrography.....	36	Yeates, W. S., Election to membership of...	36
What is a glacier?.....	37		



BULLETIN
OF THE
PHILOSOPHICAL SOCIETY
OF
WASHINGTON.

VOL. VIII.

Containing the Minutes of the Society and of the Mathematical
Section for the year 1885.

PUBLISHED BY THE CO-OPERATION OF THE SMITHSONIAN INSTITUTION.

WASHINGTON:
1885



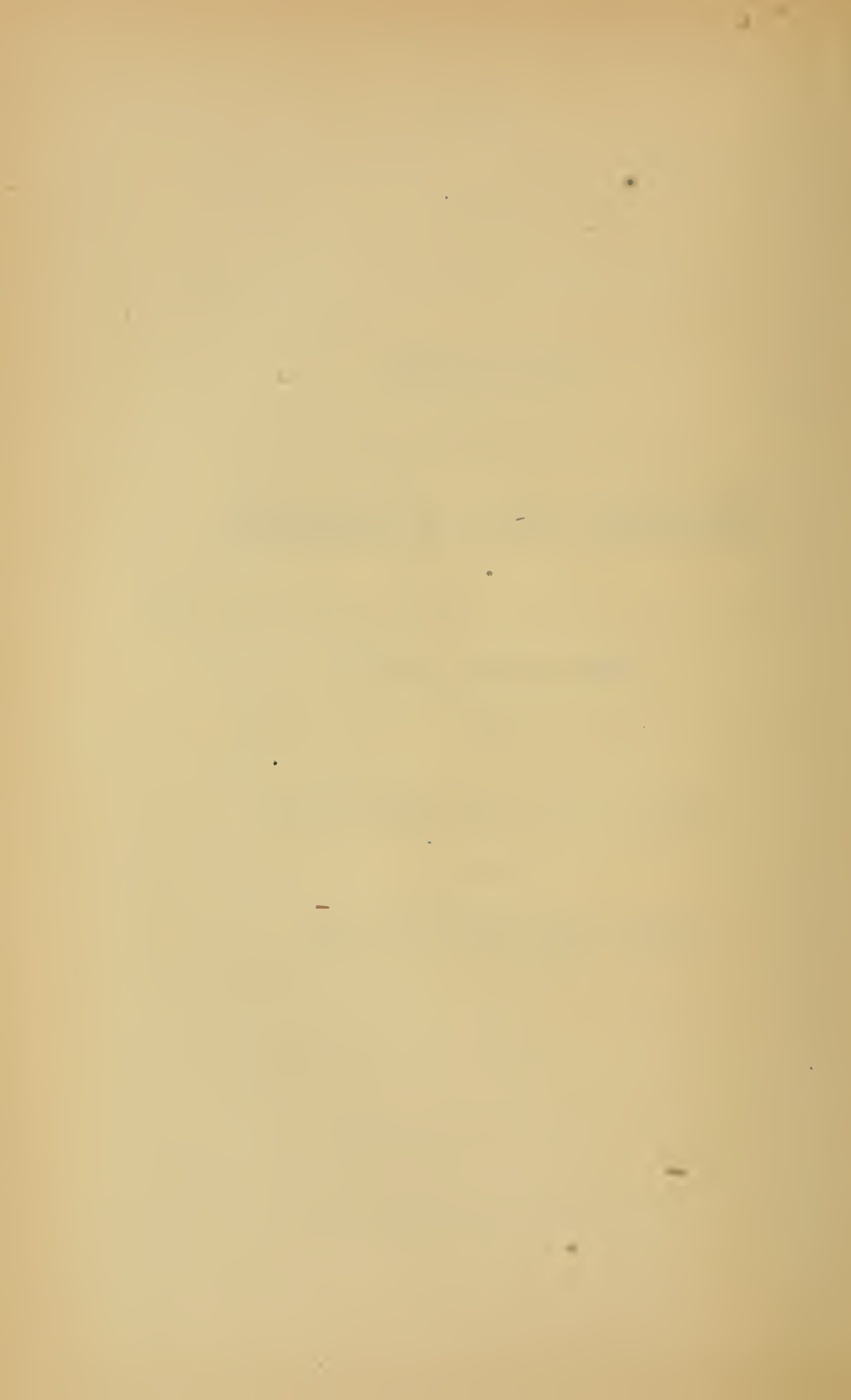
CONTENTS.

	Page.
Constitution -----	VII
Standing Rules of the Society -----	IX
Standing Rules of the General Committee -----	XII
Rules for the Publication of the Bulletin -----	XIII
Officers elected December, 1884 -----	XIV
Officers elected December, 1885 -----	XV
List of Members -----	XVI
List of deceased members -----	XXV
Annual Report of the Secretaries -----	XXVII
Annual Report of the Treasurer -----	XXVIII
Calendar -----	XXX
Annual Address of the President, Asaph Hall -----	XXXIII
Bulletin of the General Meeting -----	1
Report of the Auditing Committee -----	3
The vital statistics of the Tenth U. S. Census, J. S. Billings, (<i>Title only</i>) -----	4
Recent experiments on reaction time and the time sense, G. Stanley Hall, (<i>Title only</i>) -----	4
Practical geology versus speculative physics, C. E. Dutton, (<i>Title only</i>) -----	4, 5
Topaz from Stoneham, Maine, F. W. Clarke and J. S. Diller, (<i>Title only</i>) -----	5
Two remarkable forms of mollusks, W. H. Dall -----	5
Geological and physical theories, W. B. Taylor -----	6
Methods of verifying weather predictions, C. Abbe -----	8
Variations of latitude, A. Hall -----	10
Thunderstorms of 1884, H. A. Hazen -----	10
The Javal and Schiotz ophthalmometer, S. M. Burnett, (<i>Title only</i>) -----	11
The difficulty in determining the direction of sound, A. B. Johnson -----	11, 12
Mythological dry painting of the Navajos, W. Matthews -----	14
Comets II and III, 1884, W. C. Winlock -----	16
Problems connected with the physics of the earth's crust, H. M. Paul, (<i>Title only</i>) -----	17, 18
Modern ideas of brain mechanism, F. Baker, (<i>Title only</i>) -----	17
The flora of the Laramie group, L. F. Ward, (<i>Title only</i>) -----	17
The measurement of temperature at distant points, T. C. Men- hall, (<i>Title only</i>) -----	18
The asteroids, G. L. Ravene, (<i>Title only</i>) -----	18

	Page.
The mechanism of "clicks" and "clucks," A. G. Bell, (<i>Title only</i>)	18
The crumpling of the earth's crust, W. B. Taylor	18
The columnar structure in the diabase of Orange mountain, N. J., J. P. Iddings	19
The terraces of the Potomac valley, W J McGee, (<i>Title only</i>) ..	24
Anthropometric and reaction-time apparatus, J. S. Billings and W. Matthews	25
The condensing hygrometer and sling psychrometer, H. A. Hazen	25
A new volt-meter, T. C. Mendenhall	26
Flexures of transit instruments, W. Harkness	27
An attempt at a theory of odor, F. W. Clarke	27
The Flood Rock explosion, F. W. Clarke, C. F. Marvin, and H. M. Paul	28
The systematic care of pamphlets, G. B. Goode and C. V. Riley	29
Germ cultures, J. S. Billings	30
Presentation of the annual address	30
Annual meeting	30
Bulletin of the Mathematical Section	33
Standing Rules of the Section	35
Officers of the Section	36
Example illustrating the use of a certain symbol in the calculus of affected quantity, E. B. Elliott, (<i>Title only</i>)	37
A collection of formulæ for the area of a plane triangle, M. Baker, (<i>Title only</i>)	37
Physical observations on Wolf's comet (1884, III), W. C. Winlock	37
A slight modification of the Newtonian formula of gravitation, W. B. Taylor	39
An artifice sometimes useful for the adjustment of conditioned observations, C. H. Kummell	41
The theory of Mercury, G. L. Ravené	41
A group of circles related to Feuerbach's circle, M. Baker ..	45
Distances on any spheroid, C. H. Kummell	52
On Grassman's system of geometry, A. Ziwet	53
Cause and chance in the concurrence of phenomena, M. H. Doolittle, (<i>Title only</i>)	54
The asteroids, G. L. Ravené, (<i>Title only</i>)	54
Secular perturbations of Polyhymnia by Jupiter, W. F. McK. Ritter	54
Some practical features of a field time determination with a meridian transit, R. S. Woodward	55
Can the attraction of a finite mass be infinite? C. H. Kummell	58
Committees on mathematical communications	63
Index	65

BULLETIN
OF THE
PHILOSOPHICAL SOCIETY OF WASHINGTON.

CONSTITUTION, RULES,
LIST OF
OFFICERS AND MEMBERS,
AND REPORTS OF
SECRETARIES AND TREASURER.



CONSTITUTION

OF

THE PHILOSOPHICAL SOCIETY OF WASHINGTON.

ARTICLE I. The name of this Society shall be THE PHILOSOPHICAL SOCIETY OF WASHINGTON.

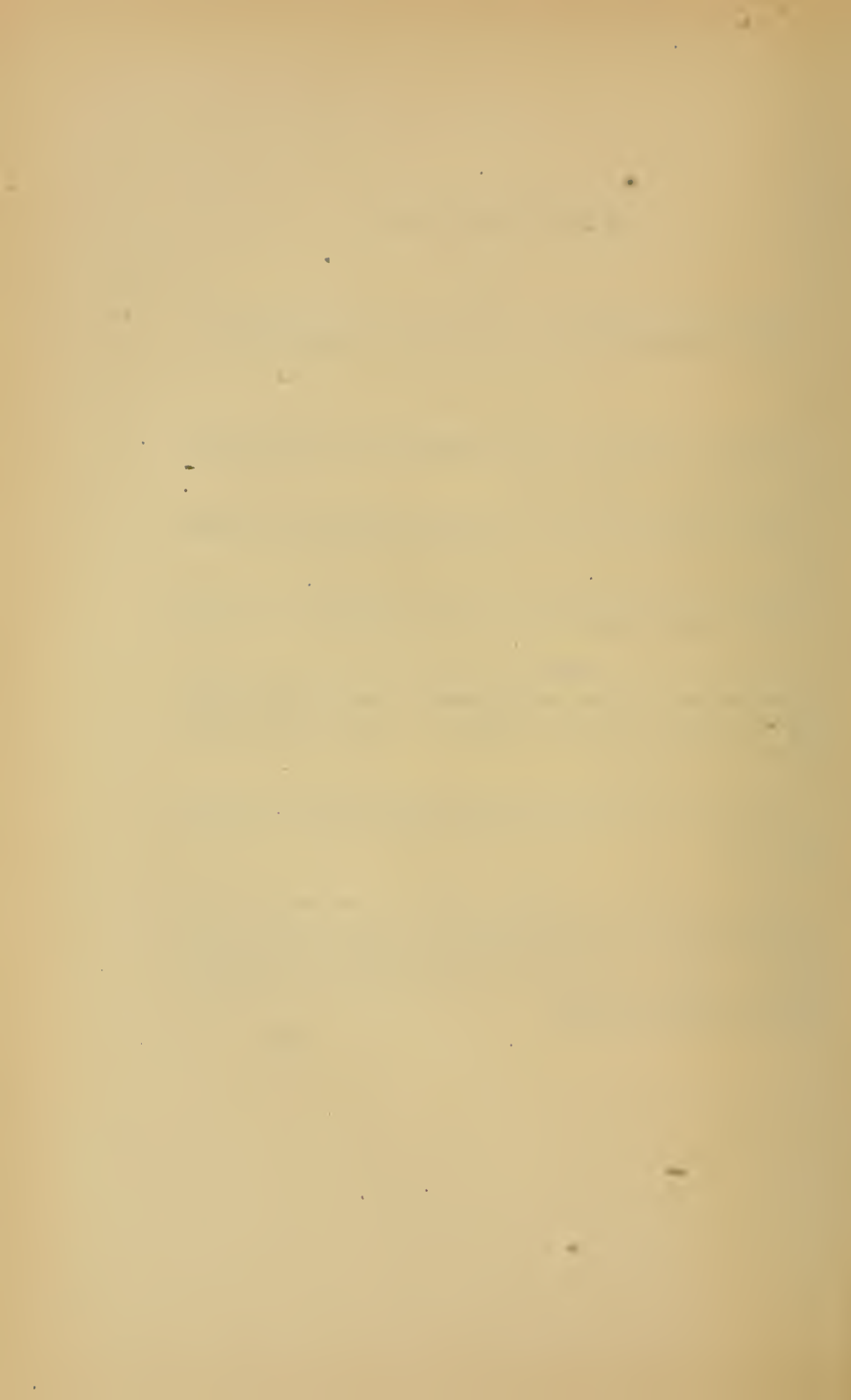
ARTICLE II. The officers of the Society shall be a President, four Vice-Presidents, a Treasurer, and two Secretaries.

ARTICLE III. There shall be a General Committee, consisting of the officers of the Society and nine other members.

ARTICLE IV. The officers of the Society and the other members of the General Committee shall be elected annually by ballot ; they shall hold office until their successors are elected, and shall have power to fill vacancies.

ARTICLE V. It shall be the duty of the General Committee to make rules for the government of the Society, and to transact all its business.

ARTICLE VI. This constitution shall not be amended except by a three-fourths vote of those present at an annual meeting for the election of officers, and after notice of the proposed change shall have been given in writing at a stated meeting of the Society at least four weeks previously.



STANDING RULES

FOR THE GOVERNMENT OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON.

1. The Stated Meetings of the Society shall be held at 8 o'clock P. M. on every alternate Saturday; the place of meeting to be designated by the General Committee.

2. Notice of the time and place of meeting shall be sent to each member by one of the Secretaries.

When necessary, Special Meetings may be called by the President.

3. The Annual Meeting for the election of officers shall be the last stated meeting in the month of December.

The order of proceedings (which shall be announced by the Chair) shall be as follows:

First, the reading of the minutes of the last Annual Meeting.

Second, the presentation of the annual reports of the Secretaries, including the announcement of the names of members elected since the last annual meeting.

Third, the presentation of the annual report of the Treasurer.

Fourth, the announcement of the names of members who, having complied with Section 14 of the Standing Rules, are entitled to vote on the election of officers.

Fifth, the election of President.

Sixth, the election of four Vice-Presidents.

Seventh, the election of Treasurer.

Eighth, the election of two Secretaries.

Ninth, the election of nine members of the General Committee.

Tenth, the consideration of Amendments to the Constitution of the Society, if any such shall have been proposed in accordance with Article VI of the Constitution.

Eleventh, the reading of the rough minutes of the meeting.

4. Elections of officers are to be held as follows :

In each case nominations shall be made by means of an informal ballot, the result of which shall be announced by the Secretary ; after which the first formal ballot shall be taken.

In the ballot for Vice-Presidents, Secretaries, and Members of the General Committee, each voter shall write on one ballot as many names as there are officers to be elected, viz., four on the first ballot for Vice-Presidents, two on the first for Secretaries, and nine on the first for Members of the General Committee ; and on each subsequent ballot as many names as there are persons yet to be elected ; and those persons who receive a majority of the votes cast shall be declared elected.

If in any case the informal ballot result in giving a majority for any one, it may be declared formal by a majority vote.

5. The Stated Meetings, with the exception of the annual meeting, shall be devoted to the consideration and discussion of scientific subjects.

The Stated Meeting next preceding the Annual Meeting shall be set apart for the delivery of the President's Annual Address.

6. Sections representing special branches of science may be formed by the General Committee upon the written recommendation of twenty members of the Society.

7. Persons interested in science, who are not residents of the District of Columbia, may be present at any meeting of the Society, except the annual meeting, upon invitation of a member.

8. * On request of a member, the President or either of the Secretaries may, at his discretion, issue to any person a card of invitation to attend a specified meeting. Five cards of invitation to attend a meeting may be issued in blank to the reader of a paper at that meeting.

9. Invitations to attend during three months the meetings of the Society and participate in the discussion of papers, may, by a vote of nine members of the General Committee, be issued to persons nominated by two members.

10. Communications intended for publication under the auspices of the Society shall be submitted in writing to the General Committee for approval.

* Amended January 17, 1885.

11. Any paper read before a Section may be repeated, either entire or by abstract, before a general meeting of the Society, if such repetition is recommended by the General Committee of the Society.

12. *It is not permitted to report the proceedings of the Society or its Sections for publication, except by authority of the General Committee.

13. New members may be proposed in writing by three members of the Society for election by the General Committee; but no person shall be admitted to the privileges of membership unless he signifies his acceptance thereof in writing within two months after notification of his election.

14. Each member shall pay annually to the Treasurer the sum of five dollars, and no member whose dues are unpaid shall vote at the annual meeting for the election of officers, or be entitled to a copy of the Bulletin.

In the absence of the Treasurer, the Secretary is authorized to receive the dues of members.

The names of those two years in arrears shall be dropped from the list of members.

Notice of resignation of membership shall be given in writing to the General Committee through the President or one of the Secretaries.

15. The fiscal year shall terminate with the Annual Meeting.

16. †Any member who is absent from the District of Columbia for more than twelve consecutive months may be excused from payment of dues during the period of his absence, in which case he will not be entitled to receive announcements of meetings or current numbers of the Bulletin.

17. Any member not in arrears may, by the payment of one hundred dollars at any one time, become a life member, and be relieved from all further annual dues and other assessments.

All moneys received in payment of life membership shall be invested as portions of a permanent fund, which shall be directed solely to the furtherance of such special scientific work as may be ordered by the General Committee.

* Adopted January 17, 1885.

† Amended December 19, 1885.

STANDING RULES

OF THE

GENERAL COMMITTEE OF THE PHILOSOPHICAL SOCIETY OF WASHINGTON.

1. The President, Vice-Presidents, and Secretaries of the Society shall hold like offices in the General Committee.

2. The President shall have power to call special meetings of the Committee, and to appoint Sub-Committees.

3. The Sub-Committees shall prepare business for the General Committee, and perform such other duties as may be entrusted to them.

4. There shall be two Standing Sub-Committees; one on Communications for the Stated Meetings of the Society, and another on Publications.

5. The General Committee shall meet at half-past seven o'clock on the evening of each Stated Meeting, and by adjournment at other times.

6. For all purposes except for the amendment of the Standing Rules of the Committee or of the Society, and the election of members, six members of the Committee shall constitute a quorum.

7. The names of proposed new members recommended in conformity with Section 13 of the Standing Rules of the Society, may be presented at any meeting of the General Committee, but shall lie over for at least four weeks before final action, and the concurrence of twelve members of the Committee shall be necessary to election.

The Secretary of the General Committee shall keep a chronological register of the elections and acceptances of members.

8. These Standing Rules, and those for the government of the Society, shall be modified only with the consent of a majority of the members of the General Committee.

RULES

FOR THE

PUBLICATION OF THE BULLETIN

OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON.

1. The President's annual address shall be published in full.
2. The annual reports of the Secretaries and of the Treasurer shall be published in full.
3. When directed by the General Committee, any communication may be published in full.
4. Abstracts of papers and remarks on the same will be published, when presented to the Secretary by the author in writing within two weeks of the evening of their delivery, and approved by the Committee on Publications. Brief abstracts prepared by one of the Secretaries and approved by the Committee on Publications may also be published.
5. If the author of any paper read before a Section of the Society desires its publication, either in full or by abstract, it shall be referred to a committee to be appointed as the Section may determine.
The report of this committee shall be forwarded to the Publication Committee by the Secretary of the Section, together with any action of the Section taken thereon.
6. Communications which have been published elsewhere, so as to be generally accessible, will appear in the Bulletin by title only, but with a reference to the place of publication, if made known in season to the Committee on Publications.

OFFICERS

OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON

ELECTED DECEMBER 20, 1884.

<i>President</i> -----	ASAPH HALL.	
<i>Vice-Presidents</i> -----	J. S. BILLINGS.	GARRICK MALLERY.
	WILLIAM HARKNESS.	J. E. HILGARD.
<i>Treasurer</i> -----	ROBERT FLETCHER.	
<i>Secretaries</i> -----	G. K. GILBERT.	HENRY FARQUHAR.

MEMBERS AT LARGE OF THE GENERAL COMMITTEE.

MARCUS BAKER.	H. H. BATES.
F. W. CLARKE.	W. H. DALL.
C. E. DUTTON.	J. R. EASTMAN.
E. B. ELLIOTT.	H. M. PAUL.
C. V. RILEY.	

STANDING COMMITTEES.

On Communications:

J. S. BILLINGS, <i>Chairman.</i>	G. K. GILBERT.	HENRY FARQUHAR.
----------------------------------	----------------	-----------------

On Publications:

G. K. GILBERT, <i>Chairman.</i>	ROBERT FLETCHER.	HENRY FARQUHAR.
	S. F. BAIRD.*	

* As Secretary of the Smithsonian Institution.

OFFICERS

OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON

ELECTED DECEMBER 19, 1885.

<i>President</i> -----	J. S. BILLINGS.	
<i>Vice-Presidents</i> -----	WILLIAM HARKNESS.	GARRICK MALLERY.
	C. E. DUTTON.	J. E. HILGARD.
<i>Treasurer</i> -----	ROBERT FLETCHER.	
<i>Secretaries</i> -----	G. K. GILBERT.	MARCUS BAKER.

MEMBERS AT LARGE OF THE GENERAL COMMITTEE.

H. H. BATES.	F. W. CLARKE.
W. H. DALL.	C. E. DUTTON.
J. R. EASTMAN.	HENRY FARQUHAR.
T. C. MENDENHALL.	H. M. PAUL.
C. V. RILEY.	

STANDING COMMITTEES.

On Communications :

WILLIAM HARKNESS, *Chairman.* G. K. GILBERT. MARCUS BAKER.

On Publications :

G. K. GILBERT, *Chairman.* ROBERT FLETCHER. MARCUS BAKER.
S. F. BAIRD.*

* As Secretary of the Smithsonian Institution.

LIST OF MEMBERS

OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON.

Corrected to January 16, 1886.

The customary titles of members are here for the first time given.

Names of gentlemen here indicated as resigned will be omitted from future lists.

NAME.	ADDRESS AND RESIDENCE.	Admitted.
ABBE, Prof. CLEVELAND	Army Signal Office. 2017 I st. N. W.	1871
ABERT, Mr. S. T. (Sylvanus Thayer)	810 19th st. N. W.	1875
ADAMS, Mr. CHARLES FREDERICK	Civil Service Commission. 2017 G st. N. W.	1885
ADAMS, Mr. HENRY	1607 H st. N. W.	1881
ALDIS, Hon. A. O. (Asa Owen)	1765 Mass. ave. N. W.	1873
ANTISELL, Dr. THOMAS (<i>Founder</i>)	Patent Office. 1311 Q st. N. W.	1871
AVERY, Mr. ROBERT S. (Robert Stanton)	320 A st. S. E.	1879
BAIRD, Prof. SPENCER F. (Spencer Fullerton) (<i>Founder</i>)	Smithsonian Institution. 1445 Mass. ave. N. W.	1871
BAKER, Dr. FRANK	326 C st. N. W.	1881
BAKER, Mr. MARCUS	Coast and Geodetic Survey Office. 1205 Rhode Island ave.	1876
BANCROFT, GEORGE	1623 H st. N. W., or Newport, R. I.	1875
BARNARD, Dr. WM. S. (William Stebbins)	917 New York ave. N. W., or Canton, Ill.	1884
BARUS, Dr. CARL	Geological Survey.	1885
BATES, Mr. HENRY H. (Henry Hobart)	Patent Office. The Portland.	1871
BEARDSLEE, Capt. L. A. (Lester Anthony) U. S. N. (<i>Absent</i>)	Navy Department.	1875
BELL, Mr. A. GRAHAM (Alexander Graham)	Scott Circle; 1500 Rhode Island ave.	1879
BELL, Dr. C. A. (Chichester Alexander)	1314 19th st. N. W.	1881
BENÉT, Gen. S. V. (Stephen Vincent) U. S. A. (<i>Founder</i>)	Ordnance Office, War Dept. 1717 I st. N. W.	1871

LIST OF MEMBERS.

XVII

NAME.	ADDRESS AND RESIDENCE.	Admitted.
BESSELS, DR. EMIL	Glenn Dale, Md.	1875
BILLINGS, DR. JOHN S. (John Shaw) U. S. A. (<i>Founder</i>)	Surg. General's Office, U. S. A. 3027 N st. N. W.	1871
BIRNEY, Gen. WILLIAM	456 Louisiana ave. 1901 Harewood ave., Le Droit Park.	1879
BIRNIE, ROGERS (<i>Absent</i>)		1876
BODFISH, Mr. S. H. (Sumner Ho- mer) (<i>Absent</i>)	Geological Survey. 605 F st. N. W.	1883
BOUTELLE, Mr. C. O. (Charles Otis)	Coast and Geodetic Survey Office.	1884
BOWLES, Asst. Nav. Constr. FRAN- CIS T. (Francis Tiffany) U. S. N.	Navy Department.	1884
BROWNE, Dr. J. MILLS (John Mills) U. S. N.	Navy Department. The Portland.	1883
BURCHARD, Hon. H. C. (Horatio Chapin) (<i>Resigned</i>)		1879
BURGESS, Mr. E. S. (Edward San- ford)	High School. 810 12th st. N. W.	1883
BURNETT, Dr. SWAN M. (Swan Moses)	1215 I st. N. W.	1879
BUSEY, Dr. SAMUEL C. (Samuel Clagett)	901 16th st. N. W.	1874
CASEY, Col. THOMAS LINCOLN, U. S. A. (<i>Founder</i>)	War Department. 1419 K st. N. W.	1871
CAZIARC, Lieut. L. V. (Louis Vasmer) U. S. A. (<i>Absent</i>)	War Department.	1882
CHAMBERLIN, Prof. T. C. (Thomas Crowder)	Geological Survey. 939 K st. N. W.	1883
CHATARD, Dr. THOMAS M. (Tho- mas Marcant)	Geological Survey. 601 13th st. N. W.	1885
CHICKERING, Prof. J. W., Jr. (John White)	Deaf Mute College, Kendall Green.	1874
CHRISTIE, Mr. ALEX. S. (Alexan- der Smyth)	Coast and Geodetic Survey Office. 507 6th st. N. W.	1880
CLARK, Mr. E. (Edward)	Architect's Office, Capitol. 417 4th st. N. W.	1877
CLARKE, Prof. F. W. (Frank Wigglesworth)	Geological Survey. 1425 Q st. N. W.	1874
COFFIN, Prof. J. H. C. (John Huntington Crane) U. S. N. (<i>Founder</i>)	1901 I st. N. W.	1871
COMSTOCK, Prof. J. H. (John Henry) (<i>Absent</i>)	Cornell University, Ithaca, N. Y.	1880
COUES, Prof. ELLIOTT	Smithsonian Institution. 1726 N st. N. W.	1874
CRAIG, Lieut. ROBERT, U. S. A. (<i>Absent</i>)	1008 I st. N. W.	1873
CRAIG, Dr. THOMAS (<i>Absent</i>)	Johns Hopkins Univ., Baltimore, Md.	1879

XVIII PHILOSOPHICAL SOCIETY OF WASHINGTON.

NAME.	ADDRESS AND RESIDENCE.	Admitted.
CURTIS, MR. GEO. E. (George Edward)	Army Signal Office. 930 18th st. N. W.	1884
DALL, MR. WM. H. (William Healey) (<i>Founder</i>)	Care Smithsonian Institution. 1119 12th st. N. W.	1871
DAVIS, Commander C. H. (Charles Henry) U. S. N.	Navy Department. 1705 Rhode Island ave.	1880
DEAN, Dr. R. C. (Richard Crain) U. S. N. (<i>Absent</i>)	Naval Hospital, New York city.	1872
DE CAINDRY, MR. Wm. A. (William Augustin)	Commissary General's Office. 1713 H st. N. W.	1881
DE LAND, MR. THEODORE L. (Theodore Louis)	Treasury Department. 126 7th st. N. E.	1880
DEWEY, MR. FRED. P. (Frederic Perkins)	National Museum. Lanier Heights.	1884
DILLER, MR. J. S. (Joseph Silas)	Geological Survey. 1804 16th st. N. W.	1884
DOOLITTLE, MR. M. H. (Myrick Hascall)	Coast and Geodetic Survey Office. 1925 I st. N. W.	1876
DUNWOODY, Lt. H. H. C. (Henry Harrison Chase) U. S. A. (<i>Absent</i>)	War Department.	1873
DUTTON, Capt. C. E. (Clarence Edward) U. S. A.	Geological Survey. 2222 G st. N. W.	1872
EARLL, MR. R. EDWARD (Robert Edward)	Smithsonian Institution. 1336 T st. N. W.	1884
EASTMAN, Prof. J. R. (John Robie) U. S. N.	Naval Observatory. 1823 I st. N. W.	1871
EIMBECK, MR. WILLIAM	Coast and Geodetic Survey Office.	1884
ELDREDGE, Dr. STEWART (<i>Absent</i>)	Yokohama, Japan.	1871
ELLIOTT, Mr. E. B. (Ezekiel Brown) (<i>Founder</i>)	Gov't Actuary, Treas. Dept. 1210 G st. N. W.	1871
EMMONS, MR. S. F. (Samuel Franklin)	Geological Survey. 1022 Vermont ave.	1883
ENDLICH, Dr. F. M. (Frederic Miller) (<i>Absent</i>)	Smithsonian Institution. Lake Valley, New Mexico.	1873
EWING, Gen. HUGH (<i>Absent</i>)	Lancaster, Ohio.	1874
FARQUHAR, MR. EDWARD	Patent Office Library. 1915 H st. N. W.	1876
FARQUHAR, MR. HENRY	Coast and Geodetic Survey Office. Brooks Station, D. C.	1881
FERREL, Prof. WILLIAM	Army Signal Office. 471 C st. N. W.	1872
FLETCHER, Dr. ROBERT	Surgeon General's Office, U. S. A. The Portland.	1873
FLINT, Mr. A. S. (Albert Stowell)	Naval Observatory. 1450 Chapin st., College Hill.	1882
FLINT, Dr. J. M. (James Milton) U. S. N.	Navy Department. U. S. S. Albatross.	1881
FRISTOE, Prof. EDWARD T	Columbian University. 1434 N st. N. W.	1873

NAME.	ADDRESS AND RESIDENCE.	Admitted.
GALLAUDET, President E. M. (Edward Miner)	Deaf Mute College, Kendall Green.	1875
GANNETT, Mr. HENRY	Geological Survey. 1881 Harewood ave., Le Droit Park.	1874
GIHON, Dr. ALBERT L. (Albert Leary) U. S. N. (<i>Resigned</i>)		1880
GILBERT, Mr. G. K. (Grove Karl)	Geological Survey. 1424 Corcoran st.	1873
GODDING, Dr. W. W. (William Whitney)	Government Hospital for the Insane.	1879
GOOCH, Dr. F. A. (Frank Austin)	Geological Survey. 825 Vermont ave.	1885
GOODE, Mr. G. BROWN (George Brown)	National Museum. 1545 T st. N. W.	1874
GOODFELLOW, Mr. EDWARD	Coast and Geodetic Survey Office.	1875
GORE, Prof. J. H. (James Howard)	Columbian University. 1305 Q st. N. W.	1880
GRAVES, Mr. WALTER H. (Walter Hayden) (<i>Absent</i>)	Denver, Colorado.	1878
GREELY, Lieut. A. W. (Adolphus Washington) U. S. A.	Army Signal Office. 1914 G st N. W.	1880
GREEN, Mr. BERNARD R. (Bernard Richardson)	1738 N st. N. W.	1879
GREEN, Commander F. M. (Francis Mathews) U. S. N. (<i>Absent</i>)	Navy Department.	1875
GREENE, Prof. B. F. (Benjamin Franklin) (<i>Founder: absent</i>)	West Lebanon, N. H.	1871
GREENE, Capt. FRANCIS V. (Francis Vinton) U. S. A. (<i>Absent</i>)	West Point, N. Y.	1875
GREGORY, Dr. JOHN M. (John Milton)	15 Grant Place.	1884
GUNNELL, FRANCIS M., M. D., U. S. N.	600 20th st., N. W.	1879
HAINS, Col. PETER C. (Peter Conover)	Engineer's Office, Potomac Riv. Improvement, 2136 Pa. ave. 1824 Jefferson Place.	1879
HAINS, Mr. ROBERT P. (Robert Peter)	Patent Office. 1714 13th st. N. W.	1885
HALL, Prof. ASAPH, U. S. N. (<i>Founder</i>)	Naval Observatory. 2715 N st. N. W.	1871
HALL, Mr. ASAPH, JR.	Yale College Observatory, New Haven, Conn. 2715 N st. N. W.	1884
HALLOCK, Dr. WILLIAM	Geological Survey.	1885
HAMPSON, Mr. THOMAS	Geological Survey. 504 Maple ave., Le Droit Park.	1885
HARKNESS, Prof. WILLIAM, U. S. N. (<i>Founder</i>)	Naval Observatory. Cosmos Club, 23 Madison Place.	1871

NAME.	ADDRESS AND RESIDENCE.	Admitted.
HASSLER, Dr. FERDINAND A. (Ferdinand Augustus) (<i>Absent</i>)	Santa Aña, Los Angeles Co., Cal.	1880
HAYDEN, Dr. F. V. (Ferdinand Vandever) (<i>Founder: absent</i>)	Geological Survey. 1805 Arch st., Phila., Pa.	1871
HAZEN, Prof. H. A. (Henry Allen)	P. O. Box No. 427. 1416 Corcoran st.	1882
HAZEN, Gen. W. B. (William Babcock) U. S. A.	Army Signal Office. 1601 K st. N. W.	1881
HEAP, Maj. D. P. (David Porter)	Light House Board, Treas. Dept. 1618 Rhode Island ave.	1884
HENSHAW, Mr. H. W. (Henry Wetherbee)	Bureau of Ethnology. 13 Iowa Circle.	1874
HILGARD, Mr. J. E. (Julius Erasmus) (<i>Founder</i>)	1739 F st. N. W.	1871
HILL, Mr. G. W. (George William)	Nautical Almanac Office. 314 Indiana ave. N. W.	1879
HITCHCOCK, Mr. ROMYN	National Museum, or P. O. Box 630.	1884
HODGKINS, Prof. H. L. (Howard Lincoln)	Columbian University. 627 N st. N. W.	1885
HOLDEN, Prest. EDWARD SINGLETON (<i>Absent</i>)	University of California, Berkeley, Cal.	1873
HOLMES, Mr. W. H. (William Henry)	Geological Survey. 1100 O st. N. W.	1879
HOWELL, Mr. EDWIN E. (Edwin Eugene) (<i>Absent</i>)	48 Oxford st., Rochester, N. Y.	1874
IDDINGS, Mr. JOSEPH P. (Joseph Paxson)	Geological Survey. 1028 Vermont ave.	1885
JAMES, Rev. OWEN (<i>Absent</i>)	Scranton, Pa.	1880
JENKINS, Rear Admiral THORNTON A. (Thornton Alexander) U. S. N. (<i>Founder</i>)	2115 Penna. ave. N. W.	1871
JOHNSON, Mr. A. B. (Arnold Burges)	Light House Board, Treas. Dept. 501 Maple ave., Le Droit Park.	1878
JOHNSON, Dr. JOSEPH TABER	926 17th st. N. W.	1879
JOHNSON, Mr. WILLARD D. (Willard Drake) (<i>Absent</i>)	Geological Survey.	1884
JOHNSTON, Dr. W. W. (William Waring)	1603 K st. N. W.	1873
KAUFFMANN, Mr. S. H. (Samuel Hays)	1000 M st. N. W.	1884
KEITH, Mr. R. (Reuel)	Nautical Almanac Office. 2219 I st. N. W.	1871
KERR, Mr. MARK B. (Mark Brickell)	Geological Survey. 722 21st st. N. W.	
KIDDER, Dr. J. H. (Jerome Henry)	Smithsonian Institution. 1816 N st. N. W.	1880

NAME.	ADDRESS AND RESIDENCE.	Admitted.
KILBOURNE, Lt. C. E. (Charles Evans) U. S. A. (<i>Absent</i>)	War Department.	1880
KING, Dr. A. F. A. (Albert Freeman Africanus)	726 13th st. N. W.	1875
KNOX, Hon. JOHN JAY (<i>Absent</i>)	Prest. Nat. Bank Republic, New York city	1874
KUMMELL, Mr. C. H. (Charles Hugo)	Coast and Geodetic Survey Office. 608 Q st. N. W.	1882
LAWRENCE, Mr. WILLIAM	1344 Vermont ave., and Bellefontaine, Ohio.	1884
LAWYER, Dr. W. P. (Winfield Peter)	Mint Bureau, Treas. Dept. 1912 I st. N. W.	1881
LEE, Dr. WILLIAM	2111 Penna. ave. N. W. 1821 I st. N. W.	1874
LEFAVOUR, Mr. EDWARD B. (Edward Brown)	905 O st. N. W.	1882
LINCOLN, Dr. N. S. (Nathan Smith)	1514 H st. N. W.	1871
LOOMIS, Mr. E. J. (Eben Jenks)	Nautical Almanac Office. 1413 Stoughton st. N. W.	1880
LULL, Capt. E. P. (Edward Phelps) U. S. N. (<i>Absent</i>)	Navy Department. 74 Cedar st., Roxbury, Mass.	1875
MCGEE, Mr. W J	Geological Survey. 1424 Corcoran st.	1883
MCGUIRE, Mr. FRED. B. (Frederick Bauders)	1416 F st. N. W. 614 E st. N. W.	1879
MCMURTRIE, Prof. WILLIAM (<i>Absent</i>)	University of Illinois, Campaign, Ill.	1876
MAHER, Mr. JAMES A. (James Arran)	Geological Survey. 21 E st. N. W.	1884
MALLERY, Col. GARRICK, U. S. A.	Bureau of Ethnology. 1323 N st. N. W.	1875
MANN, Mr. B. PICKMAN (Benjamin Pickman)	Department of Agriculture. 924 19th st. N. W.	1885
MARCOU, Mr. J. B. (John Belknap)	Geological Survey. 601 13th st. N. W.	1884
MARVIN, Prof. C. F. (Charles Frederick)	Army Signal Office. 1736 13th st. N. W.	1885
MARVIN, Mr. Jos. B. (Joseph Badger) (<i>Absent</i>)	Internal Revenue Bureau.	1878
JASON, Prof. OTIS T. (Otis Tufton)	National Museum. 1305 Q st. N. W.	1875
IATTHEWS, Dr. W. (Washington) U. S. A.	Surg. General's Office, U. S. A.	1884
NEIGS, Gen. M. C. (Montgomery Cunningham) U.S.A. (<i>Founder</i>)	1239 Vermont ave.	1871
MENDENHALL, Prof. T. C. (Thomas Corwin)	Army Signal Office.	1885
MERRILL, Mr. GEORGE P. (George Perkins)	National Museum.	1884

NAME.	ADDRESS AND RESIDENCE.	Admitted.
MORGAN, Dr. E. C. (Ethelbert Carroll)	918 E st. N. W.	1883
MOSER, Lt. J. F. (Jefferson Franklin) U. S. N.	Coast and Geodetic Survey Office. 7 2d st. S. E.	1885
MURDOCH, Mr. JOHN	Smithsonian Institution. 1441 Chapin st., College Hill.	1884
MUSSEY, Gen. R. D. (Reuben Delavan)	P. O. Box 618. 508 5th st. N. W.	1881
MYERS, Gen. WILLIAM, U. S. A.	War Department.	1871
NEWCOMB, Prof. SIMON, U. S. N. (<i>Founder</i>)	Navy Department. 941 M st. N. W.	1871
NICHOLS, Dr. CHARLES H. (Charles Henry) (<i>Absent</i>)	Bloomingtondale Asylum, Boulevard and 117th st., New York, N. Y.	1872
NICHOLSON, Mr. W. L. (Walter Lamb) (<i>Founder</i>)	Topographer, P. O. Dept. 1322 I st. N. W.	1871
NORDHOFF, Mr. CHARLES	1731 K st. N. W.	1879
NORRIS, Dr. BASIL U. S. A. (<i>Absent</i>)	Vancouver, Clarke Co., Wash. Ter.	1884
NOTT, Judge C. C. (Charles Cooper)	Court of Claims. 826 Connecticut ave. N. W.	1885
OGDEN, Mr. HERBERT G. (Herbert Gouverneur)	Coast and Geodetic Survey Office. 1324 19th st. N. W.	1884
OSBORNE, Mr. J. W. (John Walter)	212 Delaware ave. N. E.	1878
PARKE, Gen. JOHN G. (John Grubb) U. S. A. (<i>Founder</i>)	Engineer Bureau, War Dept. 16 Lafayette Square.	1871
PARKER, Dr. PETER (<i>Founder</i>)	2 Lexington Place.	1871
PARRY, Dr. CHARLES C. (Charles Christopher) (<i>Absent</i>)	Davenport, Iowa.	1871
PAUL, Mr. H. M. (Henry Martyn)	Naval Observatory. 109 1st st. N. E.	1871
PEALE, Dr. A. C. (Albert Charles)	Geological Survey. 1010 Mass. ave. N. W.	1871
PILLING, Mr. JAMES C. (James Constantine) (<i>Resigned</i>)		1881
POE, Gen. O. M. (Orlando Metcalfe) U. S. A. (<i>Absent</i>)	34 Congress st. West, Detroit, Mich.	1883
POINDEXTER, Mr. W. M. (William Mundy)	701 15th st. N. W. 806 17th st. N. W.	1884
POPE, Dr. B. F. (Benjamin Franklin) U. S. A.	Surg. General's Office, U. S. A.	1882
POWELL, Major J. W. (John Wesley)	Geological Survey. 910 M st. N. W.	1874
PRENTISS, Dr. D. W. (Daniel Webster)	1224 9th st. N. W.	380
PRITCHETT, Prof. H. S. (Henry Smith) (<i>Absent</i>)	Director of Observatory, Wash. University, St. Louis, Mo.	1879

NAME.	ADDRESS AND RESIDENCE.	Admitted.
RATHBUN, Mr. RICHARD	Smithsonian Institution. 1622 Mass. ave.	1882
RAVENÉ, Mr. GUSTAVE L. (Gustave Louis)	1417 6th st. N. W.	1885
RAY, Lieut. P. H. (Patrick Henry) U. S. A.	Fort Gaston, Cal.	1884
RENSHAWE, Mr. Jno. H. (John Henry)	Geological Survey. The Woodmont.	1883
RICHEY, Dr. S. O. (<i>Resigned</i>)		1882
RICKSECKER, Mr. EUGENE	Geological Survey. 1323 Q st. N. W.	1884
RILEY, Dr. C. V. (Charles Valentine)	Agricultural Department, or National Museum. 1700 13th st. N. W.	1878
RITTER, Mr. W. F. McK. (William Francis McKnight)	Nautical Almanac Office. 16 Grant Place.	1879
ROBINSON, Mr. THOMAS	Howard University. 6th st. N. W., cor. Lincoln.	1884
ROGERS, Mr. JOSEPH A. (Joseph Addison) (<i>Absent</i>)	Naval Observatory.	1872
RUSSELL, Mr. ISRAEL C. (Israel Cook)	Geological Survey. 1424 Corcoran st.	1882
RUSSELL, Mr. THOMAS	Army Signal Office. 1447 Corcoran st. N. W.	1883
SALMON, Dr. D. E. (Daniel Elmer)	Agricultural Department. 1337 15th st. N. W.	1883
SAMPSON, Commander WILLIAM THOMAS U. S. N. (<i>Absent</i>)	Torpedo Station, Newport, R. I.	1883
SAVILLE, Mr. J. H. (James Hamilton)	1419 F st. N. W. 1315 M st. N. W.	1871
SCHOTT, Mr. CHARLES A. (Charles Anthony) (<i>Founder</i>)	Coast and Geodetic Survey Office. 212 1st st. S. E.	1871
SHELLABARGER, Hon. SAMUEL	Room 23 Corcoran Building. 812 17th st. N. W.	1875
SHERMAN, Hon. JOHN	U. S. Senate. 1319 K st. N. W.	1874
SHUFELDT, Dr. R. W. (Robert Wilson) U. S. A. (<i>Absent</i>)	Surg. Gen'l's Office, U. S. A., or Box 144, Smithsonian Inst.	1881
SHUMWAY, Mr. W. A. (Willard Adams) (<i>Resigned</i>)		1885
SICARD, Capt. MONTGOMERY, U. S. N.	Ordnance Bureau, Navy Dept.	1877
SIGSBEE, Commander C. D. (Charles Dwight) U. S. N. (<i>Absent</i>)	Navy Department.	1879
SKINNER, Dr. J. O. (John Oscar) U. S. A.	Surg. General's Office, U. S. A. 1529 O st. N. W.	1883
SMILEY, Mr. CHAS. W. (Charles Wesley)	U. S. Fish Commission. 943 Mass. ave.	1882
SMITH, Chf. Eng. DAVID, U. S. N.	1330 Corcoran st.	1876

NAME.	ADDRESS AND RESIDENCE.	Admitted.
SMITH, Mr. EDWIN	Coast and Geodetic Survey Office. 2024 Hillyer Place.	1880
SPOFFORD, Mr. A. R. (Ainsworth Rand)	Library of Congress. 1621 Mass. Ave. N. W.	1872
STEARNS, Mr. ROBERT E. C. (Robert Edwards Carter)	Smithsonian Institution. 1635 13th st. N. W.	1884
STONE, Prof. ORMOND (<i>Absent</i>)	Leander McCormick Observatory, University of Virginia, Va.	1874
TAYLOR, Mr. F. W. (Frederick William) (<i>Absent</i>)	Lake Valley, New Mexico.	1881
TAYLOR, Mr. WILLIAM B. (William Bower) (<i>Founder</i>)	Smithsonian Institution. 306 C st. N. W.	1871
THOMPSON, Prof. A. H. (Almon Harris)	Geological Survey.	1875
THOMPSON, Mr. GILBERT	Geological Survey. 1448 Q st. N. W.	1884
TODD, Prof. DAVID P. (David Peck) (<i>Absent</i>)	Lawrence Observatory, Amherst, Mass.	1878
TONER, Dr. J. M., (Joseph Meredith)	615 Louisiana ave.	1873
TRUE, Mr. FREDERICK W. (Frederick William)	National Museum. 1335 N st. N. W.	1882
UPTON, Mr. WM. W. (William Wirt)	1416 F st. N. W. 1746 M st. N. W.	1882
UPTON, Prof. WINSLOW (<i>Absent</i>)	Brown University, Providence, R. I.	1880
WALCOTT, Mr. C. D. (Charles Doolittle)	Geological Survey; National Museum.	1883
WALDO, Prof. FRANK (<i>Absent</i>)	Army Signal Office, Fort Myer, Va.	1881
WALKER, Mr. FRANCIS A. (Francis Amasa) (<i>Absent</i>)	Massachusetts Institute of Tech- nology, Boston, Mass.	1872
WALLING, Mr. HENRY F. (Henry Francis) (<i>Absent</i>)	U. S. Geological Survey, Cam- bridge, Mass.	1883
WARD, Mr. LESTER F. (Lester Frank)	Geological Survey. 1464 Rhode Island ave.	1876
WEBSTER, Mr. ALBERT L. (Albert Lowry) (<i>Absent</i>)	West New Brighton, Staten Isl- and, N. Y.	1882
WEED, Mr. Walter H. (Walter Harvey)	Geological Survey. 1413 Rhode Island ave.	1885
WELLING, Mr. JAMES C. (James Clarke)	1302 Connecticut ave.	1872
WHEELER, Capt. GEO. M., U. S. A.	Lock Box 92.	1873
WHITE, Dr. C. A. (Charles Abia-ther)	Geological Survey. 312 Maple ave., LeDroit Park	1876
WHITE, Dr. C. H. (Charles Henry) U. S. N.	Museum of Hygiene, 1744 G st. N. W.	1884
WILLIAMS, Mr. ALBERT, Jr.	Geological Survey.	1883

NAME.	ADDRESS AND RESIDENCE.	Admitted.
WILLIS, Mr. BAILEY	Geological Survey. 2017 N st. N. W.	1885
WILSON, H. M. (Herbert Michael)	Geological Survey.	1885
WILSON, Mr. J. ORMOND (James Ormond)	1439 Massachusetts ave. N. W.	1873
WINLOCK, Mr. WILLIAM C. (William Crawford)	Naval Observatory. 718 21st st. N. W.	1880
WOOD, Mr. JOSEPH (<i>Absent</i>)	Supt. Motive Power, Penn Co., Fort Wayne, Ind.	1875
WOOD, Lt. W. M. (William Maxwell) U. S. N. (<i>Absent</i>)	Navy Department.	1871
WOODWARD, Mr. R. S. (Robert Simpson)	Geological Survey. 1125 17th st. N. W.	1883
WORTMAN, Dr. J. L. (Jacob Lawson)	Army Medical Museum. 916 14th st. N. W.	1885
WRIGHT, Mr. GEO. M. (George Mitchell)	Geological Survey. 1319 Vermont ave.	1885
YARROW, Dr. H. C. (Harry Crécy)	Surgeon General's Office, U. S. A. 814 17th st. N. W.	1874
YEATES, Mr. W. S. (William Smith)	Smithsonian Institution. 1008 E st. S. W.	1884
ZIWET, Mr. ALEXANDER	Coast and Geodetic Survey Office. 1456 Corcoran st.	1885
ZUMBROCK, Dr. A. (Anton)	455 C st. N. W.	1875

LIST OF DECEASED MEMBERS.

Name.	Admitted.
Benjamin Alvord	1872
Orville Elias Babcock	1871
Theodorus Bailey	1873
Joseph K. Barnes	Founder
Henry Wayne Blair	1884
Horace Capron	Founder
Salmon Portland Chase	Founder
Frederick Collins	1879
Benjamin Faneuil Craig	Founder
Charles Henry Crane	Founder
Josiah Curtis	1874
Richard Dominicus Cutts	1871
Charles Henry Davis	1874
Frederick William Dorr	1874

XXVI PHILOSOPHICAL SOCIETY OF WASHINGTON.

<i>Name.</i>	<i>Admitted.</i>
Alexander B. Dyer	Founder
Amos Beebe Eaton	Founder
Charles Ewing	1874
Elisha Foote	Founder
John Gray Foster	1873
Leonard Dunnell Gale	1874
Isaiah Hanscom	1873
Joseph Henry	Founder
Franklin Benjamin Hough	1879
Andrew Atkinson Humphreys	Founder
Ferdinand Kampf	1875
Washington Caruthers Kerr	1883
Jonathan Homer Lane	Founder
Oscar A. Mack	1872
Archibald Robertson Marvine	1874
Fielding Bradford Meek	Founder
James William Milner	1874
Albert J. Myer	Founder
George Alexander Otis	Founder
Carlile Pollock Patterson	1871
Titian Ramsay Peale	Founder
Benjamin Peirce	Founder
John Campbell Riley	1877
John Rodgers	1872
Benjamin Franklin Sands	Founder
George Christian Shaeffer	Founder
Henry Robinson Searle	1877
William J. Twining	1878
Joseph Janvier Woodward	Founder
John Maynard Woodworth	1874
Mordecai Yarnall	1871

SUMMARY.

Active members	179
Absent members	46
Total	225
Deceased members	45

ANNUAL REPORT OF THE SECRETARIES.

WASHINGTON, CITY, *December 19, 1885.**To the Philosophical Society of Washington:*

We have the honor to present the following statistical data for 1885.

At the beginning of the year the number of active members was	173
This number has been increased by the addition of 22* new members and by the return of 3 absent members. It has been diminished by the departure of 6 members, by the death of 1, by the resignation of 5, and by the dropping of 7 for non-payment of dues. The net increase of active members has thus been	6
And the active membership is now	179

The roll of new members is:

C. F. ADAMS.	H. L. HODGKINS.	W. A. SHUMWAY.
CARL BARUS.	J. P. IDDIGS.	W. H. WEED.
T. M. CHATARD.	B. P. MANN.	BAILEY WILLIS.
F. A. GOOCH.	C. F. MARVIN.	H. M. WILSON.
R. P. HAINS.	T. C. MENDENHALL.	J. L. WORTMAN.
WILLIAM HALLOCK.	J. F. MOSER.	G. M. WRIGHT.
THOMAS HAMPSON.	C. C. NOTT.	ALEX. ZIWET.
	G. L. RAVENÉ.	

The names of deceased members (active and absent) are:

HORACE CAPRON.	F. B. HOUGH.	W. C. KERR.	T. R. PEALE.
----------------	--------------	-------------	--------------

There have been 16 meetings for the presentation and discussion of papers (not including the public meeting of Dec. 5); the average attendance has been 48. There have been 6 meetings of the Mathematical Section; average attendance 15.

In the general meetings 32 communications have been presented; in the mathematical section 14. Altogether 46 communications have been made by 32 members and one guest. The number of members who have participated in the discussions is 41. The total number who have contributed to the scientific proceedings is 54, or 31 per cent. of the present active membership.

The General Committee has held 17 meetings. Attendance below 10 on one evening only, and four times as high as 15. Average 12.2. Corresponding average last year 11.9, and in 1883 10.3, when the attendance was below 10 at five meetings.

Very respectfully,

G. K. GILBERT,
HENRY FARQUHAR,
Secretaries.

*The figures in this report have been brought down to Jan. 16, 1886, so as to correspond with the list of members. They differ somewhat from those read to the Society at the annual meeting.

REPORT OF THE TREASURER.

Mr. President and Gentlemen:

The report which I have the honor to present to you to-night covers the pecuniary transactions of the fiscal year which terminates with this meeting.

You will see from the statement which I shall presently read that the total receipts by the Treasurer have been \$1,224.04, and the total disbursements \$740.02, leaving a cash balance of \$484.02. These sums do not, however, represent the net income and expenditure for the year, since the receipts include a balance transferred by the former Treasurer, and the amount collected of unpaid dues of previous years. The payments, also, include the sum of \$104.12, for unpaid debts of 1884.

All the liabilities of the Society have been discharged to date, and the actual income belonging to 1885 has been \$1,041.00, which includes \$205.00 of dues yet outstanding. The disbursements for the same period have been \$635.90, leaving a net saving for the current year of \$405.10.

The unpaid dues of former years which have been collected, amount to \$160.00.

The Government bonds which belong to the Society were at the beginning of the year exchanged for new issues of the same amounts and denominations. This was done, under authority of the General Committee, in order to obtain uniformity in the designation of the Society, the former bonds having varied from each other in that particular. The bonds consist of:—

1	\$1,000 00	bond,	bearing	interest	at	4	per	cent.
1	500 00	“	“	“	“	4	“	“
1	1,000 00	“	“	“	“	4½	“	“

Total, \$2,500 00.

The assets of the Society are as follows:—

Cash, with Riggs & Co.	\$482 02
Bonds	2,500 00
Unpaid dues	295 00
Total	<u>\$3,279 02</u>

The market value of the bonds is, of course, considerably in excess of their face value; on the other hand, a part of the “unpaid dues” will probably not be collected.

I have in my possession a still ample stock of the Bulletins. A copy of Vol. VII was sent directly after its publication in February last to every member entitled to receive it, as well as to the various societies and scientific journals, at home and abroad, with which it has been customary for the Society to exchange publications.

The Treasurer in account with The Philosophical Society of Washington.

D.R.

C.R.

29 1885.

<table border="0" style="width: 100%;"> <tr> <td style="width: 50%;">Jan. 5. To cash received from C. Abbe-----</td> <td style="width: 50%; text-align: right;">\$213 04</td> </tr> <tr> <td>Mar. 20. " " for sale of Bulletin-----</td> <td style="text-align: right;">1 00</td> </tr> <tr> <td>Dec. 19. " " dues of 1882-----</td> <td style="text-align: right;">5 00</td> </tr> <tr> <td>" " " " " 1883-----</td> <td style="text-align: right;">25 00</td> </tr> <tr> <td>" " " " " 1884-----</td> <td style="text-align: right;">130 00</td> </tr> <tr> <td>" " " " " 1885-----</td> <td style="text-align: right;">730 00</td> </tr> <tr> <td>" " " " " 1886-----</td> <td style="text-align: right;">15 00</td> </tr> <tr> <td>" " " for interest on bonds:—</td> <td></td> </tr> <tr> <td>On \$1,000 at 4½ per cent.-----</td> <td style="text-align: right;">\$45 00</td> </tr> <tr> <td>" 1,500 at 4 "-----</td> <td style="text-align: right;">60 00</td> </tr> <tr> <td></td> <td style="text-align: right; border-top: 1px solid black;">105 00</td> </tr> </table>	Jan. 5. To cash received from C. Abbe-----	\$213 04	Mar. 20. " " for sale of Bulletin-----	1 00	Dec. 19. " " dues of 1882-----	5 00	" " " " " 1883-----	25 00	" " " " " 1884-----	130 00	" " " " " 1885-----	730 00	" " " " " 1886-----	15 00	" " " for interest on bonds:—		On \$1,000 at 4½ per cent.-----	\$45 00	" 1,500 at 4 "-----	60 00		105 00	<table border="0" style="width: 100%;"> <tr> <td colspan="2">1885. By disbursements, as per vouchers:—</td> </tr> <tr> <td style="width: 50%;">March 17. Cash paid Judd & Detweiler, bal. found due on last year's account.-----</td> <td style="width: 50%; text-align: right;">\$40 00</td> </tr> <tr> <td>Cash paid same for printing, binding, etc. vol. 7 of the Bulletin-----</td> <td style="text-align: right;">500 63</td> </tr> <tr> <td>June 13. Cash paid janitor for attendance on 18 meetings of the Society-----</td> <td style="text-align: right;">18 00</td> </tr> <tr> <td>Dec. 19. Cash paid for miscellaneous printing, circulars, bills, postal cards, and new set of record and account books-----</td> <td style="text-align: right;">69 15</td> </tr> <tr> <td>Cash paid miscellaneous expenses of Secretaries and Treasurer, for postage, stationery, clerical work, etc.-----</td> <td style="text-align: right;">112 24</td> </tr> <tr> <td>Balance, with Riggs & Co.-----</td> <td style="text-align: right;">484 02</td> </tr> <tr> <td></td> <td style="text-align: right; border-top: 1px solid black; border-bottom: 3px double black;">\$1,224 04</td> </tr> </table>	1885. By disbursements, as per vouchers:—		March 17. Cash paid Judd & Detweiler, bal. found due on last year's account.-----	\$40 00	Cash paid same for printing, binding, etc. vol. 7 of the Bulletin-----	500 63	June 13. Cash paid janitor for attendance on 18 meetings of the Society-----	18 00	Dec. 19. Cash paid for miscellaneous printing, circulars, bills, postal cards, and new set of record and account books-----	69 15	Cash paid miscellaneous expenses of Secretaries and Treasurer, for postage, stationery, clerical work, etc.-----	112 24	Balance, with Riggs & Co.-----	484 02		\$1,224 04
Jan. 5. To cash received from C. Abbe-----	\$213 04																																						
Mar. 20. " " for sale of Bulletin-----	1 00																																						
Dec. 19. " " dues of 1882-----	5 00																																						
" " " " " 1883-----	25 00																																						
" " " " " 1884-----	130 00																																						
" " " " " 1885-----	730 00																																						
" " " " " 1886-----	15 00																																						
" " " for interest on bonds:—																																							
On \$1,000 at 4½ per cent.-----	\$45 00																																						
" 1,500 at 4 "-----	60 00																																						
	105 00																																						
1885. By disbursements, as per vouchers:—																																							
March 17. Cash paid Judd & Detweiler, bal. found due on last year's account.-----	\$40 00																																						
Cash paid same for printing, binding, etc. vol. 7 of the Bulletin-----	500 63																																						
June 13. Cash paid janitor for attendance on 18 meetings of the Society-----	18 00																																						
Dec. 19. Cash paid for miscellaneous printing, circulars, bills, postal cards, and new set of record and account books-----	69 15																																						
Cash paid miscellaneous expenses of Secretaries and Treasurer, for postage, stationery, clerical work, etc.-----	112 24																																						
Balance, with Riggs & Co.-----	484 02																																						
	\$1,224 04																																						

ROBERT FLETCHER,
Treasurer.

TREASURER'S REPORT.

XXIX

BULLETIN

OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON.

ANNUAL ADDRESS OF THE PRESIDENT.



ANNUAL ADDRESS OF THE PRESIDENT,

ASAPH HALL.

Delivered December 5, 1885.

AMERICAN SCIENTIFIC SOCIETIES.

Mr. Chairman and Fellow-Members of the Philosophical Society:

The termination of the office with which you have honored me during the past year brings, in accordance with our custom, the duty of addressing you, and I have chosen for my subject *American Scientific Societies*. The Philosophical Society of Washington is the first scientific society of which I was a member, and, having still a lively recollection of the curiosity and interest with which I watched its formation and early progress, I propose to consider briefly the history of such societies in our own country, and incidentally, some of their benefits.

Nothing can be more natural than the union of men of similar tastes and thought into associations for the investigation and discussion of matters that mutually interest them, and thus we see in all civilized countries the formation of societies in every branch of learning and of art. In the countries of Europe such bodies have been a long time in existence, and many of them are still in vigorous life. Most of these societies owe their establishment to the favor of a powerful patron, generally an emperor or a king, who was wise enough to understand that the well-being of his people would be enhanced by the progress of science and art. But whatever may have been the motive of their foundation, these academies of scientific men have exerted a great influence on the civilization of Europe. Such an assertion may seem doubtful to the readers of what is called history, but in fact the larger part of our civilization that is good and permanent will be found closely connected with the works and inventions of scientific men. It is these works that have changed our ideas and conception of the world in which we live, and of the universe around us. It is these works, also, that slowly but surely compel the changes of political and theological theories. History, as it is now written, deals mostly with battles and sieges, with the

actions of emperors and kings, the amours of princes, and the intrigues of courtiers and priests. These are the bubbles and froth of the social world that have attracted nearly all historical writers, but there is a growing feeling that such recitals do not contain the substantial parts of history. Who would not wish to know more of the social forces that have been at work in Europe and in our own country, and which have converted some of the most rugged and barren parts of the world into the richest and most prosperous—of the ingenious and persevering industry that brings about the greatest changes in the customs of men and in the political power of nations? These changes come from an increase of command over the forces of nature, and in our ability to make these forces work for us. Now it is the discovery and study of these forces and their modes of action that form a large part of scientific work; and if we turn to the academies of Europe we shall find that they have a splendid history. By their encouragement of the labors and writings of ingenious men, by just criticism, and by the publication of memoirs these academies take a prominent place in the history of science. It is in these enduring monuments of the human intellect, rather than in brazen statues or marble shafts, that the real glory of the race consists.

The men who settled our country were separated by a great ocean and a month's journey from the civilization and learning of Europe. They had ample work to do in building houses and roads, and in establishing themselves securely in this new world. However, they soon began to set up schools and colleges, so that the elements at least of learning might be kept alive. But the inhabitants were scattered over a great extent of country, and means of communication were poor. Under these circumstances concerted action and union into societies were difficult, and a century and a half passed away before the formation of a formal scientific society. The first society of this kind that I find in our country is the American Philosophical Society of Philadelphia, organized in 1769. At that time Philadelphia was the largest and the leading city of this country, and being in a good degree free of the bitter theological quibbles and disputes that embroiled New England communities, it was better adapted for the home of a scientific society. It was also the residence of Benjamin Franklin, who appears to have taken an active part in the formation of the new society, and who became its first president. Franklin was a native of Boston, but when seven-

teen years of age, having written and spoken disrespectfully of what he called "religious knaves," and having thus provoked the enmity of influential men in his native town, he sought and found a home in a more genial climate. The new society began well. Its first three presidents were Benjamin Franklin, David Rittenhouse, and Thomas Jefferson. This society formulated and published an excellent plan of scientific work, including a study of the native inhabitants of the country, an examination of the ancient mounds of the Western States, and researches in geology and natural history. In 1796 it offered several prizes, with premiums ranging from fifty to one hundred dollars. The first premium offered was "for the best system of liberal education and literary instruction adapted to the genius of the government, and best calculated to promote the general welfare of the United States, comprehending, also, a plan for instituting and conducting public schools in this country on principles of the most extensive utility." Premiums were also offered for improving the method of computing longitudes from lunar distances, for the improvement of ship pumps, for the improvement of stoves or fire-places, for the best method to prevent the premature decay of peach trees, for a treatise on native American vegetable dyes, and for the best improvement of lamps. This society published its first volume of memoirs in 1771. Among the first contributors was David Rittenhouse, the able and ingenious astronomer, and the first volume contains a very full account of the Transit of Venus that happened June 3, 1769. We find here, also, some account of improvements in the sextant, which appears to have been independently invented by Thomas Godfrey, of Philadelphia, in 1730. Franklin was an early contributor to the memoirs, his writings generally having a very practical bearing. His first paper is on the causes and cure of smoky chimneys, and occupies thirty-six quarto pages. It is an interesting paper on an important subject, much discussed at that time. A correspondent of Franklin declares its importance by quoting the lines—

"A smoky house and a scolding wife
Are two of the greatest ills in life."

This was followed by other papers of Franklin on the formation of the earth, the theory of light and heat and of magnetism, and on the manufacture of paper. Franklin thought the interior of the earth is a heavy fluid, and he imagined magnetism to be a general

property of the universe, so that one might govern his course from star to star by the compass. The succeeding volumes contain several ingenious memoirs by Joseph Priestley, in some of which he expounds the theory of phlogiston, which appears to have been purely a hypothetical substance for explaining the theory of combustion. The volume of these memoirs published in 1825 contains a letter from Albert Gallatin, Secretary of the Treasury, under date of March 25, 1807, and addressed to Mr. F. R. Hassler, of Philadelphia, relating to the survey of our coast. There is a long and interesting reply by Hassler, who gives a full account of the methods of such a survey, with descriptions of instruments, forms for keeping the observations, making maps, and carrying on the work generally. Still later these volumes contain the memoirs of Joseph Henry on his important researches in electricity and magnetism. These papers were read in January, 1835, and published in 1837. The American Philosophical Society has published twenty-one volumes of memoirs, which contain papers of enduring interest. One feels regret that a society that began so well and which has published so much of value should stop the publication of its memoirs and seem to flag in its scientific work. Let us hope that this may be only a temporary condition.

The next establishment of a scientific society in our country is that of the American Academy of Arts and Sciences in Boston. This society was chartered in 1780, James Bowdoin being the first president. The Boston society does not appear to have started under such favorable auspices as its sister society in Philadelphia, but on the other hand it has kept up its scientific work better, and is still active and efficient. Perhaps this may be owing to its proximity to a large and flourishing college, which has now developed into a university. The American Academy of Arts and Sciences has published fifteen volumes of memoirs. Among its distinguished members I cannot omit to mention Nathaniel Bowditch, the self-taught mathematician, who was probably the first man in our country to really grasp the methods of the *Mecanique Celeste*. It is one of the surprises of our prolific country that it produces so many men who, it is said, read the *Mecanique Celeste* before they graduate from college, and it is another surprise to meet these same men in after life and be convinced from their own lips that they know but little about that great work. But Nathaniel Bowditch mastered it.

These two societies, that of Philadelphia and that of Boston, are

the most widely known and they are among the best of our local societies. Many others have been established or revived recently, and some of them are doing good work. Among those which have taken a high standing by the publication of valuable memoirs is the Connecticut Academy of Arts and Sciences. Such societies deserve a hearty support, and by their encouragement and direction of local talent can render valuable service to science. But these societies are too numerous to mention here.

I cannot, however, pass from the two elder societies without noticing in the first place the gradual cessation of their memoirs and the falling into what are styled "proceedings" for publication. It seems to me a matter of regret that this should happen. Such publications are apt to degenerate into a dry account of meetings, and elections, and deaths and resignations, and lists of members. If this is all a society is able to do it may be tolerated for awhile, but it is a condition which should be outgrown. I think that keeping up a good form for printing memoirs tends to elevate the character of a society and to incite members to good works.

There is another matter in connection with these two elder societies which is curious and worthy of mention. Each of them had a list of foreign honorary members. It is interesting now after the lapse of a century to examine these lists, and to see what kind of men were selected for such honors, and also to see how far the judgment of the philosophers has been confirmed by time, which makes such havoc with the estimates of men. At the time of the organization of the American Philosophical Society, Euler was the leading mathematician of Europe. He was then sixty-two years old and at the height of his reputation. There is hardly a branch of mathematics which Euler had not enriched by his ingenious and wonderfully prolific labors. He had worked in the theory of numbers, in all parts of the calculus, and had laid the foundations of the calculus of variations. He wrote a complete treatise on dioptrics, made a laborious and valuable investigation of the lunar theory, and applied mathematical theories to a very great number of physical questions. In 1766 he became blind by his incessant labors, but still continued his work. I do not find the name of Leonard Euler in the list of the fifty-five foreign associates of the American Philosophical Society. The successor of Euler as the leading mathematician of the world was Lagrange. The *Mecanique Analytique* was not published until 1788, but Lagrange had shown his power in a great

number of memoirs on mathematical and astronomical questions. The *Mecanique Analytique* put him at the head of all living investigators in the theory of rational mechanics; and this book remains to-day a model worthy the study of every student. In fact at the present time, when so many doctors and professors seize the great analytical machine and turn out pages of elegant and trifling formulæ, there can be no better experience than to go back to the luminous pages of Lagrange. Here is a master whose symbols are always in subjection, and who has no need to startle us by mysterious phrases. His inventions and improvements are among the most valuable in the history of pure and applied mathematics. But the name of Lagrange is not on the list of honorary members of the American Philosophical Society. Laplace was a younger man than Lagrange, but he was fortunate in securing a good position in Paris in early life, and he immediately began that wonderful career of scientific labors that culminated in the *Mecanique Celeste*. The first volume of this work was published in the year *seven*, or in 1799. It is the methodical arrangement and condensation of the labors of his great predecessors and colleagues of that century, together with his own remarkable investigations—a work that placed him at the head of the philosophers of his day. But his fame was not of the kind to put him on the honorary list of the American Philosophical Society. It may be worth while to look for one name more, that of Legendre, the ingenious and persevering mathematician who lived such a quiet and unpretentious life that we are not surprised to find his name omitted. I think this example is worthy of notice, since it shows that the scales of philosophers do not weigh men much more accurately than those of other people. But it would be a mistake to suppose that this society differed in this respect very much from others of its own time. The matter may be instructive in warning us against careless estimates of our cotemporaries, and by giving us caution in judging scientific men from their social position and rank. It may also throw light on the election to positions in our scientific societies of men whose chief recommendation is a noisy and uncertain reputation. However these things may be one thing is certain: the lords, counts, and gentlemen of the honorary lists are dead, buried, and forgotten; but the names of the four men who could not command this distinction live in the memories of all men of science.

Omitting for the present any reference to the many scientific socie-

ties that have been organized recently I come to our national societies. The earliest of these is the American Association for the Advancement of Science. The first meeting of this association was held in Philadelphia in 1848, and was called to order by Professor William B. Rogers, of Virginia, who had taken a prominent part in its formation. Only one volume of memoirs has been published by the American Association, but its annual volume of proceedings has been issued with regularity. This association has embraced among its members nearly all the prominent scientific men of the country, and it is our most complete national scientific organization. The plan of its formation seems to have been a good one, and I think it has exerted an excellent influence by bringing into acquaintance and sympathy men from different parts of the country. In recent years its character has become more popular, and under the lead of its energetic secretary its membership has reached nearly two thousand. During its early days this society took an active part in discussing the scientific operations carried on by the General Government, and its influence in this direction seems to have been wise. With the increase in the number of members such discussions have been judiciously avoided, and even the passing of resolutions, so common in all American bodies, might perhaps better be omitted. In such large bodies there is apt to be so much confusion and dispute that the resolutions are made extremely vague and meaningless or are manipulated to suit the purpose of a few. There is another danger to this society arising from its easy conditions to membership and its rapid increase of members. Our country produces a large number of men and women who are born with a mission. Educated in the schools and colleges, but never attaining much distinction as scholars, these people begin in their own phrase to think for themselves. The result of this thinking is often some discovery in science, and one that contravenes doctrines established by long observation and study. The questions considered are generally vast and mysterious, such as the origin of gravitation, the nebular hypothesis, and the nature of force. Having made his discovery the author wishes of course to present it to the world, and what method is more convenient than through a scientific society, admission to which is so easy. And if we admit a person to membership and take his money how can we refuse to listen to his theories. Who that has had the honor of presiding over one of the sections of the American Association, in casting his eye over

the audience, has not had brought to mind the description of Dean Swift :

“The first man I saw was of meagre aspect, with sooty hands and face; his hair and beard long, ragged, and singed in several places.

He had been eight years upon a project for extracting sunbeams out of cucumbers, which were to be put into phials hermetically sealed, and let out to warm the air in raw and inclement summers. He told me he did not doubt in eight years more he should be able to supply the governor's gardens with sunshine at a reasonable rate; but he complained that his stock was low, and he entreated me to give him something as an encouragement to ingenuity, especially as this had been a dear season for cucumbers.”

Now although this matter has a comical phase, it has also its serious and difficult side. No man of science wishes to suppress the opinions of others, and ingenious speculations are worthy of attention, but he has a right to his own time, and should be freed from the trouble of listening to absurd projects. How this can be done with such an easy course of admission to membership I do not see. There is another hindrance to the successful operation of the American Association which comes from the great extent of our country and the cost and difficulty of attending its meetings. To those who have ample time and means at their disposal this hindrance is not, perhaps, very great. This vigorous and generous society may need a little pruning, but on the whole its influence has been good, and every one must wish it a long and honorable life.

We have another scientific organization of national character in the National Academy of Sciences, established in 1863. This is a body on a basis quite different from that of the American Association for the Advancement of Science. The National Academy was brought into existence during a great civil war, and its members were of necessity chosen from one section of the country. It was incorporated by act of Congress, and this act limited the number of its members to fifty. From the language of the act we may fairly infer that the academy was intended to be the adviser of the General Government in matters of science. During a time of great civil commotion, when the powers of the Government were greatly extended, such a society would very naturally come into existence; but when the strife had subsided it became an object of criticism.

In filling vacancies in its membership it was difficult always to

select the best man, and sometimes abler men were left out of the academy than those who had the right kind of influence to be appointed. Scientific men are like other people, and they elect their friends and those whom they think will help them. Within a few years after the close of the civil war the limitation of the number of members was removed by act of Congress. The National Academy has now the power to determine the number of its members, and for the present this has been practically fixed at one hundred. Whether this number should be increased, and whether its membership should be more evenly distributed throughout the country are questions over which the academy has entire control. Its destiny, therefore, is in its own hands, and it is to be hoped, and it is to be expected, that its career will be useful and honorable. To act such a part as this the academy must maintain a high and independent character. It should choose for its members the best and ablest scientific men of the country, and it must never become the tool of the shrewd men who deal out the rich patronage of the Government. That there is need for such an independent body to criticise and assist in the direction of the scientific work done by public authority seems beyond question. It is assumed, of course, that the General Government is to carry on scientific works of various kinds, a position which may be disputed by some, but which appears to be already practically conceded. How far the Government should enter on such works, and how much should be left to private enterprise, is a question of public policy. But there are certain works which belong almost of necessity to the General Government. Thus the survey of our coast and harbors, a general geological survey, and a good map of the country seem to belong to the work of the Government. These may be justified on the ground of their utility to the public. But there are other scientific works, not so directly connected with commercial and moneyed interests, that an enlightened government may properly undertake. Why should not there be in this country a first-class national astronomical observatory, where observations may be continued from one age to another with the best instruments of the times? Again, do not the elevated plains of the West offer an excellent opportunity for the determination of an arc of the meridian which may be extended from British America to the City of Mexico, and why cannot our General Government undertake such a determination? Must everything that is not strictly utilitarian be prohibited in the public works of our Repub-

lic? I do not think so. On the other hand the things that are purely commercial may generally be left to themselves.

But if the Government is to do scientific work it should have the aid of men of science. We all know the tendency of public officials to fall into habits of routine, and to spin out their work to an almost interminable length. There should be, therefore, a body of men who can criticise kindly, but boldly and justly, the labors of officials, and make them perform their duties as they ought. This, I think, should be one of the functions of the National Academy of Sciences. But to make this advice influential the Government must recognize the scientific men of the country, and give them some regular channel of communication through which their opinions can be made known to the public and to the executive authorities. Thus far in the history of our Government the scientific man has generally been regarded as an expert who is to be carefully watched, lest he get the better of the officials who are set over him, and who sometimes undertake to manage affairs of which they have but little knowledge. The jealousy thus engendered is unfortunate. The man of science should be treated just as other men are treated, and there should be no grumbling at paying him a fair recompense for his labor. Our national military and naval academies are costly institutions, and fortunate is the young man who has a Congressman for an uncle or a cousin; but I have never heard a word from any scientific man against the cost of these establishments. So far as I know, their universal sentiment is, let us have the best of instruction in military and naval science, for this is the cheapest. Our public buildings cost vast sums of money, but there is no objection to such expenditures if the buildings are well and solidly constructed, since here, also, the best is the cheapest. On the other hand, is there not something very absurd in the manner the politician looks on the small expenditures for science, and the lavish ones that are voted for other purposes? Let us take a single case. A public vessel is "repaired," to use an adopted euphemism, at one of our navy yards, and the cost of the repairs amounts to a million of dollars, or more than double the original cost of the ship. There is some astonishment at this, but we are told in a confident manner that the ship is greatly improved in strength and speed. The trial comes off, and while the ship is going along at her utmost speed, with the velocity of nine miles an hour, the engine breaks down. Here is a serious collapse, since before

she was repaired the vessel could make eleven miles an hour. The head of the Department very properly orders an examination. Now, it might occur to superficial persons that those who repaired that ship had made mistakes. But the examining board weighs the evidence carefully, and it deliberately comes to the conclusion that the fault lies wholly with some unknown person who is more than three thousand miles away. The matter is mysterious, but the result is certain. The Government has been cheated, the money is gone, and the local politicians are happy. And the curious thing is that the public accepts the report of the examining board as entirely satisfactory. There is not a whisper of dissent from any newspaper in the land. And, after all, it is only half a million dollars, and do we not throw away ten times as much every year on rivers and harbors? Have we not seen a Senator boasting in his speeches that during the last twenty years more of the public money has been expended on the mountain streams of his own State than that State has paid taxes into the public treasury.

Now change the case and let us suppose that some scientific man by bad management of his own or by failure of an assistant, has wasted ten thousand dollars of the public money. Ah, this is quite a different matter, and must be looked at from a different standpoint. How soon do we hear some smug official complacently remark that he always knew that scientific men cannot do business. And how eagerly the newspapers seize upon the case; how indignant the editors become, and how the head lines flare. Is there one law for the public functionary and another for the man of science?

But it is not right to leave this matter without further consideration. When we look at the advantageous position occupied by the officer of the army or navy we see immediately that this does not come from any personal merit he may have, but from the fact that he is recognized by law as an essential part of the Government. This position renders him in theory impersonal, and it is assumed that he has no private business of his own, but all his interests are one with those of the public. He has his member of the Cabinet to represent his views. His appropriations never fail, and he has no need to summon men from distant parts of the country to push his bills through Congress. Now, so long as the scientific man is looked upon merely as an expert and an adventurer, and has no regular channel of communication with the Government he will

stand at a great disadvantage. He may gain a victory now and then, just as militia may sometimes beat regular troops, but the final result is pretty sure to be defeat. The position of the man of science must, therefore, be recognized by law if he is to be connected with public works in such a way that he may act freely and usefully. Such considerations will bring up the question of how far the Government is to proceed in the cultivation of science.

If we examine the history of a country like England, where we have good records for a thousand years, we shall see that there has been a steady tendency toward three results. The first of these is personal liberty. The slave that was bought and sold has been changed to the serf, and the serf to the laborer. These changes have gone on with conflicts, and sometimes with retrograde movements, but on the whole they have proceeded until now, in nearly all civilized countries, personal liberty is secured by law. The second result is the freedom of opinion. To control such an intangible thing as the opinions of men is a difficult matter, but it is a business which many men delight in, and the contest, though old, is yet a living one. When Sir Richard Saltonstall reproached his friends in Boston for persecuting Baptists and Quakers, on the ground that such persecutions made men hypocrites, the Puritan ministers at once replied that hypocrites are much better than profane persons like Baptists and Quakers. But such people have been forced back from one position to another, explaining, apologizing, and retreating, until now in several countries opinion is nearly free. There remain a few able men who pray for more superstition and bigotry, but they are the relics of a past time. The third result is the right of free exchange, and toward this end we have gained but little, since nearly all governments exercise their power in prohibiting among men the free exchange of their products. The general course of events is thus to restrict the sphere of government, and to leave to the individual more and more freedom of action. The chief duty of government is to see that justice is done between man and man, and to this end that the courts are fair and intelligent, and that our judges are not owned by rich men and corporations; that the public service is honest and efficient, and is not used for personal or political aggrandizement. But, granting all this, it seems to me that the Government may properly undertake such great scientific works as I have mentioned, with the condition that they be placed under proper control and inspection. To the successful accomplishment

of these works the man of science must be brought into the public service. He must be held responsible, just as other officials are, in his account of public money. Such a condition would subject him to some limitations that might be irksome at first, since it is pleasant for many to have at their disposal large sums of money which they may use at their pleasure, and almost every one fancies that he could do a great deal of good in this way. But such a method of handling public money is dangerous, and is apt to lead into trouble.

Supposing that our public scientific works are to be carried on by men of science, what part the National Academy of Sciences shall act I cannot say, and it is not my province to urge on the Government the services of this academy, but here is a body of scientific men who have pledged themselves to the public service and they should be made to do their duty. And is there not ample room for intelligent criticism and suggestion in all the methods through which the public money is expended? Take the case of public schools, which is a kind of communism justified on the ground of utility to the State. What shall be the course of education in these schools? There is an unfortunate class of our fellow creatures that must be cared for at the public expense, but shall benevolent institutions encourage the production of such beings? Have we not read of the English poorhouse where were found the grandfather, the father, and the son, all hearty men,—paupers breeding paupers? Do not some of our charitable institutions give plausibility to the saying that the mistakes of the good do more harm than the vices of the wicked? In fact, turn to any of the modes of public expenditure and examples will be found where sober, scientific judgment is necessary for the wise conduct of business.

I come now to consider our own home society, the Philosophical Society of Washington. And, speaking cautiously and soberly, is it not to-day the best local scientific society in the country? This is owing partly and perhaps chiefly to our position at the Capital of a great people. Men from all sections come back to us as winter approaches, and many of them have interesting information to give. No other city of our country offers such advantages for fresh and early information of the investigations that are going on in the various departments of science. Our libraries in astronomy, mathematics, and medical science are among the best. As a general

library that of Congress must surpass all others in the country. These are advantages which make Washington an agreeable residence for men of science and literature.

I think also our society has a good plan of organization, thanks to the men who formed it. The general business can be safely confided to a committee, and in this way the meetings are made more interesting. This committee is so large that by a generous rotation in office most of the members may see and share, if they wish, the governing of the society. We have simple rules and they should always be enforced, since no society can afford to be overawed by any man, especially a society where we all meet as equals and where no favors are to be asked or granted. Our society has been established on a broad basis, to include all branches of learning, and as we have members from all the professions our meetings ought not to lack in variety of subjects. In such meetings the purpose of a paper should be to present the principal points clearly, and the author may generally trust to the intelligence of his audience to fill in the details. It is the failure to recognize this rule and the lack of arrangement that make some papers so long and tedious.

Our society has its home in a beautiful city, and who that has seen its wonderful growth during recent years can doubt its future splendor and greatness? It is a city cosmopolitan in its character. Being the seat of political power, here will come the enterprising and adventurous from all parts of the country, with additions from other lands. Some of the brightest names in our scientific annals are those of foreigners who have made their homes with us. Let us welcome all earnest men, remembering that the principles of science are universal, and are not confined to any language or country.

In respect of personal conduct we can have no better example than the noble man who was our first President, whose simple and devoted life was a model for every scientific man. If we need other inducements to devote ourselves to labors that may not give a great return of money, or lead to easy and luxurious lives, let us remember that we live in a magnificent country, and one that has been dedicated as we hope to the liberty and welfare of the human race. Each one of us may do a little in adding to her scientific renown, which is now only beginning. Let us recall the words of the great Athenian: "I would have you day by day fix your eyes upon the greatness of Athens, until you become filled with the love of her; and when you are impressed by the spectacle of her glory, reflect

that this empire has been acquired by men who knew their duty and had the courage to do it, who in the hour of conflict had the fear of dishonor always present to them, and who, if ever they failed in an enterprise, would not allow their virtues to be lost to their country, but freely gave their lives to her as the fairest offering which they could present at her feast. The sacrifice which they collectively made was individually repaid to them; for they received again each one for himself a praise which grows not old, and the noblest of all sepulchres—I speak not of that in which their remains are laid, but of that in which their glory survives, and is proclaimed always and on every fitting occasion both in word and deed. For the whole earth is the sepulchre of famous men; not only are they commemorated by columns and inscriptions in their own country, but in foreign lands there dwells also an unwritten memorial of them, graven not on stone but in the hearts of men.”



BULLETIN

OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON.

GENERAL MEETING.



BULLETIN

OF THE

GENERAL MEETING.

261ST MEETING.

JANUARY 3, 1885.

President HALL in the Chair.

The Chair announced the election to membership of Messrs. WILLIAM MUNDY POINDEXTER and ASAPH HALL, Jr.

The Auditing Committee, appointed at the annual meeting, submitted the following report:

WASHINGTON, D. C., *December 27, 1884.*

*Mr. President and Gentlemen of the
Philosophical Society of Washington :*

We, your committee, appointed at the annual meeting, December 20, 1884, to audit the report of the Treasurer for the year 1884, have the honor to submit the following report:

We have examined the statement of receipts of dues from members, and of interest on bonds, and find the former to be \$745, and the latter \$95, as appears in the Treasurer's statements of accounts for the year 1884.

In addition to the foregoing, \$15 were repaid to the Treasurer by a member for extra printing, thus making the total receipts \$855.

We have examined the vouchers for disbursements for the same period, and find them correct.

We have compared the return checks with the vouchers and with the entries in the bank book, and find them correct.

We have examined the bank book, and found the balance as set forth to be correct, said balance, deducting the amount of two checks not yet returned, being \$183.04, with Messrs. Riggs & Co.

The bonds referred to in the statement of assets were exhibited to us by the Treasurer, and consist of one \$1,000 U. S. bond @ 4½ per cent., one \$1,000 U. S. bond @ 4 per cent., and one \$500 U. S. bond also @ 4 per cent.

All of which is respectfully submitted.

H. C. YARROW,
 MARCUS BAKER,
 WILLIAM C. WINLOCK,
Committee.

On motion, the report was accepted and the committee discharged.

Mr. J. S. BILLINGS made a communication on

THE VITAL STATISTICS OF THE TENTH U. S. CENSUS,

presenting a brief outline of results soon to be published in Vol. XI of the Census Reports.

Remarks were made by Messrs. ELLIOTT, MALLERY, and ASAPH HALL.

262D MEETING.

JANUARY 17, 1885.

The President in the Chair.

The Chair communicated an invitation to the members of the Society to attend the annual meeting of the Biological Society and listen to an address by Dr. C. A. WHITE.

By request, Professor G. STANLEY HALL, of the Johns Hopkins University, made a communication on

RECENT EXPERIMENTS ON REACTION TIME, AND THE TIME SENSE,

reviewing the methods of investigation and the results attained.

An animated discussion followed by Messrs. ROBINSON, HILGARD, NEWCOMB, BILLINGS, EASTMAN, PAUL, WINLOCK, ASAPH HALL, and Professor GEORGE DAVIDSON, of San Francisco.

Mr. C. E. DUTTON then began a communication on

PRACTICAL GEOLOGY *versus* SPECULATIVE PHYSICS,

which was unfinished when the hour of adjournment arrived.

263D MEETING.

JANUARY 31, 1885.

The President in the Chair.

Fifty-eight members and guests present.

The Chair communicated an invitation to the members of the Society to attend the ninetieth regular meeting of the Anthropological Society, and listen to an address by Major J. W. POWELL.

Mr. C. E. DUTTON finished the communication begun by him at the last meeting on

PRACTICAL GEOLOGY *versus* SPECULATIVE PHYSICS,

and the subject was further discussed by Messrs. DOOLITTLE, MASON, CLARKE, WARD, WALCOTT, PAUL, TAYLOR, M. BAKER, and ROBINSON.

264TH MEETING.

FEBRUARY, 14, 1885.

The President in the Chair.

Thirty-one members present.

The Chair announced the election to membership of Messrs. CARL BARUS, FRANK AUSTIN GOOCH, and WILLIAM HALLOCK.

Messrs. F. W. CLARKE and J. S. DILLER made a joint communication on

TOPAZ FROM STONEHAM, MAINE,

describing the alteration of topaz into damourite. [The paper is published in the American Journal of Science, 3d series, Vol. XXIX, pp. 378-384.]

Mr. WILLIAM H. DALL made a communication on

TWO REMARKABLE FORMS OF MOLLUSKS.

Mr. DALL described the anatomical features of the remarkable *Chlamydoconcha Orcutti*, of San Diego, California,* which is in fact a degraded lamellibranch, in which the shell has become internal and functionless, and is no longer adjusted by adductor muscles.

He also described a remarkable feature which he had just discovered in *Milneria minima*, a small California bivalve, belonging

*The main features of this notice appear in Science, No. 76, Vol. IV, p. 50, 1884.

to the *Carditida*, and living on the backs of *Haliotis* shells. The female has the base of the shell pushed up into a dome in the median line, the opening to which is closed by an extension of the mantle. In the pocket so formed the young of the species are protected by the mother. The only other case among the lamellibranchs of such a protective modification is that of *Thecalia concamerata*, in which the same end is reached in a different manner. Both belong to the same family. The males of *Milneria* are without the pocket. Both sexes adhere by a byssus.

Mr. W. B. TAYLOR read a communication on

GEOLOGICAL AND PHYSICAL THEORIES,

in which, controverting the claims of practical or field geology—to the exclusion of physical theory—in the solution of physiographic problems, he contended that the family ties of planetary relationship cannot be disowned by geology. He thought the value of “external” inductions fully shown by the probable effects of varying eccentricity in the earth’s orbit on secular changes of climate, as well as by a reference to the general inter-relation between the meeting boundaries of astronomical, geological, physical, and chemical science. On the physical side, he maintained that the supposed demonstrations of the earth’s comparatively recent consolidation, (as well as of the limit assigned to the sun’s active life,) were entirely inconclusive: first, from the admitted uncertainty of the data, and secondly, from our ignorance that unknown factors might not enter into the problem. He therefore heartily agreed with Captain Dutton in recognizing the strong demands of geological induction for an incomparably longer chronology than terrestrial physics could as yet cipher out.* At the same time, the speaker contended that the certainty remained entirely unimpaired of an origin and a limit to solar—as well as to planetary—energy; unless we were prepared to accept the absurdity of an infinite potential. He also pointed out that the doctrine of “uniformitarianism” does not require (as sometimes too readily supposed) an unvarying degree of energy in geological dynamics throughout the distant past; but that the contrary was the more probable—if only from the broad generalization that all action whatever has its period or periods of maximum and minimum.

* Mr. Taylor’s paper was a reply to one by Mr. Dutton, of which the Society obtained no abstract. See pp. 4 and 5.

On the question whether geology itself gave us "traces of a beginning, or prospects of an end," Mr. T. argued that stratigraphical geology unmistakably indicated its own genesis in the plutonic character of its primæval "Archæan," or Laurentian—pointing to a time when the primitive surface was a molten ocean; and that when read in the light of palæontology such indication of a beginning was strengthened into convincing proof by the receding gradations of animal and vegetable life, starting in the lower Silurian and its underlying Cambrian, with the humblest invertebrate forms of molluscan and crustacean life, and the simplest cryptogamous thallogens—the marine algæ and fucaceæ. And in this connection he referred to the memorable generalization of Louis Agassiz—that the geological successions of animal types correspond remarkably with the phases of embryonic development—as one of the most suggestive contributions ever made to the theory of evolution.

The speaker then turned to the question of the earth's interior fluidity; and after stating that the celebrated mathematical arguments of Hopkins from the "precession" value, and of Thomson from the hydrographic tides, had both been practically abandoned by the latter—though he still persisted in his pre-possessions for a solid globe (mainly on the specific-gravity skepticism), Mr. T. said he felt no difficulty whatever in accepting the geological evidences of a fluid earth enveloped by a flexile, friable egg-shell. With regard to the large amount of contraction and corrugation every where exhibited by this shell, he admitted that Mr. O. Fisher had conclusively disproved the sufficiency of Élie de Beaumont's plausible hypothesis that the contraction is due to the secular cooling of the planet. Mr. Fisher had however no better speculation to offer; and the answer to the riddle must come ultimately—not from petrology; nor from structural, or stratigraphical, or physiographical geology—but from cosmological physics. In conclusion, the speaker urged that the same inductions which so clearly establish the birth, the childhood, and the manhood of our planet, as inevitably implicate its decline, decadence, and decease; and he quoted passages from Byron's familiar lines on "Darkness," as in the main a scientific prophecy.

Mr. PAUL spoke of the importance of a recent contribution to the subject of the earth's rigidity by Mr. George H. Darwin. Mr. GILBERT thought that Darwin's deduction of high rigidity was vitiated by his postulate of homogeneity.

The President remarked on the great interest of the discussion opened by Captain DUTTON's communication to a preceding meeting, and expressed his especial approval of the method in which Mr. WARD had approached the subject.

265TH MEETING.

FEBRUARY 28, 1885.

The President in the Chair.

Fifty members and guests present.

The Chair announced the election to membership of Messrs. THOMAS CORWIN MENDENHALL, ALEXANDER ZIWET, HOWARD LINCOLN HODGKINS, BAILEY WILLIS, JOSEPH PAXSON IDINGS, and C. F. MARVIN.

Announcement was also made of the death of the Hon. HORACE CAPRON.

Mr. C. ABBE made a communication on

METHODS OF VERIFYING WEATHER PREDICTIONS,

giving a general account of the rules under which the U. S. Signal Office deduces from "indications" and subsequent observations the published percentages of verifications. For purposes of prediction and verification the area of the United States is divided into a small number of districts. The "indication" for each district refers to the subsequent 24 hours, and is compared with the three next following weather-maps constructed from the observations, and the degree of correspondence for each station in the district is marked on a scale of five terms—0, 25, 50, 75, and 100. The published percentages are means of these marks. For certain special classes of phenomena—such as high-winds, frosts, and cold-waves—in which the indication only discriminates the occurrence and non-occurrence of a specific event, the formula for percentage of verification is

$$\frac{v}{n + o}$$

in which n is the whole number of times the event is predicted, v is the number of verifications, or of events coincident with predictions, and o is the number of unpredicted events.

It has been found for a large area in Europe, an area comparable

in size with one of the districts above mentioned, that, on the average, a given type of weather—*e. g.*, rain, threatening, fair, hot, cloudy, clear—can prevail simultaneously over only 85 per cent. of the area. If this law holds for the United States, we can hope for no better predictions while the existing system of districts is adhered to, for our percentage of verification is now approximately 85.

Mr. CURTIS described the method of verification adopted by the Deutsche Seewarte. It differs from that of the U. S. Signal Service in that the predictions are compared for verification with the observations at a single representative station in each district. Thus, for northwest Germany, the observations at Hamburg are employed. The limits for the prediction of stationary temperature are taken as $\pm 1^{\circ}$ C., on the basis of an investigation by Hann who found that the "change in 24 hours at Hamburg, in two-thirds of all cases, averages less than two degrees C." Mr. CURTIS showed that, for verifications to be directly comparable with respect to skill in prediction, the limits for "stationary" must vary in different districts and at different seasons of the year. Unless such variations are adopted, the verifications should exhibit a uniform geographical difference, and an annual period, if the method employed possesses any scientific accuracy. As any such change of definition would be impracticable, it would seem desirable to base the range allowed for "stationary" temperature entirely on physiological considerations, leaving the question of comparability for subsequent discussion.

In reply to a question by Mr. PAUL, Mr. ABBE said that the rules required that a prediction covering 24 hours should be verified by the maps compiled at the 8th and 16th hours, as well as by that compiled at the 24th. The desirability of subdividing the geographic sections to which the weather predictions apply was discussed by Messrs. GILBERT, PAUL, and ABBE; and Mr. ABBE said that if any change was made, it would consist in the abandonment of specially defined districts and the substitution of individual States.

Mr. H. A. HAZEN remarked that if the prevailing weather in a district treated as a unit actually pertained, on an average, to but 85 per cent. of the district, then only omniscience could attain to a success in weather prediction measured by 85 per cent. of verification.

Mr. A. HALL made a communication on

VARIATIONS OF LATITUDE,

discussing the observations tabulated by Mr. Fergola, and reaching the conclusion that the evidence fails to show that latitudes are variable.

[The paper is published in the American Journal of Science, 3d series, Vol. XXIX, pp. 223-27.]

Mr. R. S. WOODWARD said that he had recently undertaken the discussion of the subject with somewhat fuller data than those used by Mr. HALL. Postulating that the pole was changing its position by motion at a uniform rate on the arc of a great circle, he computed the direction to be along the meridian 50° west of Greenwich, and the rate of motion about $2''$ per century. His investigation was not yet completed, but he inclined to the opinion that actual change was indicated by the data used.

Other remarks were made by Messrs. FARQUHAR, BAKER, and PAUL.

266TH MEETING.

MARCH 14, 1885.

The President in the Chair.

Fifty-four members and guests present.

The Chair announced the election to membership of Messrs. ROBERT PORTER HAINS and GEORGE MITCHELL WRIGHT.

The Chair read a letter from Mr. A. C. PEALE, announcing the death, on the 13th of March, of Mr. TITIAN RAMSAY PEALE, one of the founders of the Society. Mr. Peale accompanied Colonel Long in his explorations of the Rocky Mountains as naturalist, and was afterwards a member of the Wilkes' exploring expedition.

Mr. H. ALLEN HAZEN made a communication on

THUNDERSTORMS OF 1884.

This paper was a resumé of some of the investigations made by the Signal Office, looking to a detailed study of the origin, progress, and development of thunderstorms. Over 13,000 special reports were received and studied. An attempt to connect thunderstorm frequency with the phases of the moon showed a rather marked

increase during the time of new moon, thus corroborating the result previously obtained by Dr. Köppen.

A comparison of storm frequency with the period of solar rotation gave a marked maximum during the rotation. It was shown that taking the mean temperature over the whole storm region there was a close relation between the occurrence of high temperature and storm action, the former preceding the latter by about 24 hours.

Taking the mean of the meteorological elements on 20 days of many storms at many of the stations, it was found that a marked low-pressure area was present to the northwest of the storm region, there was also a high temperature, while the humidity and weather were normal. On 20 days of few storms the reverse was found true, namely, a relatively high pressure and low temperature, the humidity and weather being normal as before. These results were highly interesting as bearing upon the conditions favorable to thunderstorm action. The detailed study gives promise of large additions to our knowledge of these meteors.

In the ensuing discussing, Messrs. MUSSEY, RAY, ANTISELL, E. FARQUHAR, PAUL, GILBERT, ROBINSON, and HAZEN spoke of the topographic, geographic, and seasonal distribution of thunderstorms and of the relation of the precipitation to the electric phenomena. Mr. ANTISELL said that moisture is essential to their generation; they are a secondary effect of the influence of the sun, not a primary. Mr. E. FARQUHAR spoke of the concentration of electricity by diminution of aqueous surface, when cloud-particles coalesce and form raindrops.

Mr. S. M. BURNETT exhibited and explained

THE JAVAL AND SCHIÖTZ OPHTHALMOMETER.

Mr. A. B. JOHNSON began a communication on

THE DIFFICULTY IN DETERMINING THE DIRECTION OF SOUND.

267TH MEETING.

MARCH 28, 1885.

The President in the Chair.

Forty-two members and guests present.

The Chair announced the election to membership of Messrs. GUSTAVE LOUIS RAVENÉ, THOMAS MAREAN CHATARD, HERBERT

MICHAEL WILSON, WILLARD ADAMS SHUMWAY, and JEFFERSON FRANKLIN MOSER.

Mr. A. B. JOHNSON then completed his communication on

THE DIFFICULTY IN DETERMINING THE DIRECTION OF SOUND,

illustrating his remarks by a model of the topophone. The following is an abstract of the entire paper.

Mr. JOHNSON said the hunter could not locate his game by the sound it made, unless the sound was frequently repeated; that the plainsmen could not locate each others' site by shouts, until they were frequently repeated; that a child calling its mother in a house could not tell which room she was in, or even the floor she was on, until her voice was heard several times; that it was hard to tell, from its noise alone, whether a street-car was going to the right or left, in approaching it at right angles; in fact that it was not easy to fix by the ear alone, the location of the source of any sound.

A dog aroused from sleep by the call of his unseen master frequently dashes in different directions before hitting the right one. Game startled by hearing a hunter's tread will as readily run into, as out of danger. Blind people, despite the highly developed condition of their remaining senses, do not appear to be more able to determine the source of sound, other things being equal, than seeing people. It seems to be a question whether people generally do not use sight, touch or smell, involuntarily in locating sound. Hence, when they are so placed that they must depend on hearing alone, and err unusually in doing so, they consider such instances as abnormal.

After referring to subjective errors in audition, which frequently arise, Mr. JOHNSON spoke of the peculiar class of errors in audition into which mariners are apt to fall, often resulting in disaster. The collision between the ocean steamers Edam and Lepanto, was referred to, in which the former was sunk, as the latter had erred an eighth of the compass circle in fixing her position by the sound of her fog signal, and thus ran into her. A lawsuit ensued, in which Judge Addison Brown, of the U. S. District Court of New York, decided against the plaintiff, holding "that an error of five points, in locating a vessel by the sound of her whistle in a fog, is not necessarily a fault, under the proved aberrations in the course of sound."

Mr. JOHNSON then read from Judge Brown's opinion, extracts from papers read before the Washington Philosophical Society by three of its former Presidents, Henry, Taylor, and Welling, and by himself, all as to the difficulty of determining the direction of sound, and he congratulated the Society that its conclusions had been adopted by the courts.

As it was evident that the unaided ear could not be relied upon to fix the direction from which sound came, Mr. JOHNSON said attention should be directed to giving the ear all possible assistance. That something of this kind could be done was proved, he thought, by Professor Morton's experimentation with the topophone. This instrument had been devised by Professor Mayer of the Stevens Institute of Technology. It consisted of an arrangement by which two Helmholtz resonators were connected on the deck of a steamer with rubber tubes running into the cabin and with bars and rods which could be moved from the cabin. The actuating principle of the device was the neutralization of the dynamic force of the full sound wave by the half sound wave, thus approximating silence, and thus indicating automatically, within ten degrees, or less than one point of the compass, the direction of the sound.

Mr. PAUL remarked that the bar connecting the resonators should be shorter than the wave length of the sound under observation, since otherwise deceptive results would be obtained with the two resonators in similar phases of different waves. Mr. TAYLOR questioned the utility of the instrument, though heartily applauding its ingenuity. The real difficulty in determining sound direction arises from the heterogeneity of the air in point of density and moisture, and especially from its indeterminate differences of movement, whereby diffractions and refractions are occasioned many times greater than those affecting light. The topophone, like the ear, is cognizant only of the final direction of the incident beam of sound, so to speak, and can tell us nothing of the direction of the source of sound. Mr. E. FARQUHAR remarked that the verdict of the ear in regard to direction is usually just; the conditions under which it errs are exceptional. He thought there was a rapid adjustment by motion of the head, from which the general direction is almost involuntarily ascertained. Mr. F. BAKER said that animals, such as, for example, the carnivora, make fewer mistakes than man, and this is probably due to their muscular control of the external ear. When the ears are pricked up in listening, special tensions may be given

to the *concha*. When man listens intently he adjusts the tensions of the *membrana tympani*.

The possible influence of wind velocity on the pitch of sound was discussed by Messrs. PAUL, TAYLOR, and GILBERT, and other remarks were made by Messrs. KING, HALL, ELLIOTT, and H. FARQUHAR.

Mr. WASHINGTON MATTHEWS began a communication on

MYTHOLOGICAL DRY PAINTINGS OF THE NAVAJOS,

which occupied the remainder of the evening. Its completion was deferred.

268TH MEETING.

APRIL 11, 1885.

Vice-President BILLINGS in the Chair.

Forty-six members and guests present.

Mr. WASHINGTON MATTHEWS concluded his paper on

MYTHOLOGICAL DRY PAINTING OF THE NAVAJOS.

This paper described an art in use among the medicine men of the Navajo Nation, by which they represent various mythological conceptions on the sanded floor of the medicine lodge with dry pigments of five different colors. These dry paintings are from ten to twelve feet in diameter, and are quite intricate, containing from five to thirteen mythological figures of large size. About a dozen men labor from eight to ten hours in making them. When completed, they are after some ceremonies completely obliterated, and even the sand on which they are drawn is carried out of the lodge and thrown away. The existence of such an art is not generally known and the figures are not copied from any visible standard but are retained in the memories of the medicine men.

The paper was illustrated with seven water-color paintings—reproductions of the Navajo drawings. Four were pictures of the esoteric portion of a Navajo ceremony called *dsilyidje-qaçal* or “song in the mountains,” and represented visions or revelations of the Indian prophet who instituted these ceremonies. The remaining three pictures were from a ceremony known as *kledje-qaçal* or “song of the night,” and represented the revelations of another Navajo

prophet, he who, according to their mythology, instituted the latter ceremonies. The symbolism of the pictures was explained, and such portions of the myths as directly referred to the pictures were related.

The first picture showed the house of the great snakes. The second represented the gods of the domestic plants, with the principal domestic plants of the Indians, corn, bean, pumpkin, and tobacco, indicated by highly conventionalized figures. The third picture was of certain goddesses of great height, called the Bitsihi-nez or Long-bodies, which the prophet is said to have seen in a house made of dewdrops. The fourth drawing depicted the sacred arrows used in the dance, which the medicine men pretend to swallow. The lecturer explained the trick by which this imposture was carried out. The fifth picture represented the peculiar myth of the tsis-naole or whirling sticks. It represents two logs placed in the center of a lake so as to form a cross. Eight divine beings sat on these logs, which were kept constantly whirling by other gods who poked the logs with plumed staves. There were twelve apotheosized human figures in the picture. The sixth picture showed the kledje qaçal as it took place in the abodes of the gods when the Navajo prophet first saw it, and is a fair representation of the dance as it is performed among the Navajos to-day. The seventh painting represented a portion of the dance among the gods, at a time when a spell had been cast upon them by the angry Coyote-god.

The figures in the east of the pictures are painted in white, those in the south blue, those in the west yellow, those in the north black. This is the usual order of Navajo color symbolism; but sometimes the white is assigned to the north and the black to the east; instances were given where this interchange took place.

The gods in many cases are shown standing on rafts made of sunbeams, such rafts being favorite vessels of the gods when they make their aerial journeys. The gods are depicted with round heads, the goddesses with quadrangular heads. In the dances, the actors wear masks of corresponding shapes to indicate males and females.

Seven of the pictures were surrounded with symbols of the rainbow deity, which with the Navajos, as with the Greeks, is a goddess.

The sandèd floor on which the pictures are drawn is slightly sprinkled with charcoal; this is to convey the idea of a surface of clouds, for it is said that in the houses of the gods these pictures were drawn on sheets of clouds.

The speaker closed by referring to the transitory nature of the pictures, and showing how it might easily have happened that no knowledge of them would ever transpire.

Mr. GILBERT THOMPSON described pictures on the walls of a shallow cave near San Antonio Spring, New Mexico, and exhibited copies of the same. The outlines of the pictures are etched on the rock, and several different colors are employed, both in the etched grooves and on the plane surface of the rock. Mr. MATTHEWS explained the relations of these drawings to Navajo myths and ceremonies.

In response to questions by Messrs. BILLINGS, M. BAKER, PAUL, and MALLERY, Mr. MATTHEWS said that individual drawings are not repeated on the same occasion. The ceremonial dances, most of which take place only during the season when the snakes hibernate, are executed for the benefit of invalids, or for the gratification of individuals who by conventional fiction are regarded as ill. They are paid for, and they are very expensive luxuries, the gross bill of expenses sometimes amounting to the value of \$300. The patient or his friends select the particular dance to be performed. After the completion of the picture, the patient enters the lodge, and is seated upon the east figure, while a litany is chanted. Sand from one of the painted figures is then applied to his body, sand from the arm being applied to his arm, &c.

Mr. PAUL described a similar art of dry-painting, practiced by the Japanese, but for amusement only. Bold designs of great variety are executed skillfully and rapidly in public places, for which the artist receives compensation from the by-standers. Wealthy Japanese also employ persons to dance for them, and, for that matter, to fish for them; but the motive appears to be pleasure, and not religion, or health.

Other remarks were made by Mr. JENKINS.

Mr. W. C. WINLOCK made a communication on

COMETS II AND III, 1884,

illustrating his subject by models exhibiting each cometary orbit in its proper relation to the earth's orbit, and also by plane diagrams and sketches of the comets.

Mr. RAVENÉ spoke of the perturbations of Barnard's comet occasioned by the attraction of Jupiter, and thought it might have been brought into the solar system by that attraction.

Other remarks were made by Mr. PAUL.

Mr. H. M. PAUL commenced a communication on

PROBLEMS CONNECTED WITH THE PHYSICS OF THE EARTH'S CRUST.

Its completion and discussion were deferred to a future meeting.

269TH MEETING.

APRIL 25, 1885.

The President in the Chair.

Fifty-three members and guests present.

Announcement was made of the election to membership of Mr. CHARLES FREDERIC ADAMS.

Mr. FRANK BAKER made a communication on

MODERN IDEAS OF BRAIN MECHANISM.

Remarks were made by Messrs. E. FARQUHAR, H. FARQUHAR, M. BAKER, and DOOLITTLE.

Mr. L. F. WARD began a communication on

THE FLORA OF THE LARAMIE GROUP,

the completion of which was deferred for lack of time.

270TH MEETING.

MAY 9, 1885.

The President in the Chair.

Forty-four members and guests present.

Announcement was made of the election to membership of Mr. WALTER HARVEY WEED.

Mr. LESTER F. WARD completed the reading of his communication on

THE FLORA OF THE LARAMIE GROUP.

[It will appear in the Sixth Annual Report of the U. S. Geological

Survey, as a portion of the author's "Synopsis of the Flora of the Laramie Group."]

Remarks followed by Messrs. GILBERT, ELLIOTT, and WHITE.
Mr. T. C. MENDENHALL made a communication on

THE MEASUREMENT OF TEMPERATURE AT DISTANT POINTS.

Remarks were made by Mr. ELLIOTT.

Mr. GUSTAVE RAVENÉ gave an abstract of a communication prepared on

THE ASTEROIDS.

Remarks were made by Messrs. TAYLOR, H. FARQUHAR, and ELLIOTT.

271ST MEETING.

MAY 23, 1885

The President in the Chair.

Forty-one members and guests present.

The Chair announced that only one more meeting would be held before the summer vacation.

Mr. A. GRAHAM BELL made a communication on

THE MECHANISM OF "CLICKS" AND "CLUCKS."

Remarks were made by Messrs. M. BAKER, GILBERT, and ROBINSON.

Mr. H. M. PAUL completed his communication on

THE CONDITION OF THE EARTH'S INTERIOR.

Mr. W. B. TAYLOR made a communication on

THE CRUMPLING OF THE EARTH'S CRUST,

in which, referring to the plausible hypothesis of contraction by cooling—which had been so largely accepted, he contended that the amount of cooling and contraction since the formation of a consistent crust had been much less than even the opponents of that hypothesis had conceded; while the maximum amounts estimated by its adherents would still be wholly inadequate to represent the

actual measure of compression indicated by the average degrees of plication of the stratified rocks. Supposing these to represent a reduction from the original circumference of the crust of one-eleventh, this would involve a former excess of volume of about one-third.

The speaker then gave an historical sketch of the growing conviction among physicists that from the tidal retardation of the earth's rotation, the length of the day must have been much shorter in remote geological eras than at present—and consequently the oblateness of the terrestrial ellipsoid considerably greater. Estimating that a day of six hours would give an equatorial enlargement of about one-tenth (without taking any account of *volumetric* change by reduction of temperature), he thought this *morphologic* change an adequate explanation of the observed crumpling of the earth's crust; and claimed that the cause assigned is both a true and a sufficient one. This larger oblateness would imply an equatorial bulge 396 miles greater in radius than the present; and a corresponding depression of the poles 658 miles below their present levels. As in a general way confirmatory of this hypothesis, Guyot's statement was quoted that "On the whole, the reliefs begin with the vast, low plains around the polar circle, and go on increasing from the shores of the Arctic ocean toward the tropical regions;" and that "the ocean basins become less deep toward the North pole—just as the lands become lower toward the same region."

[This paper is printed in full in the American Journal of Science, 3d Series, Vol. XXX, pp. 249-266.]

272ND MEETING.

JUNE 6, 1885.

The President in the Chair.

Twenty-eight members present.

Mr. J. P. IDDINGS made a communication on

THE COLUMNAR STRUCTURE IN THE DIABASE OF ORANGE
MOUNTAIN, N. J.

[Abstract.]

The paper describes the occurrence and structure of the "trap" rock in the neighborhood of Orange, with special reference to the arrangement of the columns in John O'Rourke's quarry and in the

Undercliff quarry in Llewellyn Park. The chief interest centers in the groups of radiating columns which form the upper portion of the exposures, the lower portion being divided into vertical columns or blocks of larger size. That these two portions of the lava sheet belong to one and the same mass is shown, not only by the continuity of the rock of the upper and lower parts, but also by the mutual accommodation of the different sets of columns, which taper off and curve in one direction along lines of oblique junction; and by the fact that the positions of the columns are not what they should be along the supposed lines of contact.

The columnar structure in volcanic lavas is unquestionably a cracking produced by shrinkage upon further cooling, after the mass has consolidated into rock.

Considering the origin and progress of a crack produced by the shrinkage of a homogeneous mass, we see that, starting with a plane surface over which forces producing contraction are acting uniformly, the contraction produced on the surface of the mass in a given time will be greater than that produced at some depth within the mass, and that it will decrease gradually from the surface inward. As the contraction progresses, the limit of tension in the direction of the surface will be reached before that in the direction of depth, causing a rupture across the direction of the surface, and as the limit of tension for the layer next to the surface is reached it will rupture in the same direction as the surface layer did, and so on. The direction of the crack is at right angles to that of greatest contraction, or normal to the line of maximum strain. Moreover the condition of the mass at the moment the limit of tension along the surface is reached may be graphically represented as in figure 1, the contraction being a maximum in the

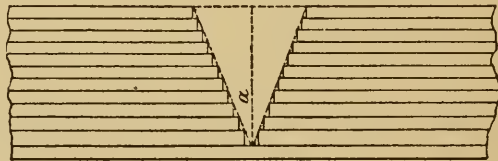


Fig. 1.

top layer and diminishing successively in each layer beneath to that with the initial expansion. The distance of this layer from the surface being taken as unity, the maximum contraction at the

moment of rupture will be equal to twice the tangent of α . In other words $2 \tan \alpha$ represents the limit of tension, and will be constant for any given substance.

As the conductivity of a cooling body is not directly proportional to the degree of radiation from its surface, the difference between the contraction of successive layers of a rapidly cooling mass will be greater than between those of one cooling less rapidly, and what may be styled the angle of contraction will be greater in the former case than in the latter. And if we assume a certain rate of cooling to have caused a single rupture in a given extent of mass (represented in fig. 1), then a greater rate of cooling, which would produce in the same extent of mass a contraction represented by a greater angle, β , will cause as many ruptures as the ratio, $\frac{\tan \beta}{\tan \alpha}$.

If the forces producing contraction are unequally distributed over the surface ab , figure 2, being a maximum at e , the maximum

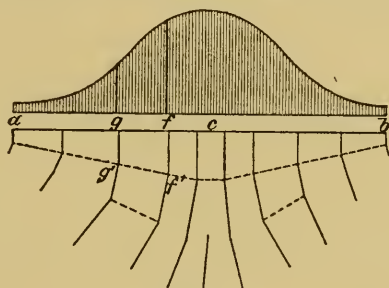


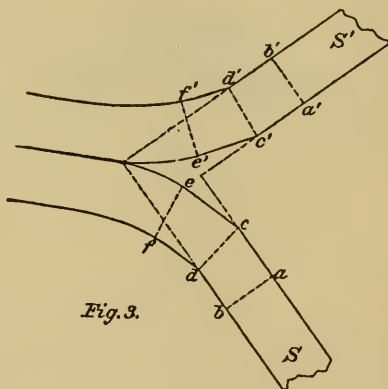
Fig. 2.

strain at the beginning will be in the direction of the surface, and the cracks will start normal to it; but their progress inward will no longer be uniform. At the end of a given time the limit of tension reached by a greater force, at f , will be farther from the surface than that reached by a less force, at g , and the line of maximum strain in this portion of the mass will be $g'f'$, to which the crack of parting will be normal. At the end of another given time the direction of the crack will be again changed, and the same action taking place in the other parts of the mass will result in a system of diverging cracks.

So far we have considered the shrinkage in one direction in one plane only, that is, parallel to the cooling surface in a plane at right angles to it. But a homogeneous mass contracts equally in all

directions, and the contractile force which produces cracks at certain distances in a given mass will exert itself equally in all directions over a surface uniformly subjected to the cooling forces, and will, at the instant of fracture, act towards centres, whose distance apart is dependent on the rate of cooling. If the mass is perfectly homogeneous the centres of contraction will be disposed over the surface with the greatest uniformity possible, that is, they will be equidistant throughout, and the resultant fractures will be in a system of hexagons. If from any irregularity in the composition or petrographic structure of the rock the contractile force acts unequally in different directions, the form of the polygons will be less regular.

The mutual influence of the forces producing different columns as they approach each other is readily understood from the foregoing. Take the case of two columns, S, S' , approaching one another (Fig. 3,) and suppose the progress of the maximum strain to have reached



a, b, a', b' , the forces producing contraction acting through a and a' will meet and react on each other before those acting through b and b' , so that the points of maximum strain at any given time will have advanced farther along the lines through a and a' than through b and b' . The lines of greatest strain will then be cd and $c'd'$, and the cracks normal to them will take the directions ce and $c'e'$. This will continue till they become parallel.

If there were but two columns forming at equal rates they would curve symmetrically and continue in parallel directions and of constant width, but if one column progresses more rapidly than the

other they will no longer curve to the same extent, and the slower one will curve more than the faster one.

Now, instead of two single columns, there are always two groups approaching one another, and these prevent the continuation of the columns beyond the bend, pinching them out and causing them to taper off as already observed in the quarry described.

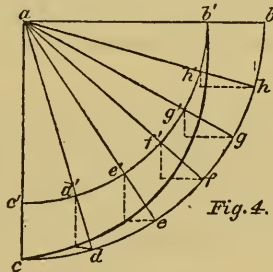
The difference in the systems of cracks of the lower and upper portion of this lava sheet may then be accounted for by a difference in the rate of cooling from the lower and upper surfaces, the more frequent fractures arising from the more rapid cooling, and the two systems proceeding from their initial planes until they blend in one another within the mass.

If for any reason the cooling from one surface should take place irregularly and from any point proceed more rapidly than from others, it is evident that there would result a set of columns diverging from this point as a focus.

Besides the columnar fracturing, a division of the mass by transverse cracks, especially near the top of the lava sheet, is more or less noticeable.

There remains to be considered the contraction exerted in all other directions through the mass. Since the uniform contraction of a homogeneous body acts equally in every direction through it, its effect corresponds to the equal shortening of the radii of a sphere of such a body. If through any resistance cracking or parting occurs it will take the form of concentric spherical shells.

If for any reason the resistance to the contracting force in a particular direction be counteracted by some other force acting in the same direction the parting will no longer be spherical, but ellipsoidal, as will be seen from Figure 4, where $a b c$ represents a section



through the sphere along the radii of which contraction takes place. A uniform resistance in the direction of the radii represented by

$c c'$, $d d'$, etc., will produce a parting parallel to the arc of the circle $c' d' e'$, etc. If, however, the resistance in a direction parallel to $a c$ be neutralized by some force, the resistance along the different radii will be diminished by the amount of the vertical component in each case, and the resulting fracture will be parallel to the ellipse $c b'$. The relative tendency to fracture also is represented by the area $b c b'$.

Such a parting is actually present in the large columns in John O'Rourke's quarry, the major axis of the ellipsoid being vertical, as it should be if the weight of the superincumbent mass counteracted any resistance to contraction in a vertical direction.

The wavy form of the columns, large and small, suggests irregularities in the mass which disturbed the uniform advance of the lines of maximum strain and caused them to deviate from parallelism.

The superficial banding of the large vertical columns by nearly horizontal notches or grooves, resembling layers of bricks or rude chiseling, appears to be simply a modification of the plane of the crack.

The paper closes with a description of the microscopical character of the Orange rock, which from its identity with many recent basalt flows leads the writer to the conclusion that it should be classed as a coarse-grained basalt or dolerite, as Prof. E. S. Dana has called the similar rocks in the Connecticut valley.

The occurrence of the rock in question as a surface flow is rendered highly probable by its glassy nature, and the disposition of the columns, which resembles that of many lava sheets in western America, as well as of those in central France. G. Poulett Scrope, in his work on "Volcanos" (2d edition, London, 1872), discusses the question of the origin and nature of columnar structure in lavas and other substances, and by a somewhat different course of reasoning arrives at essentially the same conclusions as those reached in the present paper.

Mr. W. J. MCGEE then made a communication on

THE TERRACES OF THE POTOMAC VALLEY.

Remarks were made by Messrs. WARD, TONER, ROBINSON and BATES.

273D MEETING

OCTOBER 10, 1885.

The President in the Chair.

Thirty-nine members and guests present.

Announcement was made of the death since the last meeting of two members of the Society, FRANKLIN BENJAMIN HOUGH and WASHINGTON CARUTHERS KERR.

Messrs. J. S. BILLINGS and WASHINGTON MATTHEWS made a joint communication on

ANTHROPOMETRIC AND REACTION-TIME APPARATUS.

They exhibited a set of the anthropometric apparatus, devised chiefly by Mr. Francis Galton, and recently employed in the anthropometric laboratory of the London Health Exhibition. The apparatus test acuteness of hearing, strength of vision, color discrimination, the estimation of the aliquot parts of a line, the estimation of a right angle, the rapidity of arm movement in striking a blow, the strength of certain muscles, the weight, the height (sitting and standing), span of arms, and chest capacity. Their peculiar characteristic is their simplicity, which permits of their use by the person measured, with a minimum of instruction and supervision. There was also exhibited a device by Mr. James McKeen Cattell, for the determination of the time occupied by various sensations, mental processes and muscular actions.

There followed an informal discussion by Messrs. H. A. HAZEN, E. FARQUHAR, HALL, H. FARQUHAR, HARKNESS, MUSSEY, WOODWARD and MASON.

274TH MEETING.

OCTOBER 24, 1885.

The President in the Chair.

Fifty-three members and guests present.

Mr. H. ALLEN HAZEN made a communication on

THE CONDENSING HYGROMETER AND SLING PSYCHROMETER.

[Abstract.]

By way of introduction the results of a few experiments were given, tending to show the best interval that can be obtained in the

graduation of degrees upon a thermometer scale. These were made with a common vernier of a mercurial barometer. A mark on the vernier was placed at each tenth (by estimation) of intervals of .05", .10", .15", .20", .30", and .40", marked on the limb, and the vernier read for each estimation. Over 1300 readings were made, and these showed little difference in the splitting to tenths for the last 5 intervals above, but .05" seemed too small for accurate work.

Results and methods of observing the Alluard form of Regnault's condensing hygrometer were given. It was shown that if the thermometer immersed in the liquid is placed quite near the plate where dew is to appear, there is little or no danger of the air as it passes into the liquid harmfully affecting the thermometer. The complaint of some that the dew is deposited in the air, having a temperature frequently 40 or 50 degrees above the liquid, and hence that the thermometer can hardly give a correct dew-point temperature was shown to have little weight, since the results, with a slight difference between the air and dew-point, at which time the effect would be small, are nearly identical with those where the difference is large, and the effect would be large. It was shown that the great difficulty in nearly all psychrometric work up to the present time has been the disregard of a sufficient ventilation of the wet-bulb thermometer. The sling psychrometer, with a few precautions in its use, furnishes results entirely satisfactory.

The comparisons so far made between the two instruments have shown a remarkable uniformity under all conditions of moisture and temperature, and have left little to be determined in order to make either apparatus one of precision. A probable effect of compression of ice on the wet bulb at temperatures of 0° F., and below, was shown to exist, though this may be due to the lack of conduction on the part of the ice for the residuum of heat in the bulb. The question of the effect of height above sea on the indications of the above instruments was touched upon, and it was shown that the effect was small and only to be detected by the most refined observations. Also, that until we have some law for reducing humidity results to sea level, the propriety of introducing such effect into tables is questionable.

Mr. T. C. MENDENHALL exhibited a new volt-meter devised by Sir William Thompson. The principal difficulty encountered by earlier instruments of this class has arisen from the inconstancy of the magnetic force of the terrestrial field. By this instrument ter-

restrial magnetism is eliminated. The force produced by the current is opposed by a weight and is thus measured in terms of gravity.

Mr. MENDENHALL also renewed the discussion of the preceding evening on reaction time, reciting the methods and results of his own experiments in 1871.

Remarks on the volt-meter were made by Mr. ELLIOTT, on reaction time by Messrs. PAUL, MASON, and MATHEWS.

Mr. WILLIAM HARKNESS made a communication on

FLEXURES OF TRANSIT INSTRUMENTS,

pointing out that the flexures induced by the weight of a transit, in positions other than vertical, are not eliminated by reversing the instrument, and developing equations for the discussion of the errors so far as they can be determined by the aid of collimators.

275TH MEETING.

NOVEMBER 7, 1885.

The President in the Chair.

Sixty-nine members present.

Mr. F. W. CLARKE made a communication on

AN ATTEMPT AT A THEORY OF ODOR,

in which he accounted for the lack of knowledge as to the conditions of action of this sense by the difficulty of dissociating it from taste; and, while disclaiming any thought of attempting a physiological explanation of the sense, proposed the following as the essential objective conditions:

1. To be odorous, a substance must be volatile, so that it may come into contact with the mucous tissue of the nose, and
2. It must be chemically unstable, so that it may undergo chemical changes in contact with that tissue.

Mr. Clarke gave some confirmatory instances, from the compounds of hydrogen with sulphur, selenium, and tellurium, and from the $C_n H_{2n} O_2$ group of acids (formic, acetic, etc.)

Mr. ANTISELL called attention to the connection between a low boiling-point and simplicity of chemical constitution, and to the associated fact that organic substances containing a large number

of equivalents of carbon are inodorous. He ascribed the smell of prussic acid to *arrière-gout* rather than true odor.

Mr. BILLINGS showed that from the peculiarly exposed condition of the olfactory nerve-terminal, it was subject to irritations that must be distinguished from odors properly speaking.

Mr. CLARKE then made a communication on

THE FLOOD ROCK EXPLOSION,

in which he described the arrangements for observing earth tremor at stations near New York city, and particularly that at Ward's Island, occupied by Mr. Mendenhall and himself. The tremor was felt at that station a full second before any disturbance was seen in the surface of the water above Flood Rock.

Mr. C. F. MARVIN, in a communication on the same subject, described the form of seismoscope used, in which a small agitation closed an electric circuit, and sounded an alarm.

Mr. PAUL followed with a communication on the same subject.

Mr. CLARKE quoted some results of observations made at Gen. Abbot's stations, giving a mean velocity for the tremor from Flood Rock to Pearsall's of 2.6, and to Patchogue of $2\frac{1}{4}$ miles per second, and thus indicating a retarded rate of transmission.

Mr. ROBINSON suggested that the blasts at the new water-works reservoir would afford a good opportunity for measuring the velocity of earth tremors.

Mr. H. FARQUHAR spoke of the sounds coincident with the flight of meteors reported by some observers, as indicating the need of caution in accepting observations of sound in this connection.

Mr. ROBINSON had distinctly heard two sounds after blasts at the water-works; one immediately following the tremor, through the earth, and a later one through the air.

Mr. CHATARD had made a similar observation in connection with mining blasts.

Mr. DUTTON said that his impression, from eruptions of Hawaiian volcanoes, had been otherwise, and that the general testimony with regard to earthquakes is that the sound precedes the shock.

276TH MEETING.

NOVEMBER 21, 1885.

The President in the Chair.

Fifty-seven members present.

Announcement was made of the election to membership of Mr. THOMAS HAMPSÓN.

The Chair communicated to the members an invitation from the Chemical Society to attend its meeting on December 10th and listen to the address of its retiring president, Prof. F. W. CLARKE.

Mr. G. BROWN GOODE and Mr. C. V. RILEY made communications on

THE SYSTEMATIC CARE OF PAMPHLETS,

exhibiting the appliances employed by them and illustrating their methods.

Mr. GOODE furnishes each pamphlet with a firm, durable cover, by which it is protected from injury, and at the same time kept separate for convenient use and classification. Photographs, drawings, newspaper clippings, etc., are preserved in the same manner. [A full description of his appliances may be found in Science, vol. VI, p. 337.]

Mr. RILEY employs inexpensive, flexible covers, occupying less space, and stores them in the "institute pamphlet case."

Mr. B. PICKMANN MANN, being invited to participate in the discussion, exhibited his method of binding pamphlets together, a method in which four holes are punched at standard intervals in each pamphlet and corresponding holes in flexible hinges to stiff covers, so that a convenient volume can be made up by merely inserting and tying two cords, and any desired rearrangement or insertions can be made, the holes for binding always corresponding. [See Science, vol. VI, p. 407, and Library Journal, vol. VIII, p. 6.]

Mr. BILLINGS described the tin boxes used in the storage of the immense file of pamphlets in the library of the Army Medical Museum. Mr. WARD and Mr. TONER spoke in approval of the substantial covers adopted by Mr. Goode. Messrs. GILBERT, TONER and HARKNESS opposed the binding of several pamphlets together, believing that such combination interferes with their use and ready classification and reclassification.

Other remarks were made by Messrs. DALL, MUSSEY, and DOOLITTLE.

Mr. J. S. BILLINGS made a communication on

GERM CULTURES,

exhibiting specimens of cultures of chromogenetic and pathogenetic micro-organisms, to illustrate the improvements in methods of investigating these organisms which have been made of late years.

Attention was called to the value of culture upon semi-solid media such as peptonized gelatin, agar agar, coagulated blood serum, etc., as a means of differentiating micro-organisms, and of obtaining pure cultures to be used for experimental purposes; and the applications of the method to testing the efficacy of disinfectants, to water examinations, &c., were pointed out.

277TH MEETING.

DECEMBER 5, 1885.

By courtesy of the officers of the Columbian University, the meeting was held in the law lecture room of the University building. Members of the Anthropological, Biological, and Chemical Societies and their friends were present by invitation.

Vice-President BILLINGS occupied the Chair.

Present, one hundred and sixty members and guests.

The President, Mr. ASAPH HALL, read his annual address, taking for his subject :

AMERICAN SCIENTIFIC SOCIETIES.

[Printed in full on pp. XXXIII-XLVII.]

A resolution of thanks was moved and unanimously passed.

278TH MEETING.

DECEMBER 19, 1885.

THE FIFTEENTH ANNUAL MEETING.

The President in the chair.

Thirty-eight members present.

The minutes of the 260th, 276th, and 277th meetings were read and approved.

The Chair announced the election to membership of Mr. JACOB LAWSON WORTMAN.

The report of the Secretaries was read and accepted.

The report of the Treasurer was read, received, and referred to an auditing committee, consisting of Messrs. J. M. Toner, O. T. Mason, and T. C. Mendenhall.

On motion of Mr. HARKNESS, the thanks of the Society were tendered to the Treasurer and Secretaries for the efficient performance of the duties of their offices.

Officers were then elected for the year 1886. (The list is printed on page xv.)

The rough minutes of the meeting were read, and the Society adjourned.

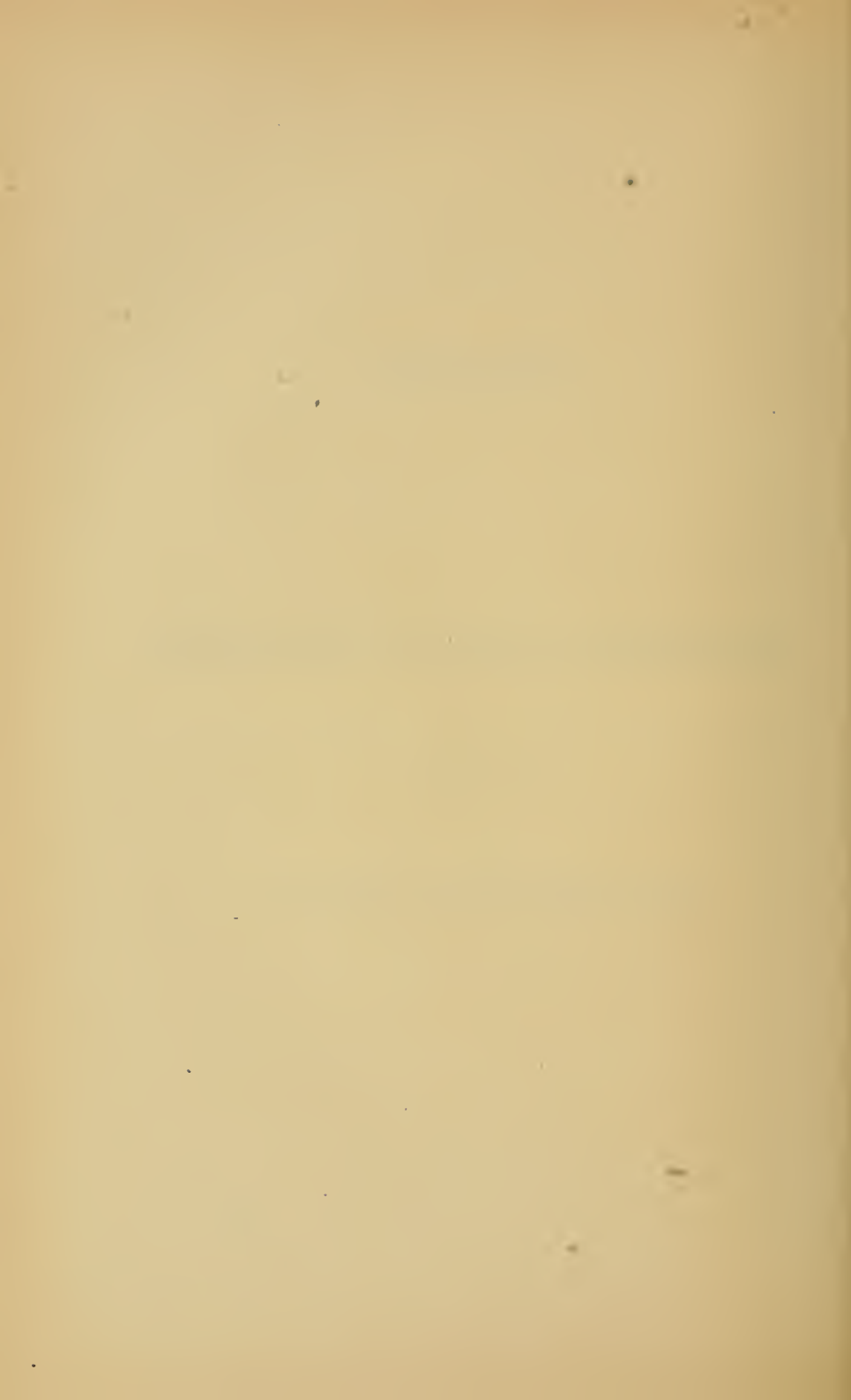


BULLETIN

OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON.

MATHEMATICAL SECTION.



STANDING RULES

OF THE

MATHEMATICAL SECTION.

1. The object of this Section is the consideration and discussion of papers relating to pure or applied mathematics.

2. The special officers of the section shall be a Chairman and a Secretary, who shall be elected at the first meeting of the Section in each year, and discharge the duties usually attaching to those offices.

3. To bring a paper regularly before the Section it must be submitted to the Standing Committee on Communications for the stated meetings of the Society, with the statement that it is for the Mathematical Section.

4. Meetings shall be called by the Standing Committee on Communications whenever the extent or importance of the papers submitted and approved appear to justify it.

5. All members of the Philosophical Society who wish to do so may take part in the meetings of this Section.

6. To every member who shall have notified the Secretary of the General Committee of his desire to receive them announcements of the meetings of the Section shall be sent by mail.

7. The Section shall have power to adopt such rules of procedure as it may find expedient.

OFFICERS

OF THE

MATHEMATICAL SECTION FOR 1885.

Chairman, G. W. HILL. *Secretary*, MARCUS BAKER.

LIST OF MEMBERS WHO RECEIVE ANNOUNCEMENT OF THE
MEETINGS.

ABBE, C.	HALL, A. JR.
AVERY, R. S.	HARKNESS, W.
BAKER, M.	HAZEN, H. A.
BATES, H. H.	HILGARD, J. E.
BILLINGS, J. S.	HILL, G. W.
BURGESS, E. S.	HODGKINS, H. L.
CHRISTIE, A. S.	KING, A. F. A.
COFFIN, J. H. C.	KUMMELL, C. H.
CURTIS, G. E.	LEFAVOUR, E. B.
DELAND, T. L.	McGEE, W. J.
DOOLITTLE, M. H.	NEWCOMB, S.
EASTMAN, J. R.	PAUL, H. M.
EIMBECK, W.	RAVENÉ, G. L.
ELLIOTT, E. B.	ITTER, W. F. M'K.
FARQUHAR, H.	ROBINSON, T.
FLINT, A. S.	SMILEY, C. W.
GILBERT, G. K.	STONE, O.
GORE, J. H.	TAYLOR, W. B.
GREEN, B. R.	UPTON, W. W.
HALL, A.	WINLOCK, W. C.

WOODWARD, R. S.

BULLETIN
OF THE
MATHEMATICAL SECTION.

16TH MEETING.

JANUARY 7, 1885.

The Chairman, Prof. ASAPH HALL, presided.

Nineteen members and guests present.

Election of officers of the Section for the year 1885 was then held and resulted in the selection of Mr. G. W. HILL as Chairman and Mr. MARCUS BAKER as Secretary.

Mr. E. B. ELLIOTT then presented a communication entitled

EXAMPLE ILLUSTRATING THE USE OF A CERTAIN SYMBOL IN THE
CALCULUS OF AFFECTED QUANTITY.

The example selected was a demonstration of the Pythagorean Theorem by the aid of a new symbol.

Mr. MARCUS BAKER presented a communication entitled

A COLLECTION OF FORMULÆ FOR THE AREA OF A PLANE
TRIANGLE,

which elicited some criticism of details and of notation.

[This paper is published in full in the *Annals of Mathematics*, vol. 1, No. 6, and vol. 2, No. 1.]

Mr. W. C. WINLOCK (by permission of Rear Admiral S. R. Franklin, Superintendent U. S. Naval Observatory) presented a communication on

PHYSICAL OBSERVATIONS OF WOLF'S COMET (1884 III).

[Abstract.]

The first observation of Wolf's comet that I obtained was with the transit circle of the U. S. Naval Observatory on September 24,

1884. The aperture of the instrument is 8 inches and the magnifying power employed 186.

On October 13, using the 9-inch equatorial and a power of 132, "the comet seemed to be a circular nebulous mass with quite a well marked central condensation. The nucleus was not sharply defined, but blended gradually into the fainter light surrounding it."

Nov. 8. Transit circle. Nucleus quite well defined. Faint but not difficult to observe.

Nov. 12. Transit circle. Nucleus elongated in the *preceding following* direction and apparently composed of a number of bright points. Faint and difficult to observe. The nebulous envelope seems to extend farther on the upper or south side than on the lower side. Seeing, very poor.

Nov. 13 with the 9-inch equatorial and the same power as before a sketch (omitted here) was made. The remarks I give substantially as in my note-book: Watched the comet carefully for about an hour (seeing not very good,—a little fog hanging over the river). It is a very slightly oval nebulous object. The central part is a little condensed; the nucleus proper more so. Filar micrometer measures give for the extent of the outer nebula, measured in the direction of a circle of declination, $1' 52''$, and for the inner disc $18''$. The nucleus is perhaps extended a little in the *preceding following* direction, but I looked in vain for any indication of the beaded appearance which I thought I saw last night with the transit circle. I might add that using the distance of the comet given in Krüger's ephemeris these measures would represent distances of 47,000 and 7,500 miles, respectively. No tail.

Nov. 20. Transit circle. Nucleus stellar, 10th magnitude.

On November 22 another observation was obtained with the 9-inch equatorial, magnifying power 132 as before. Micrometer measures of the outer nebula and the inner disc gave $1' 30''$ and $16''$, respectively, differing but little from the measures of the 13th. Seeing, fair. The following note was made: I divide the comet into three parts, the outer nebula, the inner envelope (or coma I presume it might be called), and the nucleus proper. It is almost impossible to assign a definite limit to this outer envelope, wavering and flickering like a mass of smoke, but the micrometer measures will fix it roughly. The inner envelope blends into the outer without any sharp division, though there is sufficient difference in brightness to attempt a measurement. The inner envelope condenses in turn into the brighter nucleus.

Nov. 24. Transit circle. Nucleus sharp and stellar and about 10th magnitude.

Dec. 2. Transit circle. Seeing poor. Extremely faint. Like a 12.5 magnitude star, surrounded by a large but faint nebula.

Dec. 8. 9-inch equatorial and power 132. The diameter (in declination) of the outer envelope, from a micrometer measurement, was $2' 21''$, the seeing being noted a little better than on Nov. 22. Occasionally I think I see the inner condensed disc, but am not sure of it; also think that at times there is an indication of a more or less rounded outline to the head on the *south preceding* side, but it is unstable. Cannot be sure of anything like a tail, and indeed any definite form other than an irregular circle is, after all, largely a matter of imagination.

The communication gave rise to some comment and discussion on the difficulties encountered in making satisfactory observations of faint comets and also on the resisting medium in space.

Mr. TAYLOR called the attention of the Section to

A SLIGHT MODIFICATION OF THE NEWTONIAN FORMULA OF GRAVITATION

with which he had been struck in reading Mr. Bates' paper on "The Physical Basis of Phenomena" recently read before the General Meeting. (*See* vol. vii, p. 51.)

[Abstract.]

There is a widespread fallacy—particularly displayed by those kinematists who fancy they have an exceptional insight into the "mechanism of gravitation," that this influence is simply a radiant emanation, necessarily observing the geometry of radial space relations, having as such emanation the same total energy on all concentric spheres whatever their radii, as in the case of luminous radiation for example. Of course every well instructed astronomer and physicist knows that this is not so. In truth "the inverse square" is not *geometrical*—not a square at all, having no relation whatever to surface,—but simply an *algebraical* second power, very much like the familiar "velocity squared" ($m v \times v$, or momentum multiplied by velocity), which forms the measure of all kinetic energy and which no one supposes to represent a square.

Our late colleague, General Alvord, in confutation of this not unusual misconception, made a communication to the Society some two or three years ago (as those present doubtless remember) in which he showed that as gravitation was known to act equally on every particle of matter (*i. e.* proportionally to the mass) and as solid homogeneous spheres subtending any given conical angle from a center of reference possess volumes (or masses,— d being constant) directly proportional to the cubes of the conical altitudes or radii of distance, it follows—if gravity were a radial emanation—its effect must obey the law of inverse *cubes* of distance, contrary to the facts of observation.

The fallacy here criticised springs evidently from the too common tendency to regard gravitation simply as a central force or as a single influence radial in direction, whereas it is always a duplex and reciprocal action; and however insignificant one of the terminal elements its presence and measure of distance cannot be neglected without completely nullifying all action. Thus m and m' being two masses at any given distance apart, the action in the direction and through the distance $m' m$, is as real and positive as that in the direction and through the distance $m m'$. In other words, it would seem that the *mutuality* of the re-action necessarily involved with it the idea of *reciprocity* of the distance relation. Thus, adopting the suggestion of Mr. Bates, if we write the formula of the effect as $(m \div d) \times (m' \div d)$, we have this reciprocity distinctly brought out, and obtain at once the Newtonian formula. The speaker wished to learn from those more conversant than himself with mathematical literature whether the suggested modification is new, and also whether any mathematical objection appears to its form.

Mr. HILL remarked that one fault of the notation proposed appeared to be its want of *generality*, as it is evidently inapplicable to any other force having a higher or different exponent of the space function.

Mr. DOOLITTLE observed that, admitting the "reciprocity of the distance relation," he yet failed to perceive how this function could appear in the formula as a *product*. Why should we write the distance twice taken—as d multiplied by d rather than as d plus d ?

Further remarks were made by Messrs. ELLIOTT, BATES, and ROBINSON.

17TH MEETING.

FEBRUARY 10, 1885.

The Chairman, Mr. G. W. HILL, presided.

Present, eleven members and one guest.

In the absence of the Secretary the reading of the minutes of the last meeting was deferred, and Mr. R. S. WOODWARD designated as Secretary *pro tem*.

Mr. KUMMELL made a communication on

AN ARTIFICE SOMETIMES USEFUL FOR THE ADJUSTMENT OF
CONDITIONED OBSERVATIONS.

[Abstract.]

The general process consists in multiplying equations of condition by such factors as will extinguish side-coefficients in the normal equations for correlates. This was shown to be possible in an infinite number of ways. One such way leading to linear equations for the multipliers was shown to require for the extinguishment of *all* the side-coefficients the solution of the normals, *i. e.*, the very work which was to be evaded. The method would, however, be advantageous for the partial extinguishment of large side-coefficients, and the normal equations could thus be solved with advantage by Gauss' indirect method. A useful symmetrical rule was given for extinguishing the side-coefficients for a *pair* of conditions. Illustrations of this rule in the adjustment of simple geometrical figures were given, beginning with a simple figure of two triangles and extending to a complete pentagon.

Mr. HILL remarked that Jacobi had proposed a similar method for removing side-coefficients. Further remarks were made by Mr. WOODWARD.

The next communication was by Mr. GUSTAVE L. RAVENÉ on

THE THEORY OF MERCURY.

[Abstract.]

The method here used of computing the secular variation of the elements of an orbit is due to Gauss.

The notation employed for the *disturbed* body is

π = longitude of perihelion ;

θ = longitude of the ascending node ;

i = inclination to the ecliptic ;

a = mean distance from the sun ;

n = mean annual motion ;

e = eccentricity ;

φ = eccentric angle = arc sin e ;

r = radius vector ;

f = true anomaly ;

ε = eccentric anomaly ;

m = mass ; and the same symbols with accents, π' , θ' , i' , etc, represent corresponding quantities for the *disturbing* body.

From the definition of the secular perturbations, according to Gauss, the perturbing function may be expressed by

$$V = \frac{m'}{4\pi^2} \int_0^{2\pi} \int_0^{2\pi} \frac{1 - e \cos \varepsilon}{\rho} d\varepsilon d\varepsilon'$$

in which ρ is expressed by

$$\rho^2 = a'^2 + r^2 - 2a' r \cos(a', r).$$

We also have

$$r^2 = a^2 (1 - e \cos \varepsilon)^2$$

$$a' r \cos(a', r) = a' \cos \varepsilon' \{ \cos \pi (a \cos \varepsilon - ae) - a \cos \varphi \sin \varepsilon \sin \pi \} \\ + a' \sin \varepsilon' \{ a \cos \varphi \sin \varepsilon \cos \pi + \sin \pi (a \cos \varepsilon - ae) \}.$$

Putting for brevity

$$a^2 (1 - e \cos \varepsilon)^2 = p_\varepsilon$$

$$2 \{ \cos \pi (a \cos \varepsilon - ae) - a \cos \varphi \sin \varepsilon \sin \pi \} = q_\varepsilon$$

$$2 \{ \sin \pi (a \cos \varepsilon - ae) + a \cos \varphi \sin \varepsilon \cos \pi \} = s_\varepsilon$$

we get

$$\rho^2 = (a'^2 + p_\varepsilon) - a' (q_\varepsilon \cos \varepsilon' + s_\varepsilon \sin \varepsilon').$$

The differential equation for the secular variation of the perihelion is

$$d\pi = \frac{an \sqrt{1 - e^2}}{(1 + m)e} \cdot \frac{dV}{de} dt$$

and also

$$\frac{dV}{de} = -\frac{m'}{4\pi^2} \int d\varepsilon \int \left\{ \frac{\cos \varepsilon}{\rho} + \frac{1 - e \cos \varepsilon}{2\rho^3} \cdot \frac{d(\rho^2)}{de} \right\} d\varepsilon'.$$

If we now put

$$A_\varepsilon = -a \cos \pi - ae \cos \varepsilon \cos \pi + \frac{ae}{\cos \varphi} \sin \pi \sin \varepsilon \\ - \frac{a(2 - e^2)}{\cos \varphi} \sin \pi \sin \varepsilon \cos \varepsilon + 2a \cos \pi \cos^2 \varepsilon;$$

$$B_\varepsilon = -a \sin \pi - ae \cos \varepsilon \sin \pi - \frac{ae}{\cos \varphi} \cos \pi \sin \varepsilon \\ + \frac{a(2 - e^2)}{\cos \varphi} \cos \pi \sin \varepsilon \cos \varepsilon + 2a \sin \pi \cos^2 \varepsilon;$$

we obtain

$$\frac{dV}{de} = \frac{m' a'}{4\pi^2} \int d\varepsilon \left\{ A_\varepsilon \int \frac{\cos \varepsilon'}{\rho^3} d\varepsilon' + B_\varepsilon \int \frac{\sin \varepsilon'}{\rho^3} d\varepsilon' \right\} \\ - \frac{m' a'^2}{4\pi^2} \int d\varepsilon \cos \varepsilon \int \frac{d\varepsilon'}{\rho^3}.$$

This expression contains the following integrals:

$$R = \int_0^{2\pi} \frac{d\varepsilon'}{\{(a'^2 + p_\varepsilon) - a' q_\varepsilon \cos \varepsilon' - a' s_\varepsilon \sin \varepsilon'\}^{\frac{3}{2}}},$$

$$S = \int_0^{2\pi} \frac{\sin \varepsilon' d\varepsilon'}{\{(a'^2 + p_\varepsilon) - a' q_\varepsilon \cos \varepsilon' - a' s_\varepsilon \sin \varepsilon'\}^{\frac{3}{2}}},$$

$$T = \int_0^{2\pi} \frac{\cos \varepsilon' d\varepsilon'}{\{(a'^2 + p_\varepsilon) - a' q_\varepsilon \cos \varepsilon' - a' s_\varepsilon \sin \varepsilon'\}^{\frac{3}{2}}}.$$

which must be computed for every value of ε obtained by dividing the circumference into j parts.

If we put

$$a'^2 + p_\varepsilon = \lambda; \quad a' q_\varepsilon = q \cos Q; \quad a' s_\varepsilon = q \sin Q,$$

we get

$$\{(a'^2 + p_\varepsilon) - a' q_\varepsilon \cos \varepsilon' - a' s_\varepsilon \sin \varepsilon'\}^{-\frac{3}{2}} \\ = \{\lambda - q \cos(\varepsilon' - Q)\}^{-\frac{3}{2}} \\ = a_0^{(3)} + 2a_1^{(3)} \cos(\varepsilon' - Q) + 2a_2^{(3)} \cos 2(\varepsilon' - Q) + \dots$$

The quantities a_0, a_1, a_2 , etc., may be computed by Hansen's formulæ given in his work, *Auseinandersetzung*, etc., 1 Abth., § 61, and when found R, S , and T are found from the formulæ

$$R = 2a_0\pi; S = 2a_1 \sin Q; T = 2a_2 \cos Q.$$

It would be interesting to know what influence the supposed intra-Mercurial planet would have on the other bodies of the system, especially on Venus.

The differential equation of the motion of the ascending node is

$$\frac{d\theta}{dt} = \frac{365.25 k}{\sqrt{a(1+m)} \sin i} \frac{dV}{di}.$$

The quantity k is the well known Gaussian constant, expressed in seconds of arc, and its logarithm is $\log k = 3.5500065746$.

The value of ρ^2 is expressed by

$$\rho^2 = a^2 + a'^2 - 2aa' \cos(a, a')$$

from which we have

$$\frac{d(\rho^2)}{di} = -2aa' \frac{d[\cos(a, a')]}{di}.$$

But $\cos(a, a') = \cos \epsilon \cos \epsilon' + \sin \epsilon \sin \epsilon' \cos I$,
 $\cos I = \cos i \cos i' + \sin i \sin i' \cos(\theta - \theta')$,
 $\cot \Phi \sin(\theta - \theta') - \cot i' \sin i = -\cos(\theta - \theta') \cos i$.

Differentiating we get

$$\frac{d\Phi}{di} = \frac{\sin^2 \Phi}{\sin(\theta - \theta')} (\cot i' \cos i + \cos(\theta - \theta') \sin i) = t_1.$$

We also have

$$\frac{d(\cos I)}{di} = -\cos i' \sin i + \cos i \sin i' \cos(\theta - \theta') = t_2.$$

From these expressions we obtain

$$\frac{d(\cos a, a')}{di} = (-\cos \epsilon' \sin \epsilon + \sin \epsilon' \cos \epsilon \cos I)t_1 + \sin \epsilon' \sin \epsilon t_2,$$

and therefore $d(\rho^2)$ becomes

$$\frac{d(\rho^2)}{di} = p_c \cos \epsilon' + q_c \sin \epsilon'$$

in which

$$p_c = 2aa' \sin \epsilon t_1,$$

and

$$q_c = -2aa' (\cos \epsilon \cos I t_1 + \sin \epsilon t_2).$$

The expression $\frac{d\theta}{di}$ will in the actual computation be written in the form

$$\frac{d\theta}{di} = \frac{365.25 k}{\sqrt{a(1+m)} \sin i} \frac{m'}{2\pi} \cdot C,$$

in which

$$jC = Tp_{\epsilon} + Sq_{\epsilon}.$$

Using the values $\theta' = 14^{\circ} 36'$, $a' = 0.200$, $i' = 7^{\circ}$, and $m' = \frac{1}{2000000}$ derived by me some time since for the intra-Mercurial planet, the perturbation of the node of Venus' orbit is found to be

$$\delta\theta = -3.''92120$$

in a century.

Mr. HILL, commenting on this paper, discussed briefly the probable mass and density of Mercury on grounds of probability and analogy, pointing out that its density would on such grounds appear to be far less than the ordinarily accepted value.

18TH MEETING.

APRIL 15, 1885.

In the absence of the Chairman, Mr. DOOLITTLE was made Chairman *pro tem*.

Present, ten members and one guest.

Minutes of the sixteenth and seventeenth meetings were read and approved.

Mr. MARCUS BAKER then read the following paper on

A GROUP OF CIRCLES RELATED TO FEUERBACH'S CIRCLE.

In any plane triangle the middle points of the sides and the feet of the perpendiculars drawn from the vertices to the opposite sides are *six* points in the circumference of a circle. This circle also bisects the segments of the perpendiculars between orthocenter and vertices, thus making *nine* noteworthy points. These properties

were first published in January, 1821, in Gergonnes' *Annales*, vol. II, in a memoir by Brianchon and Poncelet on the determination of an equilateral hyperbola from four given conditions.

In 1822 Prof. K. W. Feuerbach, of Nuremburg, showed that this circle is tangent to the inscribed and three escribed circles. This property is known as Feuerbach's theorem, and the circle is known to the Germans as Feuerbach's circle. In 1828 Steiner showed that this circle passed through twelve noteworthy points and was tangent to the in and escribed circles. This was done without a knowledge of the earlier work by Feuerbach.

In 1842 Terquem, the editor of the *Nouvelles Annales de Mathématiques*, called it the *nine-points circle*. In some books it has been called the *six-points circle*. In an article, by myself, in the *Mathematical Magazine* for January, 1882, I have called it the *twelve-points circle*.

Of the twelve points considered noteworthy six are in the sides of the triangle and six are not. If all the noteworthy points now known are to determine its designation, then *twelve-points circle* appears to be a proper designation. If only those points in the *sides* of the triangle should determine the designation then *six-points circle* would appropriately name it. In either case *nine-points circle* would be an imperfect designation, and as the name Feuerbach's circle was the first name it received it seems on the whole best to adhere to it. A somewhat analogous case is the *seven-points circle* known as Brocard's circle, not named for the number of noteworthy points it contains but for its discoverer. The name *twelve-points circle* may therefore be rejected and the name Feuerbach's circle adopted.

The following proof of the fundamental properties of Feuerbach's circle is offered as being simpler than that usually given :

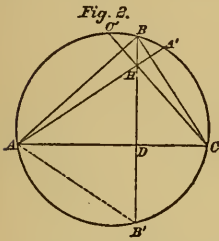
PRELIMINARY.

1. *Definition.* When we determine upon a right line AB a point C such that $AC = BC = \frac{1}{2} AB$ the line is said to be bisected. This restricts us to one point C .

Fig. 1. $C' \quad A \quad C \quad B \quad C''$

It will be found convenient in what follows to extend this definition so as to include the points C' and C'' , Fig. 1, where $AC = BC = AC' = BC'' = \frac{1}{2} AB$; *i. e.*, by considering a defi-

nite line AB to be bisected when a segment equal to one-half the line is laid off from either extremity in either direction.



2. *Theorem.* The perpendiculars of a plane triangle meet in H , and, being prolonged to intersect the circumference in A', B', C' , the segments HA', HB' and HC' are bisected by the sides of the triangle. (See Fig. 2.)

Proof: $AB'D = AHD = \text{angle } C$.

NOTE.—Here bisection is used in its ordinary sense.

H is the orthocenter, and the theorem may be otherwise stated as follows: *The segments of the perpendiculars included between the orthocenter and circum-circle are bisected by the sides of the triangle.*

The point of intersection of the medians is the eidocenter,* which we call G , and the well-known theorem that the medians are concurrent and mutually divided into segments of which the greater is twice the less may be otherwise stated thus: *The segments of the medians included between the eidocenter and vertices are bisected by the sides of the triangle.*

NOTE.—Here bisection is used in its extended sense.

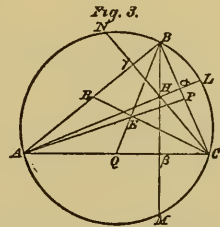
Using bisection in this extended sense it is therefore possible to unite these propositions into a single general statement, as follows:

The segments of the $\left\{ \begin{array}{l} \text{perpendiculars} \\ \text{medians} \end{array} \right.$ between the $\left\{ \begin{array}{l} \text{orthocenter} \\ \text{eidocenter} \end{array} \right.$ and circumcircle measured $\left\{ \begin{array}{l} \text{away from} \\ \text{towards} \end{array} \right.$ the vertices are bisected by the sides of the triangle.

Thus in Fig. 3.

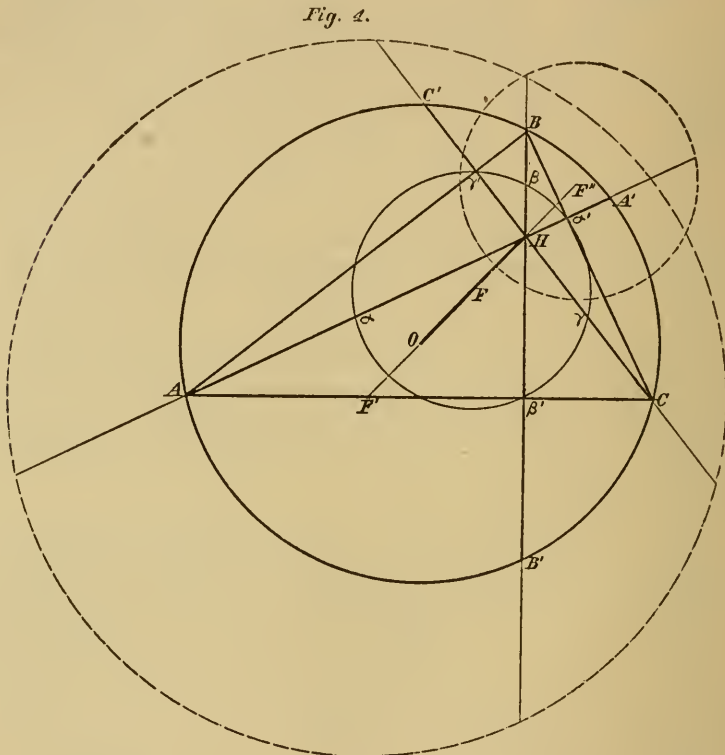
$$\begin{aligned} aH &= aL = \frac{1}{2} HL; \text{ and } EP = \frac{1}{2} EA; \\ \beta H &= \beta M = \frac{1}{2} HM; \quad EQ = \frac{1}{2} EB; \\ \gamma H &= \gamma N = \frac{1}{2} HN; \quad ER = \frac{1}{2} EC. \end{aligned}$$

3. Conceive the triangle ABC (Fig. 4) and its circumcircle O to be the base of an oblique cone withinscribed tetrahedron. Let the vertex of this cone be so taken that when the whole is projected



* This term from εἶδος, *form*, and κέντρον, *center*, has been suggested by Mr. Henry Farquhar as being a more accurate derivation than the term *centroid* often used. It is, moreover, analogous to orthocenter, circumcenter, etc.

upon the plane of the base the projection of the vertex shall fall at the orthocenter H . Now let the whole be orthogonally projected upon the plane of the base.



From this conception it is seen that HA, HB, HC and HA', HB', HC' are projections of elements of the cone and HO the projection of the axis. Let the axis of the cone be bisected by planes parallel to the base. There are three such bisecting planes: *one* midway between apex and base, *another* below the base, and a *third* above the base. Finally let all these sections be orthogonally projected upon the plane of the base.

From these conceptions it follows immediately that—

(a.) These projections are circles whose diameters are, respectively, $\frac{1}{2}, \frac{2}{3}, \frac{1}{3}$, the diameter of the circumcircle.

(b.) The centers of these circles F, F', F'' , all lie in the line HO ,

joining the circumcenter to the orthocenter, and are points of bisection, in the ordinary and extended sense, in such manner that $FH = FO = F'O = F''H = \frac{1}{2}HO$.

(c.) The segments of the perpendiculars HA, HB, HC , and HA', HB', HC' are all bisected by each of these circles. In the case of the first circle F , the segments are bisected in the ordinary sense, and since the segments HA', HB' , and HC' are also bisected by the sides of the triangle this circle passes through the feet of the perpendiculars.

The points of bisection on the perpendiculars determined by the circle F are points of bisection in the ordinary sense.

The points of bisection on the perpendiculars determined by the circle $\begin{cases} F' \\ F'' \end{cases}$ are points of bisection in the *extended* sense, and in such wise that the segments cut off from A and A', B and B', C and C' are measured from the orthocenter $\begin{cases} \text{towards} \\ \text{away from} \end{cases}$ the vertices.

(d.) Every line drawn from H to the circumcircle is bisected by the three circles F, F' , and F'' . H is therefore a *direct* center of similitude common to the circles O, F , and F' and an *inverse* center of similitude common to all four circles.

4. The eidocenter is collinear with the circumcenter, orthocenter, and Feuerbach center*; for from a known theorem we have $HB = 2OM$, and therefore HO must divide BM into segments of which the greater is twice the less, *i. e.*, it must pass through the eidocenter.

5. Again conceive the triangle ABC (Fig 5) as the base of an oblique cone, etc, as in section 3, except that its vertex is to be conceived as perpendicularly over the eidocenter instead of over the orthocenter, and the whole projected as before. In this case EA, EB, EC , and EA', EB', EC' are projections of the elements of the cone and EO , coincident with HO from section 4, the projection of the axis.

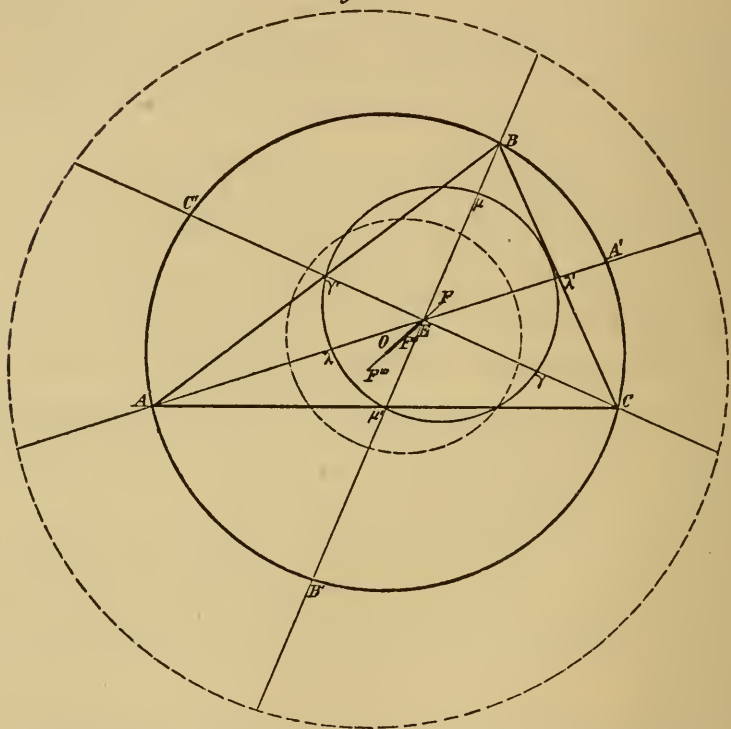
Let the axis be bisected as before by three planes parallel to the base: *one* midway between apex and base, *another* below the base, and a *third* above the apex, and the sections so formed projected upon the plane of the base.

*The center of Feuerbach's circle may be so called for brevity.

We then have—

(a.) These projections are circles whose diameters are, respectively, $\frac{1}{2}$, $\frac{2}{3}$, and $\frac{1}{3}$, the diameter of the circumcircle.

Fig. 5.



(b.) The centers of the circles F'' , F''' , F all lie in EO and therefore in HO joining circumcenter to orthocenter and are points of bisection of EO in both the ordinary and extended sense in such wise that $F''E = F''O = F'''O = FE = \frac{1}{2}EO$.

(c.) The segments of the medians EA , EB , EC and EA' , EB' , EC' are all bisected by each of the circles. In the case of the *third* circle F , the segments are bisected in the *extended* sense, and since the segments of the medians, EA , EB , EC , are also bisected in the extended sense by the sides of the triangle the circle F bisects the sides of the triangle.

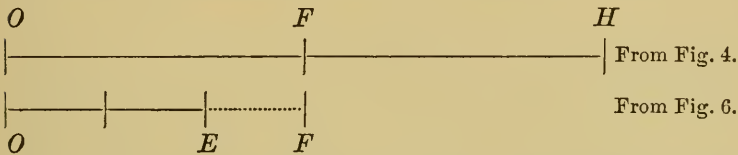
The points of bisection on the medians determined by the circle F'' are bisections in the *ordinary* sense.

The points of bisection on the medians determined by the circles $\begin{cases} F''' \\ F \end{cases}$ are points of bisection in the *extended* sense, and in such manner that the segments cut off from A and A' , B and B' , C and C' are measured from the eidocenter $\begin{cases} \text{towards} \\ \text{away from} \end{cases}$ the vertices.

(d.) Every line drawn from E to the circumcircle is bisected by the three circles F'' , F''' , F ; E is therefore a *direct* center of similitude common to three circles O , F'' , F''' and an *inverse* center of similitude common to all four circles.

6. If we now compare figures 4 and 6 and consider the three circles in each which resulted from projection, we find that circle F , and only circle F , is identical in the two figures.

This identity appears from the fact that their diameters are equal, each equaling half the diameter of the circumcircle, and their centers coincident. The coincidence of their centers appears from drawing the projections of the axes of the cones side by side, thus :



From Fig. 4 we find that this circle, Feuerbach's, passes through 6 noteworthy points, being 2 points on each perpendicular; and from Fig. 6 we find that the same circle passes through 6 other noteworthy points, being 2 on each median, or in all Feuerbach's circle passes through 12 noteworthy points.

7. It is apparent from the foregoing that if we should not bisect the axis of the cone but should cut it in any ratio (Fig. 4) by a plane parallel to the base then the projection of the section would be a circle cutting the perpendiculars in that ratio and its center F_n would divide HO in that ratio. The medians would *not* be divided in that ratio, but a point in HO exists (call it E_n) through which, if lines be drawn from the vertices to the opposite sides, *these* lines would be divided in the given ratio.

The four points O , E_n , F_n , H would in this case, as before, be four harmonic points.

8. Since Feuerbach's circle bisects the sides of the triangle it is the circumcircle of a triangle similar to the original and of half its

size. The results here deduced may therefore be considered to be results of a comparison of the circumcircles of these two triangles. A corresponding study of the relations of the tangent circles (in- and escribed) would therefore be expected to yield many more properties as there are four times as many circles to be considered.

Concerning the phrase "bisection in the extended sense," Mr. DOOLITTLE suggested that the term "sesquisection" might be advantageously employed. As to the name "nine-points circle," Mr. KUMMELL said that it was plainly defective, either "six-points" or "twelve-points" circle being satisfactory, according to the point of view taken, but that nine-points circle was not a correct designation from any point of view. Further remarks were made by Mr. ELLIOTT.

Mr. C. H. KUMMELL presented a communication entitled

DISTANCES ON ANY SPHEROID.

[Abstract.]

The present form of solution of the problem to determine the shortest distance between two points on a spheroid which are given by their latitudes and longitudes is characteristic in making use of the Gaussian algorithm of the arithmetico-geometric mean. This and a corresponding transformation of the amplitudes give the necessary elements for computing in three terms the distance precise to the eighth order *at least*. The form is also remarkable for its symmetry and easy extensibility to still higher precision.

Also the preliminary part of the problem in which the excess of the spherical longitude over the spheroidal is determined by successive approximations is much facilitated by the introduction of an angle η , which is closely related to ϵ , the angle of eccentricity, and which varies between 0 and ϵ . It was thus possible to express the excess of spherical over spheroidal longitude in one term, precise to the 6th order *at least*.

[This paper has been published in full in the *Astronomische Nachrichten*, No. 2671.]

In reply to a question, Mr. KUMMELL said that the ordinary formulæ for computing distances between intervisible points on the terrestrial spheroid are all that can be desired. The formulæ here

presented, however, are designed for much greater distances and for any spheroid, and would serve, if need ever arose, for computing the shortest distance between any two points on the terrestrial spheroid no matter how remote.

19TH MEETING.

APRIL 29, 1885.

The Chairman, Mr. G. W. HILL, presided.

Present, nineteen members and one guest.

Minutes of the eighteenth meeting read and approved.

Mr. A. ZIWET read a paper entitled

ON GRASSMANN'S SYSTEM OF GEOMETRY.

This paper will appear in full in the *Annals of Mathematics*, vol. 2, Nos. 1 and 2.

In reply to a question by Mr. Curtis as to whether Grassmann's system could be advantageously substituted for the Cartesian system, Mr. ZIWET expressed the opinion that it could not be so substituted in general, but that it might in certain special cases.

Grassmann has not, said Mr. ZIWET, made applications of his method to astronomy, nor indeed does its value consist in its adaptability to the solution of special problems. But for presenting general geometrical truths it appears superior to Hamilton's methods, to which it is closely related and with which it might be advantageously joined.

Mr. HALL remarked that he had seen planetary orbits worked out after Hamilton's method by J. Willard Gibbs, but the process appeared rather more laborious than the usual Gaussian one.

The labor of computation of results, Mr. HILL remarked, was practically the same by all methods. By introducing the needful symbols the general expressions may be made exceedingly simple, but when the numerical work begins it will be found that after paring off more or less extraneous matter there still remains a central kernel or core of computation from which there is no escape by any method whatsoever.

With this view Mr. R. S. WOODWARD heartily concurred, and added that the supreme test of the usefulness of such systems as

Grassmann's, Hamilton's, etc., consists in their ability to reveal new truths; a test which, according to Mr. Ziwet, Grassmann's system successfully stands.

Mr. M. H. DOOLITTLE presented a communication on

CAUSE AND CHANCE IN THE CONCURRENCE OF PHENOMENA.

The author's views set forth in this communication were stated to be preliminary and incomplete, and he therefore reserves them to be more fully elaborated before publication.

20TH MEETING.

MAY 13, 1885.

The Chairman, Mr. G. W. HILL, presided.

Present, eleven members and three guests.

Minutes of the nineteenth meeting, read, corrected, and adopted.

Mr. G. L. RAVENÉ read a paper entitled

THE ASTEROIDS.

This communication elicited a general discussion, participated in by Messrs. KUMMELL, RITTER, BAKER, WOODWARD, ELLIOTT, PAUL, and HILL.

Mr. RITTER then read a paper on

SECULAR PERTURBATIONS OF POLYHYMNNIA BY JUPITER.

[Abstract.]

In the computations of these perturbations Gauss's method has been employed, using the formulæ adapted to facilitate the application of this method given by Mr. G. W. Hill.

The eccentricity of Polyhymnia being very large the circumference, with reference to the eccentric anomaly of Polyhymnia, has been divided into twenty-four parts. This is a greater number than necessary, but it seemed worth the additional labor required to have the forces and the other quantities involved for as large a number of points as practicable.

The epoch for both systems of elements is 1873, July, 17.0, Berlin mean time.

The ecliptic and mean equinox are for 1873.0.

The resulting secular variations in one Julian year are the following:

Secular variation of the eccentricity, or		$\delta e = + 1''.268;$
“ “ inclination, or		$\delta i = - 1.649;$
“ “ ascending node, or		$\delta \Omega = - 61.031;$
“ “ longitude of the perihelion, or $\delta \pi = + 59.116;$		
“ “ mean longitude, or		$\delta L = - 83.429;$

The paper was discussed by Messrs. PAUL, HILL, and WOODWARD.

21ST MEETING.

MAY 27, 1885.

The meeting was called to order at 8:15 by the Chairman, Mr. G. W. HILL.

Seventeen members present.

At the request of the Chair Mr. WINLOCK acted as secretary *pro tem.*, Mr. BAKER being absent.

Mr. R. S. WOODWARD read a paper on

SOME PRACTICAL FEATURES OF A FIELD TIME DETERMINATION WITH A MERIDIAN TRANSIT.

[Abstract.]

An important desideratum in all kinds of field work is the adoption of those methods which will secure the accuracy essential in the results sought with the minimum amount of computation. It is in general easier and more conducive to precision to eliminate unnecessary factors involved with the quantity sought than to determine their values and allow for them by computation. Very frequently also a systematic arrangement of observations will secure the maximum precision with the minimum of computation.

In a field time determination for telegraphic longitude the essential quantity is the error of the time-piece used at some determinate epoch, and the unessential factors are the azimuth and collimation of the transit and the rate of the time-piece. It is evident that a

minimum of computation will be required if the observations can be so arranged as to eliminate the effect of these factors in the final value of the correction to the time-piece. Although it is usually impossible to eliminate the effect of the azimuth, collimation, and rate completely, it is generally possible to make a close approximation thereto. To show this fact analytically let

- Δt = the correction to the time-piece at the epoch t_0 ;
 t = the observed time of a star's transit;
 a = the star's right ascension;
 α = the azimuth of the transit;
 c = the collimation of the transit;
 r = the rate of the time-piece;
 A = the azimuth factor;
 C = the collimation factor;
 p = the weight of $(t - a)$;
 v = the residual error.

Then the type observation-equation will be

$$\Delta t + Aa + Cc + (t - t_0)r + t - a = v. \quad (1)$$

The normal equation in Δt , using brackets to indicate summation of like quantities, is

$$[p] \Delta t + [pA] a + [pC] c + [p(t - t_0)] r + [p(t - a)] = 0. \quad (2)$$

This shows that in order to secure the complete elimination of the effect of a , c , and r , we must have

$$[pA] = 0, [pC] = 0, [p(t - t_0)] = 0. \quad (3)$$

The last of these conditions can always be fulfilled by making

$$t_0 = \frac{[p t]}{[p]}. \quad (4)$$

It may be shown that the value of Δt corresponding to t_0 as defined by (4) has a maximum weight. A close approximation to the first two conditions of (3) can be secured by selecting for observation stars of suitable declinations and by reversals of the telescope.

If we put

$$\frac{[pA]}{[p]} = \beta, \frac{[pC]}{[p]} = \gamma, \frac{[p(t - a)]}{[p]} = \Delta t_0,$$

equation (2) gives $\Delta t = -\Delta t_0 - \beta a - \gamma c$. (5)

This shows that in case β and γ are small, as supposed above, an

approximate value of Δt is $-\Delta t_0$. After some preliminary observations at a station it is easy to render a and c small, and their approximate values may always be found from the observation equations by a brief inspection; so that with such values of a , c , β , and γ as are nearly always readily attainable Δt may be derived from (5) to the nearest $0^{\circ}.01$.

We may thus dispense entirely with the other three normal equations and reach the same result which would follow from their use. The solution may also be checked; for by one or two approximations the values of Δt , a and c which make $[pv] = 0$ can be readily found.

The practical steps in deriving Δt from (5) may be summarized as follows:

1. The mean of the observation-equations for clamp west minus the mean of those for clamp east will give an approximate value of the collimation c .

2. The application of this value of c to each observation equation will give a corrected value of $(t - a)$ for each star.

3. An approximation to the value or values of the azimuth will then result by eliminating Δt from one or more pairs of the corrected observation equations. The azimuth may then be applied to correct the values of $(t - a)$, reached in step 2.

4. The approximate values of a and c will now give an approximate value of Δt from (5), and the application of this value of Δt to the values of $(t - a)$, derived in step 3, will give approximate values of v .

5. Form $[pv]$. If this sum is not zero within $0^{\circ}.01$ or $0^{\circ}.02$, a brief inspection will show what changes in a and c (and possibly Δt) will make it zero within those limits.

By this process of determining the residuals or their approximate values as soon as possible in the computation any large errors in the values of $(t - a)$ or the azimuth and collimation factors will be easily detected.

In precise longitude determinations it is customary to have for each night's observations two complete time determinations, one immediately preceding and one immediately following the telegraphic comparison of time-pieces. In this case there will be two values of Δt . Calling these $\Delta t'$ and $\Delta t''$ and denoting the corres-

ponding epochs by t'_0 and t''_0 the rate of the time-piece will be given with sufficient accuracy for interpolation by the equation

$$r = \frac{\Delta t'' - \Delta t'}{t''_0 - t'_0}.$$

Mr. PAUL thought it an objection to this method that in arranging the groups valuable stars might be lost, so that in a limited time the accuracy of the results would be impaired by the smaller number of observations; moreover, the method did not furnish the computer with a clear idea of the performance of the instrument.

Mr. HALL said that he liked the method, and that he thought it especially good for time work. He had discovered the method once himself, and he knew that it had also been used by Prof. Ormond Stone.

Mr. KUMMELL said that in connection with this subject he had investigated the question of the advisability of using stars towards the pole for time determinations; that is, he had examined the weight co-efficient formulæ to see at what distance north of the zenith a maximum value would be obtained. He found that in general the limit of declination was about 60° .

Mr. PAUL thought that every weight-formula should take account of the increase of atmospheric disturbance with increase of zenith distance.

Mr. KUMMELL then read the following paper entitled

CAN THE ATTRACTION OF A FINITE MASS BE INFINITE?

In Price's Calculus, vol. III, art. 201, discussing the result for the attraction of a thin rectangular plate on a particle external to it and in its own plane it is found that if the attracted particle is at an angle of the rectangle the attraction is infinite. Price's method of determining the attraction of plates consists in integrating between the proper limits the following differentials:

$$d^2 X = m\theta\tau \frac{x dx dy}{(x^2 + y^2)^{\frac{3}{2}}}; \quad (1_x)$$

$$d^2 Y = m\theta\tau \frac{y dx dy}{(x^2 + y^2)^{\frac{3}{2}}}; \quad (1_y)$$

where $X = x$ — axial component of attraction;

$Y = y$ — axial component of attraction;

$m =$ mass of attracted particle;

$\theta =$ density of attracting mass, supposed homogeneous;

$\tau =$ thickness of the plate.

Referring to the attracted particle as origin let (α_0, b_0) be the corner nearest and (α_1, b_1) that farthest from the particle; then

$$\begin{aligned}
 X &= m\theta\tau \int_{b_0}^{b_1} dy \int_{\alpha_0}^{\alpha_1} \frac{x dx}{(x^2 + y^2)^{\frac{3}{2}}} \\
 &= m\theta\tau \int_{b_0}^{b_1} dy \left((a_0^2 + y^2)^{-\frac{1}{2}} - (a_1^2 + y^2)^{-\frac{1}{2}} \right) \\
 &= m\theta\tau \left\{ \frac{b_1 + (a_0^2 + b_1^2)^{\frac{1}{2}}}{b_0 + (a_0^2 + b_0^2)^{\frac{1}{2}}} \cdot \frac{b_0 + (a_1^2 + b_0^2)^{\frac{1}{2}}}{b_1 + (a_1^2 + b_1^2)^{\frac{1}{2}}} \right\} \quad (2)
 \end{aligned}$$

and a similar expression for Y by exchanging the a 's for the b 's.

If in this we place $\alpha_0 = b_0 = 0$ then $X = m\theta\tau \infty$.

This is taken by Price to be infinite; yet, since the thickness τ must be taken infinitesimal, this is an entirely unfounded conclusion.

At first, however, I did not suspect this result, and when Mr. Woodward found an infinite attraction of a circular disk on a point at its circumference, which result I checked, it seemed to be possible that the attraction of a finite mass could be infinite. Yet neither Mr. Woodward nor myself was entirely convinced. To settle this question I then resolved to determine the attraction of a right prism and also of a right circular cylinder on a particle at mid-height, which, being then moved to the surface and taking the height infinitesimal, would give the attraction of a plate on a particle in a position at which an infinite attraction had been found.

For a right rectangular prism we have, $2h$ being its height,

$$\begin{aligned}
 X &= m\theta \int_{b_0}^{b_1} dy \int_{\alpha_0}^{\alpha_1} x dx \int_{-h}^h \frac{dr}{(x^2 + y^2 + z^2)^{\frac{3}{2}}} \\
 &= m\theta \int_{b_0}^{b_1} dy \int_{\alpha_0}^{\alpha_1} \frac{2hx dx}{(x^2 + y^2)(x^2 + y^2 + h^2)^{\frac{1}{2}}} \quad (3)
 \end{aligned}$$

Comparing this with (2), putting $2h = \tau$, we readily see that these values are by no means identical, for (2) is of the form $\tau f_2(\alpha_1, \alpha_0, b_1, b_0)$ while (3) is $\tau f_3(\alpha_1, \alpha_0, b_1, b_0, \tau)$. Here f_2 is independent of τ while f_3 is not.

Placing $a_0 = b_0 = 0$ or supposing the attracted particle at the edge of the prism we have

$$\begin{aligned}
 X &= 2m\theta h \int_0^{b_1} dy \int_0^{a_1} \frac{x dx}{(x^2 + y^2)(x^2 + y^2 + h^2)^{\frac{1}{2}}} \\
 &= 2m\theta h \int_0^{b_1} dy \int_0^{\sqrt{a_1^2 + y^2 + h^2}} \frac{dr}{z^2 - h^2} \\
 &= 2m\theta h \int_0^{b_1} dy \left[\frac{1}{2h} \log \frac{z - h}{z + h} \right] \frac{\sqrt{a_1^2 + y^2 + h^2}}{\sqrt{y^2 + h^2}} \\
 &= m\theta \int_0^{b_1} dy \left[\log \frac{z - h}{z + h} \right] \frac{\sqrt{a_1^2 + y_2 + h^2}}{\sqrt{y^2 + h^2}} \quad (4)
 \end{aligned}$$

This form shows clearly that X vanishes with h ; therefore the attraction of a rectangular plate on a particle at one of its corners is not infinite, but, on the contrary, it is infinitesimal.

Similarly the attraction of a circular plate on a particle at its circumference may be found by considering the plate a vanishing cylinder. Using cylindrical co-ordinates to a vertical line through the attracted particle as axis we have, if $\rho =$ horizontal radius vector, $v =$ vectorial angle, for the attraction of a cylinder, radius r , density θ , on a particle at midheight h and distance d from axis of cylinder where

$$\cos v = \frac{\rho^2 + d^2 - r^2}{2\rho d}$$

$$\text{and } \sin v = \frac{1}{2\rho d} \sqrt{[(d+r)^2 - \rho^2][\rho^2 - (d-r)^2]}$$

$$\begin{aligned}
 A &= m\theta \int_{d-r}^{d+r} \rho^2 d\rho \int_{-v}^v \cos v dv \int_{-h}^h \frac{dr}{(\rho^2 + z^2)^{\frac{3}{2}}} \\
 &= m\theta \int_{d-r}^{d+r} \rho^2 d\rho \cdot 2 \sin v \cdot \frac{2h}{\rho^2 \sqrt{\rho^2 + h^2}}
 \end{aligned}$$

$$\begin{aligned}
 &= 2m\theta \frac{h}{d} \int_{d-r}^{d+r} \frac{d\rho}{\rho} \sqrt{\frac{[(d+r)^2 - \rho^2][\rho^2 - (d-r)^2]}{\rho^2 + h^2}} \\
 &= 2m\theta \frac{h}{d} \int \frac{d\rho}{\rho} \sqrt{\frac{\sqrt{a^2 - h^2} \sqrt{(a^2 - \rho^2 - h^2)(\rho^2 + h^2 - b^2)}}{\rho^2 + h^2}} \\
 &\quad \sqrt{b^2 - h^2}
 \end{aligned}$$

where $a = \sqrt{(d+r)^2 + h^2}$; and $b = \sqrt{(d-r)^2 + h^2}$ (5)

Assume $\tan \varphi = \frac{a}{b} \sqrt{\frac{\rho^2 + h^2 - b^2}{a^2 - \rho^2 - h^2}}$ then φ has the limits $\frac{\pi}{2}$ and

0. We have then $\rho^2 + h^2 = \frac{a^2 b^2}{a^2 \cos^2 \varphi + b^2 \sin^2 \varphi} = \frac{b^2}{\Delta \varphi^2}$, where $\Delta \varphi$

is an elliptic Δ function to the modulus $\sqrt{1 - \frac{b^2}{a^2}}$. Transform-

ing we have, expressing in Δ functions

$$\begin{aligned}
 A &= 2m\theta \frac{h}{d} \int_0^{\frac{\pi}{2}} ab^2 \frac{d\varphi}{\Delta \varphi^3} \cdot \frac{(1 - \Delta \varphi^2)(\Delta \varphi^2 - \frac{b^2}{a^2})}{b^2 - h^2 \Delta \varphi^2} \\
 &= 2m\theta \frac{ab^2}{hd} \left\{ -\frac{h^2}{a^2} \int_0^{\frac{\pi}{2}} \frac{d\varphi}{\Delta \varphi^3} + \int_0^{\frac{\pi}{2}} \frac{d\varphi}{\Delta \varphi} - \frac{(d^2 - r^2)^2}{a^2 b^2} \int_0^{\frac{\pi}{2}} \frac{d\varphi}{(1 - \frac{h^2}{b^2} \Delta \varphi^2) \Delta \varphi} \right\} \\
 &= 2m\theta \frac{ab^2}{hd} \left\{ \int_0^{\frac{\pi}{2}} \frac{d\varphi}{\Delta \varphi} - \frac{h^2}{b^2} \int_0^{\frac{\pi}{2}} d\varphi \Delta \varphi \right. \\
 &\quad \left. - \frac{(d+r)^2}{a^2} \int_0^{\frac{\pi}{2}} \frac{d\varphi}{(1 + \frac{4rdh^2}{a^2(d-r)^2} \sin^2 \varphi) \Delta \varphi} \right\} \\
 &= 2m\theta \frac{ab^2}{hd} \left\{ F - \frac{h^2}{b^2} E - \left(\frac{d+r}{a}\right)^2 \Pi \left(\frac{4rdh^2}{a^2(d-r)^2}\right) \right\} \quad (6)
 \end{aligned}$$

where F , E , and Π denote quadrantal elliptic integrals of the 1st, 2d, and 3d species, according to Legendre's notation. If our object was to obtain here a formula for convenient computation of the attraction the third term could still be expressed in integrals of the 1st and 2d species, which have been tabulated by Legendre.

Let us now move the particle to the surface of the cylinder, then we have $d = r$; $a = \sqrt{4r^2 + h^2}$; $b = h$, and (6) becomes

$$A' = 2m\theta \frac{ah}{r} (F - E). \quad (6')$$

Mr. Woodward, as already stated, had found an infinite attraction of a circular disc on a particle on its circumference by using Price's method. Now, since A' is *surely* a finite quantity, we have here the manifest absurdity that the attraction of a cylinder on a particle on its surface would be less than that of a circular disk which is only an infinitesimal part of it.

If we wish to ascertain the attraction of a circular disk of finite small thickness we may, of course, use (6'), and since then F tends to infinity, E may be neglected; therefore

$$\begin{aligned} A'_{h=0} &= \frac{2m\theta}{r} \left[ah \int_0^{\frac{\pi}{2}} \frac{d\varphi}{\sqrt{1 - \frac{4r^2}{a^2} \sin^2 \varphi}} \right]_{h=0} \\ &= 4m\theta \left[\frac{\int_0^{\frac{\pi}{2}} \frac{d\varphi}{\sqrt{1 - \frac{4r^2}{a^2} \sin^2 \varphi}}}{\frac{1}{h}} \right]_{h=0} \\ &= 4m\theta \left[\frac{- \int_0^{\frac{\pi}{2}} \frac{4r^2 \sin^2 \varphi \frac{da}{dh}}{a^3 \Delta \varphi^3} d\varphi}{-\frac{1}{h^2}} \right]_{h=0} \\ &= 4m\theta \left[\frac{\frac{4r^2 h}{a^4} \int_0^{\frac{\pi}{2}} \frac{\sin^2 \varphi d\varphi}{\Delta \varphi^3}}{\frac{1}{h^2}} \right]_{h=0} \\ &= 0 \end{aligned}$$

Since then the attraction is 0 if $h = 0$ it will be small if h is small, and will continuously grow with h .

The notion of an infinite attraction exerted by a finite mass has thus been dispelled in two special cases in which it seemed to have been proved, and I add some remarks on its general impossibility.

The attraction of a mass element on a particle at distance ρ is

$$m\theta \frac{dx \, dy \, dz}{\rho^2}$$

This is then an infinitesimal of the third order, and the summation of its components with respect to a fixed direction requires three integrations, which give surely a finite result if ρ is always finite.

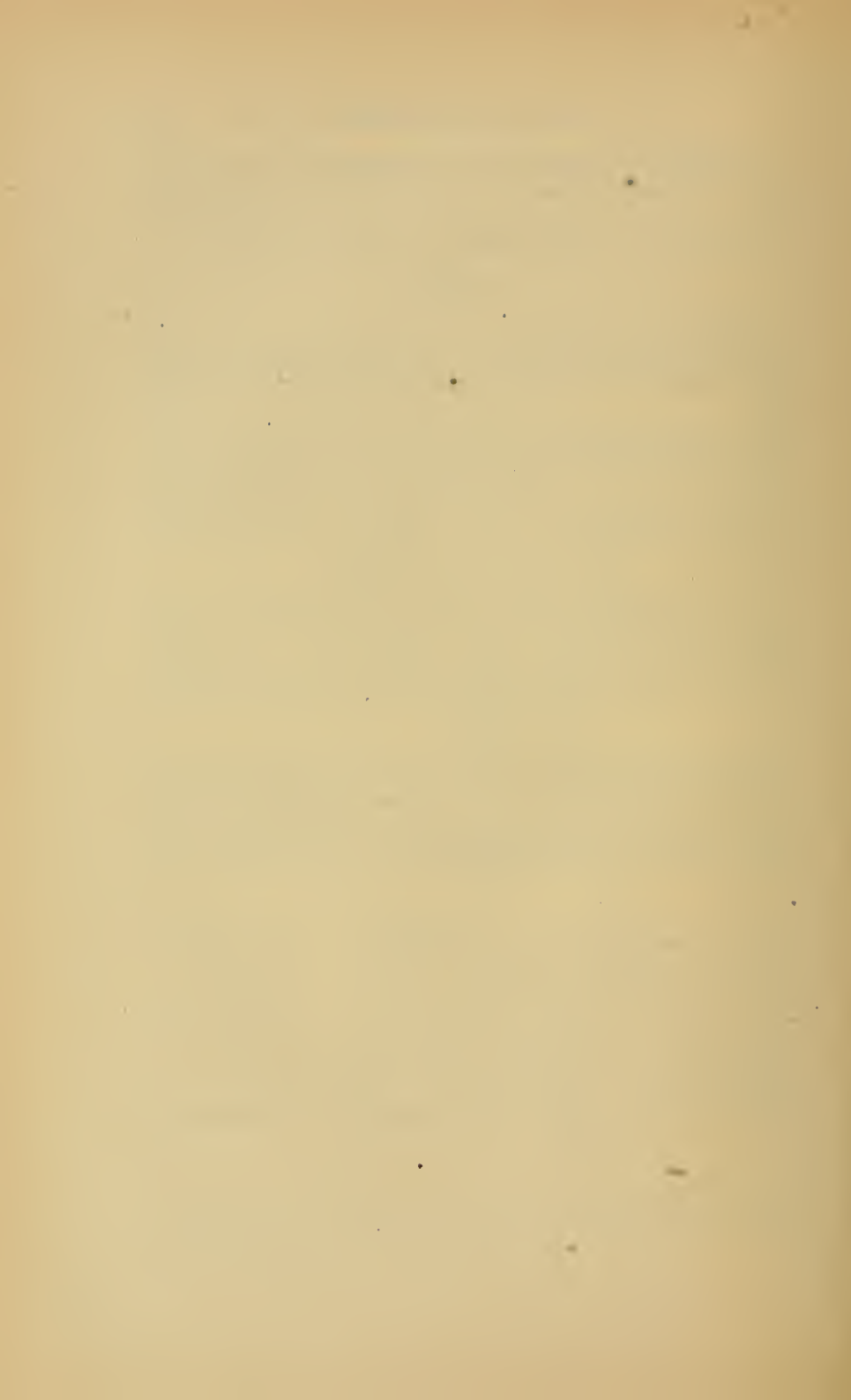
If ρ is infinitesimal there will be *one* element of attraction, which, instead of being of the third order, is only of the *first* order of infinitesimals, and this one element being added to the finite sum of the other elements has no effect. Hence I conclude that a finite mass exerts only a *finite* attraction on a particle.

The paper was discussed by Messrs. HALL, HILL, and WOODWARD. Mr. WOODWARD said that he had arrived at a result similar to Mr. Kummell's by a somewhat different route. The fallacy in Price's Calculus arose from neglecting the thickness of the plate.

NOTE.

The communications and abstracts printed in the proceedings of the Mathematical Section have each been examined by a special committee consisting of the Chairman, the Secretary, and a third member appointed by the Chairman. These third members were as follows:

<i>Title.</i>	<i>Author.</i>	<i>Third Member.</i>
Physical observations of Wolf's comet.	W. C. Winlock.	— — —
The Theory of Mercury.....	G. L. Ravené.	E. B. Elliott.
A group of circles related to Feuerbach's circle.....	Marcus Baker.	C. H. Kummell.
Some practical features of a time determination	R. S. Woodward.	H. Farquhar.
Can the attraction of a finite mass be infinite?.....	C. H. Kummell.	R. S. Woodward.



INDEX.

	Page.		Page.
Abbe, C.: communication on methods of verifying weather predictions.....	8, 9	Calendar.....	xxx
Adams, C. F., Election to membership of.....	17	Can the attraction of a finite mass be infinite?.....	58
Adjustment of conditioned observations.....	41	Capron, Horace, Death of.....	8
American Academy of Arts and Sciences.....	xxxvi	Cause and chance in the concurrence of phenomena.....	54
American Association for the Advancement of Science.....	xxxix	Chatard, T. M., Election to membership of.....	11
American Philosophical Society.....	xxxiv, xxxvii	— remarks on transmission of sounds and earth tremors.....	28
American scientific societies.....	xxxiii	Chemical Society, Invitation from.....	29
Annual address of the President.....	xxxii	Chlamydoconcha Orcutti.....	5
Annual meeting.....	30	Circles related to Feuerbach's circle.....	45
Anthropological Society, Invitation from.....	5	Clarke, F. W.: communication on an attempt at a theory of odor.....	27
Anthropometric and reaction-time apparatus.....	25	— — — the Flood Rock explosion.....	28
Antisell, T.: remarks on the nature of odors.....	27	— — — topaz from Stoneham, Maine.....	5
— — — thunderstorms.....	11	Collection of formulæ for the area of a plane triangle (Title only).....	37
Artifice sometimes useful for the adjustment of conditioned observations.....	41	Columnar structure in the diabase of Orange Mountain, N. J.....	19
Attempt at a theory of odor.....	27	Comets II and III, 1884 (Title only).....	16
Attraction, Infinite, of a finite mass.....	58	Committee, auditing, Appointment of.....	31
Auditing committee, Appointment of.....	31	— Report of.....	3
— — Report of.....	3	— General.....	xii, xiv, xv
Baker, Marcus: communication on a group of circles related to Feuerbach's circle..	45	— on communications.....	xiv, xv
— — — a collection of formulæ for the area of a plane triangle.....	37	— — mathematical communications.....	63
— elected Secretary of Mathematical Section.....	37	— — publications.....	xiv, xv
— report of auditing committee.....	3	Condensing hygrometer and sling psychrometer.....	25
Baker, Frank: communication on modern ideas of brain mechanism.....	17	Condition of the earth's interior (Title only).....	17, 18
— remarks on the recognition of the direction of sound.....	13	Conditioned observations.....	41
Barus, Carl, Election to membership of.....	5	Connecticut Academy of Arts and Sciences.....	xxxvii
Bell, A. G.: communication on the mechanism of "clicks" and "clucks".....	18	Constitution.....	vii
Billings, J. S.: communication on anthropometric and reaction time apparatus.....	25	Crumpling of the earth's crust.....	18
— — — germ cultures.....	30	Curtis, G. E.: remarks on methods of verifying weather predictions.....	9
— — — vital statistics of the tenth U. S. census.....	4	Dall, W. H.: communication on two remarkable forms of mollusks.....	5
— remarks on the olfactory sense organs.....	28	Deceased members.....	xxv, xxvii, 8, 10, 25
— — — care of pamphlets.....	29	Diabase, Columnar structure of.....	19
Biological Society, Invitation from.....	4	Diller, J. S.: communication on topaz from Stoneham, Maine.....	5
Brown, Addison, cited on aberration of sound.....	12	Distances on any spheroid.....	52
Bulletin, Rules for publication of.....	xiii		
Burnett, S. M.: communication on the Javal and Schiotz ophthalmometer.....	11		

	Page.		Page.
Doolittle, M. H.: communication on cause and chance in the concurrence of phenomena.....	54	Hallock, William, Election to membership of.....	5
— remarks on bisection and sesquisection... ..	52	Hampson, Thomas, Election to membership of.....	29
— — — notation for gravitation formula.....	40	Harkness, William: communication on flexures of transit instruments.....	27
Dutton, C. E.: communication on practical geology versus speculative physics.....	4, 5	— remarks on care of pamphlets.....	29
— remarks on transmission of sounds and earth tremors.....	28	Hazen, H. A.: communication on the condensing hygrometer and sling psychrometer.....	25
Earth, Interior of.....	7	— — — thunderstorms of 1884.....	10
Earth's crust, Crumpling of.....	18	— remarks on the verification of weather predictions.....	9
Elliott, E. B.: communication entitled Example illustrating the use of a certain symbol in the calculus of affected quantity.....	37	Hill, G. W.: elected President of Mathematical Section.....	37
Endowment of research.....	xli	— remarks on adjustment of conditioned observations.....	41
Example illustrating the use of a certain symbol in the calculus of affected quantity (Title only).....	37	— — — geometric systems.....	53
Farquhar, E.: remarks on the recognition of the direction of sound.....	13	— — — Mercury.....	45
— — — thunderstorms.....	11	— — — notation for gravitation formula.....	40
Farquhar, H.: remarks on sounds connected with meteors and earthquakes.....	28	Hodgkins, H. L., Election to membership of Honorary members of American Societies.....	8
Feuerbach's circle.....	45	xxxvii	
Flexures of transit instruments.....	27	Hough, F. B., Death of.....	25
Flood Rock explosion.....	28	Hygrometers.....	25
Flora of the Laramie group (Title only).....	17	Iddings, J. P.: communication on the columnar structure in the diabase of Orange Mountain, N. J.....	19
General Committee, Members of.....	xiv, xv	— Election to membership of.....	8
— — Rules of.....	xii	Infinite attraction of a finite mass.....	58
— government in its relations to research... ..	xli	Javal and Schiøtz ophthalmometer, Exhibition of.....	11
Geometry, Grassmann's system of.....	53	Johnson, A. B.: communication on the difficulty in determining the direction of sound.....	11, 12
Germ cultures.....	30	Kerr, W. C., Death of.....	25
Gooch, F. A., Election to membership of.....	5	Kummell, C. H.: communication entitled, Can the attraction of a finite mass be infinite?.....	58
Goode, G. B.: communication on the systematic care of pamphlets.....	29	— — — an artifice sometimes useful for the adjustment of conditioned observations.....	41
Grassmann's system of geometry.....	53	— remarks on distances on any spheroid.....	52
Gravitation, Modification of Newtonian formula of.....	39	— — — Feuerbach's circle.....	52
Group of circles related to Feuerbach's circle.....	45	— — — field-time determinations.....	58
Hann, J., cited on temperature changes at Hamburg.....	9	Latitude, Variations of.....	10
Hains, R. P., Election to membership of.....	10	List of members.....	xvi
Hall, Asaph: communication on variations of latitude.....	10	Mann, B. P.: remarks on the care of pamphlets.....	29
— Presidential address.....	xxiii	Marvin, C. F., Election to membership of....	8
— remarks on a communication by Mr. Dutton.....	8	Mathematical communications, Committees on.....	63
— — — field-time determinations.....	58	— Section, Bulletin of.....	37
— — — Hamilton's geometric system.....	53	— — Members of.....	36
Hall, Asaph, Jr., Election to membership of.....	3		
Hall, Prof. G. Stanley: communication on recent experiments on reaction time and the time sense.....	4		

	Page.		Page.
Mathematical Section, Officers of.....	36, 37	Polyhymnia, Perturbations of.....	54
— — Rules of	35	Practical geology versus speculative physics (Title only).....	4, 5, 6
Matthews, Washington: communication on mythological dry painting of the Nava- jos.....	14	President's address.....	xxxiii
— — — anthropometric and reaction time apparatus.....	25	Psychrometers.....	25
McGee, W. J.: communication on the ter- races of the Potomac valley.....	24	Publications, Committee on.....	xiv, xv
Measurement of temperature at distant points (Title only).....	18	Ravené, G. L.: communication on the aste- roids.....	18, 54
Mechanism of clicks and clucks (Title only)	18	— — — the theory of Mercury.....	41
Members, Deceased.....	xxv, xxvii, 8, 10, 25	— Election to membership of.....	11
— List of.....	xvi	— remarks on comets.....	17
— New.....	xxvii	Reaction time apparatus.....	25, 27
Mendenhall, T. C.: communication on mea- surement of temperature at distant points.....	18	Recent experiments on reaction time and the time sense (Title only).....	4
— Election to membership of.....	8	Report of Secretaries.....	xxvii, 31
— exhibition of a volt meter.....	26	— — Treasurer.....	xxviii, 31
— remarks on reaction time.....	27	Research, Endowment of.....	xli
Mercury, Mathematical theory of.....	41	Riley, C. V.: communication on the system- atic care of pamphlets.....	29
Methods of verifying weather predictions...	8	Ritter, F. W. McK.: communications on sec- ular perturbations by Jupiter.....	54
Milneria minima.....	5	Robinson, T.: remarks on the observation of earth tremors.....	28
Modern ideas of brain mechanism (Title only).....	17	Rules for the publication of the Bulletin.....	xiii
Mollusks, Two remarkable forms of.....	5	— of the General Committee.....	xii
Moser, J. F., Election to membership of.....	12	— — — Mathematical Section.....	35
Mountain structure.....	18	— — — Society.....	ix
Mythological dry painting of the Navajos...	14	Secretaries, Report of.....	xxvii, 31
National Academy of Sciences.....	xl, xlv	Secular perturbations of Polyhymnia by Jup- iter.....	54
Navajos, Painting by.....	14	Seismometric observation.....	28
Newtonian formula of gravitation.....	39	Shumway, W. A., Election to membership of	12
Nine-points circle.....	46	Signal service investigations of thunder- storms.....	10
Odor, Theory of.....	27	— — rules for verification of predictions....	8
Officers, Election of.....	31, 37	Six-points circle.....	46
— of the Mathematical Section.....	36	Slight modification of the Newtonian form- ula of gravitation.....	39
— — — Society.....	xiv, xv	Sling psychrometer.....	25
Orange Mountain, N. J.....	19	Smell, Sense of.....	27
Painting by the Navajos.....	14	Societies, American scientific.....	xxxi
Pamphlets, Care of.....	29	Some practical features of a field time de- termination with a meridian transit.....	55
Paul, H. M.: communication on the earth's interior.....	17, 18	Sound, Aberration of.....	11, 12
— — — the Flood Rock explosion.....	28	Spheroid, Distances on.....	52
— remarks on the earth's rigidity.....	7	Standing rules of the General Committee...	xii
— — — dry painting by the Japanese.....	16	— — — — Mathematical Section.....	35
— — — field time determinations.....	58	— — — — Society.....	ix
— — — the topophone.....	13	Swift, Dean, cited.....	xl
Peale, T. R., Death of.....	10	Systematic care of pamphlets.....	29
Perturbations of Polyhymnia.....	54	Taylor, W. B.: communication on the crump- ling of the earth's crust.....	18
Physical observations on Wolf's comet (1884, III).....	37	— — — geological and physical theories.....	6
Poindexter, W. M., Election to membership of.....	3	— — — a slight modification of the Newton- ian formula of gravitation.....	39

	Page.		Page.
Taylor, W. B.: remarks on the topophone....	13	Weed, W. H., Election to membership of....	17
Terraces of the Potomac valley (Title only).	24	Willis, Bailey, Election to membership of...	8
Theory of Mercury.....	41	Wilson, H. M., Election to membership of...	11
Thompson, Gilbert, on rock paintings in New Mexico.....	16	Winlock, W. C.: communication on comets II and III, 1884.....	16
Thunderstorms of 1884.....	10	— — — physical observations on Wolf's comet (1884, III).....	37
Time determination with meridian transit..	55	— report of auditing committee.....	3
Toner, J. M.: remarks on the care of pamph- lets.....	29	Woodward, R. S.: cited on infinite attrac- tion.....	59, 62
Topaz from Stoneham, Maine.....	5	— communication on some practical fea- tures of a field time determination with a meridian transit.....	55
Topophone.....	13	— remarks on geometric systems.....	53
Transit instruments, Flexures of.....	27	— — — infinite attraction of a finite mass...	63
Trap, Columbar.....	19	— — — variations of latitude.....	10
Treasurer, Report of.....	xxviii, 31	Wolf's comet.....	37
Twelve-points circle.....	46	Wortman, J. S., Election to membership of..	31
Two remarkable forms of mollusks.....	5	Wright, G. M., Election to membership of...	10
Variations of latitude.....	10	Yarrow, H. C.: Report of auditing com- mittee.....	3
Velocity of transmission of earth tremors...	28	Ziwet, Alexander: communication on Grass- mann's system of geometry.....	53
Verifying weather predictions.....	8	— Election to membership of.....	8
Vital statistics of the tenth U. S. census (Title only).....	4		
Volt-meter, Exhibition of.....	26		
Ward, L. F.: communication on the flora of the Laramie group.....	17		
Weather predictions, Verification of.....	8		

BULLETIN

OF THE

PHILOSOPHICAL SOCIETY

OF

WASHINGTON.

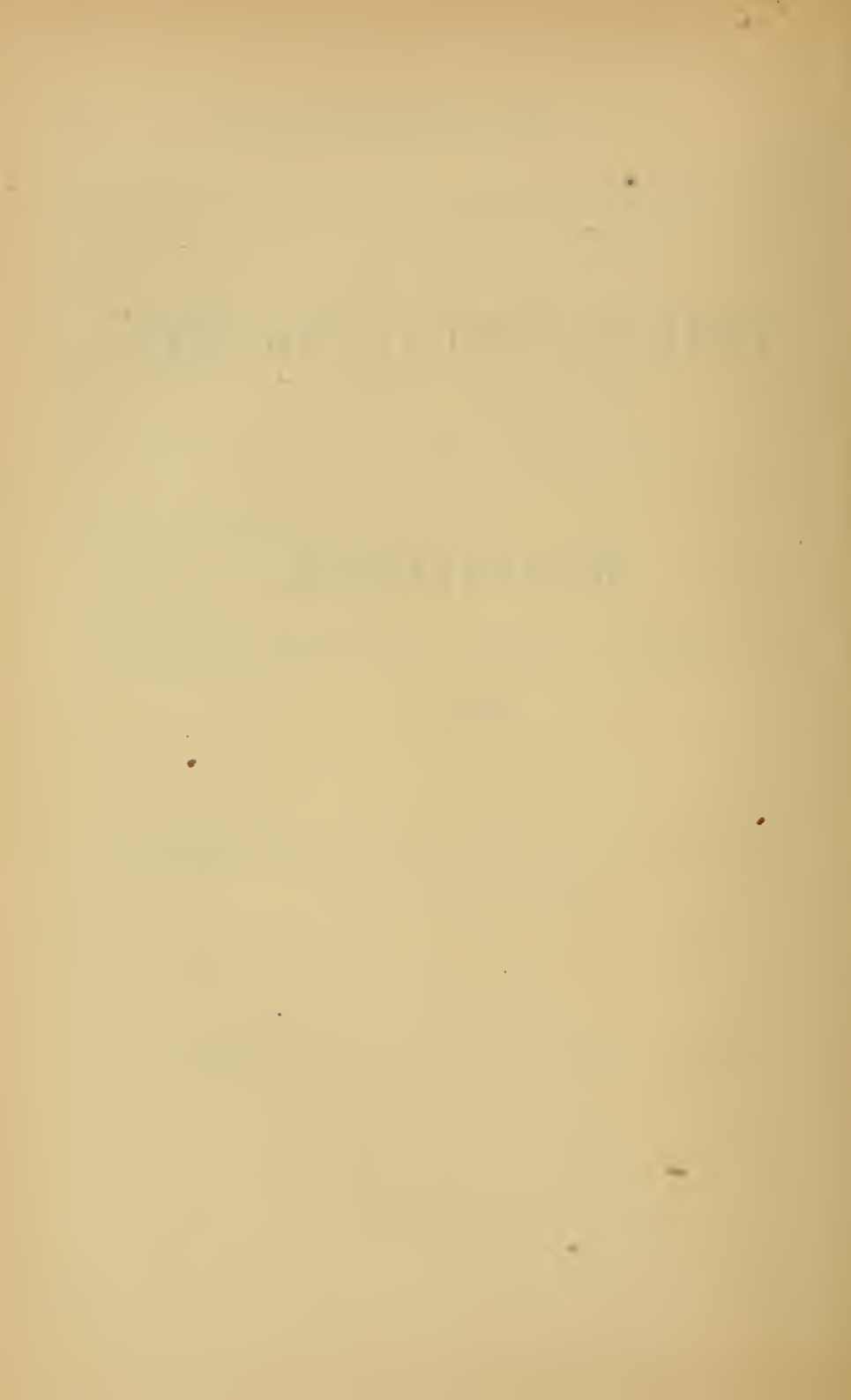
VOL. IX.

Containing the Minutes of the Society and of the Mathematical
Section for the year 1886.

PUBLISHED BY THE CO-OPERATION OF THE SMITHSONIAN INSTITUTION.

WASHINGTON:

1887.



CONTENTS.

	Page.
Constitution -----	VII
Standing Rules of the Society -----	IX
Standing Rules of the General Committee -----	XII
Rules for the Publication of the Bulletin -----	XIII
Officers elected December, 1885 -----	XIV
Officers elected December, 1886 -----	XV
List of Members -----	XVI
List of Deceased Members -----	XXVI
Calendar -----	XXVIII
Annual Report of the Secretaries -----	XXIX
Annual Report of the Treasurer -----	XXX
Annual Address of the President, J. S. Billings -----	XXXV
Bulletin of the General Meeting -----	1
Report of the Auditing Committee -----	3
Notes on the geology of northern California, J. S. Diller ----	4
Notes on the faults of the Great Basin and of the eastern base of the Sierra Nevada, I. C. Russell -----	5
Recent changes of level in the basin of Lake Ontario, G. K. Gilbert, (<i>Title only</i>) -----	8
Lieutenant Lockwood's expedition to farthest north, George E. Curtis -----	8
Two examples of similar inventions in areas widely apart, O. T. Mason -----	12
Historical sketch of deep-sea temperature observations, J. H. Kidder, (<i>Title only</i>) -----	14
Annual profit to banks of national bank note circulation, E. B. Elliott, (<i>Title only</i>) -----	14
Quantity of United States subsidiary silver coin existing and in circulation, E. B. Elliott, (<i>Title only</i>) -----	14
The new star in the nebula of Andromeda, Asaph Hall, (<i>Title only</i>) -----	14
The images of stars, Asaph Hall, (<i>Title only</i>) -----	15
On the changes of terrestrial level surfaces due to variations in distribution of superficial matter, R. S. Woodward, (<i>Title only</i>) -----	15
On the observed changes of level surfaces in the Bonneville area and their explanation, G. K. Gilbert, (<i>Title only</i>) -----	15
On the varying altitudes of former level surfaces in the Great Lake region and the applicability of proposed explanations, T. C. Chamberlin, (<i>Title only</i>) -----	15, 16
The enlargement of mineral fragments as a factor in rock alter- ation, R. D. Irving, (<i>Title only</i>) -----	16

The subaerial decay of rocks and the origin of the red clay of certain formations, I. C. Russell, (<i>Title only</i>)-----	16
Recent improvements in microscopic objectives, with demonstration of the resolving power of a new 1-16th inch, Romyn Hitchcock, (<i>Title only</i>)-----	16
A phonetic alphabet, Henry Farquhar-----	17
Customs of every-day life, Garrick Mallery-----	19
When I first saw the cholera <i>bacillus</i> , R. D. Mussey, (<i>Title only</i>)-----	22
The distribution of fishes in the oceanic abysses and middle strata, G. Brown Goode and T. H. Bean, (<i>Title only</i>)-----	22
The physical geographical divisions of the southeastern portion of the United States and their corresponding topographical types, Gilbert Thompson-----	22
Temperatures at which differences between mercurial and air thermometers are greatest, Thomas Russell, (<i>with figure</i>)---	25
The gilding of thermometer bulbs, J. H. Kidder, (<i>Title only</i>)--	33
Effects of solar radiation upon thermometer bulbs having different metallic coverings, H. A. Hazen-----	33
Organic cells of unknown origin and form found in human faeces (two cases), Newton L. Bates-----	35
On museum specimens illustrating biology, J. S. Billings, G. Brown Goode, and Frederick A. Lucas-----	35
On geological museums, George P. Merrill, (<i>Title only</i>)-----	36
The Charleston earthquake, by—	
T. C. Mendenhall-----	37
W J McGee-----	37
Charles G. Rockwood-----	37
Everett Hayden, (<i>with one plate</i>)-----	38
H. M. Paul-----	41
Bowyers and fletchers, O. T. Mason-----	44
Certain new and small mountain ranges, G. K. Gilbert, (<i>Title only</i>)-----	45
Normal barometers, T. Russell-----	46
On the occurrence of copper ores in the Trias of the eastern United States, N. H. Darton, (<i>Title only</i>)-----	46
The latest volcanic eruption in northern California and its peculiar lava; J. S. Diller, (<i>Title only</i>)-----	46
Presentation of the annual address-----	47
Annual Meeting-----	47
Bulletin of the Mathematical Section-----	49
Standing Rules of the Section-----	51
Officers of the Section-----	52
List of members who receive announcements of the meetings--	52
Comparison of the Boss and Auwers' declination standards, Henry Farquhar-----	53
On the position and shape of the geoid as dependent on local masses, R. S. Woodward, (<i>Title only</i>)-----	53, 54
On the use of Somoff's theorem for the evaluation of the elliptic integral of the 3d species, C. H. Kummell, (<i>Title only</i>)--	54
Index-----	55

BULLETIN
OF THE
PHILOSOPHICAL SOCIETY OF WASHINGTON.

CONSTITUTION, RULES,
LISTS OF
OFFICERS AND MEMBERS,
AND REPORTS OF
SECRETARIES AND TREASURER.



CONSTITUTION

OF

THE PHILOSOPHICAL SOCIETY OF WASHINGTON.

ARTICLE I. The name of this Society shall be THE PHILOSOPHICAL SOCIETY OF WASHINGTON.

ARTICLE II. The officers of the Society shall be a President, four Vice-Presidents, a Treasurer, and two Secretaries.

ARTICLE III. There shall be a General Committee, consisting of the officers of the Society and nine other members.

ARTICLE IV. The officers of the Society and the other members of the General Committee shall be elected annually by ballot; they shall hold office until their successors are elected, and shall have power to fill vacancies.

ARTICLE V. It shall be the duty of the General Committee to make rules for the government of the Society, and to transact all its business.

ARTICLE VI. This constitution shall not be amended except by a three-fourths vote of those present at an annual meeting for the election of officers, and after notice of the proposed change shall have been given in writing at a stated meeting of the Society at least four weeks previously.



STANDING RULES

FOR THE GOVERNMENT OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON.

1. The Stated Meetings of the Society shall be held at 8 o'clock P. M. on every alternate Saturday; the place of meeting to be designated by the General Committee.

2. Notice of the time and place of meeting shall be sent to each member by one of the Secretaries.

When necessary, Special Meetings may be called by the President.

3. The Annual Meeting for the election of officers shall be the last stated meeting in the month of December.

The order of proceedings (which shall be announced by the Chair) shall be as follows :

First, the reading of the minutes of the last Annual Meeting.

Second, the presentation of the annual reports of the Secretaries, including the announcement of the names of members elected since the last Annual Meeting.

Third, the presentation of the annual report of the Treasurer.

Fourth, the announcement of the names of members who, having complied with section 14 of the Standing Rules, are entitled to vote on the election of officers.

Fifth, the election of President.

Sixth, the election of four Vice-Presidents.

Seventh, the election of Treasurer.

Eighth, the election of two Secretaries.

Ninth, the election of nine members of the General Committee.

Tenth, the consideration of Amendments to the Constitution of the Society, if any such shall have been proposed in accordance with Article VI of the Constitution.

Eleventh, the reading of the rough minutes of the meeting.

4. Elections of officers are to be held as follows :

In each case nominations shall be made by means of an informal ballot, the result of which shall be announced by the Secretary ; after which the first formal ballot shall be taken.

In the ballot for Vice-Presidents, Secretaries, and members of the General Committee, each voter shall write on one ballot as many names as there are officers to be elected, viz., four on the first ballot for Vice-Presidents, two on the first for Secretaries, and nine on the first for members of the General Committee ; and on each subsequent ballot as many names as there are persons yet to be elected ; and those persons who receive a majority of the votes cast shall be declared elected.

If in any case the informal ballot result in giving a majority for any one, it may be declared formal by a majority vote.

5. The Stated Meetings, with the exception of the Annual Meeting, shall be devoted to the consideration and discussion of scientific subjects.

The Stated Meeting next preceding the Annual Meeting shall be set apart for the delivery of the President's Annual Address.

6. Sections representing special branches of science may be formed by the General Committee upon the written recommendation of twenty members of the Society.

7. Persons interested in science, who are not residents of the District of Columbia, may be present at any meeting of the Society, except the Annual Meeting, upon invitation of a member.

8. On request of a member, the President or either of the Secretaries may, at his discretion, issue to any person a card of invitation to attend a specified meeting. Five cards of invitation to attend a meeting may be issued in blank to the reader of a paper at that meeting.

9. Invitations to attend during three months the meetings of the Society and participate in the discussion of papers, may, by a vote of nine members of the General Committee, be issued to persons nominated by two members.

10. Communications intended for publication under the auspices of the Society shall be submitted in writing to the General Committee for approval.

11. Any paper read before a Section may be repeated, either entire or by abstract, before a general meeting of the Society, if such repetition is recommended by the General Committee of the Society.

12. It is not permitted to report the proceedings of the Society or its Sections for publication, except by authority of the General Committee.

13. *New members may be proposed in writing by three members of the Society for election by the General Committee; but no person shall be admitted to the privileges of membership unless he signifies his acceptance thereof in writing, and pays his dues to the Treasurer, within two months after notification of his election.

14. Each member shall pay annually to the Treasurer the sum of five dollars, and no member whose dues are unpaid shall vote at the Annual Meeting for the election of officers, or be entitled to a copy of the Bulletin.

In the absence of the Treasurer, the Secretary is authorized to receive the dues of members.

The names of those two years in arrears shall be dropped from the list of members.

Notice of resignation of membership shall be given in writing to the General Committee through the President or one of the Secretaries.

15. The fiscal year shall terminate with the Annual Meeting.

16. Any member who is absent from the District of Columbia for more than twelve consecutive months may be excused from payment of dues during the period of his absence, in which case he will not be entitled to receive announcements of meetings or current numbers of the Bulletin.

17. Any member not in arrears may, by the payment of one hundred dollars at any one time, become a life member, and be relieved from all further annual dues and other assessments.

All moneys received in payment of life membership shall be invested as portions of a permanent fund, which shall be directed solely to the furtherance of such special scientific work as may be ordered by the General Committee.

STANDING RULES
OF THE
GENERAL COMMITTEE OF THE PHILOSOPHICAL
SOCIETY OF WASHINGTON.

1. The President, Vice-Presidents, and Secretaries of the Society shall hold like offices in the General Committee.

2. The President shall have power to call special meetings of the Committee, and to appoint Sub-Committees.

3. The Sub-Committees shall prepare business for the General Committee, and perform such other duties as may be entrusted to them.

4. There shall be two Standing Sub-Committees; one on Communications for the Stated Meetings of the Society, and another on Publications.

5. The General Committee shall meet at half-past seven o'clock on the evening of each Stated Meeting, and by adjournment at other times.

6. For all purposes, except for the amendment of the Standing Rules of the Committee or of the Society, and the election of members, six members of the Committee shall constitute a quorum.

7. The names of proposed new members recommended in conformity with section 13 of the Standing Rules of the Society, may be presented at any meeting of the General Committee, but shall lie over for at least four weeks before final action, and the concurrence of twelve members of the Committee shall be necessary to election.

The Secretary of the General Committee shall keep a chronological register of the elections and acceptances of members.

8. These Standing Rules, and those for the government of the Society, shall be modified only with the consent of a majority of the members of the General Committee.

RULES

FOR THE

PUBLICATION OF THE BULLETIN

OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON.

1. The President's Annual Address shall be published in full.
2. The annual reports of the Secretaries and of the Treasurer shall be published in full.
3. When directed by the General Committee, any communication may be published in full.
4. Abstracts of papers and remarks on the same will be published, when presented to the Secretary by the author in writing within two weeks of the evening of their delivery, and approved by the Committee on Publications. Brief abstracts prepared by one of the Secretaries and approved by the Committee on Publications may also be published.
5. If the author of any paper read before a Section of the Society desires its publication, either in full or by abstract, it shall be referred to a committee to be appointed as the Section may determine.
The report of this committee shall be forwarded to the Publication Committee by the Secretary of the Section, together with any action of the Section taken thereon.
6. Communications which have been published elsewhere, so as to be generally accessible, will appear in the Bulletin by title only, but with a reference to the place of publication, if made known in season to the Committee on Publications.

OFFICERS

OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON

ELECTED DECEMBER 19, 1885.

President.....J. S. BILLINGS.

Vice-Presidents ----- WILLIAM HARKNESS. GARRICK MALLERY.
C. E. DUTTON. J. E. HILGARD.*

Treasurer..... ROBERT FLETCHER.

Secretaries ----- G. K. GILBERT. MARCUS BAKER.

MEMBERS AT LARGE OF THE GENERAL COMMITTEE.

H. H. BATES.	F. W. CLARKE.
W. H. DALL.	G. B. GOODE.
J. R. EASTMAN.	HENRY FARQUHAR.
T. C. MENDENHALL.†	H. M. PAUL.
C. V. RILEY.	

STANDING COMMITTEES.

On Communications:

WILLIAM HARKNESS, *Chairman.* G. K. GILBERT. MARCUS BAKER.

On Publications:

G. K. GILBERT, *Chairman.* ROBERT FLETCHER. MARCUS BAKER.
S. F. BAIRD.‡

* Resigned membership Nov. 20, 1886.

† Resigned Oct. 9, 1886; vacancy filled by election of W. B. Taylor, Oct. 23, 1886.

‡ As Secretary of the Smithsonian Institution.

LIST OF MEMBERS

OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON.

Corrected to December 18, 1886.

Names of gentlemen here indicated as resigned will be omitted from future lists.

NAME.	ADDRESS AND RESIDENCE.	Year of admission.
ABBE, Prof. CLEVELAND	Army Signal Office. 2017 I st. N. W.	1871
ABERT, Mr. S.T. (Sylvanus Thayer)	810 19th st. N. W.	1875
ADAMS, Mr. CHARLES FREDERICK	Civil Service Commission. 316 C st. N. W.	1885
ADAMS, Mr. HENRY	1603 H st. N. W.	1881
ALDIS, Hon. A. O. (Asa Owen)	1765 Mass. ave. N. W.	1873
ANTISELL, Dr. THOMAS (<i>Founder</i>)	Patent Office. 1311 Q st. N. W.	1871
AVERY, Mr. ROBERT S. (Robert Stanton)	320 A st. S. E.	1879
BAIRD, Prof. SPENCER F. (Spencer Fullerton) (<i>Founder</i>)	Smithsonian Institution. 1445 Mass. ave. N. W.	1871
BAKER, Prof. FRANK	1315 Corcoran st. N. W.	1881
BAKER, Mr. MARCUS	Geological Survey. 1125 17th st. N. W.	1876
BANCROFT, GEORGE	1623 H st. N. W., or, in summer, Newport, R. I.	1875
BARUS, Dr. CARL	Geological Survey.	1885
BATES, Mr. HENRY H. (Henry Hobart)	Patent Office. The Portland.	1871
BATES, Dr. N. L. (Newton Lemuel) U. S. N.	Navy Department. 1233 17th st. N. W.	1866
BEAN, Dr. T. H. (Tarleton Hoffman)	National Museum. 1616 19th st. N. W.	1884
BEARDSLEE, Capt. L. A. (Lester Anthony) U. S. N. (<i>Absent</i>)	Little Falls, N. Y.	1875
BELL, Mr. A. GRAHAM (Alexander Graham)	Scott Circle ; 1500 Rhode Island ave.	1879
BELL, Dr. C. A. (Chichester Alexander) (<i>Absent</i>)	University College. London, England.	1881
BENÉT, Gen. S. V. (Stephen Vincent) U. S. A. (<i>Founder</i>)	Ordnance Office, War Dept. 1717 I st. N. W.	1871

LIST OF MEMBERS.

XVII

NAME.	ADDRESS AND RESIDENCE.	Year of admission.
BESSELS, Dr. EMIL	Glenn Dale, Md.	1875
BEYER, Dr. H. G. (Henry Gustav)	Bureau Med. & Surg., Navy Dept. 1207 Connecticut ave.	1886
BILLINGS, Dr. JOHN S. (John Shaw) U. S. A. (<i>Founder</i>)	Surg. General's Office, U. S. A. 3027 N st. N. W.	1871
BIRNEY, Gen. WILLIAM	456 Louisiana ave. 1901 Harewood ave., Le Droit Park.	1879
BIRNIE, Capt. ROGERS, Jr., U. S. A.	Office Chief of Ordnance, U. S. A. 1341 New Hampshire ave.	1876
BODFISH, Mr. S. H. (Sumner Homer) (<i>Absent</i>)	Geological Survey. 605 F st. N. W.	1883
BOWLES, Asst. Nav. Constr. FRANCIS T. (Francis Tiffany) U. S. N. (<i>Absent</i>)	Navy Department.	1884
BROWN, Prof. S. J. (Stimson Joseph) U. S. N. (<i>Absent</i>)	Naval Academy, Annapolis, Md.	1884
BROWNE, Dr. J. MILLS (John Mills) U. S. N.	Navy Department. The Portland.	1883
BRYAN, Dr. J. H. (Joseph Hammond)	1644 Connecticut ave.	1886
BURGESS, Mr. E. S. (Edward Sandford)	High School. 1120 13th st. N. W.	1888
BURNETT, Dr. SWAN M. (Swan Moses)	1734 K st. N. W.	1879
BUSEY, Dr. SAMUEL C. (Samuel Clagett)	901 16th st. N. W.	1874
CASEY, Col. THOMAS LINCOLN, U. S. A. (<i>Founder: absent</i>)	Army Building, cor. Green and Houston sts., New York city.	1871
CAZIARC, Lieut. L. V. (Louis Vasmer) U. S. A. (<i>Absent</i>)	Little Rock Barracks, Little Rock, Ark.	1882
CHAMBERLIN, Prof. T. C. (Thomas Crowder)	Geological Survey.	1883
CHATARD, Dr. THOMAS M. (Thomas Marean)	Geological Survey. Cosmos Club.	1885
CHICKERING, Prof. J. W., Jr. (John White)	Deaf Mute College, Kendall Green.	1874
CHRISTIE, Mr. ALEX. S. (Alexander Smyth)	Coast and Geodetic Survey Office. 507 6th st. N. W.	1880
CLARK, Mr. E. (Edward)	Architect's Office, Capitol. 417 4th st. N. W.	1877
CLARKE, Prof. F. W. (Frank Wigglesworth)	Geological Survey. 1425 Q st. N. W.	1874
COFFIN, Prof. J. H. C. (John Huntington Crane) U. S. N. (<i>Founder</i>)	1901 I st. N. W.	1871
COMSTOCK, Prof. J. H. (John Henry) (<i>Absent</i>)	Cornell University, Ithaca, N. Y.	1880
COUES, Prof. ELLIOTT	Smithsonian Institution. 1726 N st. N. W.	1874
CRAIG, Lieut. ROBERT, U. S. A. (<i>Absent</i>)	War Department.	1873

NAME.	ADDRESS AND RESIDENCE.	Year of admission.
CRAIG, Dr. THOMAS (<i>Absent</i>)	Johns Hopkins Univ., Baltimore, Md.	1879
CUMMINGS, Prof. G. J. (George Jotham)	Howard University.	1886
CURTICE, Mr. COOPER	Agricultural Department.	1886
CURTIS, Mr. GEO. E. (George Edward)	Army Signal Office. 1401 16th st. N. W.	1884
DALL, Mr. WM. H. (William Healey) (<i>Founder</i>)	Care Smithsonian Institution. 1119 12th st. N. W.	1871
DARTON, Mr. NELSON H. (Nelson Horatio)	Geological Survey. 1101 K st. N. W.	1886
DAVIS, Commander C. H. (Charles Henry) U. S. N.	Navy Department. 1705 Rhode Island ave.	1880
DEAN, Dr. R. C. (Richard Crain) U. S. N. (<i>Absent</i>)	Navy Department. 45 Lafayette Place, New York city.	1872
DE CAINDRY, Mr. WM. A. (William Augustin)	Commissary General's Office. 1713 H st. N. W.	1881
DE LAND, Mr. THEODORE L. (Theodore Louis)	Treasury Department. 115 7th st. N. E.	1880
DEWEY, Mr. FRED. P. (Frederic Perkins)	National Museum. Lanier Heights.	1884
DILLER, Mr. J. S. (Joseph Silas)	Geological Survey. 1804 16th st. N. W.	1884
DOOLITTLE, Mr. M. H. (Myrick Hascall)	Coast and Geodetic Survey Office. 1925 I st. N. W.	1876
DUNWOODY, Lt. H. H. C. (Henry Harrison Chase) U. S. A. (<i>Absent</i>)	War Department.	1873
DUTTON, Capt. C. E. (Clarence Edward) U. S. A.	Geological Survey. 2119 H st. N. W.	1872
EARLL, Mr. R. EDWARD (Robert Edward)	Smithsonian Institution. 1336 T st. N. W.	1884
EASTMAN, Prof. J. R. (John Robie) U. S. N.	Naval Observatory. 1905 I st. N. W.	1871
EIMBECK, Mr. WILLIAM	Coast and Geodetic Survey Office.	1884
ELDREDGE, Dr. STEWART (<i>Absent</i>)	Yokohama, Japan.	1871
ELLIOTT, Mr. E. B. (Ezekiel Brown) (<i>Founder</i>)	Gov't Actuary, Treas. Dept. 1210 G st. N. W.	1871
EMMONS, Mr. S. F. (Samuel Franklin)	Geological Survey. 1708 H st. N. W.	1883
ENDLICH, Dr. F. M. (Frederic Miller) (<i>Absent</i>)	Reading, Pa.	1873
EWING, Gen. HUGH (<i>Absent</i>)	Lancaster, Ohio.	1874
FARQUHAR, Mr. EDWARD	Patent Office Library. 1915 H st. N. W.	1876
FARQUHAR, Mr. HENRY	Coast and Geodetic Survey Office. Brooks Station, D. C.	1881
FERREL, Prof. WILLIAM	1641 Broadway, Kansas City, Mo.	1872

NAME.	ADDRESS AND RESIDENCE.	Year of admission.
FLETCHER, Dr. ROBERT	Surgeon General's Office, U. S. A. The Portland.	1873
FLINT, Mr. A. S. (Albert Stowell)	Naval Observatory. 1330 Riggs st.	1882
FLINT, Dr. J. M. (James Milton) U. S. N.	Navy Department. U. S. S. Albatross.	1881
FRISTOE, Prof. EDWARD T	Columbian University, cor. 15th and H sts. N. W.	1873
GALLAUDET, President E. M. (Ed- ward Miner)	Deaf Mute College, Kendall Green.	1875
GANNETT, Mr. HENRY	Geological Survey. 1881 Harewood ave., Le Droit Park.	1874
GILBERT, Mr. G. K. (Grove Karl)	Geological Survey. 1424 Corcoran st.	1873
GODDING, Dr. W. W. (William Whitney)	Government Hospital for the In- sane.	1879
GOOCH, Dr. F. A. (Frank Austin) (Absent)	Yale College, New Haven, Conn.	1885
GOODE, Mr. G. BROWN (George Brown)	National Museum. Summit ave., Lanier Heights.	1874
GOODFELLOW, Mr. EDWARD	Coast and Geodetic Survey Office. 1324 19th st. N. W.	1875
GORDON, Prof. J. C. (Joseph Clay- baugh)	Deaf Mute College, Kendall Green.	1886
GORE, Prof. J. H. (James How- ard)	Columbian University. 1305 Q st. N. W.	1880
GRAVES, Mr. WALTER H. (Wal- ter Hayden) (Absent)	Denver, Colorado.	1878
GREELY, Lieut. A. W. (Adolphus Washington) U. S. A.	Army Signal Office. 1914 G st. N. W.	1880
GREEN, Mr. BERNARD R. (Bern- ard Richardson)	Office of Building for State, War and Navy Depts. 1738 N st. N. W.	1879
GREEN, Commander F. M. (Francis Mathews) U. S. N. (Absent)	Navy Department.	1875
GREENE, Prof. B. F. (Benjamin Franklin) U. S. N. (Founder: absent)	West Lebanon, N. H.	1871
GREENE, FRANCIS V. (Francis Vinton) (Absent)	280 Broadway, New York city.	1875
GREGORY, Dr. JOHN M. (John Milton)	15 Grant Place.	1884
GUNNELL, FRANCIS M., M. D., U. S. N.	600 20th st. N. W.	1879
HAINS, Col. PETER C. (Peter Con- over)	Engineer's Office, Potomac Riv. Improvement, 2136 Pa. ave. 1824 Jefferson Place.	1879
HAINS, Mr. ROBERT P. (Robert Peter)	Patent Office. 1714 13th st. N. W.	1885

NAME.	ADDRESS AND RESIDENCE.	Year of admission.
HALL, Prof. ASAPH, U. S. N. (<i>Founder</i>)	Naval Observatory. 2715 N st. N. W.	1871
HALL, Mr. ASAPH, Jr., (<i>Absent</i>)	Yale College Observatory, New Haven, Conn.	1884
HALLOCK, Dr. WILLIAM	Geological Survey.	1885
HAMPSON, Mr. THOMAS	Geological Survey. 504 Maple ave., Le Droit Park.	1885
HARKNESS, Prof. WILLIAM, U. S. N. (<i>Founder</i>)	Naval Observatory. Cosmos Club.	1871
HASSLER, Dr. FERDINAND A. (Ferdinand Augustus) (<i>Absent</i>)	Santa Aña, Los Angeles Co., Cal.	1880
HAYDEN, Dr. F. V. (Ferdinand Vandever) (<i>Founder: absent</i>)	Geological Survey. 1805 Arch st., Phila., Pa.	1871
HAZEN, Prof. H. A. (Henry Allen)	P. O. Box 427. 1416 Corcoran st.	1882
HAZEN, Gen. W. B. (William Babcock) U. S. A.	Army Signal Office. 1601 K st. N. W.	1881
HEAP, Major D. P. (David Porter)	Light House Board, Treas. Dept. 1618 Rhode Island ave.	1884
HENSHAW, Mr. H. W. (Henry Wetherbee)	Bureau of Ethnology. 13 Iowa Circle.	1874
HILGARD, Mr. J. E. (Julius Erasmus) (<i>Founder: resigned</i>)		1871
HILL, Mr. G. W. (George William)	Nautical Almanac Office. 314 Indiana ave. N. W.	1879
HILL, Mr. ROBERT T. (Robert Thomas)	National Museum. 1464 Rhode Island ave.	1886
HILLEBRAND, Dr. W. F. (William Francis)	Geological Survey. 506 Maple ave., Le Droit Park.	1886
HITCHCOCK, Mr. ROMYN	National Museum. Osaka, Japan.	1884
HODGKINS, Prof. H. L. (Howard Lincoln)	Columbian University. 627 N st. N. W.	1885
HOLDEN, Prest. EDWARD SINGLETON (<i>Absent</i>)	University of California, Berkeley, Cal.	1873
HOLMES, Mr. W. H. (William Henry)	Geological Survey. 1100 O st. N. W.	1879
HOWELL, Mr. EDWIN E. (Edwin Eugene) (<i>Absent</i>)	48 Oxford st., Rochester, N. Y.	1874
IDDINGS, Mr. JOSEPH P. (Joseph Paxson)	Geological Survey. 1028 Vermont ave.	1885
IRVING, Prof. R. D. (Roland Duer)	Geological Survey.	1886
JAMES, Rev. OWEN (<i>Absent</i>)	Scranton, Pa.	1880
JENKINS, Rear Admiral THORNTON A. (Thornton Alexander) U. S. N. (<i>Founder</i>)	2115 Penna. ave. N. W.	1871
JOHNSON, Mr. A. B. (Arnold Burges)	Light House Board, Treas. Dept. 501 Maple ave., Le Droit Park.	1878

NAME.	ADDRESS AND RESIDENCE.	Year of admission.
JOHNSON, DR. JOSEPH TABER	926 17th st. N. W.	1879
JOHNSON, MR. WILLARD D. (Willard Drake) (<i>Absent</i>)	Geological Survey.	1884
JOHNSTON, DR. W. W. (William Waring)	1603 K st. N. W.	1873
KAUFFMANN, MR. S. H. (Samuel Hay)	1000 M st. N. W.	1884
KEITH, Prof. R. (Reuel)	Nautical Almanac Office. 1017 M st. N. W.	1871
KENASTON, Prof. C. A. (Carlos Albert)	Howard University.	1886
KERR, MR. MARK B. (Mark Brickell)	Geological Survey. 722 21st st. N. W.	1884
KIDDER, DR. J. H. (Jerome Henry)	Smithsonian Institution. 1816 N st. N. W.	1880
KILBOURNE, Lieut. C. E. (Charles Evans) U. S. A. (<i>Absent</i>)	War Department.	1880
KING, DR. A. F. A. (Albert Freeman Africanus)	726 13th st. N. W.	1875
KNOX, Hon. JOHN JAY (<i>Absent</i>)	Pres. Nat. Bank Republic, New York city.	1874
KUMMELL, MR. C. H. (Charles Hugo)	Coast and Geodetic Survey Office. 608 Q st. N. W.	1882
LAWRENCE, MR. WILLIAM	Bellefontaine, Ohio.	1884
LAWYER, DR. W. P. (Winfield Peter)	Mint Bureau, Treas. Dept. 1912 I st. N. W.	1881
LEE, DR. WILLIAM	2111 Penna. ave. N. W. 1821 I st. N. W.	1874
LEFAVOUR, MR. EDWARD B. (Edward Brown)	Cambridge, Mass.	1882
LINCOLN, DR. N. S. (Nathan Smith)	1514 H st. N. W.	1871
LOOMIS, MR. E. J. (Eben Jenks)	Nautical Almanac Office. 1413 Stoughton st. N. W.	1880
LULL, Capt. E. P. (Edward Phelps) U. S. N. (<i>Absent</i>)	Navy Yard, Pensacola, Fla.	1875
MCADIE, MR. A. G. (Alexander George)	Army Signal Office. "Morleigh", Anacostia, D. C.	1886
MCDONALD, Col. MARSHALL	U. S. Fish Commission. 1515 R st. N. W.	1886
MCGEE, MR. W J	Geological Survey. 920 14th st. N. W.	1883
MCGUIRE, MR. FRED. B. (Frederick Bauders)	1416 F st. N. W. 614 E st. N. W.	1879
MCMURTRIE, Prof. WILLIAM (<i>Absent</i>)	University of Illinois, Champaign, Ill.	1876
MAHER, MR. JAMES A. (James Arran)	Geological Survey. 21 E st. N. W.	1884
MALLERY, Col. GARRICK, U. S. A.	Bureau of Ethnology. 1323 N st. N. W.	1875

NAME.	ADDRESS AND RESIDENCE.	Year of admission.
MANN, Mr. B: PICKMAN (Benjamin Pickman)	Department of Agriculture. 1918 Sunderland Place, N. W.	1885
MARCOU, Mr. J. B. (John Belknap)	Geological Survey. Cosmos Club.	1884
MARTIN, Mr. ARTEMAS	Coast and Geodetic Survey Office. 55 C st. S. E.	1886
MARVIN, Prof. C. F. (Charles Frederick)	Army Signal Office. 1736 13th st. N. W.	1885
MARVIN, Mr. Jos. B. (Joseph Badger) (<i>Absent</i>)	Internal Revenue Bureau.	1878
MASON, Prof. OTIS T. (Otis Tufton)	National Museum. 1305 Q st. N. W.	1875
MATTHEWS, Dr. W. (Washington) U. S. A.	Surg. General's Office, U. S. A.	1884
MEIGS, Gen. M. C. (Montgomery Cunningham) U. S. A. (<i>Founder</i>)	1239 Vermont ave.	1871
MENDENHALL, Prof. T. C. (Thomas Corwin) (<i>Absent</i>)	Terre Haute, Ind.	1885
MERRIAM, Dr. C. HART (Clinton Hart)	Department of Agriculture. 1912 Sunderland Place, N. W.	1886
MERRILL, Mr. GEORGE P. (George Perkins)	National Museum. 1602 19th st. N. W.	1884
MITCHELL, Prof. HENRY	Coast and Geodetic Survey Office. 1331 L st. N. W.	1886
MORGAN, Dr. E. CARROLL (Ethelbert Carroll)	918 E st. N. W.	1883
MOSER, Lt. J. F. (Jefferson Franklin) U. S. N. (<i>Absent</i>)	Coast and Geodetic Survey Office.	1885
MURDOCH, Mr. JOHN	National Museum. 1441 Chapin st., Colledge Hill.	1884
NEWCOMB, Prof. SIMON, U. S. N. (<i>Founder</i>)	Navy Department. 941 M st. N. W.	1871
NICHOLS, Dr. CHARLES H. (Charles Henry) (<i>Absent</i>)	Bloomington Asylum, Boulevard and 117th st., New York, N. Y.	1872
NICHOLSON, Mr. W. L. (Walter Lamb) (<i>Founder</i>)	Topographer, P. O. Dept. 2109 G st. N. W.	1871
NORDHOFF, Mr. CHARLES	1731 K st. N. W.	1879
NORRIS, Dr. BASIL, U. S. A. (<i>Absent</i>)	Vancouver Barracks, Wash. Ter.	1884
NOTT, Judge C. C. (Charles Cooper)	Court of Claims. 826 Connecticut ave. N. W.	1885
OGDEN, Mr. HERBERT G. (Herbert Gouverneur)	Coast and Geodetic Survey Office. 1324 19th st. N. W.	1884
OSBORNE, Mr. J. W. (John Walter)	212 Delaware ave. N. E.	1878
PARKE, Gen. JOHN G. (John Grubb) U. S. A. (<i>Founder</i>)	Engineer Bureau, War Dept. 16 Lafayette Square.	1871
PARKER, Dr. PETER (<i>Founder</i>)	2 Lafayette Square.	1871
PARRY, Dr. CHARLES C. (Charles Christopher) (<i>Absent</i>)	Davenport, Iowa.	1871

NAME.	ADDRESS AND RESIDENCE.	Year of admission.
PAUL, Mr. H. M. (Henry Martyn)	Naval Observatory. 109 1st st. N. E.	1877
PEALE, Dr. A. C. (Albert Charles)	Geological Survey. 1010 Mass. ave. N. W.	1874
POE, Gen. O. M. (Orlando Metcalfe) U. S. A. (<i>Absent</i>)	34 West Congress st., Detroit, Mich.	1873
POINDEXTER, Mr. W. M. (William Mundy)	1505 Pennsylvania ave. 1227 15th st. N. W.	1884
POPE, Dr. B. F. (Benjamin Franklin) U. S. A.	Surg. General's Office, U. S. A.	1882
POWELL, Major J. W. (John Wesley)	Geological Survey. 910 M st. N. W.	1874
PRENTISS, Dr. D. W. (Daniel Webster)	1101 14th st. N. W.	1880
PRITCHETT, Prof. H. S. (Henry Smith) (<i>Absent</i>)	Director of Observatory, Wash. University, St. Louis, Mo.	1879
RATHBUN, Mr. RICHARD	Smithsonian Institution. 1622 Mass. ave.	1882
RAY, Lieut. P. H. (Patrick Henry) U. S. A.	Fort Gaston, Cal.	1884
RENSHAWE, Mr. JNO. H. (John Henry)	Geological Survey. 1512 Kingman Place.	1883
RICKSECKER, Mr. EUGENE	Geological Survey. 1323 Q st. N. W.	1884
RILEY, Dr. C. V. (Charles Valentine)	Agricultural Department, or National Museum. 1700 13th st. N. W.	1878
RITTER, Mr. W. F. McK. (William Francis McKnight)	Nautical Almanac Office. 16 Grant Place.	1879
ROBINSON, Mr. THOMAS	Howard University. 6th st. N. W., cor. Lincoln.	1884
ROGERS, Mr. JOSEPH A. (Joseph Addison) (<i>Absent</i>)	Naval Observatory.	1872
RUSSELL, Mr. ISRAEL C. (Israel Cook)	Geological Survey.	1882
RUSSELL, Mr. THOMAS	Army Signal Office. 1447 Corcoran st. N. W.	1883
SALMON, Dr. D. E. (Daniel Elmer)	Agricultural Department. 12 Iowa Circle.	1883
SAMPSON, Commander W. T. (William Thomas) U. S. N. (<i>Absent</i>)	Naval Academy, Annapolis, Md.	1883
SAVILLE, Mr. J. H. (James Hamilton)	1419 F st. N. W. 1315 M st. N. W.	1871
SCHOTT, Mr. CHARLES A. (Charles Anthony) (<i>Founder</i>)	Coast and Geodetic Survey Office. 212 1st st. S. E.	1871
SHELLABARGER, Hon. SAMUEL	Room 31 Kellogg Building. 812 17th st. N. W.	1875
SHERMAN, Hon. JOHN	U. S. Senate. 1319 K st. N. W.	1874
SHUFELDT, Dr. R. W. (Robert Wilson) U. S. A. (<i>Absent</i>)	Surg. Gen'l's Office, U. S. A., or Box 144 Smithsonian Inst.	1881

NAME.	ADDRESS AND RESIDENCE.	Year of admission.
SIGSBEE, Commander C. D. (Charles Dwight) U. S. N. (<i>Absent</i>)	Navy Department.	1879
SKINNER, Dr. J. O. (John Oscar) U. S. A.	Surg. General's Office, U. S. A. 1529 O st. N. W.	1883
SMILEY, Mr. CHAS. W. (Charles Wesley)	U. S. Fish Commission. 943 Mass. ave.	1882
SMITH, Chf. Eng. DAVID, U. S. N.	Navy Department.	1876
SMITH, Mr. EDWIN	Coast and Geodetic Survey Office. 2024 Hillyer Place.	1880
SNELL, Mr. MERWIN M. (Merwin Marie)	National Museum. 715 Mt. Vernon Place.	1886
SPOFFORD, Mr. A. R. (Ainsworth Rand)	Library of Congress. 1621 Mass. ave. N. W.	1872
STEARNS, Mr. ROBERT E. C. (Rob- ert Edwards Carter)	Smithsonian Institution. 1635 13th st. N. W.	1884
STONE, Prof. ORMOND (<i>Absent</i>)	Leander McCormick Observa- tory, University of Virginia, Va.	1874
TAYLOR, Mr. F. W. (Frederick William) (<i>Absent</i>)	Care Smithsonian Institution.	1881
TAYLOR, Mr. WILLIAM B. (William Bower) (<i>Founder</i>)	Smithsonian Institution. 306 C st. N. W.	1871
THOMPSON, Prof. A. H. (Almon Harris)	Geological Survey.	1875
THOMPSON, Mr. GILBERT	Geological Survey. 1448 Q st. N. W.	1884
TODD, Prof. DAVID P. (David Peck) (<i>Absent</i>)	Amherst College Observatory, Amherst, Mass.	1878
TONER, Dr. J. M., (Joseph Merc- dith)	615 Louisiana ave.	1873
TRENHOLM, Hon. WILLIAM L. (William Lee.)	Controller of the Currency. 1812 N st. N. W.	1886
TRUE, Mr. FREDERICK W. (Fred- erick William)	National Museum. 1335 N st. N. W.	1882
UPTON, Mr. WM. W. (William Wirt)	1416 F st. N. W. 1746 M st. N. W.	1882
UPTON, Prof. WINSLOW (<i>Absent</i>)	Brown University, Providence, R. I.	1880
WALCOTT, Mr. C. D. (Charles Doolittle)	Geological Survey; National Museum.	1883
WALDO, Prof. FRANK (<i>Absent</i>)	Army Signal Office, Fort Myer, Va.	1881
WALKER, Mr. FRANCIS A. (Francis Amasa) (<i>Absent</i>)	Massachusetts Institute of Tech- nology, Boston, Mass.	1872
WALLING, Mr. HENRY F. (Henry Francis) (<i>Absent</i>)	U. S. Geological Survey, Cam- bridge, Mass.	1883
WARD, Mr. LESTER F. (Lester Frank)	Geological Survey. 1464 Rhode Island ave.	1876

NAME.	ADDRESS AND RESIDENCE.	Year of admission.
WEBSTER, Mr. ALBERT L. (Albert Lowry) (<i>Absent</i>)	107 Drexel Building, Broad st., New York city; West New Brighton, Staten Island, N. Y.	1882
WEED, Mr. WALTER H. (Walter Harvey)	Geological Survey. "The Grammercy", Vermont ave.	1885
WELLING, Mr. JAMES C. (James Clarke)	1302 Connecticut ave.	1872
WHEELER, Capt. GEO. M. (George Montague) U. S. E.	Lock Box 93. 930 16th st. N. W.	1873
WHITE, Dr. C. A. (Charles Abiathar)	Geological Survey. 312 Maple ave., Le Droit Park	1876
WHITE, Dr. C. H. (Charles Henry) U. S. N.	Museum of Hygiene, 1744 G st. N. W.	1884
WILLIS, Mr. BAILEY	Geological Survey. 1823 H st. N. W.	1885
WILSON, H. M. (Herbert Michael)	Geological Survey.	1885
WILSON, Mr. J. ORMOND (James Ormond)	1439 Massachusetts ave. N. W.	1873
WINLOCK, Mr. WILLIAM C. (William Crawford)	Naval Observatory. 718 21st st. N. W.	1880
WOOD, Mr. JOSEPH (<i>Absent</i>)	Supt. Motive Power, Penn. Co., Fort Wayne, Ind.	1875
WOOD, Lt. W. M. (William Maxwell) U. S. N. (<i>Absent</i>)	Navy Department.	1871
WOODWARD, Mr. R. S. (Robert Simpson)	Geological Survey. 1804 Columbia Road.	1883
WORTMAN, Dr. J. L. (Jacob Lawson)	Army Medical Museum. 1711 13th st. N. W.	1885
WRIGHT, Mr. GEO. M. (George Mitchell) (<i>Absent</i>)	Akron, Ohio.	1885
YARROW, Dr. H. C. (Harry Crécy)	Surgeon General's Office, U. S. A. 814 17th st. N. W.	1874
YEATES, Mr. W. S. (William Smith)	Smithsonian Institution. 1403 6th st. N. W.	1884
ZIWET, Mr. ALEXANDER	Coast and Geodetic Survey Office. 140 C st. S. E.	1885
ZUMBROCK, Dr. A. (Anton)		1875

LIST OF DECEASED MEMBERS.

<i>Name.</i>	<i>Admitted.</i>
Benjamin Alvord	1872
Orville Elias Babcock	1871
Theodorus Bailey	1878
Joseph K. Barnes	Founder
Henry Wayne Blair	1884
Horace Capron	Founder
Salmon Portland Chase	Founder
Frederick Collins	1879
Benjamin Faneuil Craig	Founder
Charles Henry Crane	Founder
Josiah Curtis	1874
Richard Dominicus Cutts	1871
Charles Henry Davis	1874
Frederick William Dorr	1874
Alexander B. Dyer	Founder
Amos Beebe Eaton	Founder
Charles Ewing	1874
Elisha Foote	Founder
John Gray Foster	1873
Leonard Dunnell Gale	1874
Isaiah Hanscom	1873
Joseph Henry	Founder
Franklin Benjamin Hough	1879
Andrew Atkinson Humphreys	Founder
Ferdinand Kampf	1875
Washington Caruthers Kerr	1883
Jonathan Homer Lane	Founder
Oscar A. Mack	1872
Archibald Robertson Marvine	1874
Fielding Bradford Meek	Founder
James William Milner	1874
Albert J. Myer	Founder
George Alexander Otis	Founder
Carlile Pollock Patterson	1871
Titian Ramsay Peale	Founder
Benjamin Peirce	Founder
John Campbell Riley	1877
John Rodgers	1872
Benjamin Franklin Sands	Founder
George Christian Shaeffer	Founder
Henry Robinson Searle	1877
William J. Twining	1878
Joseph Janvier Woodward	Founder
John Maynard Woodworth	1874
Mordecai Yarnall	1871

SUMMARY.

Active members	183
Absent members	54
Total	237
Deceased members	45

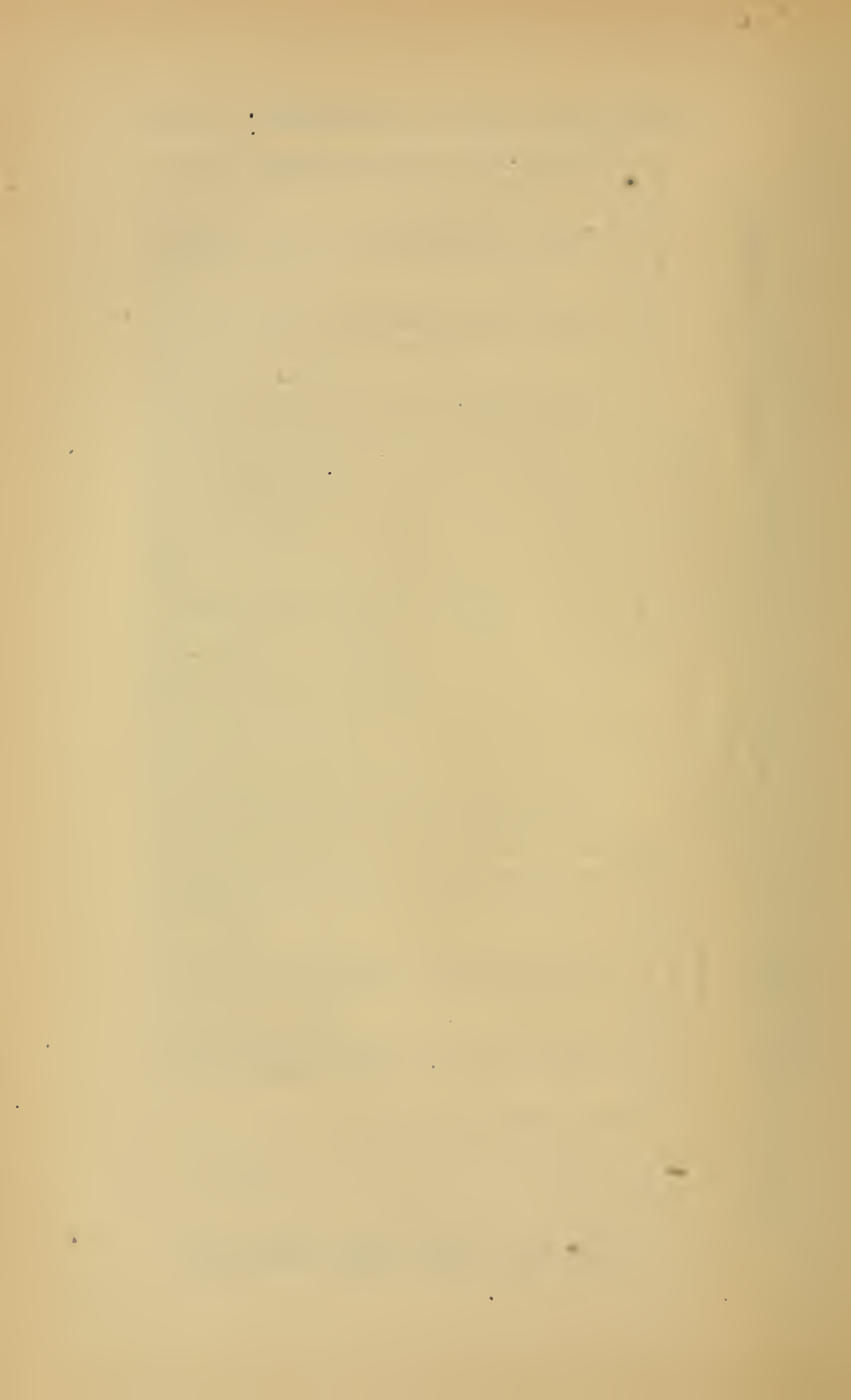
CALENDAR FOR THE USE OF THE PHILOSOPHICAL SOCIETY,

Showing the alternate SATURDAYS for holding Meetings during the several "Seasons" from 1834-85 to 1907-08, inclusive.

PREPARED BY MR. E. B. ELLIOTT.

Submitted to the General Committee June 7, 1884, and ordered published.

Years.	October.	November.	December.	Years.	January.	February.	March.	April.	May.	June.
1884.....	11, 25	8, 22	6, 20	1885.....	3, 17, 31	14, 28	14, 23	11, 25	9, 23	6, 20
1885.....	10, 24	7, 21	5, 19	1886.....	2, 16, 30	13, 27	13, 27	10, 24	8, 22	7, 21
1886.....	9, 23	6, 20	4, 18	1887.....	15, 29	12, 26	12, 26	9, 23	7, 21	5, 19
1887.....	15, 29	12, 26	10, 24	1888.....	7, 21	4, 18	3, 17, 31	14, 28	12, 26	9, 23
1888.....	13, 27	10, 24	8, 22	1889.....	5, 19	2, 16	2, 16, 30	13, 27	11, 25	8, 22
1889.....	12, 26	9, 23	7, 21	1890.....	4, 18	1, 15	1, 15, 29	12, 26	10, 24	7, 21
1890.....	11, 25	8, 22	6, 20	1891.....	3, 17, 31	14, 28	14, 28	11, 25	9, 23	6, 20
1891.....	10, 24	7, 21	5, 19	1892.....	2, 16, 30	13, 27	12, 26	9, 23	7, 21	4, 18
1892.....	15, 29	12, 26	10, 24	1893.....	7, 21	4, 18	4, 18	1, 15, 29	13, 27	10, 24
1893.....	14, 28	11, 25	9, 23	1894.....	6, 20	3, 17	3, 17, 31	14, 28	12, 26	9, 23
1894.....	13, 27	10, 24	8, 22	1895.....	5, 19	2, 16	2, 16, 30	13, 27	11, 25	8, 22
1895.....	12, 26	9, 23	7, 21	1896.....	4, 18	1, 15, 29	1, 15, 29	11, 25	9, 23	6, 20
1896.....	10, 24	7, 21	5, 19	1897.....	2, 16, 30	13, 27	13, 27	10, 24	8, 22	5, 19
1897.....	9, 23	6, 20	4, 18	1898.....	15, 29	12, 26	12, 26	9, 23	7, 21	4, 18
1898.....	15, 29	12, 26	10, 24	1899.....	7, 21	4, 18	4, 18	1, 15, 29	13, 27	10, 24
1899.....	14, 28	11, 25	9, 23	1900.....	6, 20	3, 17	3, 17, 31	1, 14, 28	12, 26	9, 23
1900.....	13, 27	10, 24	8, 22	1901.....	5, 19	2, 16	2, 16, 30	13, 27	11, 25	8, 22
1901.....	12, 26	9, 23	7, 21	1902.....	4, 18	1, 15	1, 15, 29	12, 26	10, 24	7, 21
1902.....	11, 25	8, 22	6, 20	1903.....	3, 17, 31	14, 28	14, 28	11, 25	9, 23	6, 20
1903.....	10, 24	7, 21	5, 19	1904.....	2, 16, 30	13, 27	12, 26	9, 23	7, 21	4, 18
1904.....	15, 29	12, 26	10, 24	1905.....	7, 21	4, 18	4, 18	1, 15, 29	13, 27	10, 24
1905.....	14, 28	11, 25	9, 23	1906.....	6, 20	3, 17	3, 17, 31	14, 28	12, 26	9, 23
1906.....	13, 27	10, 24	8, 22	1907.....	5, 19	2, 16	2, 16, 30	13, 27	11, 25	8, 22
1907.....	12, 26	9, 23	7, 21	1908.....	4, 18	1, 15, 29	1, 15, 29	11, 25	9, 23	6, 20



ANNUAL REPORT OF THE SECRETARIES.

WASHINGTON, D. C., *December 18, 1886.**To the Philosophical Society of Washington :*

We have the honor to present the following statistical data for 1886 :

The last Annual Report brought the record of membership down to January 16, 1886. The number of active members was then 179

This number has been increased by the addition of 18 new members, by the return of 1 absent member, and by the reinstatement of 2 members previously dropped. It has been diminished by the departure of 9 members, by the resignation of 1, and by the dropping of 7 for non-payment of dues. There has been no death. The net increase of active members has thus been 4

And the active membership is now 183

The roll of new members is :

N. L. BATES.	J. C. GORDON.	MARSHALL McDONALD.
H. G. BEYER.	R. T. HILL.	ARTEMAS MARTIN.
J. H. BRYAN.	W. F. HILLEBRAND.	C. H. MERRIAM.
G. J. CUMMINGS.	R. D. IRVING.	HENRY MITCHELL.
COOPER CURTICE.	C. A. KENASTON.	M. M. SNELL.
N. H. DARTON.	A. G. McADIE.	W. L. TRENHOLM.

There have been 14 meetings for the presentation and discussion of papers (not including the public meeting of December 4); the average attendance has been 47. There have been 2 meetings of the Mathematical Section; average attendance 16.

In the general meetings 39 communications have been presented; in the mathematical 3. Altogether 42 communications have been made by 29 members and candidates for membership and by 2 guests. The number of members who have participated in the discussions is 38. The total number who have contributed to the scientific proceedings is 49, or 27 per cent. of the present active membership.

The General Committee has held 15 meetings; average attendance 12, the smallest attendance at any meeting being 7 and the largest 15.

G. K. GILBERT,
MARCUS BAKER,
Secretaries.

THE REPORT OF THE TREASURER.

Mr. President and Gentlemen:

The report which I shall presently have the honor to submit to you shows the total receipts and disbursements for the fiscal year ending with this meeting.

The actual income belonging to the year 1886 was \$878.00, and the expenditures for the same period were \$451.50, leaving a net surplus of \$426.50.

The unpaid dues of former years which have been collected this year, amount to \$175.00.

By a resolution of the General Committee, passed May 22, 1886, the Treasurer was authorized to invest six hundred dollars of the surplus funds of the Society in six second-mortgage bonds of the Cosmos Club of this city. The present high premium on Government bonds reduces the annual interest upon them to about $2\frac{3}{4}$ per cent. The bonds purchased were obtained at par, and pay an interest of five per cent. per annum, the security being an extremely valuable piece of city property.

The assets of the Society consist of:

2 Government bonds, \$1,000 and \$500, at 4 per cent.,	\$1,500 00
1 " bond, 1,000, " $4\frac{1}{2}$ "	1,000 00
6 Cosmos Club bonds, " 5 "	600 00
Cash with Riggs & Co.	485 52
Unpaid dues	265 00
	<hr/>
Total	\$3,850 52

Of the "unpaid dues" it is probable that a part cannot be collected; on the other hand, the market value of the bonds is in excess of their face value.

Volume VIII of the Bulletin was duly sent in February to all members entitled to receive it, and to the societies and scientific journals with which it is the custom of the Philosophical Society to exchange its publications.



BULLETIN

OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON.

ANNUAL ADDRESS OF THE PRESIDENT.



ANNUAL ADDRESS OF THE PRESIDENT,

JOHN S. BILLINGS.

Delivered December 4, 1886.

SCIENTIFIC MEN AND THEIR DUTIES.

Mr. Chairman and Fellow-Members of the Philosophical Society:

The honor of the presidency of such a society as this—carrying with it, as it does, the duty of giving at the close of the term of office an address on some subject of general interest, has been aptly compared to the little book mentioned in the Revelations of St. John—the little book which was “sweet in the mouth but bitter in the belly.” I can only thank you for the honor, and ask your indulgence as to the somewhat discursive remarks which I am about to inflict upon you.

There is a Spanish proverb to the effect that no man can at the same time ring the bell and walk in the procession. For a few moments to-night I am to ring the bell, and being thus out of the procession I can glance for a moment at that part of it which is nearest. At first sight it does not appear to be a very homogeneous or well-ordered parade, for the individual members seem to be scattering in every direction, and even sometimes to be pulling in opposite ways; yet there is, after all, a definite movement of the whole mass in the direction of what we call progress. It is not this general movement that I shall speak of, but rather of the tendencies of individuals or of certain classes; some of the molecular movements, so to speak, which are not only curious and interesting of themselves, but which have an important bearing upon the mass, and some comprehension of which is necessary to a right understanding of the present condition and future prospects of science in this country.

The part of the procession of which I speak is made up of that body or class of men who are known to the public generally as “scientists,” “scientific men,” or “men of science.” As commonly used, all these terms have much the same significance; but there are, nevertheless, shades of distinction between them, and in fact we need several other

terms for purposes of classification of the rather heterogeneous mass to which they are applied. The word "scientist" is a coinage of the newspaper reporter, and, as ordinarily used, is very comprehensive. Webster defines a scientist as being "one learned in science, a savant"—that is, a wise man—and the word is often used in this sense. But the suggestion which the word conveys to my mind is rather that of one whom the public suppose to be a wise man, whether he is so or not, of one who claims to be scientific. I shall, therefore, use the term "scientist" in the broadest sense, as including scientific men, whether they claim to be such or not, and those who claim to be scientific men whether they are so or not.

By a scientific man I mean a man who uses scientific method in the work to which he specially devotes himself; who possesses scientific knowledge,—not in all departments, but in certain special fields. By scientific knowledge we mean knowledge which is definite and which can be accurately expressed. It is true that this can rarely be done completely, so that each proposition shall precisely indicate its own conditions, but this is the ideal at which we aim. There is no man now living who can properly be termed a complete savant, or scientist, in Webster's sense of the word. There are a few men who are not only thoroughly scientific in their own special departments, but are also men possessed of much knowledge upon other subjects and who habitually think scientifically upon most matters to which they give consideration; but these men are the first to admit the incompleteness and superficiality of the knowledge of many subjects which they possess, and to embrace the opportunity which such a society as this affords of meeting with students of other branches and of making that specially advantageous exchange in which each gives and receives, yet retains all that he had at first.

Almost all men suppose that they think scientifically upon all subjects; but, as a matter of fact, the number of persons who are so free from personal equation due to heredity, to early associations, to emotions of various kinds, or to temporary disorder of the digestive or nervous machinery that their mental vision is at all times achromatic and not astigmatic, is very small indeed.

Every educated, healthy man possesses some scientific knowledge, and it is not possible to fix any single test or characteristic which will distinguish the scientific from the unscientific man. There are scientific tailors, bankers, and politicians, as well as physicists,

chemists, and biologists. Kant's rule, that in each special branch of knowledge the amount of science, properly so called, is equal to the amount of mathematics it contains, corresponds to the definition of pure science as including mathematics and logic, and nothing else. It also corresponds to the distinction which most persons, consciously or unconsciously, make between the so-called physical, and the natural or biological sciences. Most of us, I presume, have for the higher mathematics, and for the astronomers and physicists who use them, that profound respect which pertains to comparative ignorance, and to a belief that capacity for the higher branches of abstract analysis is a much rarer mental quality than are those required for the average work of the naturalist. I do not, however, propose to discuss the hierarchy of the sciences; and the term science is now so generally used in the sense of knowledge, more or less accurate, of any subject, more especially in the relations of causes and effects, that we must use the word in this sense, and leave to the future the task of devising terms which will distinguish the sciences, properly so called, from those branches of study and occupation of which the most that can be said is that they have a scientific side. It is a sad thing that words should thus become polarized and spoiled, but there seems to be no way of preventing it.

In a general way we may say that a scientific man exercises the intellectual more than the emotional faculties, and is governed by his reason rather than by his feelings. He should be a man of both general and special culture, who has a little accurate information on many subjects and much accurate information on some one or two subjects, and who, moreover, is aware of his own ignorance and is not ashamed to confess it.

We must admit that many persons who are known as scientists do not correspond to this definition. Have you never heard, and perhaps assented to, some such statements as these: "Smith is a scientist, but he doesn't seem to have good, common sense," or "he is a scientific crank?"

The unscientific mind has been defined as one which "is willing to accept and make statements of which it has no clear conceptions to begin with, and of whose truth it is not assured. It is the state of mind where opinions are given and accepted without ever being subjected to rigid tests." Accepting this definition, and also the implied definition of a scientific mind as being the reverse of this, let us for a moment depart from the beaten track which presi-

dential addresses usually follow, and instead of proceeding at once to eulogize the scientific mind and to recapitulate the wonderful results it has produced, let us consider the unscientific mind a little, not in a spirit of lofty condescension and ill-disguised contempt, but sympathetically, and from the best side that we can find. As this is the kind of mind which most of us share with our neighbors, to a greater or less degree, it may be as well not to take too gloomy a view of it. In the first place, the men with unscientific minds form the immense majority of the human race.

Our associations, habits, customs, laws, occupations, and pleasures are, in the main, suited to these unscientific minds; whose enjoyment of social intercourse, of the every-day occurrences of life, of fiction, of art, poetry, and the drama is, perhaps, none the less because they give and accept opinions without subjecting them to rigid tests. It is because there are a goodly number of men who do this that the sermons of clergymen, the advice of lawyers, and the prescriptions of physicians have a market value. This unscientific public has its uses. We can at least claim that we furnish the materials for the truly scientific mind to work with and upon; it is out of this undifferentiated mass that the scientific mind supposes itself to be developed by specialization, and from it that it obtains the means of its own existence. The man with the unscientific mind, who amuses himself with business enterprises, and who does not care in the least about ohms or pangenesis, may, nevertheless, be a man who does as much good in the world, is as valuable a citizen, and as pleasant a companion as some of the men of scientific minds with whom we are acquainted.

And in this connection I venture to express my sympathy for two classes of men who have in all ages been generally condemned and scorned by others, namely, rich men and those who want to be rich.

I do not know that they need the sympathy, for our wealthy citizens appear to support with much equanimity the disapprobation with which they are visited by lecturers and writers—a condemnation which seems in all ages to have been bestowed on those who have by those who have not.

So far as those who actually are rich are concerned, we may, I suppose, admit that a few of them—those who furnish the money to endow universities and professorships, to build laboratories, or to furnish in other ways the means of support to scientific men—are not wholly bad. Then, also, it is not always a man's own fault that

he is rich ; even a scientist may accidentally and against his will become rich.

As to those who are not rich, but who wish to be rich, whose chief desire and object is to make money, either to avoid the necessity for further labor, or to secure their wives and children from want, or for the sake of power and desire to rule, I presume it is unsafe to try to offer any apologies for their existence. But when it is claimed for any class of men, scientists or others, that they do not want these things it is well to remember the remarks made by old Sandy Mackay after he had heard a sermon on universal brotherhood : "And so the deevil's dead. Puir auld Nickie ; and him so little appreciated, too. Every gowk laying his sins on auld Nick's back. But I'd no bury him until he began to smell a wee strong like. It's a greswome thing is premature interment."

I have tried to indicate briefly the sense in which the terms "scientist" and "scientific man" are to be used and understood, and you see it is not an easy matter. The difficulty is less as regards the term "man of science." By this expression we mean a man who belongs to science peculiarly and especially, whose chief object in life is scientific investigation, whose thoughts and hopes and desires are mainly concentrated upon his search for new knowledge, whose thirst for fresh and accurate information is constant and insatiable. These are the men who have most advanced science, and whom we delight to honor, more especially in these later days, by glowing eulogiums of their zeal, energy, and disinterestedness.

The man of science, as defined by his eulogists, is the *beau idéal* of a philosopher, a man whose life is dedicated to the advancement of knowledge for its own sake, and not for the sake of money or fame, or of professional position or advancement. He undertakes scientific investigations exclusively or mainly because he loves the work itself, and not with any reference to the probable utility of the results. Such men delight in mental effort, or in the observation of natural phenomena, or in experimental work, or in historical research, in giving play to their imagination, in framing hypotheses and then in endeavoring to verify or disprove them, but always the main incentive is their own personal satisfaction (with which may be mingled some desire for personal fame), and not the pleasure or the good of others. Carried to an extreme, the eulogy of such men and their work is expressed in the toast of the Mathematical Society of England : "Pure mathematics ; may it never be of use to any

man!" Now, it is one thing to seek one's own pleasure, and quite another thing to pride one's self upon doing so. • The men who do their scientific work for the love of it do some of the best work, and, as a rule, do not pride themselves on it, or feel or express contempt for those who seek their pleasure and amusement in other directions. It is only from a certain class of eulogists of pure science, so called, that we get such specimens of scientific "dudeism" as the toast just quoted, opposed to which may be cited the Arab saying that "A wise man without works is like a cloud without water."

There are other men who devote themselves to scientific work, but who prefer to seek information that may be useful; who try to advance our knowledge of Nature's laws in order that man may know how to adapt himself and his surroundings to those laws, and thus be healthier and happier. They make investigations, like the men of pure science—investigations in which they may or may not take pleasure, but which they make, even if tedious and disagreeable, for the sake of solving some problem of practical importance. These are the men who receive from the public the most honor, for it is seen that their work benefits others. After all, this is not peculiar to the votaries of science. In all countries and all times, and among all sorts and conditions of men, it has always been agreed that the best life, that which most deserves praise, is that which is devoted to the helping others, which is unselfish, not stained by envy or jealousy, and which has as its main pleasure and spring of action the desire of making other lives more pleasant, of bringing light into the dark places, of helping humanity.

But, on the other hand, the man who makes a profession of doing this, and who makes a living by so doing, the professional philanthropist, whether he be scientist or emotionalist, is by no means to be judged by his own assertions. Some wise German long ago remarked that "*Esel singen schlecht, weil sie zu hoch anstimmen*,"—that is, "asses sing badly because they pitch their voices too high," and it is a criticism which it is well to bear in mind.

In one of the sermons of Kin O* the preacher tells the story of a powerful clam who laughed at the fears of other fish, saying that when he shut himself up he felt no anxiety; but on trying this method on one occasion when he again opened his shell he found himself in a fishmonger's shop. And to rely on one's own talents,

* Cornhill Magazine, August, 1869, p. 196.

on the services one may have rendered, on cleverness, judgments strength, or official position, and to feel secure in these, is to court the fate of the clam.

There are not very many men of science, and there are no satisfactory means of increasing the number; it is just as useless to exhort men to love science, or to sneer at them because they do not, as it is to advise them to be six feet three inches high or to condemn a man because his hair is not red.

While the ideal man of science must have a "clear, cold, keen intellect, as inevitable and as merciless in its conclusions as a logic engine," it would seem that, in the opinion of some, his greatness and superiority consists not so much in the amount of knowledge he possesses, or in what he does with it, as in the intensity and purity of his desire for knowledge.

This so-called thirst for knowledge must be closely analogous to an instinctive desire for exercise of an organ or faculty, such as that which leads a rat to gnaw, or a man of fine physique to delight in exercise. Such instincts should not be neglected. If the rat does not gnaw, his teeth will become inconvenient or injurious to himself, but it is not clear that he deserves any special eulogium merely because he gnaws.

It will be observed that the definition of a scientific man or man of science, says nothing about his manners or morals. We may infer that a man devoted to science would have neither time nor inclination for dissipation or vice; that he would be virtuous either because of being passionless or because of his clear foresight of the consequences of yielding to temptation.

My own experience, however, would indicate that either this inference is not correct or that some supposed scientific men have been wrongly classified as such. How far the possession of a scientific mind and of scientific knowledge compensates, or atones for, ill-breeding or immorality, for surliness, vanity, and petty jealousy, for neglect of wife or children, for uncleanness, physical and mental, is a question which can only be answered in each individual case; but the mere fact that a man desires knowledge for its own sake appears to me to have little to do with such questions. I would prefer to know whether the man's knowledge and work is of any use to his fellow-men, whether he is the cause of some happiness in others which would not exist without him. And it may be noted that while utility is of small account in the eyes of some eulogist,

of the man of science they almost invariably base their claims for his honor and support upon his usefulness.

The precise limit beyond which a scientist should not make money has not yet been precisely determined, but in this vicinity there are some reasons for thinking that the maximum limit is about \$5,000 per annum. If there are any members of the Philosophical Society of Washington who are making more than this, or who, as the result of careful and scientific introspection, discover in themselves the dawning of a desire to make more than this, they may console themselves with the reflection that the precise ethics and etiquette which should govern their action under such painful circumstances have not yet been formulated. The more they demonstrate their indifference to mere pecuniary considerations the more creditable it is to them; so much all are agreed upon; but this is nothing new, nor is it specially applicable to scientists. Yet while each may and must settle such questions as regards himself for himself, let him be very cautious and chary about trying to settle them for other people. Denunciations of other men engaged in scientific pursuits on the ground that their motives are not the proper ones are often based on insufficient or inaccurate knowledge, and seldom, I think, do good.

This is a country and an age of hurry, and there seems to be a desire to rush scientific work as well as other things. One might suppose, from some of the literature on the subject, that the great object is to make discoveries as fast as possible; to get all the mathematical problems worked out; all the chemical combinations made; all the insects and plants properly labeled; all the bones and muscles of every animal figured and described. From the point of view of the man of science there does not seem to be occasion for such haste. Suppose that every living thing were known, figured, and described. Would the naturalist be any happier? Those who wish to make use of the results of scientific investigation of course desire to hasten the work, and when they furnish the means we cannot object to their urgency. Moreover, there is certainly no occasion to fear that our stock of that peculiar form of bliss known as ignorance will be soon materially diminished.

From my individual point of view, one of the prominent features in the scientific procession is that part of it which is connected with Government work. Our Society brings together a large number of scientific men connected with the various Departments; some of

them original investigators; most of them men whose chief, though not only, pleasure is study. A few of them have important administrative duties, and are brought into close relations with the heads of Departments and with Congress. Upon men in such positions a double demand is made, and they are subject to criticism from two very different standpoints. On the one hand are the scientists, calling for investigations which shall increase knowledge without special reference to utility, and sometimes asking that employment be given to a particular scientist on the ground that the work to which he wishes to devote himself is of no known use, and therefore will not support him. On the other hand is the demand from the business men's point of view—that they shall show practical results; that in demands for appropriations from the public funds they shall demonstrate that the use to be made of such appropriations is for the public good, and that their accounts shall show that the money has been properly expended—"properly," not merely in the sense of usefully, but also in the legal sense—in the sense which was meant by Congress in granting the funds. Nay, more, they must consider not only the intentions of Congress but the opinions of the accounting officers of the Treasury, the comptroller and auditor, and their clerks, and not rely solely on their own interpretation of the statutes, if they would work to the best advantage, and not have life made a perpetual burden and vexation of spirit.

There is a tendency on the part of business men and lawyers to the belief that scientific men are not good organizers or administrators, and should be kept in leading strings; that it is unwise to trust them with the expenditure of, or the accounting for, money, and that the precise direction in which they are to investigate should be pointed out to them. In other words, that they should be made problem-solving machines as far as possible.

When we reflect on the number of persons who, like Mark Twain's cat, feel that they are "nearly lightning on superintending;" on the desire for power and authority, which is almost universal, the tendency to this opinion is not to be wondered at. Moreover, as regards the man of science, there is some reason for it in the very terms by which he is defined, the characteristics for which he is chiefly eulogized.

The typical man of science is, in fact, in many cases an abnormality, just as a great poet, a great painter, or a great musician is

apt to be, and this not only in an unusual development of one part of the brain, but in an inferior development in others. True, there are exceptions to this rule—great and illustrious exceptions; but I think we must admit that the man of science often lacks tact, and is indifferent to and careless about matters which do not concern his special work, and especially about matters of accounts and pecuniary details. If such a man is at the head of a bureau, whose work requires many subordinates and the disbursement of large sums of money, he may consider the business management of his office as a nuisance, and delegate as much of it as possible to some subordinate official, who, after a time, becomes the real head and director of the bureau. Evil results have, however, been very rare, and the recognition of the possibility of their occurrence is by no means an admission that they are a necessity, and still less of the proposition that administrative officers should not be scientific men.

I feel very sure that there are always available scientific men, thoroughly well informed in their several departments, who are also thoroughly good business men, and are as well qualified for administrative work as any. When such men are really wanted they can always be found, and, as a matter of fact, a goodly number of them have been found, and are now in the Government service.

The head of a bureau has great responsibilities; and while his position is, in many respects, a desirable one, it would not be eagerly sought for by most scientific men if its duties were fully understood.

In the first place the bureau chief must give up a great part of his time to routine hack work. During his business, or office, hours he can do little else than this routine work, partly because of its amount, and partly because of the frequent interruptions to which he is subjected. His visitors are of all kinds and come from all sorts of motives—some to pass away half an hour, some to get information, some seeking office. It will not work well if he takes the ground that his time is too important to be wasted on casual callers and refers them to some assistant.

In the second place he must, to a great extent at least, give up the pleasure of personal investigation of questions that specially interest him, and turn them over to others. It rarely happens that he can carry out his own plans in his own way, and perhaps it is well that this should be the case. The general character of his work is usually determined for him either by his predecessors, or by Congress, or by the general consensus of opinion of scientific men interested in the

particular subject or subjects to which it relates. This last has very properly much weight; in fact, it has much more weight than one might suppose, if he judged from some criticisms made upon the work of some of our bureaus whose work is more or less scientific. In these criticisms it is urged that the work has not been properly planned and correlated; that it should not be left within the power of one man to say what should be done; that the plans for work should be prepared by disinterested scientific men—as, for instance, by a committee of the National Academy—and that the function of the bureau official should be executive only.

I have seen a good deal of this kind of literature within the last ten or twelve years, and some of the authors of it are very distinguished men in scientific work; yet I venture to question the wisdom of such suggestions. As a rule, the plans for any extended scientific work to be undertaken by a Government department are the result of very extended consultations with specialists, and meet with the approval of the majority of them. Were it otherwise the difficulties in obtaining regular annual appropriations for such work would be great and cumulative, for in a short time the disapproval of the majority of the scientific public would make itself felt in Congress. It is true that the *vis inertiae* of an established bureau is very great. The heads of Departments change with each new administration, but the heads of bureaus remain; and if an unfit man succeeds in obtaining one of these positions, it is a matter of great difficulty to displace him; but it seems to me to be wiser to direct the main effort to getting right men in right places rather than to attempt to elaborate a system which shall give good results with inferior men as the executive agents, which attempt is a waste of energy.

You are all familiar with the results of the inquiry which has been made by a Congressional committee into the organization and work of certain bureaus which are especially connected with scientific interests, and with the different opinions which this inquiry has brought out from scientific men. I think that the conclusion of the majority of the committee, that the work is, on the whole, being well done, and that the people are getting the worth of their money, is generally assented to. True, some mistakes have been made, some force has been wasted, some officials have not given satisfaction; but is it probable that any other system would give so much better results that it is wise to run the risks of change?

This question brings us to the only definite proposition which has been made in this direction, namely, the proposed Department of Science, to which all the bureaus whose work is mainly scientific, such as the Coast Survey, the Geological Survey, the Signal Service, the Naval Observatory, etc., shall be transferred.

The arguments in favor of this are familiar to you, and, as regards one or two of the bureaus, it is probable that the proposed change would effect an improvement; but as to the desirability of centralization and consolidation of scientific interests and scientific work into one department under a single head, I confess that I have serious doubts.

One of the strongest arguments in favor of such consolidation that I have seen is the address of the late president of the Chemical Society of Washington, Professor Clarke, "On the Relations of the Government to Chemistry," delivered about a year ago. Professor Clarke advises the creation of a large, completely-equipped laboratory, planned by chemists and managed by chemists, in which all the chemical researches required by any department of the Government shall be made, and the abandonment of individual laboratories in the several bureaus on the ground that these last are small, imperfectly equipped, and not properly specialized; that each chemist in them has too broad a range of duty and receives too small a salary to command the best professional ability. He would have a national laboratory, in which one specialist shall deal only with metals, another with food products, a third with drugs, etc., while over the whole, directing and correlating their work, shall preside the ideal chemist, the all-round man, recognized as the leader of the chemists of the United States. And so should the country get better and cheaper results. It is an enticing plan and one which might be extended to many other fields of work. Granting the premises that we shall have the best possible equipment, with the best possible man at the head of it, and a sufficient corps of trained specialists, each of whom will contentedly do his own work as directed and be satisfied, so that there shall be no jealousies, or strikes, or boycotting, and we have made a long stride toward Utopia. But before we centralize in this way we must settle the question of classification. Just as in arranging a large library there are many books which belong in several different sections, so it is in applied science. Is it certain that the examination of food products or of drugs should be made under the direction of the national

chemist rather than under that of the Departments which are most interested in the composition and quality of these articles? This does not seem to me to be a self-evident proposition by any means.

The opinion of a scientific man as to whether the Government should or should not undertake to carry out any particular branch of scientific research and publish the results, whether it should attempt to do such work through officers of the Army and Navy, or more or less exclusively through persons specially employed for the purpose, whether the scientific work shall be done under the direction of those who wish to use, and care only for, the practical results, or whether the scientific man shall himself be the administrative head and direct the manner in which his results shall be applied; the opinion of a scientific man on such points, I say, will differ according to the part he expects or desires to take in the work, according to the nature of the work, according to whether he is an Army or Navy officer or not, according to whether he takes more pleasure in scientific investigations than in administrative problems, and so forth.

It is necessary, therefore, to apply a correction for personal equation to each individual set of opinions before its true weight and value can be estimated, and, unfortunately, no general formula for this purpose has yet been worked out.

I can only indicate my own opinions, which are those of an Army officer, who has all he wants to do, who does not covet any of his neighbors' work or goods, and who does not care to have any more masters than those whom he is at present trying to serve. You see that I give you some of the data for the formula by which you are to correct my statements, but this is all I can do.

I am not inclined at present to urge the creation of a department of science as an independent department of the Government having at its head a Cabinet officer. Whether such an organization may become expedient in the future seems to me doubtful; but at all events I think the time has not yet come for it.

I do not believe that Government should undertake scientific work merely or mainly because it is scientific, or because some useful results may possibly be obtained from it. It should do, or cause to be done, such scientific work as is needful for its own information and guidance when such work cannot be done, or cannot be done so cheaply or conveniently, by private enterprise. Some kinds of work it can best have done by private contract, and not by

officials; others, by its own officers. To this last class belong those branches of scientific investigation, or the means for promoting them, which require long-continued labor and expenditure on a uniform plan—such as the work of the Government Observatory, of the Government surveys, of the collection of the statistics which are so much needed for legislative guidance, and in which we are at present so deficient, the formation of museums and libraries, and so forth.

Considering the plans and operations of these Government institutions from the point of view of the scientific public, it is highly desirable that they should contribute to the advancement of abstract science, as well as to the special practical ends for which they have been instituted; but from the point of view of the legislator, who has the responsibility of granting the funds for their support, the practical results should receive the chief consideration, and therefore they should be the chief consideration on the part of those who are to administer these trusts. It must be borne in mind that while the average legislator is, in many cases, not qualified to judge *a priori* as to what practical results may be expected from a given plan for scientific work, he is, nevertheless, the court which is to decide the question according to the best evidence which he can get, or, rather, which is brought before him, and it is no unimportant part of the duty of those who are experts in these matters to furnish such evidence.

But in saying that practical results should be the chief consideration of the Government and of its legislative and administrative agents it is not meant that these should be the only considerations. In the carrying out of any extensive piece of work which involves the collection of data, experimental inquiry, or the application of scientific results under new conditions there is more or less opportunity to increase knowledge at the same time and with comparatively little increased cost. Such opportunity should be taken advantage of, and is also a proper subsidiary reason for adopting one plan of work in preference to another, or for selecting for appointment persons qualified not only to do the particular work which is the main object, but also for other allied work of a more purely scientific character.

On the same principle it seems to me proper and expedient that when permanent Government employees have at times not enough to do in their own departments, and can be usefully employed in

scientific work, it is quite legitimate and proper to thus make use of them. For example, it is desirable that this country should have such an organization of its Army and Navy as will permit of rapid expansion when the necessity arises, and this requires that more officers shall be educated and kept in the service than are needed for military and naval duty in time of peace. It has been the policy of the Government to employ some of these officers in work connected with other departments, and especially in work which requires such special training, scientific or administrative, or both, as such officers possess. To this objections are raised, which may be summed up as follows :

First, that such officers ought not to be given positions which would otherwise be filled by civilian scientists, because these places are more needed by the civilians as a means of earning subsistence, and because it tends to increase the competition for places and to lower salaries. Put in other words, the argument is that it is injurious to the interests of scientific men, taken as a body, that the Government should employ in investigations or work requiring special knowledge and skill men who have been educated and trained at its expense, and who are permanently employed and paid by it. This is analogous to the trades union and the anti-convict labor platforms.

The second objection is that Army and Navy officers do not, as a rule, possess the scientific and technical knowledge to properly perform duties lying outside of the sphere of the work for which they have been educated, and that they employ as subordinates really skilled scientific men, who make the plans and do most of the work, but do not receive proper credit for it. The reply to this is that it is a question of fact in each particular case, and that if the officer is able to select and employ good men to prepare the plans and to do the work, this in itself is a very good reason for giving him the duty of such selection and employment.

A third objection is that when an officer of the Army or Navy is detailed for scientific or other special work the interests of this work and of the public are too often made subordinate to the interests of the naval or military service, more especially in the matter of change of station. For example, civil engineers object to the policy of placing river and harbor improvements in the hands of Army engineers, because one of the objects kept in view by the War Department in making details for this purpose is to vary the

duty of the individual officer from time to time so as to give him a wider experience. Hence it may happen that an officer placed on duty in connection with the improvement of certain harbors on the Great Lakes shall, after three or four years, and just as he has gained sufficient experience of the peculiarities of lake work to make his supervision there peculiarly valuable, be transferred to work on the improvement of the Lower Mississippi with which he may be quite unfamiliar.

In like manner Professor Clarke objects to having a laboratory connected with the medical department of the Navy on the ground that the officer in charge is changed every three years; consequently science suffers in order that naval routine may be preserved.

There is force in this class of objections, but the moral I should draw from them is, not that Army and Navy officers should not be allowed to do work outside their own departments or in science, but that when they are put upon such duty, the ordinary routine of change of station every three or four years should not be enforced upon them without careful consideration of the circumstances of the case, and satisfactory evidence that the work on which they are engaged will not suffer by the change. And, as a matter of fact, I believe this has been the policy pursued, and instances could be given where an officer has been kept twenty years at one station for this very reason.

I pass over a number of objections that I have heard made to the employment of Army and Navy officers as administrators, on the ground that they are too "bumptious," or "domineering," or "supercilious," or "finicky," because every one knows what these mean and their force. An Army officer is not necessarily a polished gentleman; neither is a civilian; and a good organizer and administrator, whether officer or civilian, will at times, and especially to some people, appear arbitrary and dictatorial.

There is another objection to special details of Army or Navy officers for scientific duties which comes not so much from outside persons as from the War Department and the officers themselves, and it is this: Among such officers there are always a certain number who not only prefer special details to routine duty, but who actively seek for such details, who are perpetual candidates for them.

The proportion of men whose ideas as to their own scientific ac-

quirements, merits, and claims to attention are excessive as compared with the ideas of their acquaintances on the same points is not greater in the Army than elsewhere, but when an Army officer is afflicted in this way the attack is sometimes very severe, and the so-called influence which he brings to bear may cause a good deal of annoyance to the Department, even if it be not sufficient to obtain his ends. I have heard officers of high rank, in a fit of impatience under such circumstances, express a most hearty and emphatic wish that no special details were possible, so that lobbying for them should be useless. This, however, seems to me to be too heroic a remedy for the disease, which, after all, only produces comparatively trifling irritation and discomfort.

The same evil exists, to a much greater extent, in the civil branches of the Government. Few persons can fully appreciate the loss of time, the worry, and the annoyance to which the responsible heads of some of our bureaus for scientific work are subjected through the desire of people for official position and for maintenance by the Government. They have to stand always at the bat and protect their wickets from the balls which are bowled at them in every direction, even from behind by some of their own subordinates.

It is true that a great majority of the balls go wide and cause little trouble, and a majority of the bowlers soon get tired and leave the field, but there are generally a few persistent ones who gradually acquire no small degree of skill in discovering the weak or unguarded points, and succeed in making things lively for a time. Considered from the point of view of the public interests, such men are useful, for although they cause some loss of valuable time, and occasionally do a little damage by promoting hostile legislation, yet their criticisms are often worth taking into account; they tend to prevent the machine from getting into a rut, and they promote activity and attention to business on the part of administrative chiefs. It is a saying among dog fanciers that a few fleas on a dog are good for him rather than otherwise, as they compel him to take some exercise under any circumstances.

At all events I think it very doubtful whether the jealousies and desire for position for one's self or one's friends which exist under present circumstances would be materially diminished under any other form of organization, even under a department of science.

Some conflict of interests now exists it is true; some work is dupli-

cated; but neither the conflict nor the duplication are necessarily wholly evil in themselves, nor in so far as they are evil are they necessary parts of the present system. This system is of the nature of a growth; it is organic and not a mere pudding-stone aggregation of heterogeneous materials, and the wise course is to correct improper bendings and twistings gradually, prune judiciously, and go slow in trying to secure radical changes lest death or permanent deformity result.

It will be seen that in what I have said I have not attempted to eulogize science or scientists in the abstract. I should be very sorry, however, to have given any one the impression that I think they should not be eulogized. Having read a number of eloquent tributes to their importance by way of inducing a proper frame of mind in which to prepare this address, it is possible that I overdid it a little, and was in a sort of reaction stage when I began to write. But the more I have thought on the subject, and the more carefully I have sought to analyze the motives and character of those of my acquaintances who are either engaged in scientific work or who wish to be considered as so doing, and to compare them with those who have no pretensions to science, and who make none, the more I have been convinced that upon the whole the eulogium is the proper thing to give, and that it is not wise to be critical as to the true inwardness of all that we see or hear.

At least nine-tenths of the praises which have been heaped upon scientific men as a body are thoroughly well deserved. Among them are to be found a very large proportion of true gentlemen, larger, I think, than is to be found in any other class of men—men characterized by modesty, unselfishness, scrupulous honesty, and truthfulness, and by the full performance of their family and social duties.

Even their foibles may be likable. A little vanity or thirst for publicity, zeal in claiming priority of discovery, or undue wrath over the other scientist's theory, does not and should not detract from the esteem in which we hold them. A very good way of viewing characteristics which we do not like is to bear in mind that different parts of the brain have different functions; that all of them cannot act at once, and that their tendencies are sometimes contradictory.

There are times when a scientific man does not think scientifically, when he does not want to so think, and possibly when it is best that he should not so think. There is wisdom in Sam. Lawson's remark

that "Folks that are always telling you what they don't believe are sort o' stringy and dry. There ain't no 'sorption got out o' not believing nothing." At one time the emotional, at another the intellectual, side of the scientific man has the ascendancy, and one must appeal from one state to the other. Were scientific thinking rigorously carried out to practical results in every-day life there would be some very remarkable social changes, and perhaps some very disagreeable ones.

That scientific pursuits give great pleasure without reference to their utility, or to the fame or profit to be derived from them; that they tend to make a man good company to himself and to bring him into pleasant associations is certain; and that a man's own pleasure and happiness are things to be sought for in his work and companionship is also certain. If in this address I have ventured to hint that this may not be the only, nor even the most important, object in life, that one may be a scientific man, or even a man of science, and yet not be worthy of special reverence; because he may be at the same time an intensely selfish man, and even a vicious man, I hope that it is clearly understood that it is with no intention of depreciating the glory of science or the honor which is due to the large number of scientific gentlemen whom I see around me.

A scientific gentleman—all praise to him who merits this title—it is the blue ribbon of our day.

We live in a fortunate time and place; in the early manhood of a mighty nation, and in its capital city, which every year makes more beautiful, and richer in the treasures of science, literature, and art which all the keels of the sea and the iron roads of the land are bringing to it. Life implies death; growth presages decay; but we have good reasons for hoping that for our country and our people the evil days are yet far off. Yet we may not rest and eat lotus; we may not devote our lives to our own pleasure, even though it be pleasure derived from scientific investigation. No man lives for himself alone; the scientific man should do so least of all. There never was a time when the world had more need of him, and there never was a time when more care was needful lest his torch should prove a firebrand and destroy more than it illuminates.

The old creeds are quivering; shifting; changing like the colored flames on the surface of the Bessemer crucible. They are being analyzed, and accounted for, and toned down, and explained, until many are doubting whether there is any solid substratum beneath;

but the instinct which gave those creeds their influence is unchanged.

The religions and philosophies of the Orient seem to have little in common with modern science. The sage of the east did not try to climb the ladder of knowledge step by step. He sought a wisdom which he supposed far superior to all knowledge of earthly phenomena obtainable through the senses. The man of science of the west seeks knowledge by gradual accumulation, striving by comparison and experiment to eliminate the errors of individual observations, and doubting the possibility of attaining wisdom in any other way. The knowledge which he has, or seeks, is knowledge which may be acquired partly by individual effort and partly by co-operation, which requires material resources for its development, the search for which may be organized and pursued through the help of others, which is analogous in some respects to property which may be used for power or pleasure. The theologian and the poet claim that there is a wisdom which is not acquired but attained to, which cannot be communicated or received at pleasure, which comes in a way vaguely expressed by the words intuition or inspiration, which acts through and upon the emotional rather than the intellectual faculties, and which, thus acting, is sometimes of irresistible power in exciting and directing the actions of individuals and of communities.

The answer of the modern biologist to the old Hebrew question, *viz.*, "Why are children born with their hands clenched while men die with their hands wide open?" would not in the least resemble that given by the Rabbis, yet this last it is well that the scientist should also remember: "Because on entering the world men would grasp everything, but on leaving it all slips away." There exist in men certain mental phenomena, the study of which is included in what is known as ethics, and which are usually assumed to depend upon what is called moral law. Whether there is such a law and whether, if it exists, it can be logically deduced from observed facts in nature or is only known as a special revelation, are questions upon which scientific men in their present stage of development are not agreed. There is not yet any satisfactory scientific basis for what is recognized as sound ethics and morality throughout the civilized world; these rest upon another foundation.

This procession, bearing its lights of all kinds, smoky torches, clear-burning lamps, farthing rush-lights, and sputtering brimstone

matches, passes through the few centuries of which we have a record, illuminating an area which varies, but which has been growing steadily larger. The individual members of the procession come from, and pass into, shadow and darkness, but the light of the stream remains. Yet it does not seem so much darkness, an infinite night, whence we come and whither we go, as a fog which at a little distance obscures or hides all things, but which, nevertheless, gives the impression that there is light beyond and above it. In this fog we are living and groping, stumbling down blind alleys, only to find that there is no thoroughfare, getting lost and circling about on our own tracks as on a jumbie prairie; but slowly and irregularly we do seem to be getting on, and to be establishing some points in the survey of the continent of our own ignorance.

In some directions the man of science claims to lead the way; in others the artist, the poet, the devotee. Far reaching as the speculations of the man of science may be, ranging from the constitution and nature of a universal protyle, through the building of a universe to its resolution again into primal matter or modes of motion, he can frame no hypothesis which shall explain consciousness, nor has he any data for a formula which shall tell what becomes of the individual when he disappears in the all-surrounding mist. Does he go on seeking and learning in other ways or other worlds? The great mass of mankind think that they have some information bearing on these questions; but, if so, it is a part of the wisdom of the Orient, and not of the physical or natural science of the Occident. Whether after death there shall come increase of knowledge, with increase of desires and of means of satisfying them, or whether there shall be freedom from all desire, and an end of coming and going, we do not know; nor is there any reason to suppose that it is a part of the plan of the universe that we should know. We do know that the great majority of men think that there are such things as right and duty—God and a future life—and that to each man there comes the opportunity of doing something which he and others recognize to be his duty. The scientific explanation of a part of the process by which this has been brought about, as by natural selection, heredity, education, progressive changes in this or that particular mass of brain matter, has not much bearing on the practical question of "What to do about it?" But it does, nevertheless, indicate that it is not a characteristic to be denounced, or opposed, or neglected, since, even in the "struggle-for-existence" theory, it has

been, and still is, of immense importance in human social development.

“Four men,” says the Talmud, “entered Paradise. One beheld and died. One beheld and lost his senses. One destroyed the young plants. One only entered in peace and came out in peace.” Many are the mystic and cabalistic interpretations which have been given of this saying; and if for “Paradise” we read the “world of knowledge” each of you can no doubt best interpret the parable for himself. Speaking to a body of scientific men, each of whom has, I hope, also certain unscientific beliefs, desires, hopes, and longings, I will only say: “Be strong and of a good courage.” As scientific men, let us try to increase and diffuse knowledge; as men and citizens, let us try to be useful; and, in each capacity, let us do the work that comes to us honestly and thoroughly, and fear not the unknown future.

When we examine that wonderful series of wave marks which we call the spectrum we find, as we go downwards, that the vibrations become slower, the dark bands wider, until at last we reach a point where there seems to be no more movement; the blackness is continuous, the ray seems dead. Yet within this year Langley has found that a very long way lower down the pulsations again appear, and form, as it were, another spectrum; they never really ceased, but only changed in rhythm, requiring new apparatus or new senses to appreciate them. And it may well be that our human life is only a kind of lower spectrum, and that, beyond and above the broad black band which we call death, there are other modes of impulses—another spectrum—which registers the ceaseless beats of waves from the great central fountain of force, the heart of the universe, in modes of existence of which we can but dimly dream.

BULLETIN

OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON.

GENERAL MEETING.



BULLETIN
OF THE
GENERAL MEETING.

279TH MEETING.

JANUARY 16, 1886.

President BILLINGS in the Chair.

Thirty-two members and guests present.

Announcement was made of the election to membership of Messrs. BENJAMIN PICKMAN MANN and CHARLES COOPER NOTT.

The following report of the Auditing Committee was presented by its chairman, Mr. TONER:

DECEMBER 24, 1885.

The undersigned, a committee appointed at the annual meeting of the Philosophical Society of Washington, December 19, 1885, for the purpose of auditing the accounts of the Treasurer, beg leave to report as follows:

We have examined the statement of receipts, including annual dues, sale of Bulletin, and interest on bonds, and find the same to be correct as stated.

We have examined the statement of disbursements, and compared the same with the vouchers, and find them to agree.

We have examined the returned checks and the bank account with Riggs & Co., and find the balance, \$484.02, to agree with the statements in the Treasurer's report.

We have examined the U. S. bonds belonging to the Society, and find them to be in amount and character as represented in the Treasurer's report, aggregating \$2,500.

J. M. TONER,

O. T. MASON,

T. C. MENDENHALL,

Committee.

(3)

Mr. J. S. DILLER communicated

NOTES ON THE GEOLOGY OF NORTHERN CALIFORNIA.

[Abstract.]

Under the direction of Capt. Dutton I have spent the last three summers studying the geology of northern California and the adjacent portion of Oregon. The conclusions of a general nature referring to that region may be briefly summarized as follows:

In the northern end of the Sierra Nevada and the central portion of the Coast range, among the highly plicated, more or less metamorphosed strata which are older than those of the Chico group, there appears to be but one horizon of limestone, and that is of Carboniferous age.

The northern end of the Sierra Nevada is made up of three tilted orographic blocks which are separated from each other by great faults. The westernmost of these blocks stretching far to the southeast appears to form the greater portion of the range.

As in the Great Basin region the depressed side of each block was occupied by a body of water of considerable size. The deposits formed in these lakes gave rise to the fertile soils of American and Indian valleys.

The plication of the strata in the Sierra Nevada range took place, at least in great part, about the close of the Jurassic or beginning of the Cretaceous period, but the faulting which really gave birth to the Sierra as a separate and distinct range by differentiating it from the great platform stretching eastward into the Great Basin region, did not take place until towards the close of the Tertiary or the beginning of the Quaternary.

Although the faulting may have commenced earlier, the greater portion of the displacement has taken place since the deposition of a large part of the auriferous gravels and the beginning of the great volcanic outbursts in the vicinity of Lassen's Peak. If we may accept numerous small earthquake shocks as evidence, the faulting still continues.

The distribution of the rocks of the Chico group indicates that the western coast of the continent at that time lay along the western base of the Sierra extending around the northern end of the range in the vicinity of Lassen's Peak and stretching far northeasterly into Oregon. Off the coast lay a large island which now forms

northwestern California and the adjacent portion of Oregon. This island extended as far southeast as the Pit river region where it was separated from the main land by a wide strait.

All of the ridges developed out of the Cretaceous island belong to the Coast range.

The volcanic ridge of Lassen's Peak lies between the northern end of the Sierra Nevada and the Coast range. The great volcanic field of Oregon and Washington Territory, to which Lassen's Peak and the Cascade range belong, appears in a general way to be outlined by the depression between the Cretaceous island and the main land. A general account of the facts from which these conclusions are drawn will appear in Bulletin of the U. S. Geological Survey No. 33.

Mr. I. C. RUSSELL read a supplementary paper entitled

NOTES ON THE FAULTS OF THE GREAT BASIN AND OF THE
EASTERN BASE OF THE SIERRA NEVADA.

[Abstract.]

The structure of the Great Basin was systematically studied by the geologists of the Fortieth Parallel Exploration, and subsequently by G. K. Gilbert and J. W. Powell. The results of these investigations, so far as they relate to the faults of the region, are indicated in the bibliographic list which follows.

The studies here referred to led to the recognition of a type of mountain structure named the "Great Basin system," which has been found to prevail over large portions of the United States west of the Rocky Mountains. A typical mountain of this system is a long, narrow orographic block, upraised along one edge, *i. e.* a monoclinical ridge. A mountain range having this structure usually presents an abrupt scarp, formed of the edges of broken strata, on the side bordered by the fault, and slopes much more gently in the opposite direction.

Mountain ranges of this character occupy the greater part of the area of interior drainage, known as the Great Basin, and at times overlap its borders. An older structure in which corrugation plays an important part has been recognized by several geologists in the desert ranges of Nevada and Utah, but these disturbances were produced previous to the faulting which gave origin to the present topographic relief.

The writer has observed Great Basin structure to extend throughout Western Utah, Northern Nevada, and into Oregon as far as Malheur Lake. On the west side of the Great Basin, at the immediate base of the Sierra Nevada, there is an immense compound displacement that can be followed all the way from Honey Lake on the north to beyond Owen's Lake on the south, a distance of over 350 miles. Along many of the faults composing this belt the records of a post-Quaternary movement may be clearly recognized. Fault scarps produced by recent movement have been observed in Eagle and Carson Valleys, south of Carson City, in Bridgeport Valley, and on the west side of Mono Lake. The earthquake in Owen's Valley in 1872, was caused by a movement along one of the faults of this series.

The eastern face of the Sierra Nevada is extremely abrupt and its western slope is gentle. Corrugations of older date than the faults which determine the present relief of the mountains may be observed at many localities. It thus agrees in its general features with many of the Basin ranges. The Sierra Nevada is essentially monoclinical in structure, but is traversed from north to south by faults which divide it into separate ranges, as may be seen in the neighborhood of Lake Tahoe and in the elevated region west of Mono Lake. The Great Basin structure here extends beyond the borders of the area of interior drainage, and is probably limited on the west by the great valley of California. How far north of Lake Tahoe the secondary faults that divide the mountain mass may be traced is unknown, but they can certainly be followed to where the Central Pacific railroad crosses the mountains.

The following list indicates where observations on the faults of the Great Basin system may be found:

Clarence King: Reports of the Fortieth Parallel Exploration. Vol. I, 1878, pp. 735, 744-746; Vol. III, 1870, p. 451.

J. D. Whitney: The Owens Valley earthquake. *Overland Monthly*, Aug. and Sept., 1872.

Joseph Le Conte: On the Structure and Origin of Mountains, with special reference to recent objections to the "Contraction Theory." *American Journal of Science*, Vol. XVI, 1878, pp. 95-112.

" " A theory of the formation of the great features of the earth's crust. *American Journal of Science*, Vol. IV, 1872, pp. 345-355, 460-472.

- G. K. Gilbert: Progress report upon Geographical and Geological Explorations and Surveys West of the 100th Meridian, in 1872. Washington, 1874. p. 50.
- “ “ Report upon Geographical and Geological Explorations and Surveys west of the 100th Meridian. Washington, 1875. Vol. III, Geology, pp. 21-42.
- “ “ Contributions to the history of Lake Bonneville. In Second Annual Report of the U. S. Geological Survey. Washington, 1882. pp. 192-200.
- “ “ A theory of the earthquakes of the Great Basin with a practical application. American Journal of Science, Vol. XXVII, 1884, pp. 49-53.
- J. W. Powell: Basin Range System. See Report on Lands of the Arid Region of the United States. Washington, 1879. pp. 94-95.
- “ “ Basin Range Province. See Report on the Geology of the eastern portion of the Uinta Mountains. Washington, 1876. pp. 6-7, 23-25.
- C. E. Dutton: Geology of the High Plateaus of Utah. Washington, 1880. pp. 51-53.
- I. C. Russell: Sketch of the Geological History of Lake Lahontan. Third Annual Report of the U. S. Geological Survey. Washington, 1883. p. 202.
- “ “ A Geological Reconnoissance in Southern Oregon. Fourth Annual Report of the U. S. Geological Survey. Washington, 1884. pp. 442-453.
- “ “ Lake Lahontan. Monograph No. XI, U. S. Geological Survey, pp. 24-28, 274-284.

Mr. GILBERT remarked that the section exhibited by Mr. Diller appeared to demonstrate a history comprising (1) the folding of the slates and the formation of several faults and associated monoclines, (2) the general degradation of the country until the monoclinical ridges were approximately obliterated, and (3) a renewal of movement on the old fault lines, giving rise to the existing topography.

Mr. WILLIS remarked that in 1883 he had had opportunity to study the Cascade Mountains north of the region described by Mr. Diller. The Sierra structure is apparently not found in the northern part of Washington Territory, and the eastern face of the Cascade range is probably not characterized like the Sierra by a great fault.

Mr. DILLER concurred in the statement that the Cascade range is built essentially of igneous rocks, and is not characterized by great faults, at least along its eastern base.

The topography of the Sierra has entirely changed since the deposition of the auriferous gravels, and some of the fault movements are so recent that the stream terraces to which they have given rise are still preserved.

Mr. G. K. GILBERT made a communication on

RECENT CHANGES OF LEVEL IN THE BASIN OF LAKE ONTARIO.

[The substance of this communication was presented to the American Association for the Advancement of Science at Ann Arbor, and appears in abstract in *Science*, Vol. VI, p. 222.]

Remarks were made by Mr. E. FARQUHAR.

280TH MEETING.

JANUARY 30, 1886

The President in the Chair.

Fifty-five members and guests present.

The Chair announced the appointment of the Committee on Communications.

Mr. GEORGE E. CURTIS made a communication on

LIEUTENANT LOCKWOOD'S EXPEDITION TO FARTHEST NORTH.

[Abstract.]

The paper opened with a reference to the statement in the *Encyclopædia Britannica* (article, *Polar Regions*, p. 326,) that "all this region [the northern coast of Greenland and the interior of Grinnell

Land] had already been explored and exhaustively examined by the English expedition of 1875-'76." A refutation of this statement was not now necessary inasmuch as a retraction had already been made; but an impartial examination of Lieut. Lockwood's observations was still required as a basis for our own confidence in the latitude attained.

A description of the equipment of the expedition was given, with a sketch of the events of the journey, and extracts from the narrative report. The weights of the food and equipments drawn by the dog team furnished the basis of a discussion as to the value of dogs in arctic sledging. The weight of food taken for the support of each man was about twice that taken for each dog. Now if a man can drag a sufficiently greater amount to compensate for the greater weight of his food, it is immaterial whether the motive force used be dogs or men. On this expedition the dog sledge was actually loaded so as to give a weight of about 100 lbs. to each dog; but the maximum weight that can be advantageously drawn by a man is only 125 or, perhaps, 150 lbs. The ratio of effective work performed to the weight of food consumed is, therefore, materially greater for dogs than for men, so that a substantial economical advantage is obtained by using dogs instead of men for sledge dragging. This advantage seems not to have been appreciated by the English expedition of 1875-'76, whose heavy sledges and equipments were all drawn by hand. In addition to the more conspicuous causes of the failure of Lieut. Beaumont's expedition on the Greenland coast, the neglect to make use of dogs must be added as an important element.

The sextant observations made by Lieut. Lockwood for determining the position of his farthest north were shown to be highly satisfactory. Sets of circum-meridian observations for latitude were made at midnight of May 14th and at noon of May 15th. The conditions of observation offer no sufficient reason for giving more weight to one set than to the other. The mean of these results gives $83^{\circ} 24'$ as the latitude attained by Lieut. Lockwood, and an uncertainty not greater than $1'$ represent the accuracy of its determination.

The paper closed with the following tribute to the character of Lieut. Lockwood as an arctic explorer:

I cannot close this review of Lieut. Lockwood's expedition to farthest north without turning from the cold discussion of the astro-

nomical and geographical records to speak of him of whose life and labors they constitute an imperishable memorial.

The success of the expedition was not the result of chance, but was due to Lieut. Lockwood's thorough knowledge of the details of such an undertaking, and to his indomitable energy in its execution. During the preceding winter he had devoted himself to preparation for the work; had made a careful study of the management and equipment of previous sledging expeditions—especially those of the English in 1875-'76—and profiting by the experience of his predecessors was able to avoid their mistakes. Lieut. Beaumont's journey on the Greenland coast was impeded by the heavy sledge, and the heavier equipments with which it was weighted. Lieut. Lockwood's extraordinary distance was attained with a light sledge drawn by dogs and loaded with nothing but food and the barest necessities of a camp. Regardless of all personal comforts, everything was sacrificed to the objects of the expedition.

Under the instruction of Mr. Israel, the young astronomer Lieut. Lockwood had familiarized himself during the winter with all the astronomical observations necessary to be made by an explorer, and with the return of the spring sun applied himself to practical observations with the sextant until he became an expert in its use. So good was his astronomical work that the accuracy of his observations is dependent only on the variability of the instrument and the difficulty of the conditions of observation.

In addition to a practical knowledge of arctic sledging, the expedition was undertaken with a determined energy of purpose, those qualities expressively termed "grit" and "pluck," which no obstacle could defeat. Retaining only two companions at Cape Bryant, he sent back his supporting party and continued his advance over an unknown coast. Suffering continuously from cold, hunger, or fatigue, he pushed on with unflinching perseverance until one hundred and fifty miles of new coast were traversed and the national colors unfurled in the highest latitude ever attained by man.

Simply to go a little nearer the pole than his predecessors was not, however, the controlling object of this expedition. Lieut. Lockwood's own motives, as we read them in his journal, were these: "My great wish is to accomplish something on the north coast of Greenland that will reflect credit on myself and on the expedition." Inspired by this praiseworthy ambition, his skillful management resulted in its most successful realization. His mo-

tives were not those of the visionary and enthusiast who "knows nothing and fears nothing," but of an earnest practical explorer whose ambition is to add something to the world's knowledge of the planet on which we live. The literal fidelity of his narrative, its freedom from an exaggeration that has too often marred the records of previous Arctic explorers, the exact and painstaking descriptions, and the careful distinction between what is seen and what is inferred, all bear witness to his conscientiousness in the search for truth.

As an important element in the success of Lieut. Lockwood's expeditions, due recognition must be given to the cordial, sympathetic and able co-operation of Sergeant Brainard. Chosen by Lieut. Lockwood to continue the journey to Cape Bryant, when all the remainder of the party returned, it was Brainard who pushed onward with him over one hundred and fifty miles of that desolate coast and reached the farthest north. It was likewise Lockwood and Brainard who a year later, in May, 1883, explored the interior of Grinnell Land and looked out on the shores of the western polar sea.

But only one of these companions in exploration was destined to reach home to receive the honor due to their heroic achievements—honor *due*, but, as yet, awarded neither to the living nor the dead. The story of the return is known to all, but perhaps not Lieut. Lockwood's wonderful cheerfulness of spirit through that last terrible winter at Cape Sabine with death staring him in the face. Lieut. Lockwood died on April 9, 1884, "from action of water on the heart induced by insufficient nutrition"—the official euphemism for starvation. This record of indescribable suffering, privation and death, following that of two years of heroic endeavor and achievement, is a tragedy which appeals to human hearts with a force unequalled by any story of fiction or by any drama of the stage.

To Lieut. Lockwood's achievements are applicable the familiar lines of Horace :

"Exegi monumentum aere perennius
Regalique situ pyramidum altius,
Quod non imber edax, non Aquilo impotens
Possit diruere, aut innumerabilis
Annorum series et fuga temporum."

Woven into the history of arctic discovery and engraven on our

maps, the substantial results of Lieut. Lockwood's explorations form a tablet more enduring than brass, which the corroding storm, the fierce north wind, and the flight of ages cannot efface.

In reply to a question by Mr. Mussey, Mr. CURTIS stated that the time for longitude determination was obtained from one ordinary watch of good quality, and one pocket chronometer. Messrs. DALL and ROBINSON discussed the advantages and disadvantages of the use of dogs in arctic sledging, and attention was called to the importance of using snow shoes, and of coating the sledge runners with ice.

Mr. O. T. MASON made a communication on

TWO EXAMPLES OF SIMILAR INVENTIONS IN AREAS WIDELY APART.

[Abstract.]

Anthropologists assign similar inventions observed in different parts of the world to one of the following causes:

1. The migration of a certain race or people who made the invention. Upon this theory similar inventions argue the presence of the same people or race.

2. The migration of ideas—that is, an invention may be made by a certain race or people and taught or loaned to peoples far removed in time and place. Upon this theory similar inventions argue identity of origin, but not necessarily the consanguinity of those who practice them.

3. In human culture, as in nature elsewhere, like causes produce like effects. Under the same stress and resources the same inventions will arise.

Now, the question arises, which of these causes shall be invoked in specific cases to account for resemblances.

We must first examine the word resemblance.

Taking Aristotle's four causes:

The material cause, *ex qua aliquid fit*.

The formal cause, *per quam*.

The efficient cause, *a qua*.

The final cause, *propter quam*.

We must enlarge upon them as follows: Every human activity involves six fundamental considerations.

1. The agent, or efficient cause.

2. The material cause.
3. The implemental cause.
4. The formal cause.
5. The processive cause—that is, the exact order and method of the action.
6. The motive or function.

We might, also, include a series of concomitants, such as technical vocabulary, all sorts of traditional lore and myths, social organization, and even religious rites.

Again, some of the six causes are themselves generally the outcome of other causes, so that we have concatenations and genealogies of causes.

Now for the application. Most men, when they say this thing resembles that, have reference only to one of our six causes. They mean simply that there is resemblance in form, or material, or technical method, or function. My plan would be to submit such resemblances to scrutiny to ascertain how far they extend, and, also, to examine resemblances known to be consanguine, or borrowed, or independent, to ascertain which of our characteristics are peculiar to them. In that way an inductive system of rules would be adduced.

The two independent inventions which I exhibit are a beginning in that direction. One is a stitch in basketry, found only at Cape Flattery and on the Congo. This stitch is common enough in fish-traps, wattling fences, and cages, but in only these two areas have people thought to apply it to close basketry. It consists of vertical warp, a horizontal second warp, laid behind the first, and a coiling or sewing of these two together, so as to show a diagonal stitch in front and a vertical stitch in the rear. Here the resemblance is in method alone. In all other respects the inventions differ.

The other invention referred to is the throwing-stick of Australians, Puru Purus, and Eskimo. These agree, in motive or function and in the fundamental idea of a staff and a hook. Beyond this the Eskimo have invented a dozen additional attachments never dreamed of by the others.

Mr. MURDOCH supplemented the enumeration of throwing sticks by describing an undeveloped form used by the Siberian Eskimo. In reply to a question by Mr. Goode, Mr. MASON stated that he had not seen the Brazilian sticks; they are mentioned by many

travelers. Mr. MANN and Mr. MURDOCH described the manner in which the throwing stick is used by Eskimo in kyaks. The motion centers in the wrist and not the elbow or shoulder.

281ST MEETING.

FEBRUARY 13, 1886.

The President in the Chair.

Fifty-five members and guests present. .

Mr. J. H. KIDDER communicated an

HISTORICAL SKETCH OF DEEP SEA TEMPERATURE OBSERVATIONS,
illustrating the subject by numerous diagrams and by a collection
of deep sea thermometers.

Mr. E. B. ELLIOTT made a communication on the

ANNUAL PROFIT TO BANKS OF NATIONAL BANK NOTE CIRCULATION,
and a second communication on the
QUANTITY OF UNITED STATES SUBSIDIARY SILVER COIN EXISTING
AND IN CIRCULATION.

In these papers he developed the formulæ used in computing certain tables embodied in the report of the Comptroller of the Currency.

Remarks were made by Messrs. MUSSEY and LAWRENCE.

Mr. ASAPH HALL read a paper on

THE NEW STAR IN THE NEBULA OF ANDROMEDA,

giving an historical account of its discovery, growth and decadence.
[This paper is printed in the American Journal of Science, 3d series, vol. xxxi, p. 299.]

282D MEETING.

FEBRUARY 27, 1886.

The President in the Chair.

Fifty-six members and guests present.

The Chair announced the election to membership of Mr. GEORGE JOTHAM CUMMINGS.

Mr. ASAPH HALL made a communication on

THE IMAGES OF STARS,

which was discussed by Messrs. EASTMAN, CURTIS, and PAUL.
[This paper is published in the Sidereal Messenger, April, 1886.]

Mr. R. S. WOODWARD made a communication

ON THE CHANGES OF TERRESTRIAL LEVEL SURFACES DUE TO
VARIATIONS IN DISTRIBUTION OF SUPERFICIAL MATTER.

[To appear as a Bulletin of the U. S. Geological Survey.]

He was followed by Mr. G. K. GILBERT with a paper

ON THE OBSERVED CHANGES OF LEVEL SURFACES IN THE BONNE-
VILLE AREA, AND THEIR EXPLANATION ;

and Mr. T. C. CHAMBERLIN then began a paper

ON THE VARYING ATTITUDES OF FORMER LEVEL SURFACES IN
THE GREAT LAKE REGION AND THE APPLICABILITY OF PRO-
POSED EXPLANATIONS.

283D MEETING.

MARCH 13, 1886.

Vice-President HARKNESS in the Chair.

Thirty-nine members and guests present.

The Secretary read a letter from the Secretary of the Council of the Anthropological Society, inviting the members of the Philosophical Society and their friends to attend the annual meeting of

the Anthropological Society and listen to an address by its president, Major J. W. POWELL.

The Chair announced the election to membership of Messrs. CARLOS ALBERT KENASTON, ROLAND DUER IRVING and ARTEMAS MARTIN.

Mr. T. C. CHAMBERLIN completed his communication

ON THE VARYING ATTITUDES OF FORMER LEVEL SURFACES IN
THE GREAT LAKE REGION AND THE APPLICABILITY OF
PROPOSED EXPLANATIONS.

Remarks were made by Mr. DUTTON.

Mr. R. D. IRVING made a communication on

THE ENLARGEMENT OF MINERAL FRAGMENTS AS A FACTOR IN
ROCK ALTERATION,

which was discussed by Messrs. IDDINGS, DILLER, DUTTON, and
LAWRENCE.

284TH MEETING.

MARCH 27, 1886.

The President in the Chair.

Thirty-three members and guests present.

Mr. I. C. RUSSELL made a communication on

THE SUBAERIAL DECAY OF ROCKS AND THE ORIGIN OF THE RED
CLAY OF CERTAIN FORMATIONS.

This was discussed by Prof. JOHN S. NEWBERRY, of New York city, and by Messrs. GOODE, DARTON, IRVING, and CHAMBERLIN.

Mr. ROMYN HITCHCOCK made a communication on

RECENT IMPROVEMENTS IN MICROSCOPIC OBJECTIVES, WITH DEMON-
STRATION OF THE RESOLVING POWER OF A NEW 1-16TH INCH.

Remarks were made by the President.

Mr. HENRY FARQUHAR read a communication on

A FONÉTÍK ÆLFABET.

[Æbstrækt.]

△is ælfabet cændertéyks tu reprizént ðe sawndz av Írglic spiytc æz yúwjuwali hærd, bai twénti-nain létœrz. Av ðiyz *b, d, f, g, h, k, l, m, n, p, r, s, t, v, w, y* ænd *z* hæv ðer kœstomeri sawndz; *c* hæz its sawnd æz in *beneficieri* [beneficiary] — a sawnd akéyjœnali gíven tu *s* or *t* or *ch*, or moœr ófen tu *sh*; *j* iz kanfáind tu its Frence sawnd — hwite iz ool ðæt iz left tu it hwen kambáind wið *d* in Írglic, æz in *ædjutœnt* [adjutant]; hwail ðe néyzal yúwjuwali ríten *ng*, ðe *th* flæt ænd *th* carp, ar gíven bai ðe létœrz *γ, δ* ænd *ϑ*, bárod fram ðe Griyk ælfabet. Av ðe vávewls, *a* iz æz in *wad* or *bar*, *e* æz in *pet*, *i* æz in *pit*, *o* æz in *on* or *or*, *u* æz in *put*; hwail ðe dáigræfs *æ* ænd *œ* ar yuwzd for ðe vávewl sawndz hærd in *bæt* [bat] ænd in *bœt* [but; won, burr, stir, herd, heard, word, etc.]. Dœbllð létœrz índikeyt prolóoyð sawndz: *l* in *dœbll* [double], *m* in *prízzmm* [prism], *a* in *stáari* [starry], *o* in *doon* [dawn]. Œðœr loy vávewls ar rigárded æz impyúœr sawndz; ænd slœrz bifœœr *r* ar dinówted bai *œ*, téndensi tu klowz wið ðe lips bai *w*, ænd wið ðe tœy bai *y*, fálowiγ a cort vávewl; ðœs wiy hæv *œœ, iœœ, oœœ, uœœ* in *bœœr, biœœr, boœœr, buœœr* [bear, beer, bore, boor], *aw, ow, uw* in *haws, flow, buwt* [house, flow, boot], *ey, iy, ay* in *beyt, biyt, bayt* [bait, beat, bite]. Æz egzæmpllz av œðœr kâmbinéycœenz, *oil, wain, yuwz, tényur, kyœœr* [oil, wine, use, tenure, cure] mey biy gíven. Æksénted vávewlz ar markt, sékanderi æksents (æz on ðe fœrst sílabll av *vœriabiliti*) hæviγ ðe greyv sain, prínsipal wœnz ðe ækyúwt.

Ówiγ tu ðe páwœrful ínfluwens av ðe skuwlz in kíypiγ œp æn eksésiv révœœrens for ðe kanvéncœnal stændard av spéliγ, ænd tu ðe fækt ðæt ðe mæðjáríti av ðe wœrdz av áwœr læyγwedj ar nown tu œs bai ðer æpiœœrens æz printed or ríten ræðœr ðæn bai ðer sawnd æz spówken, ðer iz lítl imíydiet práspekt av søeksés in ðe “spéliγ-rifórm” múwvment, hwite eymz tu divélap áwœr spéliγ intu wœn moœr níœœrli fonétik. Nœvœœrðelés, ðer ar præktikal yúwsez for a

gud fonétik ælfabet. Færst, it kud fœrníc a stændard av pronœnsiý-cœn in díkcœneriz av ool sorts — huwz rýdœrz wud ðæs biy seyvd ðe tæsk av lœrniz a dífœrent sístem for iytc díkcœneri, æz æt prézent. Sékand, it kud ænd cud form a régyular brænte av instrœk-cœn in skuwlz, ænd ðæs æsíst in síkýúeriz yúwniform pronœnsiýcœn. Þœrd, sœm sæte diváys iz olmowst a nisésiti, if wiy wud briy órdœr íntu a bíznes naw óltugéðœr keyátik ; træslitœrýcœn av neymz fram ðe Rúwcan, Ærabik ænd œðœr læygwedjez nat yúwziy ðe Rówman ælfabet. Æz wiy fálo now méðad kansístentli æt prézent, ðer wud pœrhæps biy now greyt dífikœlti in estæbliciý wœn ; espécali if bai it ðe sayt av a neym kud giv æn æpráksimet aidía haw it iz pronáwnst bai ðowz mowst fæmliar wið it.

Mr. MUSSEY said that the principal difficulty in all phonetic alphabets was not in the alphabets themselves, but in the existing variety of pronunciation and the disagreements as to the true pronunciation of words. Pitman's phonetic system—little short of an inspiration—was to his mind the best ever devised for practical use, though Bell's system of visible speech enabled a person familiar with it to correctly pronounce words and sentences in any language whatever.

Mr. MALLERY said that he had been connected with the preparation of a phonetic alphabet by the Bureau of Ethnology, with the object of collecting and recording the vocabularies of the languages of the North American Indians. In addition to the requisite that there should be a distinct character for every sound, it was made a fundamental rule that the characters should be limited to those in an ordinary font of English type, embracing however not only the Roman alphabet but such characters and diacritical marks as the printers' cases of average newspapers could furnish. This was accomplished so as to provide for many more sounds than are included in Mr. Farquhar's scheme, yet without resort to the Greek letters used by him in several instances. It was done by the simple device of reversing the large number of letters in the Roman alphabet which present a markedly different appearance when so reversed, from their erect position. This is entirely convenient to the printer and does not occasion awkwardness in the current script to the recorder or writer for the press, as

it is only necessary to mark the letter intended to be reversed, after writing it in the normal manner, and to notify the printer accordingly. In practice the letters intended to be reversed are marked by a cross beneath them, though a still more current method of distinction would be by the cedilla in using which the pen or pencil is not removed from the letter as formed. This is however more convenient to the writer than to the printer.

The result of this scheme in practice has solved one part of the problem of a universal phonetic alphabet. Vocabularies and chrestomathies of unwritten languages have been recorded and printed, upon which grammars and dictionaries have also been prepared and printed, and from them the languages can be learned so as to be spoken intelligibly without oral instruction. The possibility of the use of such an alphabet with only such modification as would increase its simplicity, in the reform of the English literation, is not to be doubted, in view of its success under more difficult conditions. The actual obstacles to phonetic reform of fixed alphabets are, though perhaps insuperable, non-essential in the scientific view of the question.

Concerning the gliding sounds mentioned by Mr. Farquhar, Mr. DOOLITTLE remarked that some of these appeared to be essential, while others were only accidental.

285TH MEETING.

APRIL 10, 1886.

The President in the Chair.

Fifty-nine members and guests present.

The Chair announced the election to membership of Messrs. ALEXANDER GEORGE McADIE and ROBERT THOMAS HILL.

Mr. MALLERY read a communication on

CUSTOMS OF EVERY-DAY LIFE.

[Abstract.]

The scope of the paper excluded the more commonly noted ceremonial institutions, such as appear in regal courts, courts of justice, and legislative bodies, and embraced the ordinary modes of behavior among civilized people. These all have history and significance,

are not the result of deliberate invention or convention, and in their present shape clearly exhibit the laws of evolution, though not always in the directions set forth in text-books and treatises on sociology. Comment was made upon the topics of social etiquette, precedence, titles, grammatical forms of personalty, the address and signatures of letters, forms and practices relating to written invitations and to social visits, and formularies of oral greeting, with examples or illustrations under each topic.

Fashion was distinguished from custom as being imitative and transitory, although in some few instances genuine merit in a fashion led to its permanent adoption under the same law with which the convenient and useful portions of old customs have survived in modifications.

Two points on which the paper specially declared disagreement with Herbert Spencer relate to the bow in salutation and to the hand-shake or grasp. The bow Mr. Spencer regards as but modified from the natural expressions of physical fear and bodily subjection noticed among sub-human animals and the lowest tribes of men, originating in actual prostration and groveling to which crawling and kneeling succeed, and the bow is but a simulated and partial prostration. A large class of obeisances doubtless had their origin in the attitudes of fear, and several were adduced in addition to those mentioned by Mr. Spencer, but it was contended that the subject of the bow is much more complex than as presented by him, a separate and independent course of evolution being suggested. Evidence was collected from many sources, and especially from gesture speech, relating to the concepts of, and expressions for, higher and lower, superior and inferior, assent, submission and respect, all connected with the forward and downward inclination of the head in salutation. Regarding the uncovering of the head as a part of the masculine bow, the paper offered to Mr. Spencer a new illustration of militancy, too often insisted upon in his Synthetic Philosophy but not definitely in this connection. The voluntary deprivation of removable head gear—once defensive—is often a mark of defeat and subjection. The modern formal military and naval salutes contain the same idea that the saluter is actually or symbolically powerless. Therefore the action of the removal of the hat, the present representative of the casque, helmet, or morion, is better adapted to a "surrender" theory than to that of pretended "beggary" advocated by Mr. Spencer.

That great writer believes that the hand-shake originated in a struggle, first real, afterwards fictitious, in which each of the performers attempted to kiss the hand of the other, which was resisted, thus producing a reciprocating movement of the joined hands. In examining this explanation the antiquity and prevalence of the kiss in salutation was questioned. The mutual kiss of affection or passion by the lips between opposite sexes is not found among the lower tribes and is probably not of great antiquity. It was preceded without reference to sex by patting, stroking or rubbing different parts of the body—smelling and sniffing being also common. The kiss of the hand is undoubtedly ancient and gestural, and is apparently not derived from that of the lips, which is gustatory. Instances were admitted of the identical friendly contest for priority in kissing hands relied on by Mr. Spencer, but they were considered to be connected with the topic of precedence as secondary, the joining of hands being primary and wholly unconnected with a "shake" or any motion after junction. Evidence was presented that the junction of hands in testimony and in expression of agreement and friendship is of too high antiquity and universality to be derived from a pantomimic contest about precedence for the comparatively modern and limited kiss.

Mr. MASON expressed the opinion that not all customs are indirectly derived, and cited the innovations of the day as instances of customs deliberately assumed for a definite purpose.

Mr. MENDENHALL referred to the numerous ways in which Japanese customs are the inverse of ours. In beckoning, the fingers are turned down instead of up, and this is probably explained by the fact that in Japan those who are beckoned—namely, inferiors—are by custom or in theory prostrate. The kitchen of a hotel is placed at the front against the street. A horse is backed into the stable and led out. It is a matter of etiquette, and modesty also, that ladies turn their toes in. The Japanese do not shake hands; the bow is very low, and is begun twenty feet away. There is no kiss of ceremony or friendship, but the kiss exists as an expression of passion. Japanese children play all the common games of our children in some modified form, except marbles.

In reply to a question by Mr. Mason, Mr. MENDENHALL said that a Japanese does not shake his own hands as a salutation to

another, but may join them in bowing as a merely accidental attitude. Messrs. E. FARQUHAR and MUSSEY spoke of the antiquity of kissing as indicated by Hebrew and Greek literature. Other remarks were made by the President and by Mr. CLARKE.

Mr. R. D. MUSSEY made a communication entitled

WHEN I FIRST SAW THE CHOLERA BACILLUS.

286TH MEETING.

APRIL 24, 1886.

The President in the Chair.

Thirty members present.

The President communicated an invitation from the American Historical Association to attend its sessions of April 27-29.

Mr. G. BROWN GOODE and Mr. T. H. BEAN made a joint communication on

THE DISTRIBUTION OF FISHES IN THE OCEANIC ABYSSSES AND MIDDLE STRATA.

Remarks were made by Messrs. PAUL, HARKNESS, BILLINGS, DOOLITTLE, GOODE, WELLING, and TAYLOR, and by Prof. EDWARD D. COPE, of Philadelphia.

Mr. GILBERT THOMPSON made a communication on

THE PHYSICAL-GEOGRAPHICAL DIVISIONS OF THE SOUTHEASTERN PORTION OF THE UNITED STATES AND THEIR CORRESPONDING TOPOGRAPHICAL TYPES.

[Abstract.]

Having charge of the geographical work carried on by the U. S. Geological Survey in that portion of the Appalachian region south of Pennsylvania and the Ohio river, I have had occasion to consider the classification of the region from the point of view of the geographer. It has previously been divided by many authors and into numerous sections, the basis of classification being geological botanical, agricultural, or commercial, and usually from a local standpoint. For my purposes the principal basis of classification is the character of the topographic relief, but this is so closely

related to the features controlling other classifications that a large share of the boundaries coincide with lines previously drawn and the selection of appropriate designations is little more than a choice between names previously given.

There are some parts of the United States where the drainage basin affords the best unit for the purposes of the physical geographer. This holds for the basin of the Laurentian lakes, the basin of the Red River of the North, and the great Interior basin. But in the Appalachian region the drainage cannot be used. There is however in this region a remarkable line of demarcation, known as the *fall line*, which finds its manifestation in connection with the drainage, and is the natural boundary of an important division. If we follow the course of any river in the eastern part of the United States, south of New England, from its source to the sea, we discover that at a certain point it ceases to be rapid and turbulent, and becomes broad and slow-moving, and in many cases an estuary of the sea. At the point where this change occurs there is usually a fall or rapid. The familiar local example is the Potomac at Little Falls. I have traced this fall line from near Troy, N. Y., southward by the interior cities of Washington, Richmond, Columbia, and Montgomery, and thence to the Muscle Shoals of the Tennessee river. It is always the lower limit of water power and often the upper limit of navigation, and is therefore marked, and destined to be marked, by cities and towns of importance. In its northern portion it is at the head of tide, and nowhere does it exceed an altitude of 200 feet. It may yet be determined that it crosses the Saint Lawrence at the Lachine rapids and the Mississippi above Cairo, although no rapid exists at that point. Whether it may be traced farther and into Mexico remains to be determined.

From the fall line to the shore of the sea there is a region having a gentle slope, traversed by slow-moving rivers, and fringed at almost a dead level by deltas, swamps and everglades. This I have entitled the *coastal plains*, including as subdivisions the *Atlantic plains* and the *Gulf plains*.

The area bounded by the fall line and by the Mississippi and Ohio rivers and a part of the drainage divide of the Laurentian lakes, might be taken as a whole as the Appalachian region, but it includes three sections so distinct in topographic type as to warrant separate designations.

From the Ohio river southeastward and from the Mississippi

eastward the country gradually rises until it reaches an altitude of about 2500 feet above sea level, where it is generally cut off by an escarpment facing to the southeast and about 1200 feet in height. The composite name of Cumberland-Allegheny-Catskill plateau would serve to define it, but for brevity I have designated the whole as the *Cumberland plateau*. Its general topographic character is that of a table land deeply cut by a system of ramifying drainage. At the north the surface is somewhat rolling, and the plateau ends at the south in long, finger-like spurs. Its rivers and streams rise generally near the edge of the escarpment and flow toward the northwest. The Potomac however breaks across the edge and flows eastward, while the New and Tennessee rivers enter the plateau from the east and flow westward.

From the Cumberland plateau eastward to the eastern foot of the Blue Ridge lies a belt to which the name of *Appalachian region* is applied in a restricted and definite sense. It is characterized by numerous long, narrow mountain ridges, closely parallel to each other and bending in sympathy with the local curvature of the belt. Through large areas they are approximately uniform in height, but elsewhere they are unequal. In a notable belt, everywhere recognized in the local nomenclature as a valley, and traversing the region from north to south, the ridges are so low that they rank only as hills. At the north the principal mountain area lies west of the great valley and only the Blue Ridge on the east. At the south the valley lies close to the Cumberland plateau, and the Blue Ridge is expanded into a broad mountain district, culminating in Mt. Mitchell (6711 feet), the highest summit east of the Rocky Mountains.

The remaining area is the *Piedmont region*, an undulating plain, diversified by low spurs from the mountain region, and occasional isolated hills of considerable elevation. The streams are rapid, and the topographic relief gradually diminishes toward the fall line.

The communication was fully illustrated by maps and topographic sketches, and by a profile from Louisville, Kentucky, to Charleston, South Carolina. Remarks were made by Messrs. GILBERT, HARKNESS and COPE.

287TH MEETING.

MAY 8, 1886.

The President in the Chair.

Thirty-five members present.

The Chair announced the election to membership of Messrs. JOSEPH HAMMOND BRYAN and MERWIN MARIE SNELL.

Mr. THOMAS RUSSELL made the following communication on

TEMPERATURES AT WHICH DIFFERENCES BETWEEN MERCURIAL
AND AIR THERMOMETERS ARE GREATEST.

Glass and mercury do not expand uniformly. An increase in temperature of one degree at one hundred degrees causes greater changes of volume than the same increase at zero. (In all references here to degrees and temperatures the centigrade scale is to be understood.) Normal mercurial thermometers, when corrected for their various errors of construction, differ among themselves and also from the air-thermometer.

At 40° the mercurial thermometer reads about 0.2 higher than the air-thermometer. At -38.8 , the melting point of mercury, it reads about 0.2 lower. The quality of mercury in a thermometer has an influence on its reading. A thermometer containing $\frac{1}{1000}$ of lead in the mercury will read 0.5 lower at 50° than if the mercury is pure. [H. J. Green.]

Comparisons have been made at the Signal Office between an air-thermometer and a number of mercurials. Some deductions have been made from the results of this work as to the temperatures at which the differences between the two thermometers are greatest. From the same results there have also been derived values of the coefficients of expansion of glass dependent on the second and third powers of the temperatures. It is to these I wish to call your attention.

The air-thermometer used was of the kind that measures temperatures by the varying pressure of a quantity of air kept at a constant volume. Five Tounelot mercurial thermometers were compared with this air-thermometer at temperatures from 0° to 55° . Two Baudin thermometers were compared with it from 0° to -38.8 .

The freezing points of mercurial thermometers rise with age. A few days after a thermometer is filled this rise may amount to a

whole degree. In a year after that it may rise an additional five-tenths of a degree; with succeeding years the change is less and less.

When a thermometer is raised to a high temperature its freezing point is depressed. The average depression for 100° is about $0.^{\circ}2$. On raising to a temperature lower than 100° the freezing point is also depressed, but not so much. For 50° the depression is about $0.^{\circ}05$. For temperatures as high as 100° the depressions are about proportional to the squares of the temperatures by which they are produced.

The cause of these changes of freezing point is in the nature of the glass. The mercury in the thermometer has nothing to do with them; neither has the atmospheric pressure.

The amount of the changes depends on the composition of the glass in the thermometer-bulb. It has been recently ascertained by H. F. Wiebe that the change is greatest for glass containing equal quantities of potash and soda. A thermometer made of a variety of glass containing 14 per cent. of potash, 14 per cent. of soda, the remainder silica and oxide of lead, was found to have its freezing point depressed $0.^{\circ}84$ on raising it to 100° . Thermometers in which the potash or soda in the glass was replaced by lime were found to have the freezing points depressed only $0.^{\circ}07$ for the temperature of 100° .

To produce the maximum depression of freezing point peculiar to any temperature requires that the thermometer be kept at that temperature for a certain length of time. For a temperature of 100° a half hour suffices; for 50° two hours are required.

If the thermometer is kept at 100° longer than half an hour the depressed freezing point after that time begins to rise. If continued at the higher temperature for two weeks the freezing point at the end of that time will be found to have risen about one degree. This fact is taken advantage of by some makers of thermometers to produce an instrument whose freezing point will vary but little in years subsequent to its manufacture.

The depression of freezing point produced by high temperature is only temporary. The thermometer in the course of time regains the reading of its freezing point corresponding to ordinary temperatures. The more quickly the depression is produced the more slowly the reading is regained.

After a thermometer has been subjected to a temperature of 100°

it will regain its ordinary freezing point reading in one month. The change in the first part of this period is much more rapid than towards the end. To recover the depression caused by 50° requires only two days. The older a thermometer the more quickly it gains its freezing point corresponding to ordinary temperatures. An instrument forty years old will regain its freezing point after exposure to 100° in one week while an instrument three years old requires a month.

The more alternations of temperature a thermometer is subjected to the more quickly its freezing point rises.

A thermometer subjected to a very high temperature, as 350° , will have its freezing point raised from 12° to 20° . This rise is not due to softness of the glass at the high temperature and a consequent diminution in the volume of the bulb by the atmospheric pressure. This is shown by experiments with weight-thermometers. In these the tubes are open to the pressure of the air and there is as much pressure inside as outside the bulb.

As heating to 100° depresses the freezing point while heating to 350° raises it there must be some intermediate temperature for which there is no change. This point is usually at the temperature of about 160° to 180° , but varies widely with thermometers made of different kinds of glass.

When a thermometer is subjected to a very low temperature a temporary rise in its freezing point is produced. To produce an appreciable rise requires a long-continued exposure. After being kept twenty-four hours at -30° the freezing point is found to be about 0.05° higher than at first.

One hundred degrees on the centigrade scale is taken as the temperature of steam from pure water boiling under a normal barometric pressure equal to 760 mm. of mercury. A variation of 1 mm. in the pressure will change the temperature 0.04° .

Zero is taken as the temperature at which pure ice melts when subject to an atmosphere of pressure. An increase of a whole atmosphere lowers the temperature of the melting point of ice 0.008° . This is to be distinguished from the effect of an atmosphere of pressure on the reading of a thermometer; by compressing the bulb it causes the thermometer to read about 0.2° higher than if there was no pressure.

The fundamental distance on a normal thermometer is taken as the reading it would have at a true temperature of exactly 100°

minus the reading of its depressed freezing point. This, which should be exactly one hundred degrees, rarely is so. When the fundamental distance is taken in this way it is invariable with age. It is the same forty years after the thermometer is made as four hours after, provided the thermometer is kept at ordinary temperatures. The fundamental distance is not invariable when the raised freezing point is used in forming it instead of the depressed freezing point. In this case there is a constant diminution with age as the raised freezing point rises more rapidly than the boiling point. There is not uniformity of practice in the matter of forming the fundamental distance, but it is greatly to be desired.

Heating a thermometer to 350° causes a permanent increase in its fundamental distance between depressed freezing point and boiling, varying from 0.4 to 0.9 . An increase of 0.4 in the fundamental distance corresponds to a decrease of $\frac{1}{50}$ part in the coefficient of expansion of the glass.

The total correction of a mercurial normal thermometer for errors in its construction is composed of three parts:

- 1st. The correction for erroneous fundamental distance. For any temperature this is a proportional part of the difference between the fundamental distance and 100° .
- 2nd. The calibration correction. This is the correction to the scale marks considered as subdividing the capacity of the tube from 0° to 100° into one hundred equal parts. It involves variations in the bore of the tube as well as irregularities in the placing of the marks.
- 3rd. The correction at freezing point. This is the amount the thermometer reads in melting ice above or below 0° . At any time it is the observed reading of the thermometer in melting ice immediately after exposure to the temperature measured. Sometimes it is impossible and it is almost always inconvenient to observe the freezing point of the thermometer immediately after observing a temperature. In such a case the position of the depressed freezing point for that temperature must be computed from the law of the variation of the freezing point. It is always preferable however when the highest accuracy is required to actually observe the freezing point.

When a thermometer is put in ice this is what happens: The column falls rapidly at first, then more slowly. Presently it be-

comes stationary; finally it begins to rise. Fifteen minutes after the thermometer reaches its lowest reading this rise is about 0.001 . It is best in observing the freezing point of a thermometer to put it in ice thoroughly saturated with water. The ice should be contained in a vessel from which the water cannot flow off. A thermometer put in ice in this condition takes on the temperature of 0° more quickly than if put in dry ice containing a good deal of air. This method of observing the freezing point was introduced by Baudin of Paris.

There is another correction to a normal thermometer which is little known and rarely applied. Let:

V = volume of bulb at 0° .

v = volume of tube from 0° to 100° at temperature 0° .

β = coefficient of cubical expansion of glass.

γ = coefficient of expansion of mercury.

T = thermometer-reading corrected for calibration, etc.

t = true temperature.

A consideration of the construction of the thermometer leads to this equation:

$$V(1 + \beta t) + v(1 + \beta t) \frac{T}{100} = V(1 + \gamma t). \quad (1)$$

The volume of the bulb at t° , plus the volume of that part of the tube corresponding to the thermometer reading, is equal to the volume of the mercury at t° . For $t = 100$ the equation becomes:

$$V(1 + \beta 100) + v(1 + \beta 100) = V(1 + \gamma 100). \quad (2)$$

Eliminating $\frac{v}{V}$ from (2) by means of its value found from (1) we have:

$$T = t \frac{1 + 100\beta}{1 + t\beta}. \quad (3)$$

Taking as the coefficient of cubical expansion of glass, β , the quantity 0.000026 , the following values are found for $T - t$, for the various readings of the thermometer from -40° to $+100^\circ$.

T ° c.	$T - t$ ° c.
-40.	-0.145
-20.	-0.062
0.	0.000
+20.	+0.042
40.	+0.062
50.	+0.065
60.	+0.062
80.	+0.042
100.	0.000

These are known as the Poggendorf corrections. They are due to the capacity of the tube from the zero to the one-hundred degree mark, being different at different temperatures.

In the following table are shown the results of the comparisons of a certain mercurial thermometer, Tounelot No. 4207, with the air-thermometer:

Tounelot No. 4207.

Scale reading.	Correction as a normal thermometer.	Correction to reduce to the air-thermometer.	Differences.
° c.	° c.	° c.	° c.
0.0	0.00	0.00	0.00
5.6	+ 0.05	+ 0.01	+ 0.04
11.1	+ 0.08	+ 0.00	+ 0.08
16.1	+ 0.10	+ 0.02	+ 0.08
22.2	+ 0.15	+ 0.05	+ 0.10
25.2	+ 0.16	+ 0.07	+ 0.09
30.1	+ 0.20	+ 0.09	+ 0.11
35.4	+ 0.22	+ 0.10	+ 0.12
40.4	+ 0.25	+ 0.12	+ 0.13
45.1	+ 0.25	+ 0.16	+ 0.09
50.1	+ 0.24	+ 0.15	+ 0.09
52.7	+ 0.24	+ 0.16	+ 0.08
55.3	+ 0.24	+ 0.18	+ 0.06

If it be supposed that these differences are due to sensible terms in the expansion of glass and mercury dependent on the squares of the temperatures, an equation can be derived which will show that the maximum difference must be at 50°. But this is not so; the greatest difference is at about 40°. This agrees with what has been found by others. Rowland at Baltimore found the greatest difference at 40° to 45°; Mills in England found it at 35°, and Grunmach in Berlin at 30°.

Forming a theory of the differences on the supposition that they depend on the third powers of the temperatures as well as the squares, equation (4) is obtained, which gives the relation between the thermometer reading, T , and the true temperature, t .

$$T = t \cdot \frac{1 + \beta_1 100}{1 + \beta_1 t} \cdot \frac{1 + \frac{\gamma_2 - \beta_2}{\gamma_1 - \beta_1} t + \frac{\gamma_3 - \beta_3}{\gamma_1 - \beta_1} t^2}{1 + \frac{\gamma_2 - \beta_2}{\gamma_1 - \beta_1} 100 + \frac{\gamma_3 - \beta_3}{\gamma_1 - \beta_1} (100)^2} \quad (4)$$

This is only approximate. The effects of the second and third

powers of the temperatures in changing the capacity of the tube from 0° to 100° are neglected. The capacity of the tube is only $\frac{1}{50}$ part of that of the bulb.

$\beta_1, \beta_2, \beta_3$ are the coefficients of expansion for glass for the first, second, and third powers of the temperature. $\gamma_1, \gamma_2, \gamma_3$ are the same for mercury.

To make an adjustment of the differences between the mercurial and air-thermometers equation (4) can be put in the form

$$(100t - t^2)x + (10000t - t^3)y + 0.000026t^2 - 0.0026t + \Delta = 0 \quad (5)$$

in which $x = \frac{\gamma_2 - \beta_2}{\gamma_1 - \beta_1}, y = \frac{\gamma_3 - \beta_3}{\gamma_1 - \beta_1}$ and $\Delta = T - t$. This is less approximate than (4) but still sufficiently rigorous for the purpose intended.

Forming observation-equations on this model with the observed differences Δ , as the absolute terms, and solving by the method of least squares, the values of x and y are found to be

$$\begin{aligned} x &= -0.0001391 \\ y &= +0.000000863 \end{aligned}$$

Substituting these in (5) it becomes

$$-0.00788t + 0.000165t^2 - 0.000000863t^3 + \Delta = 0. \quad (6)$$

Differentiating (6) with respect to t and Δ , and putting $\frac{dt}{d\Delta} = 0$, the following quadratic-equation is found

$$0.000002589t^2 - 0.000330t + 0.00788 = 0, \quad (7)$$

the solution of which gives for the temperatures at which the differences between the mercurial and air-thermometer are greatest $t = 31.8$ and $t = 95.8$. To find the temperatures at which the mercurial and air-thermometer agree, put $\Delta = 0$ in (6); the values of t that then satisfy the equation are $t = 0, t = 100$, and $t = 91$.

At 32° the mercurial thermometer reads higher than the air-thermometer, at 96° , it reads lower. A curve representing the differences has the following form :

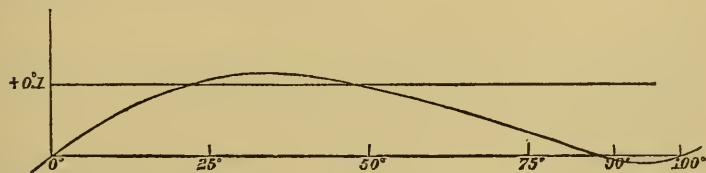


Fig. 1.— T 4207 minus Air-thermometer. Abscissas = Temperatures. Centigrade. Ordinates = Differences.

This agrees with what has been observed by Dr. Grunmach of the Berlin Aichungs Commission. He found the maximum difference on a certain thermometer to be $+ 0.^\circ 12$ at $29.^\circ 8$, and another secondary maximum of $- 0.^\circ 04$ at 82° .

A slight change in the values of x and y will make a large change in the position of the secondary maximum. For another thermometer investigated at the Signal Office this point was found to be at 130° .

The values of x and y can be analyzed still further to ascertain whether consistent with known physical properties of glass and mercury.

Taking Broch's values for the expansion of mercury, which are based on a re-reduction of Regnault's observations, it is found, adapting the figures to the notation used here, that :

$$\begin{aligned}\gamma_1 &= + 0.000181792 \\ \gamma_2 &= + 0.000000000175 \\ \gamma_3 &= + 0.000000000035116\end{aligned}$$

Substituting these values of γ_1 and γ_2 in the equations

$$x = \frac{\gamma_2 - \beta_2}{\gamma_1 - \beta_1}, \quad y = \frac{\gamma_3 - \beta_3}{\gamma_1 - \beta_1}$$

and taking $\beta = 0.000026$ we get

$$\begin{aligned}\beta_2 &= + 0.000000021859 \\ \beta_3 &= + 0.00000000099512\end{aligned}$$

The linear coefficient of expansion of a specimen of glass, such as is used in barometer-tubes and thermometers, has been very carefully determined by Dr. Benoit of the International Bureau of Weights and Measures. Deriving from this the cubical coefficient, in the notation used here, we have Dr. Benoit's values

$$\begin{aligned}\beta_1 &= + 0.0000252 \\ \beta_2 &= + 0.0000000144\end{aligned}$$

It will thus be seen that there is a good agreement between the two values of β_2 found by the two different processes.

Remarks were made by Messrs. GILBERT, HARKNESS, and PAUL.

Mr. J. H. KIDDER made a communication on

THE GILDING OF THERMOMETER BULBS,

and was followed by Mr. H. ALLEN HAZEN on

EFFECTS OF SOLAR RADIATION UPON THERMOMETER BULBS
HAVING DIFFERENT METALLIC COVERINGS.

[Abstract.]

After showing the importance of shielding from or measuring the effects of solar radiation upon thermometer bulbs used in determining the air temperature and indicating the attempts that have been made in obtaining satisfactory results in the past, Mr. HAZEN explained the most recent work of Prof. Wild, of St. Petersburg. Prof. Wild had a bulb coated with copper by the galvanoplastic method, then the copper with gold, which latter was highly polished. From theoretical considerations he established a formula as follows:

$$t_a = t_m - c(t_s - t_m),$$

in which t_a = temperature of air sought; t_m = that of the metallic-covered bulb; t_s = that of a black bulb; and c is a constant which he assumed at .15. The published observations indicated a very high reading of the metal-covered bulb, even higher than would have been obtained with a bare glass bulb.

Mr. HAZEN's own experiments consisted in comparisons between bulbs as follows: (1) black, (2) bright, (3, 4) with silver and gold deposited in an exceedingly thin layer and giving a most admirable surface, and (5, 6) with silver and gold deposited on copper as nearly as possible as suggested by Prof. WILD. These thermometers were exposed in sunshine in the open air as well as indoors. It was very difficult to shield from other radiations, dark heat, etc., but it was found that an exposure of two feet from a window pane gave fairly good results. The results are given in the accompanying table. In computing the actual value of t_a from the formula it was found necessary to take the readings of the black and bright bulbs at each set and compute the t_a by using .6 as the constant. It was found that the black and bright bulbs were the only ones that did not deteriorate from day to day. All the metal-covered bulbs were carefully polished each day.

Comparison of various coverings of thermometer bulbs (out of doors).

Date.	Black.	Bright lower than black.		Silver deposit.		Gold deposit.		Silver plated.		Gold plated.	
		o	c.	o	c.	o	c.	o	c.	o	c.
Apr. 14, '86.....	87.5	7.2	.60	9.0	.29	7.0	.65	7.7	.49	5.8	1.00
Apr. 19	76.3	6.5	.60	8.2	.28	6.3	.65	6.9	.50	5.1	1.04
"	89.0	4.9	.60	6.3	.24	4.7	.67	5.5	.42	3.7	1.11
Apr. 20	76.8	6.0	.60	7.3	.32	5.6	.71	6.3	.52	5.1	.88
"	84.9	7.3	.60	9.2	.27	6.7	.75	7.4	.50	5.8	1.02
"	89.3	5.6	.60	7.6	.18	5.8	.55	6.1	.48	5.0	.80
May 3	76.9	7.3	.60	9.4	.24	6.9	.70	7.7	.52	6.3	.86
"	82.8	6.9	.60	8.8	.25	6.6	.67	7.7	.43	5.8	.89
"	92.1	8.3	.60	10.3	.27	7.9	.66	8.2	.60	7.6	.72
Mean	83.8	6.7	.60	8.5	.26	6.4	.67	7.1	.50	5.6	.81

The results in this table may be taken as relatively accurate, though the absolute values cannot be relied on. We find the constant in the case of the silver-deposited bulb less than one-half that of the bright or bare glass bulb; the gold-deposited runs a little higher; the silver-plated somewhat lower, while the gold-plated is the highest of all. In the gold-deposited thermometer the covering was so thin that it showed a green light through. It has been shown that under these circumstances gold transmits a little heat. The gold-plated thermometer gives a remarkable result due partly to the thickness of the metal and partly to a slight roughness, it having been found impossible to deposit a perfectly smooth copper surface as a base.

Incidentally these plated bulbs have furnished corroboration of a point presented to the Society some time ago, namely, the effect of a layer of ice upon a bulb in contracting it at low temperatures. It is plain that at the temperature of deposition there would be no effect, but as the temperature was lowered, since the metal contracts faster than glass, the tendency would be to a too high reading of the thermometer—*e. g.*, Thermometer No. 840 gave too high readings at different temperatures as follows: at 12°, 3.6; 30°, 1.4; 40°, 1.0; 50°, .7; 60°, .4, and 70°, .1.

Remarks on these communications were made by Messrs. PAUL, MENDENHALL, BILLINGS, and WOODWARD.

288TH MEETING.

MAY 22, 1886.

Vice-President HARKNESS in the Chair.

Forty-eight members and visitors present.

Mr. NEWTON L. BATES read a communication entitled

ORGANIC CELLS OF UNKNOWN ORIGIN AND FORM FOUND IN
HUMAN FÆCES (TWO CASES),*

illustrating his remarks by specimens exhibited under the microscope.

Referring to the composition of these cells, reported to contain four per cent. of silica, Mr. CLARKE called attention to the desirability of testing for other inorganic substances. In reply to a question as to where in the intestinal canal the cells had been found, Mr. BATES replied that the evidence in the case indicated the lower part of the canal.

Mr. J. S. BILLINGS made a communication

ON MUSEUM SPECIMENS ILLUSTRATING BIOLOGY.

[Abstract.]

After referring to the increasing interest on the part of the public in Biology and Natural History, as theories of evolution, natural selection, etc., are becoming better understood, and to the consequent increasing importance of museums or parts of museums intended to illustrate the structure and functions of animals, several types of museums were briefly described, including the collection at Florence, the Hunterian Museum, the average Medical School Museum, the museums proposed by Drs. Roberts, Wilder, and Shufeldt, etc.

The special scope and purposes of the Army Medical Museum were stated to be to illustrate: 1. The effects, immediate and remote, of wounds and of those diseases most prevalent in the army, *i. e.*,

*These cells are now believed to have come from the banana. If a transverse slice of banana is placed in a watch glass and covered with strong nitric acid, two rows of cells become colored and are apparent to the naked eye. A note on the subject may be found in the Boston Medical and Surgical Journal, March 10th, 1883, p. 446. Similar changes doubtless take place by prolonged stay in the intestine, and when found clean and free from vegetable fiber these cells are likely to deceive expert microscopists.

the diseases and injuries of adult males. 2. The work of the medical department of an army, modes of transporting sick and wounded, hospitals, medical supplies, instruments, etc. 3. Human anatomy and pathology of both sexes and all ages. This requires many specimens in comparative anatomy and pathology, which are indispensable for a correct understanding of the structure, development, abnormalities and diseases of man. It is not however proposed to form a museum of comparative anatomy—that belongs to the functions of the National Museum. 4. To show the morphological basis, or want of such basis, for ethnological classification, more especially of the native races of America. This includes anthropometry and craniology. 5. To illustrate for medical investigators and teachers the latest methods, the newest apparatus, etc., for biological investigation, and various modes of preparing and mounting specimens. In connection with this it is hoped to induce original workers to deposit in the museum type specimens or series of specimens illustrating their discoveries and methods.

The classification and arrangement of specimens which it is proposed to carry out in the new Museum building were then briefly described.

Various modes of preparing specimens were shown, including dissections under spirit, frozen and tinted sections, injections by corrosion, etc., and the difficulties in making and preserving such specimens were explained.

A second communication on the same subject was made by Mr. G. BROWN GOODE, and a third, by request, by Mr. FREDERICK A. LUCAS, of the National Museum, who spoke more especially of osteological specimens. The papers were all fully illustrated by specimens from the Medical and National Museums.

Mr. GEORGE P. MERRILL made a communication

ON GEOLOGICAL MUSEUMS.

Remarks were made on the general subject of museums and their management by Prof. EDWARD MORSE, of Salem, Mass.

289TH MEETING.

OCTOBER 9, 1886.

The President in the Chair.

Seventy-eight members and guests present.

The Chair announced the election to membership of Messrs. COOPER CURTICE, HENRY MITCHELL, HENRY GUSTAV BEYER, and NEWTON LEMUEL BATES.

The subject for the evening was

THE CHARLESTON EARTHQUAKE,

which was discussed by Messrs. T. C. MENDENHALL and W J MCGEE and Prof. CHARLES G. ROCKWOOD of Princeton, N. J.

Mr. MENDENHALL spoke of the odor observed on Sullivan's Island previous to the shock, of the time of the clock-stopping shock in Charleston, of the detonations accompanying the various shocks and heard in Charleston, Summerville, and elsewhere, of the torsional movements of monuments, and of the directions in which various structures were thrown down. He exhibited an isoseismal map compiled from data gathered by the U. S. Signal Service. He also stated at second hand a novel theory for the origin of the earthquake, and spoke of the convergence of opinion of geologists and physicists in regard to the condition of the interior of the earth. He accepted as the time of the clock-stopping shock in Charleston 9h. 51' 20" P. M.

Mr. MCGEE described the geological relations of Charleston, showing that a depth of 2,000 feet of clastic rocks had been demonstrated beneath the city, and that the total depth to the crystalline rocks might be as much as one mile. He described the phenomena of deformation of rails and other railway structures, gave in detail an observation of a severe shock at Summerville, described the detonations, and exhibited numerous photographs illustrating the destructive work of the earthquake and the formation of craterlets and sinks.

Prof. ROCKWOOD exhibited an isoseismal map compiled from data gathered by the Earthquake Commission, and characterized by far greater irregularities in the form of contours than were shown by Mr. Mendenhall's map. He called attention to the fact that nearly all the isoseismal curves show salient angles toward the northwest. He dwelt upon the exceptional nature of this opportunity for earthquake investigation, and urged that the utmost advantage be taken

of it. He spoke also of the complexity of earthquake movements, and the difficulties to be overcome in analysing them. He thought that the conspicuous inequality in the violence of the shocks at localities not widely separated was to be ascribed to the intersection and combination of rock waves deflected by reflection and refraction. Two intersecting waves would be especially destructive at their nodal points, and comparatively harmless at their points of interference.

It was announced by the President that the discussion would be continued at the next meeting.

290TH MEETING.

OCTOBER 23, 1886.

The President in the Chair.

Sixty-seven members and guests present.

The discussion of

THE CHARLESTON EARTHQUAKE

was resumed, the principal speakers being Mr. EVERETT HAYDEN and Mr. H. M. PAUL. Remarks were made by Messrs. McGEE, BILLINGS, ROBINSON, DUTTON, BELL, CLARKE, and GILBERT, and by Dr. E. P. HOWLAND, who was present by invitation.

Mr. HAYDEN first discussed a chart on which were plotted the areas disturbed by earthquakes in the southeastern United States from 1874 to 1885, compiled from Rockwood's Notes in the American Journal of Science. This indicated two earthquake belts, one along the Appalachians, the other along the coast. In the former 28 shocks are recorded, in only 3 of which the area is as great as 1,000 square miles (2 in central Virginia, and 1 in western North Carolina and northern Georgia); in the latter 5 are recorded, only 1 of which (that of 1879 in Florida and Georgia) was at all severe. So far as this evidence goes, therefore, we should have expected a severe shock like that of August 31st to have originated in the Appalachians and to have been orogenic in character, an accompaniment of the gradual elevation of the range.

He then proceeded to give a summary of the information which had reached the Geological Survey up to date, illustrating by charts of isoseismal and coseismal lines. The geologic and physical phenomena in the region of greatest intensity having been already dis-



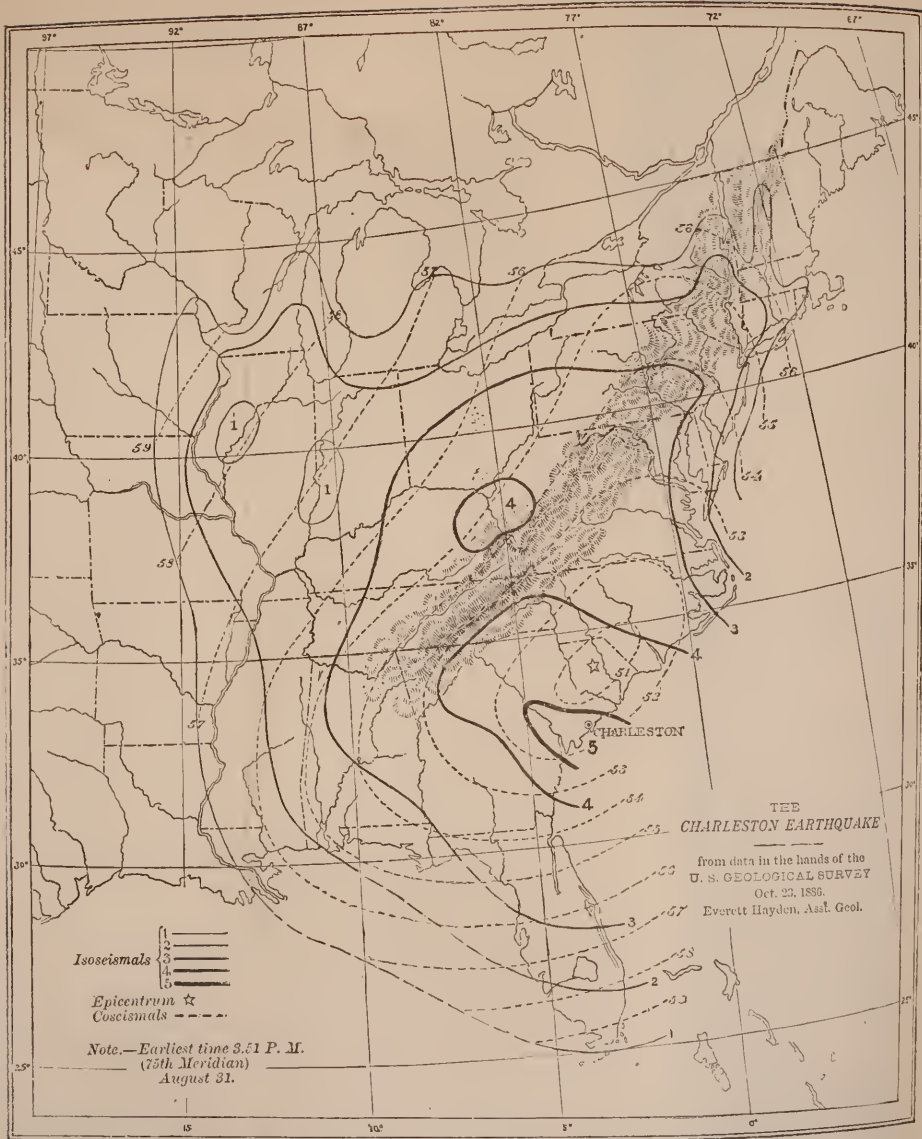
THE
CHARLESTON EARTHQUAKE

from data in the hands of the
 U. S. GEOLOGICAL SURVEY
 Oct. 23, 1886.
 Everett Hayden, Assl. Geol.

cussed at the last meeting were not touched upon. The data used came for the most part from correspondence with private parties, although some valuable information had been received from the Signal Service, Light-House Board, and Hydrographic Office—only a small portion, however, of what they would eventually furnish. The State Department had reported that the shock was felt very slightly in Bermuda, and would report later as to Cuba and the Bahamas.

The *isoseismals* were plotted on an enlarged photograph of the relief model of the eastern United States in the Coast Survey Office, which illustrated the general topographic features more graphically than an ordinary map. In the discussion special attention was paid to explaining their irregular shapes by reference to the surface configuration as well as the geologic structure of the country. The inclosed area, marked 4, in West Virginia and Kentucky, well illustrates the fact that a shock may be felt with greater severity beyond a mountain range than in its midst. The similar isolated areas of less intensity in Indiana and Illinois are also typical of variations due to local conformations; were it possible to plot intensities in still greater detail there would doubtless be hundreds of such isolated districts all through the disturbed area. Other points dwelt upon were the unobstructed transmission of the vibrations along the parallel ridges of the range and up the valleys of the Connecticut and Hudson rivers; the obstruction offered by ridges, valleys, and strike of strata transverse to the direction of propagation; and the rapid loss of energy in the sands and alluvial deposits of the northeast coast and lower Mississippi valley. The total land area included within the outer *isoseismal* is 774,000 square miles, and if we add only half as much more for ocean area it closely approximates to that given by Reclus for the great Lisbon earthquake. Special acknowledgement was made for valuable positive and negative reports received from members of the New England Meteorological Society through their secretary, Prof. W. M. Davis; they accurately fixed the limits of the disturbed area in New England.

The *coseismals* were plotted from the most reliable and consistent among a hundred or more good time observations, and special care was taken to make them conform to the actual facts, uninfluenced by any preconceived theoretical ideas. Attention was called to certain peculiarities of these lines, such as their noticeable



prolongation to the northward and southwestward; the narrow intervals where they run along the western flanks of the Appalachians and across the Florida peninsula; and the wide intervals in the Ohio and upper Mississippi valleys. The following considerations were offered as helping to explain these apparently anomalous features: The crystalline Archean rocks and parallel ridges of the mountain chain favor a rapid axial transmission of the vibrations. The first tremors spreading to the northwestward, however, are cut off and deadened by the mountains, so that it is a later phase of the wave which is felt and recorded beyond; having passed the range it then spreads with little obstruction and high velocity through comparatively level strata. Similarly in the littoral and alluvial deposits to the northeast, south, and southwest the earlier tremors are lost and later phases of the wave are successively recorded. It is especially to be remembered that all these times are from non-instrumental observations; an exact instrumental observation made at Toronto, Ontario, by Prof. Chas. Carpmael (9: 54: 50 P. M.), could not be used here because so early as to be wholly inconsistent with all other reliable but non-instrumental observations.

The epicentrum, or point on the surface directly above that part of the deep-lying fissure where the earliest vibrations originated, is placed by these coseismals about a hundred miles north of Charleston, which is not at all inconsistent with the fact that the greatest damage was caused in that city. In fact, it is to be expected that the destruction of buildings should be greater at a distance, where the angle of emergence is less. Moreover, most of the evidence seems to point to a very deep-lying origin, in which case one cannot but attribute much of the local damage, as well as the continuance of shocks of considerable intensity but small area, to the character of the recent geologic formations in that region. Borings for artesian wells at Charleston indicate that the Tertiary and Cretaceous strata are very heterogeneous in character—sands, clays, limestone-marls, and imperfectly consolidated beds of conglomerate, with occasional cavities containing running water—and much of the city is built upon made land. Such considerations may explain the extremely local character of many of the shocks which have been felt at various points in the State of South Carolina since August 31st, as well as the great intensity of the shock at Charleston on that date. Local sinks in the ground are reported even in northern Florida, far from the origin of the disturb-

ance. An analogous case is seen in the fact that the great destruction of life and property at Lisbon, in 1755, occurred in those portions of the city built on weak Tertiary formations, while houses on the firmly consolidated Secondary rocks suffered little damage.

The following velocities of wave transmission are indicated :

To—	Feet per second.	Miles per minute.
Toronto, Ontario -----	15,000	170
Washington, D. C.-----	13,000	148
Prairie du Chien, Wisc.-----	9,300	106
Average -----	12,400	141

By way of comparison the following recorded velocities are of interest: Lisbon, 1755, 2,000 feet per second; Naples, 1857, 1775; St. Lawrence valley, 1870, 12,000; England, 1884, 9,200.

Reported directions of transmission, while very often what we should expect, are yet generally so contradictory as to be of little value. Similarly the number of shocks felt is recorded so differently by different observers as to be very confusing; the occurrence of two shocks at a point at some distance from the origin is explained by the hypothesis that the first traveled rapidly through the hard under-lying rocks, and the second more slowly through the softer and more recent strata above. The shock is reported as accompanied by sounds of greater or less intensity all along the extent of Archean rocks from northern Alabama to Connecticut, and at points on the coastal plain within a radius of about 300 miles from the origin.

The coincidence of an unusually high tide is worthy of remark; the moon was near perigee, and there had been an eclipse of the sun only three days previously. The fact that no sea-wave was caused by the shock confirms the conclusion that the origin was inland. The weather is generally reported to have been very still and sultry, although there were no unusual barometric conditions. The summer had been an unusually dry one.

Only two other recorded earthquakes in North America can be compared with this in either area or intensity: that at New Madrid, Missouri, in 1811, which was probably fully its equal, and that in the St. Lawrence valley in 1870, equal possibly in area but not in intensity.

Mr. PAUL explained the generally received classification of earthquake waves, described some of the results of the Tokio earthquake

studies, discussed the relation of destructiveness to amplitude of vibration and to rate of acceleration, and requested Mr. McGee to describe more specifically than at the last meeting the phenomena observed by him in connection with a severe shock in Summerville.

Mr. MCGEE said that during the tremor the bedstead upon which he lay left the floor from fifteen to thirty times, the departures being roughly estimated at three per second. The clear ascent, as judged from the force of the return blow, ranged from one-fourth inch to two or three inches. The bed stood on the ground floor of a wooden house, supported on piers. Earlier shocks had crushed or driven down the piers under the heavier parts of the house, so that the weight was borne in large part by piers under verandas, etc.

Mr. PAUL said that if the floor in descending separated from the legs of the bedstead its acceleration of motion must exceed that due to gravitation. The fall of the earth manifestly could not be faster than that of the bedstead. Assuming the accuracy of the observation the only possible explanation would seem to be that the floor had behaved as an elastic spring.

Dr. HOWLAND described a shock observed by himself, and said that of some hundreds of chimneys observed by him in Charleston 75 per cent. had fallen to the west.

The PRESIDENT spoke of the bearing of the earthquake upon sanitary matters. The water mains in Charleston had been run in some places through sewers, and there is no assurance that these mains are now in such condition as to render contamination impossible.

Mr. DUTTON inferred from the magnitude of the area through which the shock was felt, as compared with its moderate destructiveness in the central region, that the centrum lay at great depth.

Mr. BELL was much interested in the statement that, even at considerable distances from the centre of disturbance, the noise accompanying the earthquake either preceded the shock or was perceived simultaneously with it. This, he thought, indicated that the sound was of local origin. The great velocity with which the earthquake disturbance had been propagated seemed to him to preclude the idea of a sound-wave from the centre of disturbance as the cause of the noise perceived. Any sound due to this cause should, he thought, at considerable distances, have been observed after the experience of the shock.

He also spoke of the worthlessness of testimony regarding the

direction of sounds proceeding from points below the observer. In this connection he directed attention to experiments relating to Binaural Audition which he had communicated to the American Association for the Advancement of Science in 1879;* and he recommended any one who placed reliance on the testimony that had been adduced relating to the direction of the earthquake noises to try the following experiment:

To one end of a long pole attach an ordinary electric call-bell, and at the other end place a push-knob, by means of which the experimenter can at will ring the bell. Let the person whose credibility as a witness is to be tested stand with his feet considerably apart, with his eyes closed and head still. The experimenter can then silently move the call-bell into any desired position before ringing, and the observer can indicate his appreciation of the direction of the sound by pointing to the place from whence he conceives it to have emanated,

Such being the disposition of the parties the experiment Mr. Bell would recommend is the following: Carefully and silently introduce the end of the pole between the legs of the observer so that the bell is directly underneath him. Now ring and ask your witness to indicate by pointing the position of the bell. He had tried the experiment many times, and had been surprised, and even startled, by the result. The observer usually formed a distinct judgment as to the direction of the sound, but the one feature that was common to all the experiments was *that the indicated direction was wrong.*

Mr. GILBERT remarked that the simultaneous occurrence of detonations and tremors indicated that the sound waves were identical with some at least of the waves constituting the earthquake. It was therefore legitimate to compare the velocity of transmission of the earthquake waves with the velocity of transmission of sound in various media, and such comparison indicates that the portion of the crust traversed by the earthquake waves was characterized by an elasticity between that of gold and that of iron.

Mr. BELL thought that deductions based upon the assumption that the disturbance had been propagated with the velocity of

*The paper was published *in extenso* in the American Journal of Otology for July, 1880, vol. II, p. 169. See also Nature, vol. XXI, p. 310, and vol. XXII, pp. 586-7.

sound should be received with caution; for it is well known that very great and sudden disturbances may be propagated through a medium with a greater velocity than the normal velocity of sound in that medium. In Captain Parry's Arctic expedition it was noticed that distant observers heard the report of cannon before hearing the command to fire.

The PRESIDENT announced that Mr. T. C. MENDENHALL, having removed from the city, had resigned his position on the General Committee of the Society, and that the committee had filled the vacancy by the election of Mr. WILLIAM B. TAYLOR.

291ST MEETING.

NOVEMBER 6, 1886.

Vice-President MALLERY in the Chair.

Twenty-three members and guests present.

Mr. O. T. MASON made a communication on

BOWYERS AND FLETCHERS.

[Abstract.]

Whatever may be our theory of creation, the arts of mankind proceed from the same sources as the genera and species of natural objects. The design of this paper is to demonstrate, by means of an art almost universally dispersed in time and place, that we may regard the implements and products of human industry in the light of biological specimens. They may be divided into families, genera, and species. They may be studied in their several ontogenies (that is, we may watch the unfolding of each individual thing from its raw material to its finished production). They may be regarded as the products of specific evolution out of natural objects serving human wants and up to the most delicate machine performing the same function. They may be modified by their relationship, one to another, in sets, outfits, apparatus, just as the insect and flower are co-ordinately transformed. They observe the law of change under environment and geographical distribution.

The bow, at first, was only an elastic limb or branch transformed little or none at all. From this parent form have developed three

types under the control of the material, namely, the perfect, simple bow, in lands where elastic woods abound; the compound bow, in localities where, by choice or necessity, horn, bone, and antler are preferred as material; and the sinew-backed bow, with its two subtypes of the corded back and the solid back. Each one of these types may be subdivided indefinitely by ethnic marks.

The arrow, at first a reed or twig unmodified, was only a shaft with merely an indication of a head as in some of the lower forms. From this, by a normal evolution, have come the feather, fore-shaft, head, and barbs, differentiating into endless varieties under the stress of material, definite functions, and the thousand and one forces which together we may call its environment.

A large collection of bows and arrows varying in material, form, and origin was exhibited to exemplify the theory set forth.

The communication was discussed by Messrs. TAYLOR, E. FARQUHAR, RILEY, HARKNESS, DALL, and ELLIOTT. Mr. Taylor called attention to the break in the evolutionary history of the bow at its very beginning. The stride from the elastic throwing-stick to the bow is immense. The discussion turned chiefly upon the proper basis for museum classification of ethnological material, Messrs. Riley, Dall, and Elliott advocating a classification primarily by peoples or races, and Mr. Mason defending the evolutionary system, where classification by races is supplemented and traversed by a classification in which articles of a kind are placed together.

Mr. G. K. GILBERT began a communication on

CERTAIN NEW AND SMALL MOUNTAIN RANGES,

which was unfinished when the hour for adjournment arrived.

292D MEETING.

NOVEMBER 20, 1886.

The President in the Chair.

Forty-two members and guests present.

Mr. G. K. GILBERT completed his communication

ON CERTAIN NEW AND SMALL MOUNTAIN RANGES,

and remarks were made by Messrs. BILLINGS and HAZEN.

Mr. THOMAS RUSSELL presented a communication on

NORMAL BAROMETERS,

which was discussed by Messrs. BILLINGS and HARKNESS.

Mr. N. H. DARTON read a paper

ON THE OCCURRENCE OF COPPER ORE IN THE TRIAS OF THE
EASTERN UNITED STATES,

and Mr. J. S. DILLER followed with a communication on

THE LATEST VOLCANIC ERUPTION IN NORTHERN CALIFORNIA AND
ITS PECULIAR LAVA.

[Published in Am. Jour. Sci., 3d series, vol. xxxiii.]

Remarks on the last paper were made by Mr. IDDINGS.

293D MEETING.

DECEMBER 4, 1886.

By courtesy of the trustees of the Columbian University the meeting was held in the law lecture-room of the University building. Invitation to attend the meeting was extended to the members of the Anthropological, Biological, and Chemical societies and of the Cosmos Club. Two hundred and two persons were present.

Vice-President MALLERY presided.

The Chair read a letter from the secretary of the Chemical Society inviting the members of the Philosophical Society to listen, on the evening of Dec. 9, to an address by Prof. H. W. WILEY, retiring president of the Chemical Society, on "Our Sugar Supply."

President BILLINGS then presented his annual address, the subject being

SCIENTIFIC MEN AND THEIR DUTIES.

[Printed in full on pp. xxxv-lvi of this volume.]

A vote of thanks for the address was passed by the audience.

294TH MEETING.

DECEMBER 18, 1886.

THE SIXTEENTH ANNUAL MEETING.

The President in the Chair.

The minutes of the 292d and 293d meetings were read and approved.

The Chair read the order of business as prescribed by the Standing Rules.

The Secretary read the minutes of the fifteenth annual meeting.

The Chair announced the election to membership of Messrs. JOSEPH CLAYBAUGH GORDON, NELSON HORATIO DARTON, MARSHALL McDONALD, WILLIAM LEE TRENHOLM, and WILLIAM FRANCIS HILLEBRAND.

The annual report of the Secretaries was read. [See page XXIX.]

The annual report of the Treasurer was read [see page XXX] and referred to an Auditing Committee, consisting of Messrs. R. S. Woodward, S. M. Burnett, and J. H. Kidder.

The Treasurer read the list of members entitled, under Standing Rule 14, to vote for officers.

After a recess of five minutes, the Society proceeded to the election of officers for the year 1887. [The result of the election appears on page xv.]

The following amendment to the Constitution was offered by Mr. W. H. Dall, and laid on the table, as required by Article VI of the Constitution.

In Article III insert, after "consisting of," the words *the ex-presidents of the Society*.

In Article IV insert, before "other members," the word *nine*. [The effect of the amendment is to make ex-presidents of the Society permanent members of the General Committee.]

The rough minutes of the meeting were then read, and the Society adjourned.



BULLETIN

OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON.

MATHEMATICAL SECTION.



STANDING RULES

OF THE

MATHEMATICAL SECTION.

1. The object of this Section is the consideration and discussion of papers relating to pure or applied mathematics.

2. The special officers of the Section shall be a Chairman and a Secretary, who shall be elected at the first meeting of the Section in each year, and discharge the duties usually attaching to those offices.

3. To bring a paper regularly before the Section it must be submitted to the Standing Committee on Communications for the stated meetings of the Society, with the statement that it is for the Mathematical Section.

4. Meetings shall be called by the Standing Committee on Communications whenever the extent or importance of the papers submitted and approved appear to justify it.

5. All members of the Philosophical Society who wish to do so may take part in the meetings of this Section.

6. To every member who shall have notified the Secretary of the General Committee of his desire to receive them, announcements of the meetings of the Sections shall be sent by mail.

7. The Section shall have power to adopt such rules of procedure as it may find expedient.

OFFICERS

OF THE

MATHEMATICAL SECTION FOR 1886.

Chairman, WM. B. TAYLOR.

Secretary, MARCUS BAKER.

LIST OF MEMBERS WHO RECEIVE ANNOUNCEMENT OF THE MEETINGS.

ABBE, C.	HARKNESS, W.
AVERY, R. S.	HAZEN, H. A.
BAKER, M.	HILL, G. W.
BATES, H. H.	HODGKINS, H. L.
BILLINGS, J. S.	KING, A. F. A.
BURGESS, E. S.	KUMMEL, C. H.
CHRISTIE, A. S.	LEFAVOUR, E. B.
COFFIN, J. H. C.	McGEE, W J
CURTIS, G. E.	MARTIN, A.
DELAND, T. L.	NEWCOMB, S.
DOOLITTLE, M. H.	PAUL, H. M.
EASTMAN, J. R.	RITTER, W. F. M'K.
EIMBECK, W.	ROBINSON, T.
ELLIOTT, E. B.	SMILEY, C. W.
FARQUHAR, H.	STONE, O.
FLINT, A. S.	TAYLOR, W. B.
GILBERT, G. K.	UPTON, W. W.
GORE, J. H.	WINLOCK, W. C.
GREEN, B. R.	WOODWARD, R. S.
HALL, A.	ZIWET, A.

BULLETIN
OF THE
MATHEMATICAL SECTION.

22D MEETING.

MARCH 24, 1886.

The Chairman, Mr. G. W. HILL, presided.

Present, fourteen members and one invited guest.

Election of officers of the section for the year 1886 was conducted by ballot, and resulted in the choice of Mr. W. B. TAYLOR as chairman and Mr. MARCUS BAKER as secretary.

Mr. HENRY FARQUHAR made a communication on

A COMPARISON OF THE BOSS AND AUWERS DECLINATION
STANDARDS,

in which the systematic difference between the standard of Dr. Auwers' "Fundamental-Catalog" and the "Normal System of Prof. Boss was considered as a function of declination, and shown to be almost completely explained by the supposition of a tube-flexure inadequately allowed for, in the observations on which one or other standard depends.

[A paper covering the same ground was afterward read by Mr. FARQUHAR before the American Association for the Advancement of Science, and an abstract of it will appear in the proceedings of that body for the Buffalo meeting, 1886.]

The paper was briefly discussed by Messrs. HALL, HILL, and WOODWARD.

Mr. R. S. WOODWARD then read a paper entitled

ON THE POSITION AND SHAPE OF THE GEOID AS DEPENDENT ON
LOCAL MASSES.

[This will be published as a Bulletin of the United States Geological Survey.]

23D MEETING.

APRIL 14, 1886.

The Chairman, Mr. WILLIAM B. TAYLOR, elected at the last meeting, presided, and upon taking the chair offered a few remarks expressive of his appreciation of the honor conferred upon him and of his desire for the prosperity of the Section.

Present, seventeen members and one guest.

Mr. R. S. WOODWARD recited, in abstract, the principal points of his paper of the preceding meeting, and there ensued a general discussion of the subject, in which Messrs. BAKER, DOOLITTLE, HILL, PAUL, THOMAS RUSSELL, STONE, TAYLOR, AND WOODWARD participated.

Mr. C. H. KUMMELL then presented a paper

ON THE USE OF SOMOFF'S THEOREM FOR EVALUATION OF THE
ELLIPTIC INTEGRAL OF THE THIRD SPECIES.

[This paper will appear in full in *Annals of Mathematics*, vol. 2, Nos. 4 and 5.]

Remarks were made by Mr. HILL.

INDEX.

	Page.		Page.
Address of the President.....	xxxv, 46	Clarke, F. W. : cited on the relations of Government to chemistry	xlv, 1
Administration of research.....	xlii	— remarks on problematic cells.....	35
Amendment to the constitution.....	47	Committee on communications.....	xiv, xv
American Historical Association, Invitation from the.....	22	— publications.....	xiv, xv
Annual meeting.....	47	— Report of auditing.....	3
Anthropological Society, Invitation from the	15	— Rules of the general.....	xii
Appalachian region, Physical divisions of the.....	22	Comparison of the Boss and Auwers declination standards	53
Arctic exploration.....	8	Constitution.....	vii
Arrow, Development of the.....	44	Constitution, Proposed amendment to.....	47
Auditing committee, Appointment of.....	47	Cummings, G. J., Election to membership of	15
— Report of.....	3	Curtice, Cooper, Election to membership of	37
Bates, Newton L. : communication on organic cells of unknown origin and form found in human feces.....	35	Curtis, George E. : communication on Lieut. Lockwood's expedition to farthest north	8
— election to membership.....	37	Customs of every day life.....	19
Bean, T. H. : communication on the distribution of fishes in the oceanic abysses and middle strata (<i>Title</i>).....	22	Dall, W. H. : offers amendment to the constitution of the Society.....	47
Bell, A. Graham : remarks on aural determination of the direction of sound.....	42	— remarks on museum classification.....	45
— remarks on identity of sound and earthquake-waves.....	43	Darton, N. H. : communication on the occurrence of copper ore in the Trias of the eastern United States (<i>Title</i>).....	46
Beyer, H. G., Election to membership of.....	37	— Election to membership of.....	47
Bibliography of faults of the Great Basin....	6	Deceased members.....	xxvi
Billings, J. S. : annual address as President.....	xxxv, 46	Declination standards.....	53
— communication on museum specimens illustrating biology.....	35	Diller, J. S. : communication on the geology of northern California.....	4, 8
— remarks on the Charleston earthquake... ..	42	— — — latest volcanic eruption in northern California and its peculiar lava (<i>Title</i>)	46
Bowyers and fletchers.....	44	Doolittle, M. H. : remarks on a phonetic alphabet.....	19
Bryan, J. H., Election to membership of.....	25	Duties of scientific men.....	xxxv
Bulletin, Rules for publication of.....	xiii	Earthquakes.....	37, 38
Calendar.....	xxviii	Effects of solar radiation upon thermometer bulbs having different metallic coverings..	33
California, Notes on geology of northern.....	4	Election of officers.....	47
Cells, Problematic.....	35	Elliott, E. B. : communication on the annual profit to banks of national bank note circulation (<i>Title</i>).....	14
Ceremonial institutions.....	19	— — — quantity of United States subsidiary silver coin existing and in circulation (<i>Title</i>).....	14
Chamberlin, T. C. : communication on the varying attitudes of former level surfaces in the Great Lake region and the applicability of proposed explanations (<i>Title</i>).....	15, 16	— remarks on museum classification.....	45
Charleston earthquake.....	37, 38	Farquhar, Henry : communication on a comparison of the Boss and Auwers declination standards.....	53
Chemical Society of Washington, Invitation from the.....	46		

Page.	Page.		
Farquhar, Henry: communication on a phonetic alphabet.....	17	Lucas, Frederick A.: communication on museum specimens illustrating biology (Title).....	36
Faults of the Great Basin and Sierra Nevada	5	McAdie, A. G., Election to membership of...	19
Fletchers and bowyers.....	44	McDonald, Marshall, Election to membership of.....	47
General committee, Rules of.....	xii	McGee, W J: communication on the Charleston earthquake.....	37
— meeting, Minutes of.....	3	— remarks on the Charleston earthquake....	42
Geology of northern California.....	4	Mallery, Garrick: communication on customs of every day life.....	19
Gilbert, G. K.: communication on certain new and small mountain ranges (Title)..	45	— remarks on phonetic alphabets.....	18
— — — the observed changes of level surfaces in the Bonneville area, and their explanation (Title).....	15	Mann, B. Pickman: election to membership	3
— — — recent changes of level in the basin of Lake Ontario (Title).....	8	— remarks on throwing sticks.....	14
— remarks on geology of Sierra Nevada.....	7	Martin, Artemas, Election to membership of	16
— — — the Charleston earthquake.....	43	Mason, O. T.: communication on bowyers and fletchers.....	44
Goode, G. Brown: communication on the distribution of fishes in the oceanic abysses and middle strata (Title).....	22	— — — two examples of similar inventions in areas widely apart.....	12
— — — museum specimens illustrating biology (Title).....	36	— remarks on derivation of social customs..	21
Gordon, J. C., Election to membership of....	47	Mathematical section, Members of.....	52
Governmental administration of research... xlii		— — Minutes of.....	53
Great Basin, Faults of the.....	5	— — Officers of.....	52
Hall, Asaph: communication on the images of the stars (Title).....	15	— — Rules of.....	51
— — — new star of Andromeda (Title).....	14	Members, Deceased.....	xxvi
Hayden, Everett: communication on the Charleston earthquake.....	38	— List of.....	xvi
Hazen, H. Allen: communication on effects of solar radiation upon thermometer bulbs having different metallic coverings	33	— New.....	xxix, 3, 15, 16, 19, 25, 37, 47
Hill, R. T., Election to membership of.....	19	Mendenhall, T. C.: communication on the Charleston earthquake.....	37
Hillebrand, W. F., Election to membership of	47	— remarks on Japanese customs.....	21
Hitchcock, Romyn: communication on recent improvements in microscopic objectives, with demonstration of the resolving power of a new 1-16 inch (Title)..	16	— resignation from General Committee.....	44
Howland, Dr. E. P.: remarks on the Charleston earthquake.....	38	Merrill, George P.: communication on geological museums (Title).....	36
Irving, R. D.: communication on the enlargement of mineral fragments as a factor in rock alteration (Title).....	16	Metallic coverings of thermometer bulbs... 33	
— election to membership.....	16	Minutes of the General Meeting.....	3
Institutions, Ceremonial.....	19	Mitchell, Henry, Election to membership of	37
Kenaston, C. A., Election to membership of	16	Murdoch, John: remarks on throwing sticks.....	13, 14
Kidder, J. H.: communication entitled, historical sketch of deep sea temperature observations (Title).....	14	Museum classification.....	45
— — — the gilding of thermometer bulbs (Title).....	33	Museum specimens illustrating biology.....	35
Kummell, C. H.: communication on the use of Somoff's theorem for the evaluation of the elliptic integral of the third species.....	54	Mussey, R. D.: communication entitled, when I first saw the cholera <i>Bacillus</i> (Title).....	22
		— remarks on phonetic alphabets.....	18
		New members.....	xxix, 3, 15, 16, 19, 25, 37, 47
		Notes on the faults of the Great Basin and of the eastern base of the Sierra Nevada...	5
		— — — geology of northern California.....	4
		Nott, C. C., Election to membership of.....	3
		Officers of Army and Navy in relation to scientific work.....	xlix
		— elected December, 1885.....	xiv
		— — — 1886.....	xv
		Organic cells of unknown origin and form found in human feces.....	35

Page.		Page.
41, 42	Paul, H. M.: communication on the Charleston earthquake.....	20
17	Phonetic alphabet.....	xiv, xv
22	Physical-geographical divisions of the southeastern portions of the United States and their corresponding topographical types.....	xii
xxxv, 46	President's address.....	51
xxix, 47	Report, Annual, of the secretaries.....	ix
xxx, 47	— — — treasurer.....	13
3	— of auditing committee.....	44
45	Riley, C. V.: remarks on museum classification.....	54
37	Rockwood, Prof. Charles G.: communication on the Charleston earthquake.....	45
xiii	Rules for publication of Bulletin.....	25
xii	— of the General Committee.....	25, 33
51	— — — Mathematical Section.....	22
ix	— — — Society.....	13
5	Russell, I. C.: communication on faults of the Great Basin and the eastern base of the Sierra Nevada.....	xxx, 47
16	— — — the subaerial decay of rocks and the origin of the red clay of certain formations (<i>Title</i>).....	47
46	Russell, Thomas: communication on normal barometers (<i>Title</i>).....	12
25	— — — temperatures at which differences between mercurial and air thermometers are greatest.....	15
xxxv	Scientific men and their duties.....	53, 54
xxix, 47	Secretaries, Annual report of.....	
4, 5	Sierra Nevada, Faults of the.....	
12	Similar inventions in areas widely apart.....	
25	Snell, M. M., Election to membership of.....	
	Spencer, Herbert: cited on ceremonial institutions.....	
	Standing committees.....	
	Standing rules of the General Committee.....	
	— — — Mathematical Section.....	
	— — — Society.....	
	Stitch in basketry.....	
	Taylor, W. B.: appointment to vacancy in General Committee.....	
	— remarks as chairman of Mathematical Section.....	
	— — on the evolution of the bow.....	
	Temperatures at which differences between mercurial and air thermometers are greatest.....	
	Thermometry.....	
	Thompson, Gilbert: communication on the physical-geographical divisions of the southeastern portion of the United States and their corresponding topographical types.....	
	Throwing sticks.....	
	Treasurer, Annual report of.....	
	Trenholm, W. L.: election to membership.....	
	Two examples of similar inventions in areas widely apart.....	
	Willis, Bailey: remarks on geology of Cascade Mountains.....	
	Woodward, R. S.: communication on the changes of terrestrial level surfaces due to variations in distribution of superficial matter (<i>Title</i>).....	
	— — — position and shape of the geoid as dependent on local masses (<i>Title</i>).....	



BULLETIN
OF THE
PHILOSOPHICAL SOCIETY
OF
WASHINGTON.

VOL. X.

1887.

Containing the Minutes of the Society and of the Mathematical
Section for the year 1887; together with the pro-
ceedings of the Baird Memorial Meeting

AND

AN INDEX TO THE FIRST TEN VOLUMES.

PUBLISHED BY THE CO-OPERATION OF THE SMITHSONIAN INSTITUTION.

WASHINGTON:
1888.



CONTENTS.

	Page.
Constitution -----	VII
Standing Rules of the Society -----	IX
Standing Rules of the General Committee -----	XII
Rules for the Publication of the Bulletin -----	XIII
Officers elected December 18, 1886 -----	XIV
Officers elected December 21, 1887 -----	XV
List of Members -----	XXVII
List of Deceased Members -----	XXVIII
Summary of Membership -----	XXIX
Calendar -----	XXXI
Annual Report of the Secretaries -----	XXXII
Annual Report of the Treasurer -----	XXXIV
Annual Address of the President, William Harkness -----	XXXIX
Bulletin of the General Meetings -----	1
Report of the Auditing Committee -----	3
Graphic methods in research, G. K. Gilbert -----	4
Geologic age of the lowest formation of Emmon's Taconic system, C. D. Walcott, (<i>Title only</i>) -----	5
Present status of mineralogy, F. W. Clarke, (<i>Title only</i>) -----	6
Topography and geology of the cross timbers of Texas, R. T. Hill, (<i>Title only</i>) -----	6
Sky glows of 1883, H. A. Hazen, (<i>Title only</i>) -----	6
Topography and structure in the Bays Mountains, Tennessee, Bailey Willis, (<i>Title only</i>) -----	7
Geographical distribution of scientific men and institutions in the United States, G. Brown Goode, (<i>Title only</i>) -----	7
Our city shade trees, their foes and their future, C. V. Riley, (<i>Title only</i>) -----	7
Frequency of coincidences, Lester F. Ward -----	8
Theory of the wind-vane, G. E. Curtis, (<i>Title only</i>) -----	9
Electrometer as used in observations of atmospheric electricity, C. F. Marvin, (<i>Title only</i>) -----	9
Development of perspective map from contour map, Bailey Willis, (<i>Title only</i>) -----	9
Plane table exhibited and explained, W. D. Johnson -----	9
Relation between wind velocity and pressure, H. A. Hazen, (<i>Title only</i>) -----	10
Mt. Rainier and its glaciers, Bailey Willis -----	10
What is a topographic map? Marcus Baker -----	11
Counting-out rhymes of children, H. C. Bolton, (<i>Title only</i>) -----	13
On a device for viewing the sun by light of any desired wave length, William Harkness -----	13
What is topography? by M. H. Doolittle, W. D. Johnson, H. G. Ogden, Gilbert Thompson -----	14, 15
The Muir glacier, Alaska, J. W. Chickering, (<i>Title only</i>) -----	15
Economic phase of the English sparrow question, C. Hart Merriam, (<i>Title only</i>) -----	16
The quaternary deposits and the great displacement of the middle Atlantic slope, W J McGee, (<i>Title only</i>) -----	16
Visit to scene of Charleston earthquake and resulting conclusions, C. E. Dutton, (<i>Title only</i>) -----	16

	Page.
South Florida notes, W. H. Dall, (<i>Title only</i>) -----	16
Depth of earthquake foci, C. E. Dutton -----	17
Manchester meeting of the British Association for the advance- ment of Science, 1887, F. W. Clarke, (<i>Title only</i>) -----	19
Signal Service bibliography of meteorology, C. Abbe -----	20
Geographical distribution of fossil plants, L. F. Ward, (<i>Title only</i>) -----	28
Speed of propagation of the Charleston earthquake, C. E. Dutton and Simon Newcomb, (<i>Title only</i>) -----	28
Representation of comet orbits by models, William Harkness, (<i>Title only</i>) -----	28
Statistics of the Philosophical Society, G. K. Gilbert -----	29
Newton's <i>vis</i> , M. H. Doolittle, (<i>Title only</i>) -----	38
Reference indexing, B. Pickman Mann -----	38
Presentation of the annual address -----	39
Annual meeting -----	39
Proceedings at the Baird memorial meeting -----	41
Introduction -----	43
Relation of Professor Baird to participating societies, Garrick Mallery -----	45
Professor Baird as administrator, Wm. B. Taylor -----	49
Professor Baird in science, W. H. Dall -----	61
Personal characteristics of Professor Baird, J. W. Powell -----	71
Bulletin of the Mathematical Section -----	79
Standing rules of the section -----	81
List of officers and members of the section -----	82
Association ratios, M. H. Doolittle -----	83
The rotten apple problem, a question in probabilities, Marcus Baker, M. H. Doolittle, G. W. Hill, G. E. Curtis, E. B. Elliott, Henry Farquhar, Artemas Martin, Alex. S. Christie, Ormond Stone -----	87-89
Free cooling of a homogeneous sphere, R. S. Woodward, (<i>Title only</i>) -----	90
Brachisthode on the helicoid, C. H. Kummell -----	90
Motion of Hyperion, G. W. Hill -----	90
Parallax of α Tauri, Asaph Hall -----	91
Most probable value of latitude from entangled observations in use of Talcott's method, A. S. Flint -----	91
Mutual action of elements of electric currents, E. B. Elliott -----	92
Association ratios, M. H. Doolittle -----	93
Solution of a problem in <i>Science</i> , Henry Farquhar, (<i>Title only</i>) -----	96
Solutions of the trisection problem, Marcus Baker, G. E. Curtis -----	96, 98
Integration of differential equations admitting periodic inte- grals, G. W. Hill -----	100
Euler's theorem (generally called Lambert's), Asaph Hall -----	101
New form of computing machine, E. B. Elliott -----	102
The constant P in observations of terrestrial magnetism, Wm. Harkness -----	102
Conditioned cooling of a homogeneous sphere, R. S. Woodward -----	103
The orbit of Hyperion, Ormond Stone -----	104
Quotients of space-directed lines, E. B. Elliott -----	105
Methods of finding n^{th} power numbers whose sum is an n^{th} power, Artemas Martin -----	107
Committees on mathematical communications -----	111
Note on the publications of the Society -----	113
Index to Volumes I-X -----	117

BULLETIN
OF THE
PHILOSOPHICAL SOCIETY OF WASHINGTON.

CONSTITUTION, RULES,
LISTS OF
OFFICERS AND MEMBERS,
CALENDAR,
AND REPORTS OF
SECRETARIES AND TREASURER.



CONSTITUTION
OF
THE PHILOSOPHICAL SOCIETY OF WASHINGTON.

ARTICLE I. The name of this Society shall be THE PHILOSOPHICAL SOCIETY OF WASHINGTON.

ARTICLE II. The officers of the Society shall be a President, four Vice-Presidents, a Treasurer, and two Secretaries.

ARTICLE III. There shall be a General Committee, consisting of the ex-Presidents of the Society, the officers of the Society, and nine other members.*

ARTICLE IV. The officers of the Society and the *nine* other members of the General Committee shall be elected annually by ballot; they shall hold office until their successors are elected, and shall have power to fill vacancies.*

ARTICLE V. It shall be the duty of the General Committee to make rules for the government of the Society, and to transact all its business.

ARTICLE VI. This constitution shall not be amended except by a three-fourths vote of those present at an annual meeting for the election of officers, and after notice of the proposed change shall have been given in writing at a stated meeting of the Society at least four weeks previously.

* Amended December 21, 1887.



STANDING RULES

FOR THE GOVERNMENT OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON.

1. The Stated Meetings of the Society shall be held at 8 o'clock P. M. on every alternate Saturday; the place of meeting to be designated by the General Committee.

2. Notice of the time and place of meeting shall be sent to each member by one of the Secretaries.

When necessary Special Meetings may be called by the President.

3. The Annual Meeting for the election of officers shall be the last stated meeting in the month of December.

The order of proceedings (which shall be announced by the Chair) shall be as follows :

First, the reading of the minutes of the last Annual Meeting.

Second, the presentation of the annual reports of the Secretaries, including the announcement of the names of members elected since the last Annual Meeting.

Third, the presentation of the annual report of the Treasurer.

Fourth, the announcement of the names of members who, having complied with section 14 of the Standing Rules, are entitled to vote on the election of officers.

Fifth, the election of President.

Sixth, the election of four Vice-Presidents.

Seventh, the election of Treasurer.

Eighth, the election of two Secretaries.

Ninth, the election of nine members of the General Committee.

Tenth, the consideration of Amendments to the Constitution of the Society, if any such shall have been proposed in accordance with Article VI of the Constitution.

Eleventh, the reading of the rough minutes of the meeting.

4. *Elections of officers are to be held as follows :

In each case nominations shall be made by means of an informal

* Amended May 7, 1887.

ballot, the result of which shall be announced by the Secretary; after which the first formal ballot shall be taken.

In the ballot for Vice-Presidents, Secretaries, and members of the General Committee, each voter shall write on one ballot as many names as there are officers to be elected, viz., four on the first ballot for Vice-Presidents, two on the first for Secretaries, and nine on the first for members of the General Committee; and on each subsequent ballot as many names as there are persons yet to be elected; and those persons who receive a majority of the votes cast shall be declared elected; *Provided* that the number of persons receiving a majority does not exceed the number of persons to be elected, in which case the vacancies shall be filled by the candidates receiving the highest majorities.

If in any case the informal ballot result in giving a majority for any of the candidates, it may be declared formal by a majority vote.

5. The Stated Meetings, with the exception of the Annual Meeting, shall be devoted to the consideration and discussion of scientific subjects.

The Stated Meeting next preceding the Annual Meeting shall be set apart for the delivery of the President's Annual Address.

6. Sections representing special branches of science may be formed by the General Committee upon the written recommendation of twenty members of the Society.

7. Persons interested in science, who are not residents of the District of Columbia, may be present at any meeting of the Society, except the Annual Meeting, upon invitation of a member.

8. On request of a member, the President or either of the Secretaries may, at his discretion, issue to any person a card of invitation to attend a specified meeting. Five cards of invitation to attend a meeting may be issued in blank to the reader of a paper at that meeting.

9. Invitations to attend during three months the meetings of the Society and participate in the discussion of papers, may, by a vote of nine members of the General Committee, be issued to persons nominated by two members.

10. Communications intended for publication under the auspices of the Society shall be submitted in writing to the General Committee for approval.

11. Any paper read before a Section may be repeated, either entire or by abstract, before a general meeting of the Society, if such repetition is recommended by the General Committee of the Society.

12. It is not permitted to report the proceedings of the Society or its Sections for publication, except by authority of the General Committee.

13. *New members may be proposed in writing by three members of the Society for election by the General Committee; but no person shall be admitted to the privileges of membership unless he signifies his acceptance thereof in writing, and pays his dues to the Treasurer, within two months after notification of his election.

14. Each member shall pay annually to the Treasurer the sum of five dollars, and no member whose dues are unpaid shall vote at the Annual Meeting for the election of officers, or be entitled to a copy of the Bulletin.

In the absence of the Treasurer, the Secretary is authorized to receive the dues of members.

The names of those two years in arrears shall be dropped from the list of members.

Notice of resignation of membership shall be given in writing to the General Committee through the President or one of the Secretaries.

15. The fiscal year shall terminate with the Annual Meeting.

16. Any member who is absent from the District of Columbia for more than twelve consecutive months may be excused from payment of dues during the period of his absence, in which case he will not be entitled to receive announcements of meetings or current numbers of the Bulletin.

17. Any member not in arrears may, by the payment of one hundred dollars at any one time, become a life member, and be relieved from all further annual dues and other assessments.

All moneys received in payment of life membership shall be invested as portions of a permanent fund, which shall be directed solely to the furtherance of such special scientific work as may be ordered by the General Committee.

*Amended Oct. 9, 1886.

STANDING RULES

OF THE

GENERAL COMMITTEE OF THE PHILOSOPHICAL SOCIETY OF WASHINGTON.

1. The President, Vice-Presidents, and Secretaries of the Society shall hold like offices in the General Committee.

2. The President shall have power to call special meetings of the Committee, and to appoint Sub-Committees.

3. The Sub-Committees shall prepare business for the General Committee, and perform such other duties as may be entrusted to them.

4. There shall be two Standing Sub-Committees; one on Communications for the Stated Meetings of the Society, and another on Publications.

5. The General Committee shall meet at half-past seven o'clock on the evening of each Stated Meeting, and by adjournment at other times.

6. For all purposes, except for the amendment of the Standing Rules of the Committee or of the Society, and the election of members, six members of the Committee shall constitute a quorum.

7. The names of proposed new members recommended in conformity with Section 13 of the Standing Rules of the Society, may be presented at any meeting of the General Committee, but shall lie over for at least four weeks before final action, and the concurrence of twelve members of the Committee shall be necessary to election.

The Secretary of the General Committee shall keep a chronological register of the elections and acceptances of members.

8. These Standing Rules, and those for the government of the Society, shall be modified only with the consent of a majority of the members of the General Committee.

RULES

FOR THE

PUBLICATION OF THE BULLETIN

OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON.

1. The President's Annual address shall be published in full.
2. The annual reports of the Secretaries and of the Treasurer shall be published in full.
3. When directed by the General Committee, any communication may be published in full.
4. Abstracts of papers and remarks on the same will be published, when presented to the Secretary by the author in writing within two weeks of the evening of their delivery, and approved by the Committee on Publications. Brief abstracts prepared by one of the Secretaries and approved by the Committee on Publications may also be published.
5. If the author of any paper read before a Section of the Society desires its publication, either in full or by abstract, it shall be referred to a committee to be appointed as the Section may determine.
The report of this committee shall be forwarded to the Publication Committee by the Secretary of the Section, together with any action of the Section taken thereon.
6. Communications which have been published elsewhere, so as to be generally accessible, will appear in the Bulletin by title only, but with a reference to the place of publication, if made known in season to the Committee on Publications.

OFFICERS

OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON

ELECTED DECEMBER 21, 1887.

<i>President</i>	GARRICK MALLERY.	
<i>Vice-Presidents</i>	J. R. EASTMAN.	C. E. DUTTON.
	G. K. GILBERT.	G. BROWN GOODE.
<i>Treasurer</i>	ROBERT FLETCHER.	
<i>Secretaries</i>	MARCUS BAKER.	W. C. WINLOCK.

MEMBERS AT LARGE OF THE GENERAL COMMITTEE.

H. H. BATES.	F. W. CLARKE.
W. H. DALL.	E. B. ELLIOTT.
J. H. KIDDER.	S. P. LANGLEY.
H. M. PAUL.	C. V. RILEY.

R. S. WOODWARD.

PAST PRESIDENTS OF THE SOCIETY AND EX-OFFICIO MEMBERS OF THE GENERAL COMMITTEE.

J. S. BILLINGS, 1886.	SIMON NEWCOMB, 1879, 1880.
ASAPH HALL, 1885.	J. W. POWELL, 1883.
WM. HARKNESS, 1887.	W. B. TAYLOR, 1882.
J. C. WELLING, 1884.	

STANDING COMMITTEES.

On Communications :

G. K. GILBERT, *Chairman*. J. R. EASTMAN. G. BROWN GOODE.

On Publications :

MARCUS BAKER, *Chairman*. ROBERT FLETCHER. W. C. WINLOCK.
S. P. LANGLEY.



LIST OF MEMBERS

OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON;

TOGETHER WITH

YEAR OF ADMISSION TO THE SOCIETY, POST-OFFICE
ADDRESS, AND RESIDENCE.

Corrected to December 31, 1887.

- | | |
|--|--|
| 1871. ABBE, Prof. Cleveland,
Signal Office, War Department. | 2017 I street. |
| 1875. ABERT, Mr. S. T. (Sylvanus Thayer) | 810 19th street. |
| 1881. ADAMS, Mr. Henry, | 1603 H street. |
| 1873. ALDIS, Hon. A. O. (Asa Owen), | 1765 Mass. avenue. |
| 1871. ANTISELL, Dr. Thomas (<i>Founder</i>),
Patent Office. | 1311 Q street. |
| 1879. AVERY, Mr. Robert S. (Robert Stanton), | 320 A street se. |
| 1887. BABCOCK, Mr. Wm. H. (William Henry),
P. O. Box 220. | |
| 1881. BAKER, Prof. Frank, | 1315 Corcoran street. |
| 1876. BAKER, Mr. Marcus,
Geological Survey. | 1125 17th street. |
| 1875. BANCROFT, George, | 1623 H street; in summer, Newport, R. I. |
| 1885. BARUS, Dr. Carl,
Geological Survey. | 2750 Q street. |
| 1871. BATES, Mr. H. H. (Henry Hobart),
Patent Office. | The Portland. |
| 1886. BATES, Dr. N. L. (Newton Lemuel), U. S. N.,
283 Henry street, Brooklyn, N. Y. | |
| 1884. BEAN, Dr. T. H. (Tarleton Hoffman),
National Museum. | 1616 19th street |

XVIII PHILOSOPHICAL SOCIETY OF WASHINGTON.

1875. BEARDSLEE, Capt. L. A. (Lester Anthony), U. S. N. (*Absent*),
Little Falls, N. Y.
1879. BELL, Mr. A. Graham (Alexander Graham),
1336 19th street.
1881. BELL, Dr. C. A. (Chichester Alexander) (*Absent*),
University College. London, England.
1871. BENÉT, Gen. S. V. (Stephen Vincent), U. S. A. (*Founder*),
Ordnance Office, War Dept. 1717 I street.
1875. BESSELS, Dr. Emil,
Glenn Dale, Md.
1886. BEYER, Dr. H. G. (Henry Gustav) (*Absent*),
Navy Department.
1871. BILLINGS, Dr. John S. (John Shaw), U. S. A. (*Founder*),
Army Medical Museum. 3027 N street.
1876. BIRNIE, Capt. Rogers, Jr., U. S. A.,
Office Chief of Ordnance, U. S. A. 1841 N. H. avenue.
1883. BODFISH, Mr. S. H. (Sumner Homer),
Geological Survey. 807 H street.
1884. BOUTELLE, Capt. C. O. (Charles Otis),
Coast and Geodetic Survey.
1884. BOWLES, Asst. Nav. Constr. Francis T. (Francis Tiffany),
U. S. N. (*Absent*),
Navy Department.
1884. BROWN, Prof. S. J. (Stimson Joseph), U. S. N. (*Absent*),
Washburn Observatory. Madison, Wis.
1883. BROWNE, Dr. J. Mills (John Mills), U. S. N.,
Navy Department. The Portland.
1886. BRYAN, Dr. J. H. (Joseph Hammond),
1644 Connecticut avenue.
1883. BURGESS, Mr. E. S. (Edward Sandford),
High School. 1120 13th street.
1879. BURNETT, Dr. Swan M. (Swan Moses),
1734 K street.
1874. BUSEY, Dr. Samuel C. (Samuel Clagett),
901 16th street.
1871. CASEY, Col. Thomas Lincoln, U. S. A. (*Founder, absent*),
Army Building, cor. Green and Houston Sts., New York city.
1882. CAZIARC, Lieut. L. V. (Louis Vasmer), U. S. A. (*Absent*),
Fortress Monroe, Va.
1883. CHAMBERLIN, Pres. T. C. (Thomas Crowder) (*Absent*),
Madison, Wis.
1885. CHATARD, Dr. Thomas M. (Thomas Marean),
Geological Survey. Cosmos Club.
1874. CHICKERING, Prof. J. W., Jr. (John White),
Deaf Mute College, Kendall Green.
1880. CHRISTIE, Mr. Alex. S. (Alexander Smyth),
Coast and Geodetic Survey. 204 4th street se.

1877. CLARK, Mr. Edward,
Architect's Office, Capitol. 417 4th street.
1874. CLARKE, Prof. F. W. (Frank Wigglesworth),
Geological Survey. 1425 Q street.
1871. COFFIN, Prof. J. H. C. (John Huntington Crane), U. S. N.
(*Founder*),
1901 I street.
1880. COMSTOCK, Prof. J. H. (John Henry) (*Absent*),
Cornell University, Ithaca, N. Y.
1874. COUES, Prof. Elliott,
Smithsonian Institution. 1726 N street.
1873. CRAIG, Lieut. Robert, U. S. A. (*Absent*),
War Department.
1879. CRAIG, Dr. Thomas (*Absent*),
Johns Hopkins University, Baltimore, Md.
1886. CUMMINGS, Prof. G. J. (George Jotham),
Howard University.
1886. CURTICE, Dr. Cooper,
Agricultural Department.
1884. CURTIS, Mr. Geo. E. (George Edward) (*Absent*),
Washburn College, Topeka, Kansas.
1871. DALL, Mr. Wm. H. (William Healey) (*Founder*),
Smithsonian Institution. 1119 12th street.
1886. DARTON, Mr. N. H. (Nelson Horatio),
Geological Survey. 1412 N street.
1880. DAVIS, Commander C. H. (Charles Henry), U. S. N.,
Navy Department.
1872. DEAN, Dr. R. C. (Richard Crain), U. S. N. (*Absent*),
Navy Department. 45 Lafayette Place, N. Y. city.
1881. DE CAINDRY, Mr. Wm. A. (William Augustin),
War Department. 1014 17th street.
1884. DEWEY, Mr. Fred. P. (Frederic Perkins),
National Museum. Lanier Heights.
1884. DILLER, Mr. J. S. (Joseph Silas),
Geological Survey. 1804 16th street.
1876. DOOLITTLE, Mr. M. H. (Myrick Hascall),
Coast and Geodetic Survey. 1925 I street.
1873. DUNWOODY, Lt. H. H. C. (Henry Harrison Chase), U. S. A.
(*Absent*),
War Department.
1872. DUTTON, Capt. C. E. (Clarence Edward), U. S. A.,
Geological Survey. 2119 H street.
1884. EARLL, Mr. R. Edward (Robert Edward),
National Museum. 1336 T street.
1871. EASTMAN, Prof. J. R. (John Robie), U. S. N.,
Naval Observatory. 1905 N street.
1884. EIMBECK, Mr. William,
Coast and Geodetic Survey.

1871. ELDREDGE, Dr. Stewart (*Absent*),
Yokohama, Japan.
1871. ELLIOTT, Mr. E. B. (Ezekiel Brown) (*Founder*),
Gov't Actuary, Treas. Dept. 1210 G street.
1883. EMMONS, Mr. S. F. (Samuel Franklin),
Geological Survey. 1708 H street.
1873. ENDLICH, Dr. F. M. (Frederic Miller) (*Absent*),
Reading, Pa.
1874. EWING, Gen. Hugh (*Absent*),
Lancaster, Ohio.
1876. FARQUHAR, Mr. Edward,
Patent Office Library. 1915 H street.
1881. FARQUHAR, Mr. Henry,
Coast and Geodetic Survey. Brooks Station, D. C.
1887. FERNOW, Mr. B. E. (Bernhard Eduard),
Department of Agriculture. Cor. 8th and B streets sw.
1872. FERREL, Prof. William,
1641 Broadway, Kansas City, Mo.
1873. FLETCHER, Dr. Robert,
Army Medical Museum. The Portland.
1882. FLINT, Mr. A. S. (Albert Stowell),
Naval Observatory. 1441 Chapin street.
1881. FLINT, Dr. J. M. (James Milton), U. S. N.,
Smithsonian Institution. The Portland.
1873. FRISTOE, Prof. Edward T,
Columbian University, cor. 15th and H streets.
1875. GALLAUDET, President E. M. (Edward Miner),
Deaf Mute College, Kendall Green.
1874. GANNETT, Mr. Henry,
Geological Survey. 1881 Harewood ave., LeDroit Park.
1873. GILBERT, Mr. G. K. (Grove Karl),
Geological Survey. 1424 Corcoran street.
1879. GODDING, Dr. W. W. (William Whitney),
Government Hospital for the Insane.
1885. GOOCH, Dr. F. A. (Frank Austin) (*Absent*),
Yale College, New Haven, Connecticut.
1874. GOODE, Mr. G. Brown (George Brown),
Smithsonian Institution. 1203 N. H. ave.
1875. GOODFELLOW, Mr. Edward,
Coast and Geodetic Survey.
1886. GORDON, Prof. J. C. (Joseph Claybaugh),
Deaf Mute College, Kendall Green.
1880. GORE, Prof. J. H. (James Howard),
Columbian University. 1305 Q street.
1878. GRAVES, Mr. Walter H. (Walter Hayden) (*Absent*),
Denver, Colorado.
1880. GREELY, Gen. A. W. (Adolphus Washington), U. S. A.,
Signal Office, War Department. 1914 G street.

1879. GREEN, Mr. Bernard R. (Bernard Richardson),
Office of Building for State, War, and
Navy Departments. 1738 N street.
1875. GREEN, Commander F. M. (Francis Mathews), U. S. N.
(*Absent*),
Navy Department.
1871. GREENE, Prof. B. F. (Benjamin Franklin), U. S. N. (*Founder*,
absent),
West Lebanon, N. H.
1875. GREENE, Francis V. (Francis Vinton) (*Absent*),
No. 1, Broadway, New York city.
1884. GREGORY, Dr. J. M. (John Milton) (*Absent*),
45 Albert st., Regent's Park, London, England.
1879. GUNNELL, Surg. Gen'l F. M. (Francis M.), U. S. N.,
Navy Department. 600 20th street.
1879. HAINS, Lt.-Col. P. C. (Peter Conover), U. S. A.,
Engineer's Office, Potomac River Improve-
ment, 2136 Pa. ave. 1824 Jefferson place.
1871. HALL, Prof. Asaph, U. S. N. (*Founder*),
Naval Observatory. 2715 N street.
1884. HALL, Mr. Asaph, Jr. (*Absent*),
Yale Observatory, New Haven, Conn.
1885. HALLOCK, Dr. William,
Geological Survey. 2923½ M street.
1885. HAMPSON, Mr. Thomas,
Geological Survey. Lanier avenue.
1871. HARKNESS, Prof. William, U. S. N. (*Founder*),
Naval Observatory. Cosmos Club.
1880. HASSLER, Dr. F. A. (Ferdinand Augustus) (*Absent*),
Santa Aña, Los Angeles Co., Cal.
1886. HAYDEN, Lieut. Everett, U. S. N.,
Hydrographic Office.
1882. HAZEN, Prof. H. A. (Henry Allen),
P. O. Box 427. 1416 Corcoran street.
1884. HEAP, Major D. P. (David Porter), U. S. A. (*Resigned*),
Engineer 3d and 4th Light House District, Tompkins-
ville, N. Y.
1874. HENSHAW, Mr. H. W. (Henry Wetherbee),
Bureau of Ethnology. 13 Iowa Circle.
1879. HILL, Mr. G. W. (George William),
Nautical Almanac Office. 314 Indiana ave.
1886. HILL, Mr. R. T. (Robert Thomas),
Geological Survey. 1626 15th street.
1886. HILLEBRAND, Dr. W. F. (William Francis),
Geological Survey. 506 Maple ave., Le Droit Park.
1884. HITCHCOCK, Mr. Romya,
National Museum. Osaka, Japan.
1885. HODGKINS, Prof. H. L. (Howard Lincoln),
Columbian University. 1532 19th street.

1873. HOLDEN, Prof. E. S. (Edward Singleton) (*Absent*),
Lick Observatory, San José, Cal.
1887. HOLMES, Mr. J. H. (Jesse Herman),
1811 I street.
1879. HOLMES, Mr. W. H. (William Henry),
Geological Survey. 1444 Stoughton street.
1874. HOWELL, Mr. E. E. (Edwin Eugene) (*Absent*),
48 Oxford street, Rochester, N. Y.
1885. IDDINGS, Mr. J. P. (Joseph Paxson),
Geological Survey. 1028 Vermont ave.
1886. IRVING, Prof. R. D. (Roland Duer),
Geological Survey. Madison, Wis.
1880. JAMES, Rev. Owen (*Absent*),
Scranton, Pa.
1871. JENKINS, Rear Admiral T. A. (Thornton Alexander), U.S. N.
(*Founder*),
2115 Pennsylvania ave.
1878. JOHNSON, Mr. A. B. (Arnold Burges),
Light House Board, Treas. Dept. 501 Maple ave.,
Le Droit Park.
1879. JOHNSON, Dr. Joseph Taber,
Private Hospital, 1728 K street.
1884. JOHNSON, Mr. Willard D. (Willard Drake),
Geological Survey. 501 Maple ave., Le Droit Park.
1873. JOHNSTON, Dr. W. W. (William Waring),
1603 K street.
1884. KAUFFMANN, Mr. S. H. (Samuel Hay),
1000 M street.
1886. KENASTON, Prof. C. A. (Carlos Albert),
Howard University.
1884. KERR, Mr. Mark B. (Mark Brickell),
Geological Survey. 2104 H street.
1880. KIDDER, Dr. J. H. (Jerome Henry),
Smithsonian Institution. 1606 N. H. ave.
1880. KILBOURNE, Lieut. C. E. (Charles Evans), U. S. A. (*Absent*),
War Department.
1875. KING, Dr. A. F. A. (Albert Freeman Africanus),
726 13th street.
1887. KING, Mr. Harry,
Geological Survey. 1819 Q street.
1887. KNIGHT, Mr. Fred J. (Fred Jay),
Geological Survey.
1874. KNOX, Hon. John Jay (*Absent*),
Pres. Nat. Bank Republic, New York city.
19 E. 41st street.
1887. KNOWLTON, Mr. F. H. (Frank Hall),
National Museum. 202 5th street se.
1882. KUMMELL, Mr. C. H. (Charles Hugo),
Coast and Geodetic Survey. 608 Q street.

1887. LANGLEY, Prof. S. P. (Samuel Pierpont),
Secretary Smithsonian Institution.
1884. LAWRENCE, Mr. William,
Bellefontaine, Ohio.
1874. LEE, Dr. William,
2111 Penna. ave. 1821 I street.
1882. LEFAVOUR, Mr. E. B. (Edward Brown) (*Absent*),
Cambridge, Mass.
1871. LINCOLN, Dr. N. S. (Nathan Smith),
1514 H street.
1880. LOOMIS, Mr. E. J. (Eben Jenks),
Nautical Almanac Office. 1443 Stoughton street.
1886. MCADIE, Mr. A. G. (Alexander George),
U. S. Signal Office, St. Paul, Minn.
1886. McDONALD, Col. Marshall,
U. S. Fish Commission. 1515 R street.
1883. MCGEE, Mr. W J,
Geological Survey.
1879. MCGUIRE, Mr. Fred. B. (Frederick Bauders),
1416 F street. 614 E street.
1876. MCMURTRIE, Prof. William (*Absent*),
University of Illinois, Champaign, Ill.
1884. MAHER, Mr. James A. (James Arran),
Geological Survey. 15 Grant Place.
1875. MALLERY, Col. Garrick, U. S. A.,
Bureau of Ethnology. 1323 N street.
1885. MANN, Mr. B: Pickman (Benjamin Pickman),
Patent Office. 1918 Sunderland Place.
1886. MARTIN, Mr. Artemas,
Coast and Geodetic Survey. 55 C street se.
1885. MARVIN, Prof. C. F. (Charles Frederick),
Signal Office, War Department. 1736 13th street.
1878. MARVIN, Mr. Jos. B. (Joseph Badger),
Lock Box 379.
1875. MASON, Prof. O. T. (Otis Tufton),
National Museum. 1305 Q street.
1884. MATTHEWS, Dr. W. (Washington), U. S. A.,
Army Medical Museum. 1262 New Hampshire ave.
1871. MEIGS, Gen. M. C. (Montgomery Cunningham), U. S. A.
(*Founder*),
1239 Vermont avenue.
1885. MENDENHALL, Prof. T. C. (Thomas Corwin) (*Absent*),
Terre Haute, Ind.
1886. MERRIAM, Dr. C. Hart (Clinton Hart),
Department of Agriculture. 1919 16th street.
1884. MERRILL, Mr. George P. (George Perkins),
National Museum. 1602 19th street.
1886. MITCHELL, Prof. Henry,
Coast and Geodetic Survey. 1331 L street.

1883. MORGAN, Dr. E. Carroll (Ethelbert Carroll),
918 E street.
1885. MOSER, Lieut. J. F. (Jefferson Franklin), U. S. N. (*Absent*),
Navy Department.
1884. MURDOCH, Mr. John,
Smithsonian Institution. 1429 Stoughton street.
1881. MUSSEY, Gen. R. D. (Reuben Delavan),
P. O. Box 618.
1871. NEWCOMB, Prof. Simon, U. S. N. (*Founder*),
Navy Department.
1872. NICHOLS, Dr. C. H. (Charles Henry) (*Absent*),
Bloomingdale Asylum, Boulevard and 117th street,
New York city, N. Y.
1871. NICHOLSON, Mr. W. L. (Walter Lamb) (*Founder*),
2222 G street.
1879. NORDHOFF, Mr. Charles,
1732 H street.
1884. NORRIS, Dr. Basil, U. S. A. (*Absent*),
Vancouver Barracks, Wash. Ter.
1885. NOTT, Judge C. C. (Charles Cooper),
Court of Claims. 826 Connecticut ave.
1884. OGDEN, Mr. H. G. (Herbert Gouverneur),
Coast and Geodetic Survey. 1324 19th street.
1878. OSBORNE, Mr. J. W. (John Walter),
212 Delaware ave ne.
1871. PARKE, Gen. John G. (John Grubb), U. S. A. (*Founder*),
West Point, N. Y.
1871. PARKER, Dr. Peter (*died Jan. 10, 1888*) (*Founder*),
1871. PARRY, Dr. C. C. (Charles Christopher) (*Absent*),
Davenport, Iowa.
1877. PAUL, Mr. H. M. (Henry Martyn),
Naval Observatory. 1915 G street.
1874. PEALE, Dr. A. C. (Albert Charles),
Geological Survey. 1446 Stoughton street.
1873. POE, Gen. O. M. (Orlando Metcalfe), U. S. A. (*Absent*),
34 West Congress street, Detroit, Mich.
1884. POINDEXTER, Mr. W. M. (William Mundy),
1505 Pennsylvania ave. 1227 15th street.
1882. POPE, Dr. B. F. (Benjamin Franklin), U. S. A. (*Absent*),
Surg. General's Office, U. S. A.
1874. POWELL, Major J. W. (John Wesley),
Geological Survey. 910 M street.
1880. PRENTISS, Dr. D. W. (Daniel Webster),
1101 14th street.
1879. PRITCHETT, Prof. H. S. (Henry Smith) (*Absent*),
Director of Observatory, Washington University,
St. Louis, Mo.

1882. RATHBUN, Mr. Richard,
National Museum.. 1622 Massachusetts ave.
1884. RAY, Lieut. P. H. (Patrick Henry), U. S. A.,
Fort Gaston, Cal.
1883. RENSHAWE, Mr. Jno. H. (John Henry),
Geological Survey. 1215 L street.
1884. RICKSECKER, Mr. Eugene,
Geological Survey. 904 14th street.
1878. RILEY, Dr. C. V. (Charles Valentine),
Department of Agriculture. 1700 13th street.
1879. RITTER, Mr. W. F. McK. (William Francis McKnight)
(*Absent*),
P. O. Box 50, Milton, Pa.
1884. ROBINSON, Mr. Thomas,
U. S. Engineer Service. Vienna, Va.
1872. ROGERS, Mr. Joseph A. (Joseph Addison) (*Absent*),
Naval Observatory.
1882. RUSSELL, Mr. Israel C. (Israel Cook),
Geological Survey. 42 B street ne.
1883. RUSSELL, Mr. Thomas,
Signal Office, War Department. 1344 Wallach Place.
1883. SALMON, Dr. D. E. (Daniel Elmer),
Agricultural Department. 1716 13th street.
1883. SAMPSON, Commander W. T. (William Thomas), U. S. N.
(*Absent*),
Naval Academy, Annapolis, Md.
1871. SAVILLE, Mr. J. H. (James Hamilton),
1419 F street. 1315 M street.
1871. SCHOTT, Mr. Charles A. (Charles Anthony) (*Founder*),
Coast and Geodetic Survey. 212 1st street se.
1887. SEELY, Col. F. A. (Franklin Austin),
Patent Office.
1875. SHELLABARGER, Hon. Samuel,
Room 31 Kellogg Building. 812 17th street.
1874. SHERMAN, Hon. John,
U. S. Senate. 1319 K street.
1881. SHUFELDT, Dr. R. W. (Robert Wilson), U. S. A. (*Absent*),
Care Smithsonian Institution.
1879. SIGSBEE, Commander C. D. (Charles Dwight), U. S. N.
(*Absent*),
Naval Academy, Annapolis, Md.
1883. SKINNER, Dr. J. O. (John Oscar), U. S. A. (*Absent*),
Surg. General's Office, U. S. A.
1882. SMILEY, Mr. Chas. W. (Charles Wesley),
U. S. Fish Commission. 943 Massachusetts ave.
1876. SMITH, Chf. Eng. David, U. S. N.,
Navy Department.

1880. SMITH, Mr. Edwin,
Coast and Geodetic Survey. 2024 Hillyer Place.
1887. SMYTH, Mr. H. L. (Henry Lloyd),
Geological Survey.
1886. SNELL, Mr. Merwin M. (Merwin-Marie),
National Museum. 732 6th street.
1887. SPENCER, Dr. J. W. (Joseph William),
1012 17th street.
1872. SPOFFORD, Mr. A. R. (Ainsworth Rand),
Library of Congress. 1621 Massachusetts ave.
1884. STEARNS, Mr. R. E. C. (Robert Edwards Carter),
Geol. Survey; Smithsonian Institution. 1213 12th St.
1874. STONE, Prof. Ormond (*Absent*),
Leander McCormick Observatory, Univ. of Virginia.
1887. SYMONS, Capt. T. W. (Thomas William), U. S. A.,
District Building. 1727 De Sales street.
1881. TAYLOR, Mr. F. W. (Frederick William) (*Absent*),
Smithsonian Institution.
1871. TAYLOR, Mr. William B. (William Bower) (*Founder*),
Smithsonian Institution. 306 C street.
1875. THOMPSON, Prof. A. H. (Almon Harris),
Geological Survey.
1884. THOMPSON, Mr. Gilbert,
Geological Survey. 1448 Q street.
1878. TODD, Prof. David P. (David Peck) (*Absent*),
Amherst College Observatory, Amherst, Mass.
1873. TONER, Dr. J. M. (Joseph Meredith),
615 Louisiana ave.
1886. TRENHOLM, Hon. W. L. (William Lee),
Comptroller of the Currency. 1815 M street.
1882. TRUE, Mr. F. W. (Frederick William),
National Museum. 1101 14th street.
1882. UPTON, Mr. Wm. W. (William Wirt),
1416 F street. 1746 M street.
1880. UPTON, Prof. Winslow (*Absent*),
Brown University, Providence, R. I.
1883. WALCOTT, Mr. C. D. (Charles Doolittle),
Geological Survey; National Museum.
1881. WALDO, Prof. Frank (*Absent*),
Forest ave., Cincinnati, Ohio.
1872. WALKER, Mr. F. A. (Francis Amasa) (*Absent*),
Massachusetts Institute of Technology, Boston, Mass.
1883. WALLING, Mr. H. F. (Henry Francis) (*Absent*),
Mass. Trigonometrical Survey, Cambridge, Mass.
1876. WARD, Mr. Lester F. (Lester Frank),
Geological Survey. 1464 Rhode Island ave.

1882. WEBSTER, Mr. A. L. (Albert Lowry) (*Absent*),
107 Drexel Building, Broad street, New York city;
West New Brighton, Staten Island, N. Y.
1885. WEED, Mr. W. H. (Walter Harvey),
Geological Survey. 825 Vermont ave.
1882. WELLING, Mr. J. C. (James Clarke),
1302 Connecticut ave.
1873. WHEELER, Capt. Geo. M. (George Montague), U. S. A.,
Lock Box 93. 930 16th street.
1876. WHITE, Dr. C. A. (Charles Abiathar),
Geological Survey. 312 Maple ave., Le Droit Park.
1884. WHITE, Dr. C. H. (Charles Henry), U. S. N.,
Museum of Hygiene.
1887. WHITING, Mr. H. L. (Henry Laurens),
Coast and Geodetic Survey. West Tisbury, Mass.
1885. WILLIS, Mr. Bailey,
Geological Survey. 1739 G street.
1887. WILSON, Mr. H. C. (Herbert Couper) (*Absent*),
Carleton College Observatory, Northfield, Minn.
1885. WILSON, Mr. H. M. (Herbert Michael),
Geological Survey. 1715 G street.
1873. WILSON, Mr. J. Ormond (James Ormond),
1439 Massachusetts ave.
1880. WINLOCK, Mr. W. C. (William Crawford),
Naval Observatory. 1923 H street.
1875. WOOD, Mr. Joseph (*Absent*),
Pittsburgh, Penn.
1871. WOOD, Lieut. W. M. (William Maxwell), U. S. N. (*Absent*),
Navy Department.
1883. WOODWARD, Mr. R. S. (Robert Simpson),
Geological Survey. 1804 Columbia road.
1885. WORTMAN, Dr. J. L. (Jacob Lawson),
Army Medical Museum. 1711 13th street.
1885. WRIGHT, Mr. Geo. M. (George Mitchell) (*Absent*),
Akron, Ohio.
1887. WÜRDEMANN, Mr. H. V. (Harry Vanderbilt),
Geological Survey. 1235½ 5th street.
1874. YARROW, Dr. H. C. (Harry Crécy),
Army Medical Museum. 814 17th street.
1884. YEATES, Mr. W. S. (William Smith),
Smithsonian Institution. 631 T street.
1885. ZIWET, Mr. Alexander,
64 Sibley street, Detroit, Mich.

LIST OF DECEASED MEMBERS.

<i>Name.</i>	<i>Admitted.</i>
Benjamin Alvord	1872
Orville Elias Babcock	1871
Theodorus Bailey	1873
Spencer Fullerton Baird	Founder
Joseph K. Barnes	Founder
Henry Wayne Blair	1884
Horace Capron	Founder
Salmon Portland Chase	Founder
Frederick Collins	1879
Benjamin Faneuil Craig	Founder
Charles Henry Crane	Founder
Josiah Curtis	1874
Richard Dominicus Cutts	1871
Charles Henry Davis	1874
Frederick William Dorr	1874
Alexander B. Dyer	Founder
Amos Beebe Eaton	Founder
Charles Ewing	1874
Elisha Foote	Founder
John Gray Foster	1873
Leonard Dunnell Gale	1874
Isaiah Hanscom	1873
William Babcock Hazen	1881
Joseph Henry	Founder
Franklin Benjamin Hough	1879
Andrew Atkinson Humphreys	Founder
Ferdinand Kampf	1875
Washington Caruthers Kerr	1883
Jonathan Homer Lane	Founder
Edward Phelps Lull	1875
Oscar A. Mack	1872
Archibald Robertson Marvine	1874
Fielding Bradford Meek	Founder
James William Milner	1874
Albert James Myer	Founder
George Alexander Otis	Founder
Peter Parker	Founder
Carlile Pollock Patterson	1871
Titian Ramsay Peale	Founder
Benjamin Peirce	Founder
John Campbell Riley	1877
John Rodgers	1872

LIST OF MEMBERS.

XXIX

<i>Name.</i>	<i>Admitted.</i>
Benjamin Franklin Sands	Founder
George Christian Shaeffer	Founder
Henry Robinson Searle	1877
William J. Twining	1878
Joseph Janvier Woodward	Founder
John Maynard Woodworth	1874
Mordecai Yarnall	1871

SUMMARY.

Active members	182
Absent members	58
Total	<u>240</u>
Deceased members	49



CALENDAR FOR THE USE OF THE PHILOSOPHICAL SOCIETY,
Showing the alternate SATURDAYS for holding Meetings during the several "Seasons" from 1884-'85 to 1907-'08, inclusive.

PREPARED BY MR. E. B. ELLIOTT.

Submitted to the General Committee June 7, 1884, and ordered published.

Years.	October.	November.	December.	Years.	January.	February.	March.	April.	May.	June.
1884.....	11, 25	8, 22	6, 20	1885.....	3, 17, 31	14, 23	14, 23	11, 25	0, 23	6, 20
1885.....	10, 24	7, 21	5, 19	1886.....	2, 16, 30	13, 27	13, 27	10, 24	8, 22	5, 19
1886.....	9, 23	6, 20	4, 18	1887.....	13, 27	12, 26	12, 26	9, 23	7, 21	4, 18
1887.....	15, 29	12, 26	10, 24	1888.....	7, 21	4, 18	3, 17, 31	14, 23	12, 26	9, 23
1888.....	13, 27	10, 24	8, 22	1889.....	6, 19	2, 16	2, 16, 30	13, 27	11, 25	8, 22
1889.....	12, 26	9, 23	7, 21	1890.....	4, 18	1, 15, 29	1, 15, 29	12, 26	10, 24	7, 21
1890.....	11, 25	8, 22	6, 20	1891.....	3, 17, 31	14, 23	14, 23	11, 25	9, 23	6, 20
1891.....	10, 24	7, 21	5, 19	1892.....	2, 16, 30	13, 27	12, 26	9, 23	7, 21	4, 18
1892.....	15, 29	12, 26	10, 24	1893.....	7, 21	4, 18	4, 18	1, 15, 29	13, 27	10, 24
1893.....	14, 23	11, 25	9, 23	1894.....	6, 20	3, 17	3, 17, 31	14, 23	12, 26	9, 23
1894.....	13, 27	10, 24	8, 22	1895.....	6, 19	2, 16	2, 16, 30	13, 27	11, 25	8, 22
1895.....	12, 26	9, 23	7, 21	1896.....	4, 18	1, 15, 29	1, 15, 29	11, 25	9, 23	6, 20
1896.....	10, 24	7, 21	5, 19	1897.....	2, 16, 30	13, 27	13, 27	10, 24	8, 22	5, 19
1897.....	9, 23	6, 20	4, 18	1898.....	15, 29	12, 26	12, 26	9, 23	7, 21	4, 18
1898.....	15, 29	12, 26	10, 24	1899.....	7, 21	4, 18	4, 18	1, 15, 29	13, 27	10, 24
1899.....	14, 23	11, 25	9, 23	1900.....	6, 20	3, 17	3, 17, 31	14, 23	12, 26	9, 23
1900.....	13, 27	10, 24	8, 22	1901.....	6, 19	2, 16	2, 16, 30	11, 25	11, 25	8, 22
1901.....	12, 26	9, 23	7, 21	1902.....	4, 18	1, 15, 29	1, 15, 29	13, 27	10, 24	7, 21
1902.....	11, 25	8, 22	6, 20	1903.....	3, 17, 31	14, 23	14, 23	11, 25	9, 23	6, 20
1903.....	10, 24	7, 21	5, 19	1904.....	2, 16, 30	13, 27	12, 26	0, 23	7, 21	4, 18
1904.....	15, 29	12, 26	10, 24	1905.....	7, 21	4, 18	4, 18	1, 15, 29	13, 27	10, 24
1905.....	14, 23	11, 25	9, 23	1906.....	6, 20	3, 17	3, 17, 31	14, 23	12, 26	9, 23
1906.....	13, 27	10, 24	8, 22	1907.....	5, 19	2, 16	2, 16, 30	11, 25	11, 25	8, 22
1907.....	12, 26	9, 23	7, 21	1908.....	4, 18	1, 15, 29	1, 15, 29	11, 25	9, 23	6, 20

ANNUAL REPORT OF THE SECRETARIES.

WASHINGTON, D. C., December 21, 1887.

To the Philosophical Society of Washington :

We have the honor to present the following statistical data for 1887 :

The last Annual Report brought the record of membership down to December 18, 1886. The number of active members was then 183
 This number has been increased by the addition of 14 new members, by the return of 1 absent member, and by the reinstatement of 2 members previously dropped. It has been diminished by the departure of 7 members, by the resignation of 1, and by the death of 3 members. The net increase of active members has thus been 6
 And the active membership is now 189

The roll of new members is :

W. H. BABCOCK.	F. H. KNOWLTON.	T. W. SYMONS.
EVERETT HAYDEN.	S. P. LANGLEY.	H. L. WHITING.
J. H. HOLMES.	F. A. SEELY.	H. C. WILSON.
HARRY KING.	H. L. SMYTH.	H. V. WÜRDEMAN.
F. J. KNIGHT.	J. W. SPENCER.	

The roll of deceased members is :

S. F. BAIRD.	W. B. HAZEN.	E. P. LULL.
--------------	--------------	-------------

There have been 16 meetings, of which 14 have been for the presentation and discussion of papers, 1 for the President's Annual Address, and 1 for the Annual Reports and election of officers; the average attendance (at the 14 meetings for presentation of papers), has been 49. There have been 12 meetings of the Mathematical Section; average attendance 17.

The first 5 meetings of the year were held in the library of the Surgeon General's Office, at which meetings the average attendance was 40; the 9 remaining meetings were held in the Assembly Hall of the Cosmos Club, at which the average attendance was 54.

In the general meetings 37 communications have been presented; in the Mathematical Section 20. Altogether 57 communications

have been made by 37 members and 1 guest. The number of members and guests who have participated in the discussions is 40. The total number who have contributed to the scientific proceedings is 47, or 25 per cent. of the present active membership.

The General Committee has held 16 meetings; average attendance 13, the smallest attendance at any meeting being 11 and the largest 15.

Of the present active membership 146, or 77 per cent., are employed in the service of the Government, and 44, or 23 per cent., are not so employed.

MARCUS BAKER,
J. H. KIDDER,
Secretaries.

REPORT OF THE TREASURER.

Mr. President and Gentlemen:

The report which I shall presently have the honor to submit to you exhibits the total receipts and disbursements for the fiscal year ending with this meeting.

The receipts, however, include amounts received for outstanding dues of previous years, and it is, therefore, proper to say that the income belonging to the year 1887 was \$1,035.75, and the expenditure \$568.22, leaving a net surplus for the year of \$467.53.

The unpaid dues of former years which have been collected in 1887 amount to \$120.

The assets of the Society consist of:

2 Government bonds, \$1,000 and \$500, at 4 per cent.,	\$1,500 00
1 " bond, 1,000, " 4½ "	1,000 00
6 Cosmos Club mortgage bonds, " 5 "	600 00
Cash with Riggs & Co.	942 05
Unpaid dues	265 00
Total	<u>\$4,307 05</u>

The removal of the Society from its old place of meeting at the Army Medical Museum made it necessary to provide certain articles of furniture and equipment for use in its new quarters.

The ninth volume of the Bulletin was duly issued in January to all members entitled to receive it, and to the societies and scientific journals with which it is customary for the Philosophical Society to exchange publications.



BULLETIN

OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON.

ANNUAL ADDRESS OF THE PRESIDENT.



ANNUAL ADDRESS OF THE PRESIDENT,

WILLIAM HARKNESS.

Delivered December 10, 1887.

THE PROGRESS OF SCIENCE AS EXEMPLIFIED IN THE ART OF WEIGHING AND MEASURING.

Two centuries ago the world was just beginning to awaken from an intellectual lethargy which had lasted a thousand years. During all that time the children had lived as their parents before them, the mechanical arts had been at a standstill, and the dicta of Aristotle had been the highest authority in science. But now the night of mediævalism was approaching its end, and the dawn of modern progress was at hand. Galileo had laid the foundation for accurate clocks by discovering the isochronism of the simple pendulum; had proved that under the action of gravity light bodies fall as rapidly as heavy ones; had invented the telescope and with it discovered the spots on the sun, the mountains on the moon, the satellites of Jupiter, and the so-called triple character of Saturn; and after rendering himself immortal by his advocacy of the Copernican system, had gone to his grave, aged, blind, and full of sorrows. His contemporary, Kepler, had discovered the laws which, while history endures, will associate his name with the theory of planetary motion, and he also had passed away. The first Cassini was still a young man, his son was a little child, and his grandson and great-grandson, all of whom were destined to be directors of the Paris Observatory, were yet unborn. The illustrious Huyghens, the discoverer of Saturn's rings and the father of the undulatory theory of light, was in the zenith of his powers. The ingenious Hooke was a little younger, and Newton, towering above them all, had recently invented fluxions, and on the 28th of April, 1686, had presented his *Principia* to the Royal Society of London and given the theory of gravitation to the world. Bradley, who discovered nutation and

the aberration of light; Franklin, the statesman and philosopher, who first drew the lightning from the clouds; Dollond, the inventor of the achromatic telescope; Euler, the mathematician who was destined to accomplish so much in perfecting algebra, the calculus, and the lunar theory; Laplace, the author of the *Mécanique Céleste*; Rumford, who laid the foundation of the mechanical theory of heat; Dalton, the author of the atomic theory upon which all chemistry rests; and Bessel, the greatest of modern astronomers—these and others almost as illustrious, whom we cannot even name to-night, were still in the womb of time.

Pure science first felt the effects of the new intellectual life and it was more than a century later before the arts yielded to its influence. Then came Hargreaves, the inventor of the spinning-jenny; Arkwright, the inventor of the cotton-spinning frame; Watt, who gave us the condensing steam engine; Jacquard, the inventor of the loom for weaving figured stuffs; Murdock, the originator of gas lighting; Evans, the inventor of the high-pressure steam engine; Fulton, the father of steam navigation; Trevithick, who ranks very near Watt and Evans in perfecting the steam engine; and Stephenson, the father of railroads. If now we add the names of those who have given us the telegraph, to wit: Gauss, the eminent physicist and the greatest mathematician of the present century; Weber, Wheatstone, and Henry—all famous physicists—and Morse, the inventor and engineer; we have before us the demi-gods who have transformed the ancient into the modern world, given us machinery which has multiplied the productive power of the human race many fold, annihilated time and space, and bestowed upon toiling millions a degree of comfort and luxury which was unknown to kings and emperors of old.

The discoveries and inventions of the last two centuries have so far exceeded all others within historic times that we are amply justified in calling this an age of phenomenal progress, and under the circumstances a little self-glorification is pardonable—perhaps even natural. The weekly and monthly records of scientific events which appear in so many newspapers and magazines are the immediate result of this, and the great increase of ephemeral scientific literature has led multitudes of educated people to believe that such records represent actual progress. The multiplication of bricks facilitates the building of houses, but does not necessarily

improve architecture. Similarly, the multiplication of minor investigations improves our knowledge of details, but rarely affects the great philosophic theories upon which science is founded. The importance of human actions is measured by the degree in which they affect human thought, and the only way of permanently affecting scientific thought is by modifying or extending scientific theories. The men who do that are neither numerous, nor do they require weekly paragraphs to record their deeds; but their names are honored by posterity. Even in this golden age the advance of science is not steady, but is made by spasmodic leaps and bounds. Mere scientific brick making, commonly called progress, is always the order of the day until some genius startles the world by a discovery affecting accepted theories. Then every effort is directed in the new line of thought until it is measurably worked out, and after that brick making again resumes its place. While the progress in two centuries has been immense, the progress in a week or a month is usually almost nil. Optimism has its uses in many departments of human affairs, but science should be cool and dispassionate, having regard only for the truth. To make a trustworthy estimate of the actual state of the whole vast realm of science would be a task beyond the powers of any one man; but perhaps it will not be amiss to spend the time at our disposal this evening in briefly reviewing the recent progress and present condition of the fundamental processes upon which the exact sciences rest—I allude to the methods of weighing and measuring.

Physical science deals with many quantities, but they are all so related to each other that almost every one of them can be expressed in terms of three fundamental units. As several systems of such units are possible, it is important to select the most convenient, and the considerations which guide us in that respect are the following:

1. The quantities selected should admit of very accurate comparison with other quantities of the same kind.
2. Such comparisons should be possible at all times, and in all places.
3. The processes necessary for making such comparisons should be easy and direct.

4. The fundamental units should be such as to admit of easy definitions and simple dimensions for the various derived units.

Scientific men have long agreed that these requirements are best fulfilled by adopting as the fundamental units, a definite length, a definite mass, and a definite interval of time. Length is an element which can be very accurately measured and copied, but it must be defined by reference to some concrete material standard, as for example, a bar of metal, and as all substances expand and contract with changes of temperature, it is necessary to state the temperature at which the standard is correct. A standard of mass, consisting of a piece of platinum, quartz, or other material not easily affected by atmospheric influences, probably fulfills the conditions set forth above better than any other kind of magnitude. Its comparison with other bodies of approximately equal mass is effected by weighing, and as that is among the most exact of all laboratory operations, very accurate copies of the standard can be made, and they can be carried from place to place with little risk of injury. Time is also an element which can be measured with extreme precision. The immediate instruments of measurement are clocks and chronometers, but their running is checked by astronomical observations and the ultimate standard is the rotation of the earth itself.

It is important to note that the use of three fundamental units is simply a matter of convenience and not a theoretical necessity, for the unit of mass might be defined as that which at unit distance would generate in a material point unit velocity in unit time; and thus we should have a perfectly general system of measurement based upon only two fundamental units—namely, those of space and time. Such a system is quite practicable in astronomy, but cannot yet be applied with accuracy to ordinary terrestrial purposes. According to the law of gravitation

$$\text{Mass} = \text{Acceleration} \times (\text{Distance})^2$$

and as in the case of the earth we can measure the quantities on the right-hand side of that equation with considerable accuracy, we can satisfactorily determine the earth's mass in terms of the supposed unit. That suffices for the needs of astronomy, but for other scientific and commercial purposes a standard of mass having a magnitude of about a pound is necessary, and as two such masses can be compared with each other from five to ten thousand times more

accurately than either of them can be determined in terms of the supposed unit, three fundamental units are preferable to two.

The Chaldeans, Babylonians, Persians, Greeks, and Romans all seem to have had systems of weights and measures based upon tolerably definite standards, but after the decline of the Roman Empire these standards seem to have been forgotten, and in the beginning of the sixteenth century the human body had so far become the standard of measurement that the units in common use, as for example, the foot, palm, etc., were frequently taken directly from it. The complete table of measures of length was then as follows: the breadth (not the length) of four barley corns make a digit, or finger breadth; four digits make a palm, (measured across the middle joints of the fingers;) four palms are one foot; a foot and a half is a cubit; ten palms, or two feet and a half, are a step; two steps, or five feet, are a pace; ten feet are a perch; one hundred and twenty-five paces are an Italic stadium; eight stadia, or one thousand paces, are an Italic mile; four Italic miles, are a German mile; and five Italic miles are a Swiss mile. It was then the practice to furnish standards of length in books by printing in them lines a foot or a palm long, according to the size of the page, and from these and other data it appears that the foot then used on the continent of Europe had a length of about ten English inches.

In England the first attempts at scientific accuracy in matters of measurement date from the beginning of the seventeenth century, when John Greaves, who must be considered as the earliest of the scientific metrologists, directed attention to the difference between the Roman and English foot by tolerably accurate determinations of the former, and also attempted the investigation of the Roman weights. He was followed by Dr. Edward Bernard, who wrote a treatise on ancient weights and measures about 1685, and towards the end of the century the measurements of the length of a degree by Picard and J. D. Cassini awakened the attention of the French to the importance of rigorously exact standards. In considering the progress of science with respect to standards of length we may safely confine our inquiries to the English yard and the French toise and meter, for during the last two hundred years they have been almost the only standards adopted in scientific operations.

The English measures of length have come down from the Saxons, but the oldest standards now existing are the Exchequer yards of

Henry VII (1490)¹ and Elizabeth (1588).² These are both brass end measures, the former being an octagonal rod about half an inch in diameter, very coarsely made, and as rudely divided into inches on the right hand end and into sixteenths of a yard on the left hand end; the latter a square rod with sides about half an inch wide, also divided into sixteenths of a yard and provided with a brass bed having end pieces between which the yard fits. One end of the bed is divided into inches and half inches. Francis Baily, who saw this Elizabethan standard in 1836, speaks of it as "this curious instrument, of which it is impossible, at the present day, to speak too much in derision or contempt. A common kitchen poker, filed at the ends in the rudest manner by the most bungling workman, would make as good a standard. It has been broken asunder; and the two pieces have been dove-tailed together: but so badly that the joint is nearly as loose as that of a pair of tongs. The date of this fracture I could not ascertain, it having occurred beyond the memory or knowledge of any of the officers at the Exchequer. And yet, till within the last 10 years, to the disgrace of this country, copies of this measure have been circulated all over Europe and America, with a parchment document accompanying them (charged with a stamp that costs £3. 10s. exclusive of official fees) certifying that they are true copies of the English *standard*."³

In the year 1742 certain members of the Royal Society of London, and of the Royal Academy of Sciences of Paris, proposed that, in order to facilitate a comparison of the scientific operations carried on in the two countries, accurate standards of the measures and weights of both should be prepared and preserved in the archives of each of these societies. This proposition having been approved, Mr. George Graham at the instance of the Royal Society had two substantial brass rods made, upon which he laid off, with the greatest care, the length of three English feet from the standard yard kept at the Tower of London. These two rods, together with a set of troy weights, were then sent over to the Paris Academy, which body, in like manner, had the measure of a French half toise set off upon the rods, and keeping one, as previously agreed, returned the other, together with a standard weight of two marcs, to the Royal Society. In 1835, Baily declared this copy of the half

¹ 43, p. 34, and 44, pp. 51-2. (See Bibliography on page lxxix.)

² 43, p. 25.

³ 34, p. 146.

toise to be of little value because the original toise-étalon was of iron, and the standard temperature in France differed from that in England.¹ In his opinion the French should have sent over an iron half toise in exchange for the English brass yard; but this criticism loses much of its force when it is remembered that in 1742 neither England nor France had fixed upon a temperature at which their standards were to be regarded as of the true length. On the return of the rod from Paris Mr. Graham caused Jonathan Sisson to divide the English yard and the French half toise each into three equal parts, after which the rod was deposited in the archives of the Royal Society, where it still remains.² Objection having been made that the original and legal standard yard of England was not the one at the Tower, but the Elizabethian standard at the Exchequer, the Royal Society requested Mr. Graham to compare his newly-made scale with the latter standard, and on Friday, April 22, 1743, he did so in the presence of a committee of seven members of the Royal Society. In the following week the same gentlemen compared the Royal Society's scale with the standards at Guildhall and the Tower, and also with the standard of the Clock-makers' Company. These comparisons having shown that the copy of the Tower yard upon the Royal Society's scale was about 0.0075 of an inch longer than the standard at the Exchequer, Mr. Graham inscribed upon the Royal Society's scale a copy of the latter standard also, marking it with the letters Exch., to distinguish it from the former, which was marked E. (English), and from the half toise which was marked F. (French).³

In the year 1758 the House of Commons appointed a committee to inquire into the *original* standards of weights and measures of England; and, under instructions from that committee, the celebrated instrument maker, John Bird, prepared two brass rods, respecting which the committee speak as follows in their report: "And having those rods, together with that of the Royal Society laid in the same place, at the receipt of the Exchequer, all night with the standards of length kept there, to prevent the variation which the difference of air might make upon them, they the next morning compared them all, and, by the means of beam compasses brought by Mr. Bird, found them to agree as near as it was possible."⁴ One of these rods was arranged as a matrix for testing end meas-

¹ 34, p. 37.² 6, pp. 185-8.³ 7, pp. 541-556.⁴ 11, p. 434.

ures, and the other was a line measure which the committee recommended should be made the legal standard of England, and which has since been known as Bird's standard of 1758. Respecting the statement that after lying together all night the rods were *all* found to agree as near as it was possible, Baily says: "This is somewhat remarkable, and requires further explanation, which unfortunately cannot now be accurately obtained. For it is notorious that the measure of the yard of the Royal Society's scale differs very considerably from the standard yard at the Exchequer: * * * Owing to this singular confusion of the lengths of the measures, which does not appear to have been unraveled by any subsequent Committee, it has happened that the Imperial standard yard * * * has been assumed nearly $1 \div 140$ of an inch longer than the ancient measure of the kingdom."¹ There is little difficulty in surmising what Bird did. The Exchequer standard consisted of a rod and its matrix. The Royal Society's committee assumed the rod to be the true standard of 36 inches, and upon that assumption Graham's measurements gave for the length of the matrix 36.0102 inches, and for the length of the Royal Society's yard 36.0075 inches. The Parliamentary committee of 1758 probably assumed the standard to consist of the rod and matrix together, which seems the better view; and by laying the rod in its matrix and measuring to the joint between them, Bird would have got a length of about 36.0051 inches. The mean between that and 36.0075 would be 36.0063, which differs very little from the length of Bird's standard resulting from Sir George Shuckburgh's measurements. Thus the committee's statement is justified, and there has been no falsification of the ancient standards.

On December 1, 1758, Parliament created another committee on weights and measures which in April, 1759, repeated the recommendation that Bird's standard of 1758 should be legalized, and further recommended that a copy of it should be made and deposited in some public office, to be used only on special occasions.² The copy was made by Bird in 1760, but owing to circumstances entirely unconnected with the subject, no legislation followed for sixty-four years.

The Royal Commission appointed during the reign of George III, to consider the subject of weights and measures, made its first report

¹ 34, p. 43.

² 12, p. 463.

on June 24, 1819, and therein recommended the adoption of the standard of length which had been used by General Roy in measuring the base on Hounslow Heath;¹ but in a second report made July 13, 1820, they wrote, "We * * * have examined, since our last report, the relation of the best authenticated standards of length at present in existence, to the instruments employed for measuring the base on Hounslow Heath, and in the late trigonometrical operations—But we have very unexpectedly discovered, that an error has been committed in the construction of some of these instruments.² We are therefore obliged to recur to the originals which they were intended to represent, and we have found reason to prefer the Parliamentary standard executed by Bird in 1760, which we had not before received, both as being laid down in the most accurate manner, and as the best agreeing with the most extensive comparisons, which have been hitherto executed by various observers, and circulated through Europe; and in particular with the scale employed by the late Sir George Shuckburgh."³

Accordingly, when in 1824 Parliament at length took action, Bird's standard of 1760 was adopted instead of that of 1758. The former being a copy of a copy, its selection as a national standard of length seems so singular that the circumstances which brought about that result should scarcely be passed over in silence. Bird had a very accurate brass scale 90 inches long, which he used in all his dividing operations, whether upon circles or straight lines, and which Dr. Maskelyne said was 0.001 of an inch shorter on three feet than Graham's Royal Society yard E.⁴ In the year 1792, or 1793, the celebrated Edward Troughton made for himself a five foot scale, which conformed to Bird's, and which he afterwards used in laying down the divisions of the various instruments that passed through his hands. This was the original of all the standard scales he ever made, and at the beginning of the present century he believed these copies, which were made by the aid of micrometer microscopes, to be so exact that no variations could possibly be detected in them, either from the original or from each other. Among the earliest of the scales so made by Troughton was the one used by Sir George Shuckburgh in 1796–8 in his important scientific operations for the improvement of the standards. Subsequently, the length of the meter was determined by comparison with this scale

¹ 23, p. 4.² 27, p. 92.³ 24, p. 3; also, 25 and 26.⁴ 13, p. 326.

and with the supposed fac-simile of it made by Troughton for Professor Pictet, of Geneva, and thus it happened that on the continent of Europe all measures were converted into English units by a reference to Sir George Shuckburgh's scale. The Royal Commission of 1819, believed Bird's standard of 1760 to be identical with Shuckburgh's scale, and they legalized it rather than the standard of 1758, in order to avoid disturbing the value of the English yard which was then generally accepted for scientific purposes.

There are yet four other scales of importance in the history of English standards—namely, the brass five-foot scale made for Sir George Shuckburgh by Troughton in 1796; two iron standard yards, marked 1A and 2A, made for the English Ordnance Survey department by Messrs. Troughton and Simms in 1826-'7, and the Royal Society's standard yard constructed by Mr. George Dollond, under the direction of Captain Henry Kater, in 1831.

Bearing in mind the preceding history, the genesis of the present English standard yard may be thus summarized: In 1742 Graham transferred to a bar made for the Royal Society a length which he intended should be that of the Tower yard, but which was really intermediate between the Exchequer standard yard of Elizabeth and its matrix. That length he marked with the letter E, and, although destitute of legal authority, it was immediately accepted as the scientific standard and was copied by the famous instrument makers of the time with all the accuracy then attainable. Thus it is in fact the prototype to which all the accurate scales made in England between 1742 and 1850 can be traced. Bird's standard of 1758 was compared with the Exchequer standard and with the Royal Society's yard E, and was of a length between the two. Bird's standard of 1760, legalized as the Imperial standard in June, 1824, was copied from his standard of 1758. After becoming the Imperial standard, Bird's standard of 1760 was compared with Sir George Shuckburgh's scale by Captain Kater in 1830 and by Mr. Francis Baily in 1834; with the Ordnance yards 1A and 2A in 1834 by Lieutenant Murphy, R. E., Lieutenant Johnson, R. N., and Messrs. F. Baily and Donkin; and with Kater's Royal Society yard by Captain Kater in 1831. On October 16th, 1834, the Imperial standard (Bird's standard of 1760) was destroyed by the burning of the Houses of Parliament, in which it was lodged, and very soon thereafter the Lords of the Treasury took measures to

recover its length. Preliminary inquiries were begun on May 11, 1838, and on June 20, 1843, they resulted in the appointment of a Commission to superintend the construction of new Parliamentary standards of length and weight, among whose members the Astronomer Royal (now Sir George B. Airy), Messrs. F. Baily, R. Sheepshanks, and Prof. W. H. Miller, were prominent. The laborious investigations and experiments carried out by that Commission cannot be described here, but it will suffice to say that for determining the true length of the new standard Mr. Sheepshanks employed a provisional yard, marked upon a new brass bar designated "Brass 2," which he compared as accurately as possible with Sir George Shuckburgh's scale, the two Ordnance yards, and Kater's Royal Society yard. The results in terms of the lost Imperial standard were as follows:

Brass bar 2 = 36·000084	from comparison with Shuckburgh's scale,	0·36 in.
36·000280	" " " "	10·46 in.
36·000303	from comparison with the Ordnance yard,	1A.
36·000275	" " " "	2A.
36·000229	from Capt. Kater's Royal Society yard.	

Mean = 36·000234

Respecting this mean Mr. Sheepshanks wrote: "This should be pretty near the truth; but I prefer 36·00025, if in such a matter such a difference be worth notice. I propose, therefore, in constructing the new standard to assume that—

Brass bar 2 = 36·00025 inches of lost Imperial standard at 62° Fah."

And upon that basis the standard now in use was constructed.¹

Turning now to the French standards of length, it is known that the ancient toise de maçons of Paris was probably the toise of Charlemagne (A. D. 742 to 814), or at least of some Emperor Charles, and that its étalon was situated in the court yard of the old Châtelet, on the outside of one of the pillars of the building. It still existed in 1714, but entirely falsified by the bending of the upper part of the pillar. In 1668 the ancient toise of the masons was reformed by shortening it five lines; but whether this reformation was an arbitrary change, or merely a change to remedy the

¹41, p. 664.

effects of long use and restore the *étalon* to conformity with some more carefully preserved standard, is not quite clear.¹ These old *étalons* were iron bars having their two ends turned up at right angles so as to form *talons*, and the standardizing of end measures was effected by fitting them between the *talons*. Being placed on the outside of some public building, they were exposed to wear from constant use, to rust, and even to intentional injury by malicious persons. Under such conditions every *étalon* would, sooner or later, become too long and require shortening.

Respecting the ancient toise of the masons there are two contradictory stories. On December 1, 1714, La Hire showed to the French Academy what he characterized as "a very ancient instrument of mathematics, which has been made by one of our most accomplished workmen with very great care, where the foot is marked, and which has served to re-establish the toise of the Châtelet, as I have been informed by our old mathematicians."² Forty-four years later, on July 29, 1758, La Condamine stated to the Academy that "We know only by tradition that to adjust the length of the new standard, the width of the arcade or interior gate of the grand pavilion, which served as an entrance to the old Louvre, on the side of the rue Fromenteau was used. This opening, according to the plan, should have been twelve feet wide. Half of it was taken to fix the length of the new toise, which thus became five lines shorter than the old one."³ Of these two contradictory statements that of La Hire seems altogether most trustworthy, and the ordinary rules of evidence indicate that it should be accepted to the exclusion of the other.

In 1668 the *étalon* of the new toise, since known as the toise-*étalon* du Châtelet, was fixed against the wall at the foot of the staircase of the grand Châtelet de Paris—by whom or at what season of the year is not known. Strange as it now seems, this standard—very roughly made, exposed in a public place for use or abuse by everybody, liable to rust, and certain to be falsified by constant wear—was actually used for adjusting the toise of Picard, that of Cassini, the toise of Peru and of the North, that of La Caille, that of Mairan—in short, all the toises employed by the French in their geodetic operations during the seventeenth and eighteenth centuries. The lack of any other recognized standard made the use of this one im-

¹ 1, p. 536 and 2, p. 395.

² 2, p. 395.

³ 14, p. 484.

perative, but the French academicians were well aware of its defects and took precautions to guard against them.

The first toise copied from the étalon of the Châtelet for scientific purposes was that used by Picard in his measurement of a degree of the meridian between Paris and Amiens.¹ It was made about the year 1668, and would doubtless have become the scientific standard of France had it not unfortunately disappeared before the degree measurements of the eighteenth century were begun. The second toise copied from the étalon of the Châtelet for scientific purposes was that used by Messrs. Godin, Bouguer, and La Condamine for measuring the base of their arc of the meridian in Peru. This toise, since known as the toise du Pérou, was made by the artist Langlois under the immediate direction of Godin in 1735, and is still preserved at the Paris Observatory.² It is a rectangular bar of polished wrought iron, having a breadth of 1.58 English inches and a thickness of 0.30 of an inch. All the other toises used by the Academy in the eighteenth century were compared with it, and, ultimately, it was made the legal standard of France by an order of Louis XV, dated May 16, 1766. As the toise of Peru is the oldest authentic copy of the toise of the Châtelet, the effect of this order was simply to perpetuate the earliest known state of that ancient standard.

The metric system originated from a motion made by Talleyrand in the National Assembly of France, in 1790, referring the question of the formation of an improved system of weights and measures, based upon a natural constant, to the French Academy of Sciences; and the preliminary work was entrusted to five of the most eminent members of that Academy—namely, Lagrange, Laplace, Borda, Monge, and Condorcet. On March 19, 1791, these gentlemen, together with Lalande, presented to the Academy a report containing the complete scheme of the metric system. In pursuance of the recommendations in that report, the law of March 26, 1791, was enacted for the construction of the new system, and the Academy of Sciences was charged with the direction of the necessary operations. Those requisite for the construction of a standard of length were:

1. The determination of the difference of latitude between Dunkirk and Barcelona.

¹ 5, Art. 4, p. 15.

² 14, p. 487 and 46, p. C.2.

2. The remeasurement of the ancient bases which had served for the measurement of a degree at the latitude of Paris, and for making the map of France.

3. The verification by new observations of the series of triangles employed for measuring the meridian, and the prolongation of them as far as Barcelona.

This work was entrusted to Méchain and Delambre, who carried it on during the seven years from 1791 to 1798, notwithstanding many great difficulties and dangers. The unit of length adopted in their operations was the toise of Peru, and from the arc of $9^{\circ} 40' 45''$ actually measured, they inferred the length of an arc of the meridian extending from the equator to the pole to be 5,130,740 toises. As the meter was to be one ten millionth of that distance, its length was made 0.5130740 of a toise, or, in the language of the committee, 443.296 lines of the toise of Peru at a temperature of 13° Reaumur ($16\frac{1}{4}^{\circ}$ C. or $61\frac{1}{4}^{\circ}$ F.).¹

Before attempting to estimate how accurately the standards we have been considering were intercompared it will be well to describe briefly the methods by which the comparisons were effected. In 1742 Graham used the only instruments then known for the purpose—namely, very exact beam compasses of various kinds, one having parallel jaws for taking the lengths of the standard rods, another with rounded ends for taking the lengths of the hollow beds, and still another having fine points in the usual manner. The jaws, or points, of all these instruments were movable by micrometer screws having heads divided to show the eight hundredth part of an inch directly, and the tenth of that quantity by estimation; but Mr. Graham did not consider that the measurements could be depended upon to a greater accuracy than one 1600th of an inch.²

Troughton is generally regarded as the author of the application of micrometer microscopes to the comparison of standards of length, but the earliest record of their use for that purpose is by Sir George Shuckburgh in his work for the improvement of the standards of weight and measure in 1796–8.³ Since then their use has been general; first, because they are more accurate than beam compasses,

¹ 19, pp. 432, 433 and 642.

² 7, pp. 545–6.

³ 18, p. 137.

and, second, because they avoid the injury to standard scales which necessarily results from placing the points of beam compasses upon their graduations. As the objective of the microscope forms a magnified image of the standard, upon which the micrometer wires are set by the aid of the eye piece, it is evident that in order to reduce the effect of imperfections in the micrometer, the objective should have the largest practicable magnifying power. To show the progress in that direction the optical constants of the microscopes, by means of which some of the most important standards have been compared, are given in the accompanying table.

Date.	Observer.	Power of microscope.	Magnifying power of objective.	Equivalent focus of eye-piece.	Value of one revolution of micrometer screw.
				<i>Inches.</i>	<i>Inches.</i>
1797	Sir Geo. Shuckburgh -----	14	1.7	1.50	0.01000
1817	Capt. Henry Kater -----	18	(2.3)	-----	.00428
1834	Francis Baily -----	27	(2.0)	$\frac{1}{2}$.00500
1834	Lieut. Murphy, R. E. -----	-----	(2.0)	-----	.00500
1850	R. Sheepshanks -----	-----	(2.8)	-----	.00358
1864	Gen. A. R. Clarke, R. E. -----	60	4.	0.67	.00287
1880	Prof. W. A. Rogers, 1 in. obj. -----	-----	(12.7)	-----	.00079
	" " $\frac{1}{2}$ in. obj. -----	-----	(28.6)	-----	.00035
	" " $\frac{1}{4}$ in. obj. -----	-----	(52.7)	-----	.00019
1883	International Bureau -----	90	7.5	0.83	0.00394

NOTE.—The magnifying power of Sir Geo. Shuckburgh's microscope seems to be referred to a distance of twelve inches for distinct vision. The powers inclosed in parentheses are estimated upon the assumption that the respective micrometer screws had one hundred threads per inch.

In the memoirs of the French Academy nothing is said respecting the method adopted by the Academicians for comparing their various toises; but in his astronomy, Lalande states that the comparisons were effected partly by beam compasses, and partly by superposing the toises upon each other and examining their ends, both by touch and with magnifying glasses; they being all end standards.¹ For the definitive adjustment of the length of their

¹16, p. 8.

meters, which were also end standards, the French Metric Commission used a lever comparator by Lenoir.

In 1742 Graham used beam compasses, which he considered trustworthy to 0·00062 of an inch, in comparing standards of length; but at that time the French Academicians made their comparisons of toises only to one twentieth, or one thirtieth of a line, say 0·00300 of an inch, and it was not until 1758 that La Condamine declared they should be compared to 0·01 of a line, or 0·00089 of an English inch "if our senses aided by the most perfect instruments can attain to that."¹ Half a century later, ten times that accuracy was attained by the lever comparator of Lenoir, which was regarded as trustworthy to 0·000077 of an inch.²

The heads of micrometer microscopes are usually divided into one hundred equal parts, and if we regard one of these parts as the least reading of a microscope, then in 1797, Sir George Shuckburgh's microscopes read to one ten thousandth of an inch; and the least reading of microscopes made since that date has varied from one twenty thousandth to one thirty-five thousandth of an inch. A few investigators, among whom may be mentioned Professor W. A. Rogers, of Colby University, have made the least reading of their microscopes as small as one 90,000 of an inch, but it is doubtful if there is any advantage in so doing. At the present day the errors committed in comparing standards arise, not from lack of power in the microscopes, but from the difficulty of determining sufficiently exactly the temperature of the standard bars, and the effect of flexure upon the position of their graduations. In order to ascertain the length of a three foot standard with an error not exceeding 0·000020 of an inch, its temperature must be known to 0·06° F. if it is of brass, or to 0·09° F. if it is of iron. To get thermometers that will indicate their own temperature to that degree of accuracy is by no means easy, but to determine the temperature of a bar from their readings is far more difficult. Again, we imagine the length of our standards to follow their temperature rigorously, but what proof is there that such is the case? If we determine the freezing point of an old thermometer, then raise it to the temperature of boiling water, and immediately thereafter again determine its freezing point, we invariably find that the freezing point has fallen a little; and we explain this by saying that the glass has taken a set, from which it

¹14, p. 483.

²Base du Système Métrique. T. 3, pp. 447-462.

requires time to recover. Is it not probable that an effect similar in kind, although less in degree, occurs in all solids when their temperature is varying? When we look at the highly polished terminals of an end standard, we are apt to regard them as mathematical surfaces, separated by an interval which is perfectly definite, and which could be measured with infinite precision if we only had the necessary instrumental appliances; but is that a correct view? The atomic theory answers emphatically, No. According to it, all matter consists of atoms, or molecules, of a perfectly definite size, and with definite intervals between them; but even if that is denied, the evidence is now overwhelming that matter is not homogeneous, but possesses a grain of some kind, regularly repeated at intervals which cannot be greater than one 2,000,000th nor less than one 400,000,000th of an inch. Accordingly, we must picture our standard bar as a conglomeration of grains of some kind or other, having magnitudes of the order specified, and all in ceaseless motion, the amplitude of which depends upon the temperature of the bar. To our mental vision the polished terminals are therefore like the surface of a pot of boiling water, and we recognize that there must be a limit to the accuracy with which the interval between them can be measured. As a basis for estimating how near this limit we have approached, it will suffice to say that for fifty years past it has been customary to state comparisons of standards of length to one 1,000,000th of an inch. Nevertheless, most authorities agree that although one 100,000th of an inch can be distinguished in the comparators, one 25,000th of an inch is about the limit of accuracy attainable in comparing standards. Possibly such a limit may be reached under the most favorable circumstances, but in the case of the yard and the meter, which are standard at different temperatures, the following values of the meter by observers of the highest repute render it doubtful if any thing like that accuracy has yet been attained.

1818.	Capt. Henry Kater	39.37079 inches.
1866.	Gen. A. R. Clarke	39.37043 “
1883.	Prof. Wm. A. Rogers	39.37027 “
1885.	Gen. C. B. Comstock	39.36985 “

The earliest standard of English weight of which we have any very definite knowledge is the mint pound of the Tower of London. It weighed 5,400 troy grains, and the coinage was regulated by it

up to the year 1527, when it was abolished in favor of the troy pound of 5,760 grains. Contemporaneously with the tower pound there was also the merchant's pound, whose exact weight is now involved in so much doubt that it is impossible to decide whether it consisted of 6,750 or of 7,200 grains. The tower pound and the troy pound were used for weighing only gold, silver, and drugs, while all other commodities were weighed by the merchant's pound until the thirteenth or fourteenth century, and after that by the avoirdupois pound. It is not certainly known when the troy and avoirdupois pounds were introduced into England, and there is no evidence of any relation between them when they first became standards. The present avoirdupois pound can be clearly proved to be of similar weight to the standard avoirdupois pound of Edward III (A. D. 1327-1377), and there is good reason for believing that no substantial change has occurred either in its weight or in that of the troy pound since their respective establishment as standards in England.

The oldest standard weights now existing in the English archives date from the reign of Queen Elizabeth, and consist of a set of bell-shaped avoirdupois weights of 56, 28, and 14 pounds, made in 1582 and 7, 4, 2, and 1 pounds made in 1588; a set of flat circular avoirdupois weights of 8, 4, 2, and 1 pounds, and 8, 4, 2, 1, $\frac{1}{2}$, $\frac{1}{4}$, $\frac{1}{8}$, and $\frac{1}{16}$ ounces, made in 1588; and a set of cup-shaped troy weights, fitting one within the other, of 256, 128, 64, 32, 16, 8, 4, 2, 1, $\frac{1}{2}$, $\frac{1}{4}$, $\frac{1}{8}$ (hollow), and $\frac{1}{16}$ (solid) ounces, also made in 1588.¹ All these standards were constructed by order of Queen Elizabeth, under the direction of a jury composed of eighteen merchants and eleven goldsmiths of London; the avoirdupois weights being adjusted according to an ancient standard of 56 pounds, remaining in the Exchequer from the time of Edward III; and the troy weights being adjusted according to the ancient standard in Goldsmiths' Hall.²

In view of the fact that the weight mentioned in all the old acts of Parliament, from the time of Edward I (A. D. 1274-1307) is universally admitted to be troy weight, the Parliamentary Committee of 1758, appointed to inquire into the original standards of weights and measures in England, recommended that the troy pound should be made the unit or standard by which the avoirdupois and other weights should be regulated; and by their order three several

¹11, p. 430.

²11, pp. 435 and 443-448.

troy pounds of soft gun-metal were very carefully adjusted under the direction of Mr. Joseph Harris, who was then assay master of the Mint. To ascertain the proper mass for these pounds the committee caused Messrs. Harris and Gregory, of the Mint, to perform the following operations in their presence:¹

First.—In the before-mentioned set of troy weights, made in 1588, which were then the Exchequer standard, each weight, from that of 4 ounces up to that of 256 ounces, was compared successively with the sum of all the smaller weights; and by a process for which no valid reason can be assigned,² it was concluded from these weighings that the troy pound composed of the 8 and 4 ounce weights was $1\frac{1}{2}$ grains too light.

Second.—The aforesaid 8 and 4 ounce weights of the Exchequer were compared with five other authoritative troy pounds, four of which belonged to the Mint and one to Mr. Freeman, who, like his father before him, was scale maker to the mint, and from the mean of these weighings it appeared that the sum of the Exchequer 8 and 4 ounce weights was one grain too light.

The Committee adopted the mean between the latter result and that which they had deduced from the Exchequer weights alone,² and accordingly Mr. Harris made each of his three troy pounds $1\frac{1}{4}$ grains heavier than the sum of the Exchequer 8 and 4 ounce weights; but sixty-six years were destined to elapse before Parliament took action respecting them.

The Commissioners appointed in 1818 to establish a more uniform system of weights and measures, repeated the recommendations of the committee of 1758,³ and as the avoirdupois pound which had long been used, although not legalized by any act of the legislature, was very nearly 7,000 troy grains, they recommended that 7,000 such troy grains be declared to constitute a pound avoirdupois.⁴ These recommendations were embodied in the act of Parliament of June 17, 1824, and thus one of the troy pounds made in 1758 became the Imperial standard. That standard, like Bird's standard yard, was deposited in the Houses of Parliament and was burned up with them in October, 1834.

The present English standard pound was made in 1844-46 by Prof. W. H. Miller, who was one of the members of the Commission appointed in 1843 to superintend the construction of the new par-

¹ 11, p. 437. ² See Note B, below. ³ See 23, 24, and 25. ⁴ 28, pp. 4-5.

liamentary standards of length and weight destined to replace those destroyed in 1834. A number of weights had been very accurately compared with the lost standard; namely, in 1824 or 1825, by Capt. Kater, five troy pounds of gun-metal, destined respectively for the use of the Exchequer, the Royal Mint, and the cities of London, Edinburgh, and Dublin; and in 1829, by Capt. v. Nehus, two troy pounds of brass and one of platinum, all in the custody of Prof. Schumacher, and a platinum troy pound belonging to the Royal Society. The first step for recovering the mass of the lost standard was manifestly to compare these weights among themselves, and upon so doing it was found that for the brass and gun-metal weights the discrepancies between the weighings made in 1824 and 1844 amounted to $0\cdot0226^1$ of a grain, while for the two platinum weights the discrepancies between the weighings made in 1829 and 1845 was only $0\cdot00019^2$ of a grain. With a single exception, all the *new* brass or gun-metal weights had become heavier since their first comparison with the lost standard, the change being probably due to oxydation of their surfaces, and on that account the new standard was made to depend solely upon the two platinum weights. For convenience of reference these weights were designated respectively Sp (Schumacher's platinum), and RS (Royal Society). A provisional platinum troy pound, T, intermediate in mass between Sp and RS was next prepared, and from 286 comparisons made in January, February, July, and August, 1845, it was found that in a vacuum³

$$T = \text{Sp} + 0\cdot00105 \text{ grain,}$$

while from 122 comparisons made in January, July, and August, 1845,

$$T = \text{RS} - 0\cdot00429 \text{ grain.}$$

By combining these values with the results of the weighings made in 1824-29, namely,

$$\text{Sp} = \text{U} - 0\cdot52956 \text{ grain,}$$

$$\text{RS} = \text{U} - 0\cdot52441 \text{ grain,}$$

where U designates the lost standard—the comparisons with Sp gave

$$T = \text{U} - 0\cdot52851 \text{ grain,}$$

while those with RS gave

$$T = \text{U} - 0\cdot52870 \text{ grain.}$$

¹ 40, p. 772.

² 40, p. 941.

³ 40, pp. 819-20.

To the first of these expressions double weight was assigned, because the comparisons of T and U with Sp were about twice as numerous as those with RS. The resulting mean was therefore

$$T = U - 0.52857 \text{ grains} = 5759.47143 \text{ grains,}$$

and from that value of T the new standard avoirdupois pound of 7000 grains was constructed.

From some time in the fifteenth century until the adoption of the metric system in August, 1793, the system of weights employed in France was the *poids de marc*, having for its ultimate standard the *pile de Charlemagne*, which was then kept in the Mint, and is now deposited in the Conservatoire des Arts et Métiers. The table of this weight was

72 grains = 1 gros =	72 grains.
8 gros = 1 once =	576 "
8 onces = 1 marc =	4608 "
2 marcs = 1 livre =	9216 "

The origin of the *pile de Charlemagne* is not certainly known, but it is thought to have been made by direction of King John (A. D. 1350-1364). It consists of a set of brass cup-weights, fitting one within the other, and the whole weighing fifty marcs. The nominal and actual weights of the several pieces are as follows:¹

	<i>Marcs.</i>	<i>Grains.</i>
Boîte de 20 marcs . . .	20	+ 1.4
Pièce de 14 " . . .	14	+ 4.5
de 8 " . . .	8	— 0.4
de 4 " . . .	4	— 2.1
de 2 " . . .	2	— 1.0
de 1 " . . .	1	— 0.7
Marc divisé . . .	1	— 1.7
	50	± 0.0

In determining the relation of the *poids de marc* to the metric weights, the committee for the construction of the kilogram regarded the entire *pile de Charlemagne* as a standard of fifty marcs, and considered the individual pieces as subject to the corrections stated. On that basis they found

$$1 \text{ kilogram} = 18827.15 \text{ French grains}^2$$

and as a kilogram is equal to 15432.34874³ English troy grains, we have

$$\begin{aligned} 1 \text{ livre, poids de marc} &= 7554.22 \text{ troy grains.} \\ &= 489.506 \text{ grams.} \end{aligned}$$

¹17, pp. 270-71. ²Base du Système Métrique. T. 3, p. 638. ³40, p. 893.

The metric standard of weight, called a kilogram, was constructed under the direction of the French Academy of Sciences simultaneously with the meter; the work being done principally by Lefèvre-Gineau and Borda. It was intended that the kilogram should have the same mass as a cubic decimeter of pure water at maximum density, and the experimental determination of that mass was made by finding the difference of weight in air and in water of a hollow brass cylinder whose exterior dimensions at a temperature of 17.6° C. were, height = 2.437672 decimeters, diameter = 2.428368 decimeters, volume = 11.2900054 cubic decimeters. The difference of weight in question was first measured in terms of certain brass weights, by the aid of which the platinum kilogram of the archives was subsequently constructed, special care being taken to apply the corrections necessary to reduce all the weighings to what they would have been if made in a vacuum.¹

The best results hitherto obtained for the weight of a cubic decimeter of water, expressed in terms of the kilogram of the archives, are as follows:²

Date.	Country.	Observer.	Weight of a cubic decimeter of water at 4° C.
1795	France	Lefèvre-Gineau	<i>Grams.</i> 1000.000
1797	England	Shuckburgh and Kater	1000.480
1821			
1825	Sweden	Berzelius, Svanberg, and Akermann	1000.296
1830	Austria	Stampfer	999.653
1841	Russia	Kupffer	999.989
		Mean	1000.084

¹ Base du Système Métrique, T. 3, pp. 574-5.

² This table has been deduced from the data given by Prof. Miller in 40, p. 760.

These results show the extreme difficulty of determining the exact mass of a given volume of water. The discordance between the different observers amounts to more than one part in a thousand, while good weighings are exact to one part in eight or ten millions. Without doubt two weights can be compared at least a thousand times more accurately than either of them can be reproduced by weighing a specified volume of water, and for that reason the kilogram, like the English pound, can now be regarded only as an arbitrary standard of which copies must be taken by direct comparison. As already stated, the kilogram is equivalent to 15432.34874 English troy grains, or about two pounds three ounces avoirdupois.

In consequence of the circumstance that the mass of a body is not affected either by temperature or flexure, weighing is an easier process than measuring; but in order to obtain precise results many precautions are necessary. Imagine a balance with a block of wood tied to its right-hand pan and accurately counterpoised by lead weights in its left-hand pan. If with things so arranged the balance were immersed in water the equilibrium would be instantly destroyed and to restore it all the weights would have to be removed from the left-hand pan, and some of them would have to be placed in the right-hand pan to overcome the buoyancy of the wood. The atmosphere behaves precisely as the water does, and although its effect is minute enough to be neglected in ordinary business affairs, it must be taken into account when scientific accuracy is desired. To that end the weighing must either be made in a vacuum, or the difference of the buoyant effect of the air upon the substances in the two pans must be computed and allowed for. As very few vacuum balances exist, the latter method is usually employed. The data necessary for the computation are the latitude of the place where the weighing is made and its altitude above the sea level; the weights, specific gravities, and coefficients of expansion of each of the substances in the two pans; the temperature of the air, its barometric pressure, and the pressure, both of the aqueous vapor, and of the carbonic anhydride, contained in it.

Judging from the adjustment of the *pile de Charlemagne*, and the Exchequer troy weights of Queen Elizabeth, the accuracy attained in weighing gold and silver at the mints during the fourteenth, fifteenth, and sixteenth centuries must have been about one part in ten thousand. The balance which Mr. Harris of the Lou-

don mint used in 1743 indicated one-eighth of a grain on a troy pound, or about one part in 50,000; while according to Sir George Shuckburgh the balance used by Messrs. Harris and Bird in making their observations upon the Exchequer weights, apparently in 1758 or 1759, turned with one 230,000th part of its load.¹ In 1798 Sir George Shuckburgh had a balance sensitive enough to indicate 0.01 of a grain when loaded with 16,000 grains, or about one part in 1,600,000. The balance used by Fortin in 1799, in adjusting the kilogram of the archives, was not quite so delicate, its sensitiveness being only the 1,000,000th part of its load; but in 1844, for the adjustment of the present English standard pound, Professor Miller employed a balance whose index moved about 0.01 of an inch for a change of 0.002 of a grain in a load of 7,000 grains.² He read the index with a microscope, and found the probable error of a single comparison of two avoirdupois pounds to be one 12,000,000th of either, or about 0.00058 of a grain. At the present time it is claimed that two avoirdupois pounds can be compared with an error not exceeding 0.0002 of a grain; and two kilograms with an error not exceeding 0.02 of a milligram.

The mean solar day is the natural unit of time for the human race, and it is universally adopted among all civilized nations. Our ultimate standard of time is therefore the rotation of the earth upon its axis, and from that rotation we determine the errors of our clocks and watches by astronomical observations. For many purposes it suffices to make these observations upon the sun, but when the utmost precision is desired it is better to make them on the stars. Until the close of the seventeenth century quadrants were employed for that purpose, and so late as 1680 Flamsteed, the first English astronomer royal, thought himself fortunate when he succeeded in constructing one which enabled him to be sure of his observed times within three seconds.³ About 1690 Roemer invented the transit instrument, which soon superseded the quadrant, and still remains the best appliance for determining time. Most of his observations were destroyed by a fire in 1728, but the few which have come down to us show that as early as 1706 he determined time with an accuracy which has not yet been very greatly sur-

¹ 18, p. 148. ² 40, pp. 762 and 943.

³ Account of the Rev. John Flamsteed. By Francis Baily. pp. 45-6. (London, 1835. 4to.)

passed. Probably the corrections found in the least square adjustment of extensive systems of longitude determinations afford the best criterion for estimating the accuracy of first-class modern time observations, and from them it appears that the error of such observations may rise as high as ± 0.05 of a second.

During the intervals between successive observations of the heavenly bodies we necessarily depend upon clocks and chronometers for our knowledge of the time, and very erroneous ideas are frequently entertained respecting the accuracy of their running. The subject is one upon which it is difficult to obtain exact information, but there are few time-pieces which will run for a week without varying more than three-quarters of a second from their predicted error. As the number of seconds in a week is 604,800, this amounts to saying that the best time-pieces can be trusted to measure a week within one part in 756,000. Nevertheless, clocks and chronometers are but adjuncts to our chief time-piece, which is the earth itself, and upon the constancy of its rotation depends the preservation of our present unit of time. Early in this century Laplace and Poisson were believed to have proved that the length of the sidereal day had not changed by so much as the one hundredth part of a second during the last 2,500 years, but later investigations show that they were mistaken, and, so far as we can now see, the friction produced by the tides in the ocean must be steadily reducing the velocity with which the earth rotates about its axis. The change is too slow to become sensible within the lifetime of a human being, but its ultimate consequences will be most momentous.

Ages ago it was remarked that all things run in cycles, and there is enough truth in the saying to make it as applicable now as on the day it was uttered. The Babylonian or Chaldean system of weights and measures seems to be the original from which the Egyptian system was derived, and is probably the most ancient of which we have any knowledge. Its unit of length was the cubit, of which there were two varieties, the natural and the royal. The foot was two-thirds of the natural cubit. Respecting the earliest Chaldean and Egyptian system of weights no very satisfactory information exists, but the best authorities agree that the weight of water contained in the measure of a cubic foot constituted the talent, or larger unit of weight, and that the sixtieth or fiftieth parts of the talent constituted, respectively, the Chaldean and Egyptian values of the mina, or lesser unit of commercial weight. Doubtless these weights

varied considerably at different times and places, just as the modern pound has varied, but the relations stated are believed to have been the original ones. The ancient Chaldeans used not only the decimal system of notation, which is evidently the primitive one, but also a duodecimal system, as shown by the division of the year into twelve months, the equinoctial day and night each into twelve hours, the zodiac into twelve signs, etc., and a sexagesimal system by which the hour was divided into sixty minutes, the signs of the zodiac into thirty parts or degrees, and the circle into 360 degrees, with further sexagesimal subdivisions. The duodecimal and sexagesimal systems seem to have originated with the Chaldean astronomers, who, for some reason which is not now evident, preferred them to the decimal system, and by the weight of their scientific authority impressed them upon their system of weights and measures. Now observe how closely the scientific thought of to-day repeats the scientific thought of four thousand years ago. These old Chaldeans took from the human body what they regarded as a suitable unit of length, and for their unit of mass they adopted a cube of water bearing simple relations to their unit of length. Four thousand years later, when these simple relations had been forgotten and impaired, some of the most eminent scientists of the last century again undertook the task of constructing a system of weights and measures. With them the duodecimal and sexagesimal systems were out of favor, while the decimal system was highly fashionable, and for that reason they subdivided their units decimally instead of duodecimally, sexagesimally, or by powers of two; but they reverted to the old Chaldean device for obtaining simple relations between their units of length and mass, and to that fact alone the French metric system owes its survival. Every one now knows that the meter is not the ten millionth part of a quadrant of the earth's meridian, and in mathematical physics, where the numbers are all so complicated that they can only be dealt with by the aid of logarithms, and the constant π , an utterly irrational quantity, crops up in almost every integral, mere decimal subdivision of the units counts for very little. But in some departments of science, as, for example, chemistry, a simple relation between the unit of length (which determines volume), the unit of mass, and the unit of specific gravity, is of prime importance; and wherever that is the case the metric system will be used. To engineers such relations are of small moment, and consequently among English-speaking engineers the metric system is making no

progress, while, on the other hand, the chemists have eagerly adopted it. As the English yard and pound are the direct descendants of the Chaldean-Babylonian natural cubit and mina, it is not surprising that the yard should be only 0.48 of an inch shorter than the double cubit, and the avoirdupois pound only 665 grains lighter than the Babylonian commercial mina; but, considering the origin of the metric system, it is rather curious that the meter is only 1.97 inches shorter than the Chaldean double royal cubit, and the kilogram only 102 grains heavier than the Babylonian royal mina. Thus, without much exaggeration, we may regard the present English and French fundamental units of length and mass as representing respectively the commercial and royal units of length and mass of the Chaldeans of four thousands years ago.

Science tells us that the energy of the solar system is being slowly dissipated in the form of radiant heat; that ultimately the sun will grow dim; life will die out on the planets; one by one they will tumble into the expiring sun; and at last darkness and the bitter cold of the absolute zero will reign over all. In that far-distant future imagine some wandering human spirit to have penetrated to a part of space immeasurably beyond the range of our most powerful telescopes, and there, upon an orb where the mechanical arts flourish as they do here, let him be asked to reproduce the standards of length, mass, and time with which we are now familiar. In the presence of such a demand the science of the seventeenth and eighteenth centuries would be powerless. The spin of the earth which measures our days and nights would be irretrievably gone; our yards, our meters, our pounds, our kilograms would have tumbled with the earth into the ruins of the sun, and become part of the debris of the solar system. Could they be recovered from the dead past and live again? The science of all previous ages mournfully answers, No; but with the science of the nineteenth century it is otherwise. The spectroscope has taught us that throughout the visible universe the constitution of matter is the same. Everywhere the rhythmic motions of the atoms are absolutely identical, and to them, and the light which they emit, our wandering spirit would turn for the recovery of the long-lost standards. By means of a diffraction grating and an accurate goniometer he could recover the yard from the wave length of sodium light with an error not exceeding one or two thousandths of an inch. Water is everywhere, and with his newly re-

covered yard he could measure a cubic foot of it, and thus recover the standard of mass which we call a pound. The recovery of our standard of time would be more difficult; but even that could be accomplished with an error not exceeding half a minute in a day. One way would be to perform Michelson's modification of Foucault's experiment for determining the velocity of light. Another way would be to make a Siemen's mercury unit of electrical resistance, and then, either by the British Association method, or by Lord Rayleigh's modification of Lorenz's method, find the velocity which measures its resistance in absolute units. Still another way would be to find the ratio of the electro-static and electro-magnetic units of electricity. Thus all the units now used in transacting the world's business could be made to reappear, if not with scientific, at least with commercial accuracy, on the other side of an abyss of time and space before which the human mind shrinks back in dismay. The science of the eighteenth century sought to render itself immortal by basing its standard units upon the solid earth, but the science of the nineteenth century soars far beyond the solar system and connects its units with the ultimate atoms which constitute the universe itself.

NOTE A.

The appended table exhibits the principal comparisons hitherto made of the more important early English standards of length. The significations of the reference numbers, and the authorities for the descriptions of the standards, are as follows:

No. 1. Standard yard of Henry VII (1490); an end measure formed of an octagonal brass rod half an inch in diameter.

No. 2. Standard yard of Queen Elizabeth (1588); an end measure formed of a brass rod six-tenths of an inch square.

No. 3. Matrix to Queen Elizabeth's standard yard (1588); of brass, $1\frac{1}{2}$ inches wide, 1 inch thick, and 49 inches long.

No. 4. Standard ell of Queen Elizabeth (1588); an end measure of brass, six-tenths of an inch square.

No. 5. Standard yard of the Clock-makers' Company (1671); a matrix, formed by two pins in an octagonal brass rod half an inch in diameter.

No. 6. Standard yard at the Tower; a line measure, marked on a brass bar seven-tenths of an inch square and 41 inches long.

No. 7. Graham's Royal Society scale (1742); a line measure, on a brass bar half an inch wide, one-quarter of an inch thick, and 42 inches long. Line marked E. Mem. Roy. Ast. Soc., Vol. 9, p. 82.

No. 8. Ditto. Line marked Exch.

No. 9. Ditto. Paris half toise; marked F.

Numbers 1 to 9 are described in the Philosophical Transactions, 1743, pp. 547-550.

No. 10. Bird's standard yard of 1758; a line measure, on a brass bar 1.01 inches square, and 39.06 inches long. Mem. Roy. Ast. Soc., Vol. 9, p. 80.

No. 11. Bird's standard yard of 1760; a line measure, on a brass bar 1.05 inches square, and 39.73 inches long. Mem. Roy. Ast. Soc., Vol. 9, pp. 80-82.

No. 12. General Roy's scale; a line measure, upon a brass bar 0.55 of an inch broad, about 0.22 of an inch thick, and 42.8 inches

long; divided by Bird. *Phil. Trans.*, 1785, p. 401, and Measurement of Lough Foyle Base, p. 73.

No. 13. Ramsden's bar, used in the trigonometrical survey of Great Britain. *Phil. Trans.*, 1821, p. 91; and Measurement of Lough Foyle Base, pp. 73-4.

No. 14. Sir Geo. Shuckburgh's scale (1796); a line measure, upon a brass bar 1.4 inches broad, 0.42 of an inch thick, and 67.7 inches long. Space compared, 0ⁱⁿ to 36ⁱⁿ. *Phil. Trans.*, 1798, p. 133, and *Mem. Roy. Ast. Soc.*, Vol. 9, pp. 84-5.

No. 15. Ditto. Space compared, 10ⁱⁿ to 46ⁱⁿ.

No. 16. Ordnance yard 1A (1827); a line measure, upon an iron bar 1.45 inches broad, 2.5 inches deep, and rather more than 3 feet long. Measurement of Lough Foyle Base, pp. 71, 82 and [28].

No. 17. Ordnance yard 2A (1827). Similar to 1A. Same authorities.

No. 18. Captain Kater's Royal Society yard (1831); a line measure, upon a brass plate 0.07 of an inch thick. *Phil. Trans.*, 1831, p. 345.

No. 19. The Royal Astronomical Society's standard scale (1834); a line measure, upon a brass tube 1.12 inches exterior diameter, 0.74 of an inch interior diameter, and 63 inches long. The central yard was the space compared. *Mem. Roy. Ast. Soc.*, Vol. 9, p. 69.

No. 20. "Col. Lambton's standard;" a line measure, upon a brass plate 0.92 of an inch broad, 0.21 of an inch thick, and 66½ inches long; strengthened by an edge bar of nearly the same breadth, but only 0.08 of an inch thick. *Phil. Trans.*, 1821, p. 88, and *Mem. Roy. Ast. Soc.*, Vol. 9, pp. 82-3.

The authorities for the comparisons given in the various columns of the table are as follows:

Column A.—Comparisons by Mr. George Graham. *Phil. Trans.*, 1743, pp. 187, and 547-550.

Column B.—Comparisons by Sir Geo. Shuckburgh. *Phil. Trans.*, 1798, pp. 167-181.

Column C.—Comparisons by Capt. Kater. *Phil. Trans.*, 1818, p. 55, and 1821, p. 91.

Column D.—Comparisons by Capt. Kater. Phil. Trans., 1830, p. 377, and 1831, p. 347.

Column E.—Comparisons by Francis Baily, Esq. Mem. Roy. Ast. Soc., Vol. 9, p. 145.

Column F.—Comparisons by Francis Baily, Esq. Mem. Roy. Ast. Soc., Vol. 9, p. 120.

Column G.—Values adopted by R. Sheepshanks, Esq. Phil. Trans., 1857, p. 661.

The values used by Mr. Sheepshanks in 1848 to determine the length of the present Imperial standard yard were Nos. 14 D, 15 F, 16 and 17 G, and 18 D.

It will be observed that several different units are employed in the various columns of the table, and care must be taken to allow for that circumstance when comparing numbers not situated in the same column.

Comparisons of the Fundamental English Standards of Length.

Ref. No.	A.	B.	C.	D.	E.	F.	G.
	<i>Inches.</i>	<i>Inches.</i>	<i>Inches.</i>	<i>Inches.</i>	<i>Inches.</i>	<i>Inches.</i>	<i>Inches.</i>
1.....	35·9929	35·966					
2.....	36·0000	35·993					
3.....	36·0102						
4.....	45·0494	44·964					
5.....	35·9790						
6.....	36·0111						
7.....	36·0075	36·0013	36·002007	36·001473		
8.....	36·0000	35·9933	35·993684		
9.....	38·355	38·3561					
10.....	36·00023	36·000802				
11.....	36·000659	36·000000	35·999624	36·000000	36·000000
12.....	36·001537				
13.....	36·003147				
14.....	36·000642	36·00009	36·000185		
15.....	36·0000	35·999921	36·000058	
16.....	35·999716
17.....	35·999892
18.....	35·99938			
19.....	36·000000		
20.....	36·000000				

NOTE B.

By direction of the Parliamentary Committee of 1758, and in the presence both of that body and of Mr. Farley, deputy chamberlain, Messrs. Harris and Gregory of the London Mint compared the several standard troy weights of the Exchequer, with the following results :

4-oz. weight	=	All smaller weights	-	$\frac{1}{4}$ grain.
8-oz. " "	=	" "	+	$\frac{1}{2}$ "
16-oz. " "	=	" "	+	$\frac{1}{4}$ "
32-oz. " "	=	" "	+	2 grains.
64-oz. " "	=	" "	+	3 "
128-oz. " "	=	" "	+	14 "
256-oz. " "	=	" "	-	21 "

The weighings which yielded these results were made at the London Mint; the instruments employed being "a very curious and exact pair of scales, belonging to Mr. Harris, and the scales used at the Mint for the weighing of gold." After recording the results in their report,¹ the Committee continued as follows :

"Therefore beginning the difference from the sixteen-ounce weight, and carrying it on to the greatest troy weight in the Exchequer, the total difference will be eight grains and one-half."

"The fourth part of which is two grains upon sixteen ounces, which is a grain and a half upon the twelve ounces or pound troy."

"Then the eight and four ounces troy of the Exchequer were compared with the following weights :

"*First*, with the pound troy used at the Mint in weighing of gold, which was heavier than that at the Exchequer one grain."

"*Secondly*, with the eight and four ounces at the Mint of the 6th of Queen Anne, 1707, which was heavier than that at the Exchequer half a grain."

"The eight and four ounces of Queen Elizabeth 1588 at the Mint, was heavier than that at the Exchequer three quarters of a grain; another of the same year of Queen Elizabeth at the Mint, stamp'd with a tower, a thistle and crown, and EL and crown, was heavier than that at the Exchequer one grain."

“Mr. *Freeman* produced a four and eight ounce of the 6th of Queen *Anne* 1707 by which he makes weights for sale, which was heavier than the same weights at the Exchequer one grain and three quarters: Therefore, upon an average of all these weights, the pound troy should be one grain heavier than the weights at the Exchequer, and that added to the grain and a half, which, upon the former experiments, the weights at the Exchequer are too light a medium taken from thence makes the proper increase of the Exchequer pound troy to be one grain and one quarter.”

“And it is to be observed, that the pound troy weight at the Mint, which is now used for gold, and the eight and four ounces at the Mint, marked with a tower, and in the time of Queen *Elizabeth*, are both one grain heavier than the eight and four ounces of the Exchequer.”

“And considering that the Exchequer weights have been used ever since the 30th of Queen *Elizabeth*, 1588, one hundred and seventy years to size other weights by, it is highly probable that the difference may have been occasioned by the frequent use of the standard.”

“Your Committee endeavored to compare the troy weights with the original standard at *Goldsmith's Hall*, from whence it is said, in the afore-said verdict of the 29th and 30th of *Elizabeth*, that the weights now at the Exchequer were made, and for that purpose sent to *Goldsmith's Hall* for the said weights; but were informed that no such were to be found there, the Goldsmith's having no weights older than those at the Exchequer;”

The Committee's statement respecting the way in which the correction of $1\frac{1}{2}$ grains was deduced from the weighings of the Exchequer weights is very obscure, and the result is not justified by generally accepted principles. If we put x for the sum of all the weights smaller than 4 ounces, then the results of the weighings made by the Committee may be written in the form:

$$\begin{aligned}
 4\text{-oz. divided} &= 1 x \\
 4\text{-oz. weight} &= 1 x - \frac{1}{4} \text{ grain.} \\
 8\text{-oz. weight} &= 2 x + \frac{1}{4} \text{ grain.} \\
 16\text{-oz. weight} &= 4 x + \frac{1}{4} \text{ grain.} \\
 32\text{-oz. weight} &= 8 x + 2\frac{1}{4} \text{ grains.} \\
 64\text{-oz. weight} &= 16 x + 5\frac{1}{2} \text{ grains.} \\
 128\text{-oz. weight} &= 32 x + 22 \text{ grains.} \\
 256\text{-oz. weight} &= 64 x + 9 \text{ grains.}
 \end{aligned}
 \tag{1}$$

Before proceeding further we must decide in what sense these weights are to be regarded as standards, and perhaps the most natural course will be to regard the entire set as a standard of 512

troy ounces. In that case the summation of the several columns gives

$$512 \text{ ounces} = 128 x + 39 \text{ grains}$$

whence

$$x = 4 \text{ ounces} - 0.3047 \text{ grain} \quad (2)$$

and by substituting that value in the equations (1) we obtain the corrections to the several weights given in the second column of Table I.

TABLE I.—*Corrections to the Exchequer Standard Troy Weights of 1588, derived from the Weighings made by Messrs. Harris and Chisholm.*

Denomination of Weight.	Apparent correction in 1758.	Committee's correction in 1758.	Chisholm's correction in 1873.	Loss by wear in 115 years.
	<i>Grains.</i>	<i>Grains.</i>	<i>Grains.</i>	<i>Grains.</i>
4 ounces divided...	— 0.30	— 0.42	— 1.69	— 1.27
4 ounces55	.67	0.68	0.01
8 ounces36	0.58	1.09	0.51
16 ounces97	1.42	3.84	2.42
32 ounces	— 0.19	1.08	3.82	2.74
64 ounces	+ 0.62	— 1.17	— 5.04	3.87
128 ounces	+ 12.25	+ 8.67	+ 4.28	4.39
256 ounces	— 10.50	— 17.67	— 53.58	— 35.91
Sums	± 0.00	— 14.34	— 65.46	— 51.12

From equations (1) and (2) we have

$$4 \text{ ounces} = 4\text{-oz. weight} + 0.5547 \text{ grain.}$$

$$8 \text{ ounces} = 8\text{-oz. weight} + 0.3594 \text{ grain.}$$

whence it follows that the sum of the eight and four ounce weights, which constituted the Exchequer standard troy pound, was too light by 0.9141 of a grain. As the mean correction obtained from the four weights belonging respectively to the Mint and to Mr. Freeman agrees closely with this result, the true correction to the Exchequer standard must have been very approximately one grain;

and in adopting one and one-quarter grains the Committee seem to have augmented the weight of the troy pound by about one-quarter of a grain. The corrections which result to the Exchequer troy weights upon the Committee's assumption that the sum of the eight and four ounce weights was one and one-quarter grains too light are given in the third column of Table I; while the fourth column contains the corrections found by Mr. Chisholm in 1873,¹ and the fifth column shows the loss of weight which occurred between 1758 and 1873. In view of the fact that these weights were constantly used for comparing local standards during a period of no less than 225 years, from 1588 to 1825, their excellent preservation is very remarkable.

In the report of the Committee of 1758 there is another set of comparisons of the Exchequer troy weights;² said comparisons having been made on April 14, 1758, in accordance with the directions of the Committee, by Mr. Freeman and Mr. Reed, expert scale makers, in the presence of Mr. Farley, deputy chamberlain. They are as follows:

$\frac{1}{8}$ -oz. hollow	=	$\frac{1}{8}$ -oz. solid	+ $\frac{1}{2}$ grain.
$\frac{1}{4}$ -oz. weight	=	All smaller weights	- $\frac{1}{2}$ grain.
$\frac{1}{2}$ -oz. "	=	"	- $\frac{1}{2}$ "
1-oz. "	=	"	- $\frac{1}{2}$ "
2-oz. "	=	"	- $\frac{1}{2}$ "
4-oz. "	=	"	± 0 grains.
8-oz. "	=	"	± 0 "
16-oz. "	=	"	± 0 "
32-oz. "	=	"	- 2 "
64-oz. "	=	"	± 0 "
128-oz. "	=	"	+ 15 "
256-oz. "	=	"	- 24 "

In these equations the symbol ± 0 is used to indicate the relation which the Committee expressed by saying that the weights "very nearly agreed."

Regarding the entire set of weights as a standard of 512 ounces, and putting x for the mass of the $\frac{1}{8}$ -oz. solid weight, we have

$$\begin{aligned}\frac{1}{8}\text{-oz. solid} &= 1x. \\ \frac{1}{8}\text{-oz. hollow} &= 1x + \frac{1}{2}\text{ grain.}\end{aligned}$$

¹43, p. 21.

²11, p. 435.

$\frac{1}{4}$ -oz. weight	=	$2x$.	
$\frac{1}{2}$ -oz. "	=	$4x$.	
1-oz. "	=	$8x$.	
2-oz. "	=	$16x$.	
4-oz. "	=	$32x + \frac{1}{2}$ grain.	(3)
8-oz. "	=	$64x + 1$ "	
16-oz. "	=	$128x + 2$ grains.	
32-oz. "	=	$256x + 2$ "	
64-oz. "	=	$512x + 6$ "	
128-oz. "	=	$1024x + 27$ "	
256-oz. "	=	$2048x + 15$ "	

Summing the various columns

$$512 \text{ ounces} = 4096x + 54 \text{ grains}$$

whence

$$x = \frac{1}{8} \text{ ounce} - 0.01318 \text{ grains,} \quad (4)$$

and by substituting that value in the equations (3) we obtain the corrections given for the several weights in the second column of Table II. The third column contains the corrections which result upon the Committee's assumption that the sum of the eight and four ounce weights was one and one-quarter grains too light; and the fourth and fifth columns contain corrections given by Mr. Chisholm in his seventh annual report.¹ Mr. Chisholm does not explain how he obtained the corrections quoted in the fourth column of the table, but their close agreement with those in the third column renders it almost certain that they were computed from the comparisons made by Messrs. Freeman and Reed. As the Committee of 1758 used Mr. Harris' weighings *to the exclusion of those by Messrs. Freeman and Reed*, the adoption of the opposite course by Mr. Chisholm is perhaps explained by the circumstance that in his report on the Exchequer standards² *he has quoted the weighings by Messrs. Freeman and Reed and has attributed them to Mr. Harris.*

In addition to being less exact, the weighings by Mr. Freeman differ from those by Mr. Harris principally in the sign of the correction to the 32-ounce weight; the former stating that the 32-ounce weight was lighter than the sum of all the smaller weights, and the latter that it was heavier. To ascertain which was right we have

¹43, p. 21.

²48, p. 11.

only to compare the resulting systems of corrections with those found by Mr. Chisholm in 1873. Table I shows that according to Mr. Harris' weighings all the weights have grown lighter during the interval from 1758 to 1873, while Table II shows that according to Mr. Freeman's weighings some have grown lighter and others heavier, and that by quantities which cannot be attributed to accidental errors in the weighings. In view of these facts there cannot be a doubt that the Committee of 1758 was right in using only Mr. Harris' weighings, and it seems equally certain that the numbers in Table I should be adopted to the exclusion of those in Table II.

TABLE II.—*Corrections to the Exchequer Standard Troy Weights of 1588, derived from the Weighings made by Messrs. Freeman and Chisholm.*

Denomination of Weight.	Apparent correction in 1758.	Committee's correction in 1758	Corrections given by Mr. Chisholm	
			in 1758.	in 1873.
	<i>Grains.</i>	<i>Grains.</i>	<i>Grains.</i>	<i>Grains.</i>
$\frac{1}{8}$ ounce solid -----	— 0·01	— 0·03	0·0	— 0·06
$\frac{1}{8}$ ounce hollow ---	+ 0·49	+ 0·47	+ 0·5	+ 0·40
$\frac{1}{4}$ ounce -----	— 0·03	— 0·06	·0	— 0·21
$\frac{1}{2}$ ounce -----	·05	·11	·0	·36
1 ounce -----	·11	·23	0·0	0·45
2 ounces -----	— 0·21	·46	— 1·0	1·01
4 ounces -----	+ 0·08	·42	0·5	0·68
8 ounces -----	·16	0·83	0·75	1·09
16 ounces -----	+ 0·31	1·68	1·75	3·84
32 ounces -----	— 1·38	5·36	5·5	3·82
64 ounces -----	— 0·75	8·70	— 9·0	— 5·04
128 ounces -----	+ 13·50	2·40	+ 3·0	+ 4·28
256 ounces -----	— 12·00	— 43·81	— 45·0	— 53·58
Sums -----	± 0·00	— 63·62	— 61·0	— 65·46

From comparisons of their troy pound with their avoirdupois pound, and with the two-marc weight sent to them by the French Academy in 1742, the Royal Society of London found¹—

1. That the English avoirdupois pound weighed 7,004 troy grains;
2. That the French *livre*, consisting of two marcs, weighed 7,560 troy grains;

and for three-quarters of a century the latter value was universally accepted. Further, when the metric system came into being, the kilogram was declared to consist of 18,827·15 French grains, of which the *livre* contained 9216²; or, in other words, the kilogram was declared equal to 2·04288 *livres*; whence, *with the Royal Society's value of the livre*, the English equivalent of the kilogram was computed to be 15,444 troy grains.

During some experiments at the London Mint in March, 1820, it was found that the French *livre* belonging to that institution weighed only 7555 troy grains. This discovery led to an examination of the Royal Society's standards of 1742, which had been carefully preserved, and it was found that their *livre* agreed with that at the Mint, but their troy pound was nearly four grains lighter than the Imperial standard of 1758, and their avoirdupois pound weighed only 7000 troy grains instead of 7004.³ Thus it was rendered almost certain that the accepted English equivalent of the kilogram was about ten grains too large, and to remove all possible doubt, a direct comparison of the English and French standards of weight was effected in 1821⁴, through the co-operation of the respective governments, and then it was definitively ascertained that the weight of the kilogram is only 15,433 troy grains.

The facts respecting the Royal Society's standards of 1742 are as follows:

1. The weighings recorded in the Philosophical Transactions, 1743, pages 553 and 556, give

¹6, p. 187. It is usual to designate 1742 as the date of the exchange of standards, but the remark of Cassini de Thury (4, p. 135) shows that the true date must have been prior to April, 1738. In his paper of November, 1742, Graham makes only the indefinite statement that the exchange was "proposed some time since."

²Base du Système Métrique, T. 3, p. 638.

³See 36, Vol. 1, p. 140, and 28, p. 19.

⁴28, pp. 19-22.

$$\text{R. S. troy lb.} = \text{Exch. (8 oz. + 4 oz.)} - \frac{1}{2} \text{ grain.} \quad (5)$$

$$\text{R. S. troy lb.} = \text{Mint (8 oz. + 4 oz.)} - 2\frac{3}{8} \text{ grains.} \quad (6)$$

whence

$$\text{Exch. (8 oz. + 4 oz.)} = \text{Mint (8 oz. + 4 oz.)} - 1\frac{7}{8} \text{ grains.} \quad (7)$$

2. The weighings by Mr. Harris, for the Parliamentary Committee of 1758, give¹

$$\text{Exch. (8 oz. + 4 oz.)} = \text{Mint (8 oz. + 4 oz.)} - \frac{1}{2} \text{ grain.} \quad (8)$$

whence, by (6),

$$\text{R. S. troy lb.} = \text{Exch. (8 oz. + 4 oz.)} - 1\frac{3}{8} \text{ grains.} \quad (9)$$

In equations (6) and (8) the weights at the Mint were those of the sixth of Queen Anne, 1707.

3. In the Philosophical Transactions, 1742, page 187, it is stated that the Paris two-marc weight weighs 7560 troy grains. As the true weight of two marcs is 7554.22 grains, this implies that the Royal Society's troy pound was too light by $5.78 (7560 \div 7560) = 4.40$ grains.

In the Philosophical Transactions, 1742, page 187, it is stated that the Royal Society's avoirdupois pound weighed 7004 troy grains, while the comparisons made in 1820 show that its weight was then only 7000 such grains. This implies that the Royal Society's troy pound was too light by $4.00 (7560 \div 7000) = 3.29$ grains.

Finally, the comparisons of 1820 showed that the Royal Society's troy pound was "nearly four grains too light."

The mean of these three independent results shows that the Royal Society's troy pound was 3.9 grains lighter than the Imperial standard of 1758; whence

$$\text{R. S. troy lb.} + 3.9 \text{ grains} = \text{Standard of 1758} \quad (10)$$

but

$$\text{Standard of 1758} = \text{Exch. (8 oz. + 4 oz.)} + 1\frac{1}{4} \text{ grains} \quad (11)$$

and therefore

$$\text{R. S. troy lb.} = \text{Exch. (8 oz. + 4 oz.)} - 2\frac{5}{8} \text{ grains.} \quad (12)$$

Considering the indefiniteness of the data respecting the weigh-

¹ 11, p. 437.

ings made in 1820, equations (9) and (12) agree fairly well, but equation (5) is very discordant, as are also equations (7) and (8). All the evidence seems to point to an error of about one and one half grains in equation (5); and if instead of (5) we write

R. S. Troy lb. = Exch. (8 oz. + 4 oz.) - 2 grains (5')
(7) will become

Exch. (8 oz. + 4 oz.) = Mint (8 oz. + 4 oz.) - $\frac{3}{8}$ grain (7')
and then all the equations will be reasonably accordant.

LIST OF THE PRINCIPAL AUTHORITIES CONSULTED IN
THE PREPARATION OF THE FOREGOING ADDRESS.

NOTE.—The abbreviation “E. P. P.” is used to designate English Parliamentary Papers. Some of these papers are of folio size and others of octavo size, but in the official sets they are all bound up indiscriminately in volumes of folio size, measuring 13 by 8½ inches.

Throughout the preceding pages authorities in this list are usually cited by number and page. For example, “27, p. 91” would indicate page 91 of Capt. Kater’s account of his comparisons of various British standards of linear measure, contained in the Philosophical Transactions for 1821.

1.—PICARD; M. L’ABBÉ. De Mensuris. Divers ouvrages. Mem. de l’Acad. Roy. des Sciences, 1666–1699, Tome 6, pp. 532–549. Paris, 1730.

2.—HIRE; M. DE LA. Comparaison du pied antique Romain a celui du Châtelet de Paris, avec quelques remarques sur d’autres mesures. Mem. de l’Acad. Roy. des Sciences, 1714, pp. 394–400. Paris, 1717.

3.—MAUPERTUIS. La figure de la terre, déterminée par les observations de MM. de Maupertuis, Clairaut, Camus, le Monnier, * * * Outhier, * * * Celsius, * * * faites par ordre du Roy au cercle polaire. Paris, 1738. 16mo., pp. xxviii + 184.

4.—CASSINI DE THURY. Sur la propagation du son. (On p. 135 has statement respecting standards of length exchanged between the French Academy and the English Royal Society.) Mem. de l’Acad. Roy. des Sciences, 1738, pp. 128–146. Paris, 1740.

5.—Dégré du méridien entre Paris et Amiens, déterminé par la mesure de M. Picard et par les observations de MM. de Maupertuis, Clairaut, Camus, le Monnier, * * * Paris, 1740, 16mo, pp. lvj + 116.

6.—GRAHAM; GEORGE. An account of the proportions of the English and French measures and weights, from the standards of the same, kept at the Royal Society. Phil. Trans., 1742, pp. [185–188].

7.—GRAHAM; GEORGE. An account of a comparison lately made by some gentlemen of the Royal Society, of the standard of a yard, and the several weights lately made for their use; with the original standards of measures and weights in the Exchequer, and some others kept for public use, at Guild-hall, Founders-hall, the Tower, etc. Phil. Trans., 1743, pp. [541–556].

8.—CASSINI DE THURY. La meridienne de l’observatoire royal de Paris, vérifiée dans toute l’étendue du royaume par de nouvelles observations: Paris, 1744. 8vo, pp. 292 + ccxxxvj.

9.—CONDAMINE; M. DE LA. Nouveau projet d'une mesure invariable, propre à servir de mesure commune à toutes les nations. Mem. de l'Acad. Roy. des Sciences, 1747, pp. 489-514. Paris, 1752.

10.—BOUGUER, CAMUS, CASSINI DE THURY & PINGRÉ. Operations faites par ordre de l'Académie pour mesurer l'intervalle entre les centres des Pyramides de Villejuive & de Juvisy, &c. Mem. de l'Acad. Royale des Sciences, 1754, pp. 172-186. Paris, 1759.

11.—1758. Report from the Committee appointed to inquire into the original standards of weights and measures in this Kingdom, and to consider the laws relating thereto. (Agreed to by the House June 2, 1758.) Printed on pp. 411-451 of Reports from Committees of the House of Commons, which have been printed by order of the House, and are not inserted in the Journals. Reprinted by order of the House. Vol. 2. (June 10, 1737, to May 21, 1765). Folio, $16\frac{3}{4}'' \times 10\frac{3}{4}''$. pp. 468.

12.—1759. Report from the Committee appointed (upon the first day of Dec., 1758) to inquire into the original standards of weights and measures in this Kingdom, and to consider the laws relating thereto. (Agreed to by the House April 12, 1759.) Printed on pp. 453-463 of Reports from Committees of the House of Commons, which have been printed by order of the House, and are not inserted in the Journals. Reprinted by order of the House. Vol. 2. (June 10, 1737, to May 21, 1765). Folio, $16\frac{3}{4}'' \times 10\frac{3}{4}''$. pp. 468.

13.—MASKELYNE; Rev. NEVIL (Ast. Royal). The length of a degree of latitude in the province of Maryland and Pennsylvania, deduced from the foregoing operations (by Messrs. Chas. Mason and Jeremiah Dixon); by the Astronomer Royal. Phil. Trans., 1768, pp. 323-325.

14.—CONDAMINE; M. DE LA. Remarques sur la toise-étalon du Châtelet, et sur les diverses toises employées aux mesures des degrés terrestres & à celle du pendule à secondes. Mem. de l'Acad. Roy. des Sciences, 1772, 2^e partie. pp. 482-501. Paris, 1776.

15.—ROY; Maj.-Gen. WM. An account of a measurement of a base on Hounslow Heath. (Four large folding plates.) Phil. Trans., 1785, pp. 385-480.

16.—LA LANDE; JEROME LE FRANÇAIS. De la grandeur et de la figure de la terre. Astronomie, Tome 3, pp. 1-47. (3d edition; Paris, 1792.)

17.—BORDA, COULOMB, LEGENDRE, LAPLACE, PRONY, et BRISSON. Rapport sur la vérification de l'étalon qui doit servir pour la fabrication des poids républicains. Annales de Chimie, Paris, 1797, Tome 20, pp. 269-273.

18.—SHUCKBURGH EVELYN; Sir GEO. An account of some endeavors to ascertain a standard of weight and measure. Phil. Trans., 1798, pp. 133-182.

19.—VAN-SWINDEN, TRALLÈS, LAPLACE, LEGENDRE, MÉCHAIN, DELAMBRE, CISCAR. Rapport sur la détermination de la grandeur de l'arc du méridien compris entre les parallèles de Dunkerque et Barcelone, et sur la longueur du mètre qu'on en déduit. Base du Système Métrique Décimal, Tome 3, pp. 415-433. Paris, 1810. 4to.

20.—KATER; Capt. HENRY. An account of experiments for determining the length of the pendulum vibrating seconds in the latitude of London. Phil. Trans., 1818, pp. 33-102.

21.—KATER; Capt. HENRY. On the length of the French mètre estimated in parts of the English standard. Phil. Trans., 1818, pp. 103-109.

22.—Experiments relating to the pendulum vibrating seconds of time in the latitude of London. 41 pp. (E. P. P.) Accounts and papers. Session, 27 Jan.-10 June, 1818. Vol. 15. Folio, $13\frac{1}{4}'' \times 8\frac{1}{2}''$. This is a verbatim reprint of Capt. Kater's papers in the Phil. Trans., 1818, pp. 33 to 109.

23.—BANKS, CLERK, GILBERT, WOLLASTON, YOUNG, and KATER. First Report of the Commissioners appointed to consider the subject of weights and measures. (Dated 24 June, 1819) 17 pp. (E. P. P.) Report from Commissioners. Session, 21 Jan.-13 July, 1819. Vol. 11. Folio, $13\frac{1}{4}'' \times 8\frac{1}{2}''$.

24.—CLERK, GILBERT, WOLLASTON, YOUNG & KATER. Second Report of the Commissioners appointed by His Majesty to consider the subject of weights and measures. (Dated July 13, 1820) 40 pp. (E. P. P.) Reports from Commissioners. Session, 21 April to 23 Nov. 1820. Vol. 7. Folio, $13\frac{1}{4}'' \times 8\frac{1}{2}''$.

25.—CLERK, GILBERT, WOLLASTON, YOUNG & KATER. Third Report of the Commissioners appointed by His Majesty to consider the subject of weights and measures. (Dated Mar. 31, 1821) 6 pp. (E. P. P.) Reports from Committees. Session, 23 Jan. to 11 July, 1821. Vol. 4. Folio, $13\frac{1}{4}'' \times 8\frac{1}{2}''$.

26.—Report from the Select Committee on weights and measures. (Dated May 28, 1821) 7 pp. (E. P. P.) Reports from Committees. Session, 23 Jan. to 11 July, 1821. Vol. 4. Folio, $13\frac{1}{4}'' \times 8\frac{1}{2}''$.

27.—KATER; Capt. HENRY. An account of the comparison of various British standards of linear measure. Phil. Trans., 1821, pp. 75-94.

28.—Report from the Select Committee of the House of Lords * * * (on petition from Glasgow relative to) * * * the bill entitled "An act for ascertaining and establishing uniformity of weights and measures" * * * together with the minutes of evidence taken before said Committee. (Dated 2 Mar., 1824) 35 pp. (E. P. P.) Reports from Committees. Session, 3 Feb. to 25 June, 1824. Vol. 7. Folio, $13'' \times 8\frac{1}{2}''$.

29.—KATER; Capt. HENRY. An account of the construction and adjust-

ment of the new standards of weights and measures of the United Kingdom of Great Britain and Ireland. *Phil. Trans.*, 1826, part 2, pp. 1-52.

30.—KATER; Capt. HENRY. On errors in standards of linear measure, arising from the thickness of the bar on which they are traced. *Phil. Trans.*, 1830, pp. 359-381.

31.—KATER, Capt. HENRY. An account of the construction and verification of a copy of the imperial standard yard made for the Royal Society. *Phil. Trans.*, 1831, pp. 345-347.

32.—Minutes of evidence taken before the Select Committee on bill to amend and render more effectual two acts of the 5th and 6th years of the reign of his late Majesty King George the 4th, relating to weights and measures. 67 pp. (E. P. P.) Reports from Committees. 1834. Vol. 18, part 1. Folio, 13'' × 8½''.

33.—Report from the Select Committee on the weights and measures act; together with the minutes of evidence. (Dated 17 June, 1835) 60 pp. (E. P. P.) Reports from Committees. Session, 19 Feb.-10 Sep., 1835. Vol. 18. Folio, 13'' × 8½''.

34.—BAILY; FRANCIS. Report on the new Standard Scale of this (the Royal Astronomical) Society. (Gives also a history of English standards of length.) *Mem. Roy. Ast. Soc.*, 1836. Vol. 9, pp. 35-184.

35.—AIRY, BAILY, BETHUNE, HERSCHEL, LEFEVRE, LUBBOCK, PEACOCK, SHEEPSHANKS. Report of the Commissioners appointed to consider the steps to be taken for restoration of the standards of weight and measure. (Dated 21 Dec., 1841) 106 pp.. (E. P. P.) Reports from Commissioners. Session, 3 Feb.-12 Aug., 1842. Vol. 25. Folio.

36.—KELLY; PATRICK. The universal cambist: being a full and accurate treatise on the exchanges, coins, weights, and measures of all trading nations and their colonies. By P. Kelly, LL.D. 2nd edition. London, 1835. 2 vols., 4to. Vol. 1, pp. xl + 422; Vol. 2, pp. xxiv + 380.

37.—YOLLAND; Capt. WM. An account of the measurement of Lough Foyle base in Ireland, with its verification and extension by triangulation; etc., etc. Pub. by order of the Hon. Board of Ordnance. London, 1847. 4to, pp. 154 + [117].

38.—AIRY, ROSSE, WROTTESELEY, LEFEVRE, LUBBOCK, PEACOCK, SHEEPSHANKS, HERSCHEL, MILLER. Report of the Commissioners appointed to superintend the construction of new parliamentary standards of length and weight. (Dated March 28, 1854) 23 pp. (E. P. P.) Reports from Commissioners. Session, 31 Jan.-12 Aug., 1854. Vol. 19. Folio, 13'' × 8½''.

39.—Abstract of "Report of the Commissioners appointed to consider the steps to be taken for restoration of the standards of weight and measure." 16 pp. (E. P. P.) Reports from Commissioners. Session, 12 Dec., 1854-14 Aug., 1855. Vol. 15. Folio, 13'' × 8½''.

40.—MILLER; Prof. W. H. On the construction of the new imperial

standard pound, and its copies of platinum; and on the comparison of the imperial standard pound with the Kilogramme des Archives. *Phil. Trans.*, 1856. pp. 753-946.

41.—AIRY; Sir GEO. B. Account of the construction of the new national standard of length, and of its principal copies. *Phil. Trans.*, 1857. pp. 621-702.

42.—CLARKE; Capt. A. R. Comparisons of the standards of length of England, France, Belgium, Prussia, Russia, India, Australia, made at the Ordnance Survey Office, Southampton. Published by order of the Secretary of State for War. London, 1866. 4to, pp. 287.

43.—CHISHOLM; HENRY WILLIAMS. Seventh annual report of the Warden of the Standards on the proceedings and business of the standard weights and measures department of the Board of Trade. For 1872-3. 8vo, pp. 105. (Contains: Appendix IV.—Account of the standard weights and measures of Queen Elizabeth. pp. 10-26: Appendix V.—Account of the standard weights and measures of Henry VII. pp. 27-34: Appendix VI.—New standard weights and measures constructed and legalised from the reign of Queen Elizabeth to George IV. pp. 35-40.) (E. P. P.) Reports from Commissioners. Session, 6 Feb.-5 Aug., 1873. Vol. 38.

44.—CHISHOLM; H. W. On the science of weighing and measuring, and standards of measure and weight. By H. W. Chisholm, warden of the standards. 16mo, pp. xvi + 192. London: Macmillan & Co. 1877.

45.—HILGARD; JULIUS E. Report on the comparison of American and British standard yards. Report of the Superintendent of the U. S. Coast Survey, 1877. Appendix No. 12, pp. 148-181. 4to.

46.—WOLF; C. Recherches historiques sur les étalons de poids et mesures de l'Observatoire, et les appareils qui ont servi à les construire. *Annales de l'Observatoire de Paris. Mémoires, Tome 17, pp. C.1-C.78.* (Published in 1883.)

47.—WOLF; C. Résultats des comparaisons de la toise du Pérou au mètre international, exécutées au Bureau international des Poids et Mesures par M. Benoît. *Comptes Rendus, 3 Avril, 1888. Tome 106. pp. 977-982.*

48.—Copies "of a letter from the Comptroller General of the Exchequer to the Treasury, dated 3 June, 1863, transmitting a report on the Exchequer standards of weight and measure, dated 27 April, 1863, by Mr. Chisholm, chief clerk in the office of the Comptroller General of the Exchequer; together with a copy of his report:" and, of a memorandum by the Astronomer Royal, dated 24 April, 1862, containing notes for the Committee on Weights and Measures, 1862. 51 pp. (Contains a complete descriptive list of all the old Exchequer standards; a discussion on the moneyer's pound; and a history of English legislation on weights and measures.) (E. P. P.) Trade (Generally). Session, 4 Feb.-29 July, 1864. Vol. 58. Folio.

49.—Annual reports of the Warden of the Standards on the proceedings and business of the standard weights and measures department of the Board

LXXXIV PHILOSOPHICAL SOCIETY OF WASHINGTON.

of Trade. 8vo. (Printed as English Parliamentary Papers, and contained in the volumes of "Reports from Commissioners.")

No. of Report	Date.	No. of Pages.	Volume of Reports from Commissioners.
1st -----	1866-7	19	1867, Vol. 19.
2d -----	1867-8	18	1867-8, Vol. 27.
3d -----	1868-9	18	1868-9, Vol. 23.
4th -----	1869-70	25	1870, Vol. 27.
5th -----	1870-1	46	1871, Vol. 24.
6th -----	1871-2	203	1872, Vol. 35.
7th -----	1872-3	105	1873, Vol. 38.
8th -----	1873-4	138	1874, Vol. 32.
9th -----	1874-5	58	1875, Vol. 27.
10th -----	1875-6	68	1876, Vol. 26.
11th -----	1876-7	12	1877, Vol. 33.
12th -----	1877-8	12	1878, Vol. 36.

50.—Reports of the Commissioners appointed to inquire into the condition of the Exchequer (now Board of Trade) standards. Presented to both Houses of Parliament by command of Her Majesty. Folio. (Printed as English Parliamentary Papers, and contained in the volumes of "Reports from Commissioners.")

No. of Report.	Date.	No. of Pages.	Volume of Reports from Commissioners.
1st -----	24 July, 1868-----	8	1867-8, Vol. 27.
2d -----	3 April, 1869-----	133	1868-9, Vol. 23.
3d*-----	1 February, 1870--	159	1870, Vol. 27.
4th†-----	21 May, 1870 -----	438	1870, Vol. 27.
5th -----	3 August, 1870----	265	1871, Vol. 24.
General Index-----		101	1873, Vol. 38.

* On the abolition of troy weight.

† On the inspection of weights and measures, etc.

51.—AIRY; Sir GEO. B. Extracts of papers, printed and manuscript, laid before the Commission appointed to consider the steps to be taken for restoration of the standards of weight and measure, and the subjects connected therewith. Arranged by G. B. Airy, Esq., Astronomer Royal. Printed by order of the Lords Commissioners of the Treasury. London, 1840. 4to, 155 pp. (Consists of a vast number of brief extracts giving the opinions of many experts upon various points connected with the construction and use of standards of weight and measure, and the advantages and disadvantages of various systems of such standards.)

52.—CLARKE; Lt. Col. A. R. Results of the comparisons of the standards of length of England, Austria, Spain, the United States, Cape of Good Hope, and of a second Russian Standard, made at the Ordnance Survey Office, Southampton. By Lieutenant-Colonel A. R. Clarke, C. B., R. E., F. R. S., &c., under the direction of Major-General Sir Henry James, R. E., F. R. S., &c., director-general of the Ordnance Survey. With a preface and notes on the Greek and Egyptian measures of length by Sir Henry James. Phil. Trans., 1873, pp. 445-469.

53.—ADAMS; JOHN QUINCY. Report upon weights and measures, by John Quincy Adams, Secretary of State of the United States. Prepared in obedience to the resolution of the Senate of the 3d of March, 1817. Washington: printed by Gales & Seaton. 1821. 8vo, pp. 245. (Contains report of F. R. Hassler on comparisons of English and French measures. pp. 153-170.)

54.—ALEXANDER; J. H. Report (made to the governor of Maryland) on the standards of weight and measure for the State of Maryland; and on the construction of the yard-measures. Baltimore, Dec. 13, 1845. 8vo, pp. iv + 213.

55.—HASSLER; FERDINAND RODOLPH. Comparison of weights and measures of length and capacity. Reported to the Senate of the United States by the Treasury Department in 1832, and made by Ferd. Rod. Hassler. 22d Congress, 1st Session, Ho. of Reps., Doc. No. 299. Washington, 1832. 8vo, 122 pp., with 4 folding plates. (Contains a paper by Trallès giving important details, not published elsewhere, respecting the original iron meters of the Commission des Poids et Mesures of 1799.)

56.—HASSLER; F. R. Report from the Secretary of the Treasury, transmitting the report of F. R. Hassler, superintendent of the Coast Survey, and of the fabrication of standard weights and measures. 25th Congress, 2d Session, Senate, Doc. No. 79. Washington, 1837. 8vo, 16 pp. (Explains method adopted for determining subdivisions of the troy pound.)

57.—HASSLER; F. R. Report upon the standards of the liquid capacity measures of the system of uniform standards for the United States; with description of a new original barometer, and of the balance for adjusting the half bushels by their weight of distilled water. By F. R. Hassler. 27th

Congress, 2d Session, Senate, Doc. No. 225. Washington, 1842. 8vo, 26 pp. and 3 folding plates.

58.—BACHE, A. D., & McCULLOH, R. S. Reports from the Secretary of the Treasury, of scientific investigations in relation to sugar and hydrometers, made, under the superintendence of Prof. A. D. Bache, by Prof. R. S. McCulloh. 30th Congress, 1st Session, Senate, Ex. Doc. No. 50. Washington, 1848. 8vo, pp. 653.

59.—BACHE; Prof. ALEXANDER D. Report to the Treasury Department on the progress of the work of constructing standards of weights and measures for the custom-houses, and balances for the States, and in supplying standard hydrometers to the custom-houses, from 1 Jan., 1848, to 31 Dec., 1856. 34th Congress, 3d Session, Senate, Ex. Doc. No. 27. Washington, 1857. 8vo, 218 pp. with 6 folding plates. (Contains descriptions of yard dividing engine, and various comparators.)

60.—ROGERS; Prof. W. A. On the present state of the question of standards of length. (Contains a bibliography.) Proceed. Amer. Acad. of Arts and Sciences, 1879-80. Vol. 15. pp. 273-312.

61.—ROGERS; Prof. W. A. On two forms of comparators for measures of length. 8vo, 12 pp. American Quarterly Microscopical Journal, April, 1879.

62.—ROGERS; Prof. WM. A. Studies in metrology. 5 Plates. (Contains description of the Rogers-Bond universal comparator.) Proceed. Amer. Acad. of Arts and Sciences, 1882-'3. Vol. 18, pp. 287-398. 8vo.

63.—ROGERS; Prof. W. A. An examination of the standards of length constructed by the Société Gènevoise. Proceed. Amer. Acad. of Arts and Sciences, 1884-'5. Vol. 20, pp. 379-389. 8vo.

64.—ROGERS; Prof. W. A. A study of the centimeter marked "A," prepared by the U. S. Bureau of Weights and Measures for the Committee on Micrometry. 8vo, 23 pp. Proc. Amer. Society of Microscopists. Vol. 32, p. 184.

65.—ROGERS; Prof. WM. A. On a practical solution of the perfect screw problem. 8vo, 44 pp. Trans. Amer. Soc. of Mechanical Engineers. Vol. 5.

66.—ROGERS; Prof. W. A. A critical study of the action of a diamond in ruling lines upon glass. 8vo, 17 pp. Proc. Amer. Society of Microscopists. Vol. 32, p. 149.

67.—Travaux et mémoires du Bureau International des Poids et Mesures, publiés sous l'autorité du Comité International, par le Directeur du Bureau. Paris. 4to. Tome 1, 1881, 391 pp.; T. 2, 1883, 413 pp.; T. 3, 1884, 348 pp.; T. 4, 1885, 421 pp.; T. 5, 1886, 416 pp.

BULLETIN

OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON.

GENERAL MEETINGS.



BULLETIN
OF THE
GENERAL MEETINGS.

295TH MEETING.

JANUARY 15, 1887.

President HARKNESS in the Chair.

Fifty-one members present.

Announcement was made of the election to membership of Messrs. HENRY LAURENS WHITING and THOMAS WILLIAM SYMONS.

The following report of the Auditing Committee was presented by its chairman, Mr. WOODWARD, and was accepted :

JANUARY 15, 1887.

The undersigned, a committee appointed at the annual meeting of the Philosophical Society of Washington, December 18, 1886, for the purpose of auditing the accounts of the Treasurer, beg leave to report as follows :

We have examined the statement of receipts, including annual dues, sale of Bulletin, and interest on bonds, and find the same to be correct.

We have examined the statement of disbursements and compared the same with the vouchers, and find them to agree.

We have examined the returned checks and the bank account with Riggs & Co., and find the balance, \$485.52, to agree with the statement of the Treasurer's report.

We have examined the United States and other bonds belonging to the Society, and find them to be in amount and character as represented in the Treasurer's report, aggregating \$3,100.

R. S. WOODWARD,
SWAN M. BURNETT,
J. H. KIDDER,

Committee.

(3)

Mr. G. K. GILBERT presented a communication entitled

GRAPHIC METHODS IN RESEARCH.

[Abstract.]

An algebraic equation between two variables is the equivalent of a plane curve, or, more strictly, of a line lying in a plane. An equation containing three variables is the equivalent of a surface. If in such an equation one of the variables be assumed equal to 1, 2, 3, etc., successively, there result a series of equations involving the other two variables. Each of these equations may be represented by a line in a plane, and the system of lines thus produced is the representative of the original equation between three variables. The single curve may be called a *nomogram*, the system of curves an *isogram*.

In the simplest use of the graphic method in research the simultaneous quantitative observations of two phenomena are represented on cross-section paper by a dot, a series of observations are represented by a system of dots, and a line is drawn through or among these dots. This line expresses the law of the relation between the two phenomena and is a nomogram.

When simultaneous observations are made of three phenomena, two of the observations are expressed by a dot on section paper and the third by a number attached to the dot. All the observations having been represented by such numbered dots, a system of lines is drawn over the area occupied by the dots, each line representing an integral value of one of the variable phenomena, and being drawn so as to pass through the dots marked with the corresponding number. An isogram is thus produced without recourse to the algebraic equation.

In the *compound nomogram*, two or more curves are drawn on the same sheet, and with one system of ordinates in common. Each of these curves represents an equation with two variables, one variable being common to all the equations. By this means two or more variable phenomena are compared with each other through the mediation of another phenomenon with which they are related.

In the *compound isogram* two or more isograms are drawn on the same sheet. Each isogram is the equivalent of an equation between three variables, two variables being common to all the isograms,

and one peculiar to each. By this means, variable phenomena are compared with each other with reference to two other phenomena.

There are also phases of the graphic method in which lines are not drawn, the arrangement of the platted dots being such that they cannot be replaced by lines, but nevertheless lead to legitimate inferences.

The function of the graphic method in research is the classification of observations and their generalization, or the discovery of their laws of relation. The same function is performed by mathematical analysis, both processes being restricted to the discussion of quantitative observations. As compared to the mathematical method, the graphic is more rapid and less precise. In matters difficult of comprehension it aids the imagination by introducing a sensory impression, and in this manner it suggests inferences and hypotheses which might readily be overlooked if mathematical methods were employed alone.

Mr. H. A. HAZEN remarked upon the importance of this method in meteorology. He suggested some precautions to be taken in attempting to trace a connection by maximum or minimum epochs between elements which are not clearly related or caused by the same force.

Mr. MARCUS BAKER thought that the graphic method had its chief use in rough approximations, and drew attention to the great strides which had been made in geometry by the introduction of analytical methods, supplementing and in part supplanting graphic methods.

Mr. PAUL remarked that the graphic method might be useful in a preliminary determination of the most promising of several methods of possible analysis.

Mr. C. D. WALCOTT read a paper entitled

THE GEOLOGIC AGE OF THE LOWEST FORMATION OF EMMONS'
TACONIC SYSTEM,

illustrated by maps, drawings, etc.

[This paper, in abstract, appeared in the American Journal of Science, 3d series, 8°, New Haven, 1887, February, vol. 33, pp. 153-154.]

296TH MEETING.

JANUARY 29, 1887.

The President in the Chair.

Thirty-six members present.

Announcement was made by the President of the death of General WILLIAM B. HAZEN, a member of the Society, which took place at 8 p. m., January 16.

Mr. F. W. CLARKE read a paper entitled

THE PRESENT STATUS OF MINERALOGY.

[This paper is expected to appear in the Popular Science Monthly.]

A paper by Mr. R. T. HILL, entitled

THE TOPOGRAPHY AND GEOLOGY OF THE CROSS TIMBERS OF TEXAS, was then read by Mr. W J McGEE, as Mr. HILL had been called away from the city after his paper was placed upon the programme.

[This paper appeared in full in the American Journal of Science, 3d series, 8^o, New Haven, 1887, April, vol. 33, pp. 291-303.]

297TH MEETING.

FEBRUARY 12, 1887.

The President in the Chair.

Forty-one members and guests present.

The President announced that Mr. FRANK HALL KNOWLTON had been elected to and had accepted membership in the Society.

A letter was read from the secretary of the Anthropological Society announcing that Mr. Alfred Russell Wallace would deliver an address Tuesday evening, February 15, on "Social *versus* Political Economy" before the Anthropological Society, and inviting the members of the Philosophical Society and their friends to be present on that occasion.

Mr. H. A. HAZEN made a communication on

THE SKY GLOWS OF 1883.

This communication was discussed by Messrs. PAUL, E. FARQUHAR, WINLOCK, and the author.

Mr. BAILEY WILLIS presented a paper on

THE TOPOGRAPHY AND STRUCTURE IN THE BAYS MOUNTAINS,
TENNESSEE.

[This paper appeared in the School of Mines Quarterly, Columbia College, 8°, New York, 1887, April, vol. 8, No. 3, pp. 242-252.]

Mr. G. BROWN GOODE made a communication on

THE GEOGRAPHICAL DISTRIBUTION OF SCIENTIFIC MEN AND INSTITUTIONS IN THE UNITED STATES.

[An abstract of this communication appeared in The Epoch, 4°, New York, 1887, June 24, vol. 1, pp. 467-468.]

298TH MEETING.

FEBRUARY 26, 1887.

The President in the Chair.

Thirty-nine members and guests present.

The President announced the election to and acceptance of membership of Mr. FRANKLIN AUSTIN SEELY.

Mr. C. V. RILEY read a paper upon

OUR CITY SHADE-TREES, THEIR FOES AND THEIR FUTURE,

illustrated by drawings and specimens.

[This paper was afterwards elaborated and published as Bulletin No. 10 of the entomological division of the Department of Agriculture, published May 7, 1887, with the following title :

U. S. Department of Agriculture. Division of Entomology. Bulletin No. 10. Our shade-trees and their insect defoliators. Being a consideration of the four most injurious species which affect the trees of the capital; with means of destroying them. By C. V. Riley, entomologist. Washington: Government Printing Office, 1887. 69 pp., 8°, illustrated.]

This communication was discussed by MESSRS. GILBERT, MERRIAM, and ELLIOTT.

MR. LESTER F. WARD made a communication entitled

THE FREQUENCY OF COINCIDENCES.

[Abstract.]

Every one is constantly meeting with coincidences in every-day life, but few ever take the trouble to record them. Mr. Ward had always been struck by their frequent occurrence and remarkable character, but until within about fifteen years had been content, as most people are, to allow them to pass with only a momentary expression of surprise. Certain comments upon them, however, which he had met with in the writings of Auguste Comte and Dr. George M. Beard had led him to take a wider view of their significance and to commence in the year 1875 the practice of jotting down in his note-book some of the more interesting and striking of them. In this way a large collection of instances had accumulated, a few of which were selected for presentation to the Society. These were read directly from his notes, without change of phraseology, in order to preserve their literal accuracy. Most of them were of a character which, according to the mathematical law of probabilities, would not occur again within any finite limitation of the events with which they were associated.

The only application which it was attempted to make of the facts was to point out their bearing upon the investigations which had been recently conducted by the British Society for Psychological Research, from which, in Mr. Ward's opinion, unwarranted conclusions had been drawn, and which, he believed, receive their true explanation only when the frequency of coincidences is fully recognized.

This communication was discussed by Messrs. WOODWARD and CLARKE.

299TH MEETING.

MARCH 12, 1887.

The President in the Chair.

Thirty-four members and guests present.

The President announced the death on March 5th, at Pensacola,

Florida, of Capt. EDWARD PHELPS LULL, U. S. N., a member of this Society.

The President also announced that Mr. HERBERT COUPER WILSON had been elected to and had accepted membership in the Society.

Mr. G. E. CURTIS read a paper on

THE THEORY OF THE WIND-VANE.

[This paper appeared in the American Journal of Science, 3d series, 8°, New Haven, 1887, July, vol. 34, pp. 44-52. It has also been reprinted in the American Meteorological Journal, 8°, Ann Arbor, Mich., 1887, September, vol. 4, No. 5, pp. 215-224.]

Mr. H. A. HAZEN thought that Mr. CURTIS's formulæ showed that a single-tailed vane is more sensitive than a doubled-tailed one and would define a *sensitive* vane as that one which most quickly assumes the direction of the wind.

Mr. BATES regarded these formulæ, presented by Mr. CURTIS, which had been deduced for inelastic fluids moving in right lines as inapplicable to elastic fluids moving in curved lines and often affected by vortices.

Further remarks were made by Messrs. ABBE, WOODWARD, and CURTIS.

Mr. C. F. MARVIN made a communication on

THE ELECTROMETER AS USED IN OBSERVATIONS OF ATMOSPHERIC ELECTRICITY,

exhibiting in connection with it a diagram and the instrument itself.

Mr. BAILEY WILLIS made a communication on the

DEVELOPMENT OF A PERSPECTIVE MAP FROM A CONTOUR MAP, illustrated by three sketches and diagrams.

Mr. W. D. JOHNSON exhibited and explained a new plane table, presenting a number of improvements, especially as to increased stability, compactness, levelling, and mode of attaching the paper to the board.

300TH MEETING.

MARCH 26, 1887.

The President in the Chair.

Seventy-one members and guests present.

This meeting was held in the Assembly Hall of the Cosmos Club, southeast corner of H street and Madison Place, the Club having offered the use of its hall as a meeting place for the Society. Preceding meetings during this year and during several former years, were by the courtesy of the Surgeon General of the United States Army, held in the library of the Surgeon General's Office on the east side of 10th and between E and F streets N. W.

The President briefly alluded to this removal to more commodious quarters upon the 300th meeting of the Society as marking an epoch in its history.

Announcement was made of the election to membership of Mr. SAMUEL PIERPONT LANGLEY and Mr. HARRY KING.

Mr. H. A. HAZEN read a paper upon the

RELATION BETWEEN WIND VELOCITY AND PRESSURE,

illustrated by an apparatus resembling that used by him in recent experiments at the Smithsonian Institution.

[This paper appeared in the American Journal of Science, 3d series, 8°, New Haven, 1887, October, vol. 34, pp. 241-248.]

The paper was discussed by Messrs. BILLINGS, WOODWARD, HARKNESS, PAUL, and the author.

Mr. BAILEY WILLIS made a communication on

MT. RAINIER AND ITS GLACIERS,

illustrated by perspective drawings of Rainier and Shasta, derived from contour maps by the method explained at the last meeting. The facts brought out by the illustrations and remarks indicate that Rainier was a point of intense volcanic activity long since extinct, and Shasta one of long continued less violent eruption. Rainier is a ruin, Shasta a complete cone.

Mr. DILLER followed with an account of Mt. Shasta, contrasting it with Mt. Rainier.

These communications were discussed by Messrs. DUTTON and WILLIS.

Mr. MARCUS BAKER made a communication entitled

WHAT IS A TOPOGRAPHIC MAP?

[Abstract.]

Referring to the volume of testimony taken by a joint committee of the two houses of Congress charged with the duty of investigating the relations of certain scientific bureaus, Mr. Baker remarked that the time seemed opportune to discuss dispassionately certain points previously discussed controversially.

Great diversity of view and of usage as to what constitutes *topography*, *topographic survey*, *topographic map*, etc., was brought out by citations from various authors and witnesses.

According to some, the relief of a portion of country constitutes its topography; according to others, relief, drainage, and culture together make up topography; still others find that the delineation or representation of such features constitutes topography. Topography is also defined as "description of places" and as "a branch of surveying."

A rather large and mixed assortment of maps was exhibited. These maps, made by different nations, on different scales, in different styles and colors, with different conventions and symbols, and differing as to accuracy and completeness, were offered as samples of a very large assortment, which it was proposed to classify. "Topographic maps" should form one of the various classes into which it would be desirable or convenient to divide maps. To determine what principles should be adopted as guides for including or excluding from this class was the object of the enquiry.

It was suggested that a satisfactory definition of "topographic map" must take account of four things, viz.:

- (a) scale.
- (b) purpose.
- (c) features to be represented.
- (d) accuracy.

(a) Maps on a *very small* scale may be called generalized maps, and, though showing topographic features as fully and completely as the scale will permit, are still not properly topographic but generalized maps.

Maps on *very large* scales, on the other hand, though sometimes containing curves of equal altitude or contours, are yet rather diagrams or plans than topographic maps.

The topographic map requires a scale somewhere between the small scale generalized map and the very large scale plan.

(b) The class to which any given map must be referred further depends upon its purpose. If the purpose is to exhibit the geologic structure, it is a geologic map; if designed for military purposes, a military map; if for nautical purposes, a nautical map—or, as it is called, a chart—and if for exhibiting the topography, a topographic map. If a topographic map is colored to exhibit the geologic structure of the region shown, it is no longer a topographic but a geologic map, etc. Most of the maps of the Coast Survey, though exhibiting more or less topography, would not be classed with topographic maps, but with charts, being designed for nautical purposes.

(c) The features to be exhibited on a map, in order that it may be classed as topographic, are (1) the relief, (2) the drainage, including in this term the whole water system of ponds, lakes, swamps, streams, etc., and (3) the culture, this term implying the works of man of such size or importance as to warrant their being classed as topographic features. What features are topographic depends upon the scale of the map.

(d) With respect to accuracy we shall have topographic maps and topographic sketches. A topographic sketch controlled by locations is a topographic map; not so controlled, it remains a sketch.

This communication was discussed by Messrs. G. THOMPSON, H. FARQUHAR, R. D. MUSSEY, and the author.

301ST MEETING.

APRIL 9, 1887.

The President in the Chair.

Seventy-three members and guests present.

Prof H. CARRINGTON BOLTON, of Hartford, Conn., read, by invitation, a paper on the

COUNTING-OUT RHYMES OF CHILDREN, THEIR ANTIQUITY, ORIGIN
AND WIDE DISTRIBUTION.

[Published in a volume of same name by Elliot Stock, London. Also read before the New York Academy of Sciences.]

This paper was discussed by Messrs. EASTMAN, BILLINGS, MUSSEY, HAZEN, WARD, MASON, EDWARD EGGLESTON, BABCOCK, and by the author. In the course of the discussion several new rhymes were brought forward together with many interesting references to particular customs and formulæ of speech.

302D MEETING.

APRIL 23, 1887.

The President in the Chair.

Sixty members and guests present.

Mr. HARKNESS presented a communication

ON A DEVICE FOR VIEWING THE SUN BY LIGHT OF ANY DESIRED
WAVE LENGTH.

[Abstract.]

If two precisely similar prisms are placed in contact, with their refracting angles facing in opposite directions, the outer surfaces of the combination will be parallel to each other, and light falling upon the first prism will emerge from the second parallel to its original direction and without suffering any dispersion whatever. So long as the two prisms remain in contact the combination is, in effect, a piece of thick plano-parallel glass, and objects seen through it present only their natural colors. If, however, the prisms are separated by a considerable interval a different action occurs. A

small pencil of nearly parallel rays falling upon the first prism then suffers so much dispersion before reaching the second prism that the latter can no longer reunite the rays of different wave-lengths, but it will still render them parallel to the directions they had before entering the first prism. Thus all the conditions necessary for affording distinct vision of the radiant to an eye situated behind the second prism are fulfilled, and at the same time the wave-length of the light received by the eye can be completely controlled by the adjustment of the prisms.

In the experimental apparatus actually constructed two sixty-degree prisms were employed, separated by an interval of thirty-eight inches. These prisms were fixed relatively to each other, and behind the second one a viewing telescope of 6.5 inches focal distance and 0.84 of an inch clear aperture was mounted in such a way that it could be moved through an arc sufficient to bring rays of any desired wave-length to the center of its field. Slits were placed immediately behind the first prism and before the objective of the viewing telescope. Thus arranged, the instrument gave images of the *whole sun* composed of tolerably homogeneous light; but the image of the surrounding sky was not composed of homogeneous light, and to remedy that defect a somewhat different arrangement of the slits will be tried.

This communication was followed by a symposium upon the question,

WHAT IS TOPOGRAPHY?

participated in by Messrs. M. H. DOOLITTLE, W. D. JOHNSON, H. G. OGDEN, and GILBERT THOMPSON.

Mr. DOOLITTLE began by declaring his ignorance until recently of the subject and his resulting fitness to investigate without prejudice. He then pointed out the origin and development of the terms geography, chorography, and topography, referring to the death of the term chorography at the ripe old age of 1,500 years or thereabouts and the alteration with time of the meaning of the words geography and topography. The early meaning of topography, description of places, appears to be obsolete or obsolescent. The existing confusion concerning the meaning of the word topography was made strikingly manifest by quotations from dictionaries.

Mr. W. D. JOHNSON followed with a written communication, in which he took the ground that topography had within recent years lost almost or quite completely its old significance of description of places, and was now almost universally understood to refer to surface forms, the ups and downs, the hills and valleys, etc., and to nothing else. This position was defended by very diverse and numerous citations.

Mr. H. G. OGDEN followed with a written communication, in which he argued that the topographical features which, taken together, constitute topography, comprise not only natural relief, but artificial relief also, such as railway cuts and embankments, dams, mounds, etc., and that generally hills and valleys, streams and ponds, towns and roads, etc., should be, as they have been, regarded as topographical features.

Mr. GILBERT THOMPSON held that permanent hill features alone constitute topography, and set forth the general applicability of this view by illustrative crayon drawings.

A general discussion followed, participated in by Messrs. W. D. JOHNSON, G. THOMPSON, DOOLITTLE, WINLOCK, HARKNESS, E. FARQUHAR, and M. BAKER.

303D MEETING.

MAY 7, 1887.

The President in the Chair.

Forty-four members and guests present.

Announcement was made of the election to membership of Mr. HARRY VANDERBILT WURDEMANN.

Mr. J. W. CHICKERING read a paper on

THE MUIR GLACIER, ALASKA,

illustrated by a map and diagram.

Mr. MARCUS BAKER commented on this communication and remarked that in a careful inspection of the shores of Lynn Canal in 1880 he was unable to discover more than a small proportion of the glaciers reported by Mr. Muir.

Mr. C. HART MERRIAM read a paper upon

THE ECONOMIC PHASE OF THE ENGLISH SPARROW QUESTION.

[This paper appeared in the Report of the Commissioner of Agriculture, 1886, 8°, Washington, Government Printing Office, 1887, pp. 227-246; with map.]

Respecting the law protecting sparrows Mr. HAZEN drew attention to the fact that a colored boy had recently been fined two dollars in the Police Court of Washington for throwing stones at sparrows.

Mr. W J MCGEE made an oral communication entitled

THE QUATERNARY DEPOSITS AND THE GREAT DISPLACEMENT OF
THE MIDDLE ATLANTIC SLOPE,

embodying the results of investigations set forth in part in a memoir on the geology of the head of Chesapeake Bay, contained in the Seventh Annual Report of the U. S. Geological Survey, and in part in an article entitled Three Formations of the Middle Atlantic Slope, which is expected to appear in the American Journal of Science for February, and March, 1888.

304TH MEETING.

MAY 21, 1887.

The President in the Chair.

Forty-five members and guests present.

Mr. C. E. DUTTON made a communication on

A RECENT VISIT TO THE SCENE OF THE CHARLESTON EARTH-
QUAKE AND RESULTING CONCLUSIONS.

Mr. W. H. DALL made a communication entitled

SOUTH FLORIDA NOTES.

Remarks on this communication were made by Messrs. BOUTELLE, HEAD, and TONER.

Adjourned to October 15.

305TH MEETING.

OCTOBER 15, 1887.

The President in the Chair.

Fifty-one members and guests present.

The President announced the death at Wood's Holl, Massachusetts, on August 19, 1887, of Prof. SPENCER FULLERTON BAIRD, one of the original members of the Society.

Mr. C. E. DUTTON made a communication

ON THE DEPTH OF EARTHQUAKE FOCI.

[Abstract.]

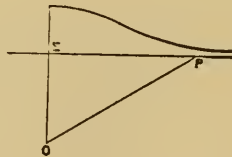
Mr. Dutton first referred to the various methods which had been resorted to in order to ascertain the depths of earthquake foci. The method suggested by Mallet and based on the assumption that the lines of fracture in the walls of buildings tended to arrange themselves transversely to the direction of propagation, he believed to be unavailable and not sustained by observation. The motions of buildings and of the ground itself during an earthquake were highly complex, and, moreover, the lines of fracture, he believed, were influenced far more forcibly by the nature of the structure, the openings in the walls, and the natural directions of vibration than by the directions of the impulses themselves.

Seebach's method, by ascertaining the variation of the speed of the wave along the surface of the ground in the vicinity of the epicentrum, was regarded as impracticable, though the mathematical considerations upon which it was founded were doubtless correct. The speed of propagation is so high and the difficulty of obtaining time observations of sufficient precision is so great that this mode of solution must fail for want of the requisite data. Seebach seems to have been under the impression that this speed was not more than a very few hundred metres per second. The Charleston earthquake was transmitted with a speed probably exceeding 5,000 metres per second, and Mr. Dutton was of the opinion that all true earthquakes were propagated with a speed differing but little from that; but, even if the speed were no greater than Seebach supposed, it

would still be expecting too much of human fallibility to suppose that data of sufficient accuracy could ever be obtained.

There is, however, a method which is dependent, not upon time data, but upon observations of intensity, which seems to offer the means of computing the desired quantity. It is well known that the intensity or energy per unit area of wave front diminishes as the wave moves outwards from the centrum. Like all radiant energy, it must be subject to the law of variation inversely as the square of the distance. If the elasticity of the medium were perfect and its density uniform the law would be rigorous. As a matter of fact, it is not so; but, on the other hand, we are assured that the elasticity cannot be very imperfect, since if it were so the propagation of impulses to very great distances would be impossible, and the waves would soon be extinguished in work done upon the medium itself. Nor is there reason to suppose that the variations of density are extreme. Thus, while the law of inverse squares may be in some measure impaired, it may still be assumed as an approximate expression of the reality.

If, then, we were able to form a just estimate of the rate of variation of the intensity along lines radiating from the epicentrum, we should have the means of computing the depth of the focus. Thus, if O be the focus and E the epicentrum and P any point at a dis-



tance from the epicentrum, the intensity at P would be inversely proportional to the square of OP. Calling EP = x , OP = r , and OE = q , and designating by a the intensity at unit distance and by y the intensity at any other distance x , we have the equation :

$$y = \frac{a}{r^2} = \frac{a}{q^2 + x^2}$$

This equation corresponds to a curve whose figure is approxi-

mately represented in the diagram, and the curve will have a point of inflexion at which the decrease in the value of y as EP increases will be a maximum. Differentiating the equation twice and equating the value of the second differential coefficient to zero will give us the co-ordinates of this point of inflexion. The value of the abscissa of this point will be

$$x = \frac{q}{\sqrt{3}}$$

From this value the constant a has disappeared, showing that it is independent of the intensity of the original shock and dependent upon the depth alone. The application of this analysis to the problem is as follows: As we recede from the epicentrum the intensity diminishes, but it does not diminish at a uniform rate with the distance. There is some critical distance from the epicentrum at which the rate of decrease of intensity has a maximum value. This critical distance depends upon the depth of the focus and upon nothing else, and the magnitude of this distance is equal to the depth divided by $\sqrt{3}$, and, conversely, the depth of the focus is equal to the critical distance multiplied by $\sqrt{3}$. If, then, we can locate the epicentrum and the points where the intensity diminishes with greatest rapidity, we have at once the means of determining the depth of the focus. In the case of the Charleston earthquake this location has been approximately made and a depth of about twelve miles has been deduced for the focus of the principal shock.

After a description of Mallet's second method of investigation by the observation of the overturning power of earthquakes, the subject was discussed by the President and by Messrs. H. FARQUHAR, GILBERT, and DUTTON.

Mr. F. W. CLARKE made an oral communication on the

MANCHESTER MEETING OF THE BRITISH ASSOCIATION FOR THE
ADVANCEMENT OF SCIENCE, 1887.

Remarks upon this communication were made by Mr. ABBE.

306TH MEETING.

OCTOBER 29, 1887.

The President in the Chair.

Forty-one members and guests present.

Announcement was made by the President of the election to and acceptance of membership of Mr. JESSE HERMAN HOLMES.

The President also referred to the loss sustained by the scientific world in the death of Prof. SPENCER F. BAIRD, and announced that the General Committee had taken the preliminary steps for arranging a memorial meeting in commemoration of his life and scientific work.

Mr. CLEVELAND ABBE read the following paper entitled

THE SIGNAL SERVICE BIBLIOGRAPHY OF METEOROLOGY.

Mr. ABBE stated that in 1872 he began, at his own expense and for personal use, a more systematic collection of the titles of works bearing upon all subjects that he was interested in, especially meteorology. After corresponding in 1874 with the committee of the Royal Society as to the probability of the publication of their proposed subject-index to their *Catalogue of scientific papers*, and being officially informed that this work would not be undertaken, he decided to complete his systematic examination of all the titles in that great work and copy the appropriate ones for his own use. In 1878, when this work was nearly completed, so far as regards the first six volumes, he addressed a note to Prof. Hann, of Vienna, stating what he had done and inquiring whether any one in Europe was similarly engaged. Almost simultaneously with this Prof. Hann received and published¹ a letter from Dr. Hellmann, of Berlin, dated January 10, 1879, urging the importance of a general index to the literature of meteorology. This letter had evidently been suggested by a circular issued in October, 1878, by the permanent committee of the first meteorological congress at Vienna, proposing a programme for the second congress about to be held at Rome in the approaching month of April, 1879. In this circular the committee asked that the delegates prepare catalogues

¹Ztschr. Met., Wien, 1879, xiv, 96.

of the meteorological observations, published or unpublished, for their respective countries.

At the Rome conference Dr. Hellmann's letter was presented on April 21 and by the congress referred to the newly-appointed International meteorological committee. The congress also adopted resolutions² asking the delegates to prepare lists of the observations for their respective countries, and the directors of meteorological libraries to add lists of the works not found in the published library catalogues of the Meteorological society of London and the observatory at Brussels, or in Mr. Abbe's cards.

After the meeting at Rome Mr. Abbe received a letter from Dr. Hellmann, to which he replied August 22, 1879, offering to cooperate in the preparation of a general bibliography and to transfer his cards either to the International meteorological committee or to Dr. Hellmann personally, on the repayment of his expenses.

At the same time a similar offer was made to General Myer, Chief signal officer, under the impression that the latter would be pleased to complete the work as an official matter.

At the first or Berne meeting of the International meteorological committee in August, 1880, letters of Dr. Hellmann were read dated January 20 and July 20, 1880, giving a detailed scheme for combining the various works and for the preparation of a catalogue, and embodying Mr. Abbe's proposal of August, 1879, as well as a similar one from Mr. G. J. Symons of London³. The committee, however, resolved that each country be requested to furnish lists of observations and that Messrs. Scott and Hellmann be a sub-committee to consider the means of carrying out Dr. Hellmann's scheme.⁴

In the fall of 1881, Mr. Abbe wrote to Mr. Symons for more details as to his work. Mr. Symons' reply and Mr. Abbe's renewal of his previous offer were then laid before General Hazen, Chief signal officer, who decided to purchase the catalogues of both these gentlemen with a view to their combination and completion by the Signal office in case the International committee did not do this. In November, 1881, Mr. Symons was authorized to prepare at the expense of the Signal office, a copy of all meteorological titles in his

² Rep. pr. internat. meteorol. cong. Rome 1879, Lond., 1879, p. 21, 75.

³ Rep. pr. internat. meteorol. comm. Berne 1880, Lond., 1881, p. 38, 40.

⁴ *Ibid.*, p. 8-9.

collection, and in December, 1881, M. Abbe's cards were purchased.

Mr. Symons' catalogue was received in October, 1883, and on March 4, 1884, Mr. C. J. Sawyer, librarian of the Signal office, was relieved from the care of the library, and, as bibliographer, ordered to devote his whole time to the completion of this work, which was then transferred from the library to the study room division of the Signal office.

At the second meeting of the International meteorological committee, at Copenhagen, in August, 1882, Messrs. Scott and Hellmann reported that the Meteorological office could not print the proposed catalogue and that subscriptions were not practicable. They therefore recommended each meteorological service to publish a national bibliography, for which Hellmann's *Repertorium der deutschen Meteorologie*, prepared in accordance with the ideas of the committee and now just about to be published, should serve as a model. It need only be added that since 1882 the International meteorological committee have, with other meteorologists, acquiesced in the arrangement by which the Signal service has undertaken to complete and, if possible, publish for its own and for general use a general index to the literature of meteorology.

The importance of this work is especially endorsed by General Greely, who, in his current annual report, October, 1887, as Chief signal officer, says :

The practical value of such a bibliography has been fully shown by its constant use in current office work, and, in addition to the official demands, almost daily calls for information have been received from parties not connected with the service. The result of this work is the collection of special bibliographies, which ensures those consulting it a complete index of what has been accomplished in each special line of meteorology. As has been well said, the progress of meteorology is retarded and labor therein wasted owing to the impossibility of ascertaining what has been done in its various branches—an experience which, as scientific men well know, is by no means confined to this science. The cost of time and labor to the Government for the preparation of this work cannot be less than \$12,000 to \$15,000, and the result of these labors has been the completion of a work which is of great value, both practically and scientifically, to the entire world. The catalogue in its present condition is valuable, and sufficient for the pressing needs of this service, but to view it in this light would evince a narrow and selfish disposition not in keeping with the scientific spirit of the age. At a cost

of probably \$8,000 or \$10,000 this work can be printed and distributed to the world as a monument and evidence of the growing scientific tendency of this nation. If such action is taken by Congress, the Chief Signal Officer has no doubt, from the willing spirit and hearty co-operation shown by leading scientists of other countries, that future international co-operation will secure, by a system of rotation, from the various European governments the publication of a series of supplements which will keep the world abreast of the steadily increasing volume of meteorological publications. A large number of American and foreign meteorologists and librarians have given largely of their time and energy in the compilation of this bibliography, as is shown by the fact that over one-half of the material has been contributed from foreign countries, so that the bibliography represents not only a large expenditure on the part of the United States, but also many years of additional gratuitous labor. The material could not be duplicated, and it would seem but a respectable reciprocity of exchange that the Government should print the catalogue, so as to enable the voluntary contributors to avail themselves of the complete work. This fulfilment of obligations to contributors by a public catalogue is an act of justice; but, in addition, it should be considered that this bibliography will be of great practical value to the agricultural, commercial, engineering, and medical interests not only of the United States, but of the world.

Mr. ABBE stated that he had asked Mr. Sawyer to present to the Philosophical society some account of his work, now nearing completion, but, as he could not be present, Mr. Abbe read the following memorandum prepared by Mr. Sawyer :

MEMORANDUM ON THE SIGNAL SERVICE BIBLIOGRAPHY OF
METEOROLOGY AND TERRESTRIAL MAGNETISM.

The bibliographical work of the Signal office dates from 1881, and officially originated in correspondence begun by Prof. Abbe with Prof. G. J. Symons, of London, Dr. G. Hellmann, of Berlin, and Dr. A. Lancaster, of Brussels, who all manifested the greatest interest in the proposed catalogue and have been the most important contributors to it.

The meteorological titles in the *Catalogue of scientific papers. Compiled by the Royal society of London, vols. i-vi (1800-1863)*, had already been selected and extracted by Prof. Abbe and were transferred to the Signal office in December, 1881, on the repayment of the expenses incurred by him in the work. At the request of the Signal office, Prof. Symons undertook to furnish copies of all titles on meteorology and terrestrial magnetism contained in his extensive

collection of titles on astronomy, meteorology, and allied sciences, the expense to the office to be only his actual outlay for clerical assistance. Prof. Symons' catalogue already represented many years of bibliographical research, and to it he now added many titles, securing the co-operation of European meteorologists by personal visits and by correspondence, and including the more important English libraries.

This catalogue was received late in 1883, about two years having been spent in its compilation; it consisted of about 18,000 titles, chiefly of separate works, and may be considered as the foundation of the present bibliography. No further work was done until March, 1884, when an effort to secure the services of Prof. Lancaster having failed, the librarian of the Signal office was assigned to the work of preparing the catalogue for publication.

The original intention had been to extend Prof. Symons' work only by the combination of titles from the Royal Society catalogue, including those in vols. vii and viii (1864-1873), selected but not yet copied by Prof. Abbe, the catalogue to be arranged by authors and to form only a first contribution to the general meteorological bibliography desired.

But the large amount of material on hand, and the conviction that some recent contributions to the subject, especially the *Repertorium der deutschen Meteorologie* by Dr. Hellmann, should be included, and that the periodical literature previous to 1800 and subsequent to 1873 should be represented, led to the consideration of an enlargement in the scope of the work. It was foreseen that the necessary delay in securing an appropriation for publication would afford opportunity for still further extension, and it was decided March 15, 1884, to complete the compilation so far as possible without postponing publication for this purpose and to issue an approximately complete general bibliography, of such form as to serve as a basis for supplementary volumes.

In pursuance of this plan, every effort has been made to secure contributions, especially by indexing periodicals, by examination of printed and manuscript catalogues and bibliographies, and by correspondence with meteorologists and librarians.

The lacunæ in periodical literature have been filled by indexing all periodicals available previous to 1800 and subsequent to 1873, and by the examination of all indexes, bibliographies, &c., available, such as Reuss, Young, Poggendorff, Kerl, Fortschritte der

Physik, and many others. It was found that the general indexing of the Royal Society for the period from 1800 to 1873, was not full enough for this special bibliography, and all periodicals rich in meteorological literature were reindexed.

The International meteorological committee had already considered the subject of meteorological bibliography, and, unable to secure at once the publication of a general bibliography, had recommended that each country compile a list of its own observations and that special national bibliographies be prepared wherever possible. Some work had been done in accordance with this recommendation, especially in Germany and Russia, and an attempt was made by the Signal office to secure the extension of this work and to obtain from foreign meteorologists and librarians, bibliographies for their respective countries. The great interest in the work was shown by the hearty co-operation from all sections.

Among the special bibliographies received the following may be mentioned as among the most complete and valuable: Germany, by Dr. Hellmann; Japan, by Dr. Knipping; Norway, by Prof. Mohu; Poland, by Prof. Karlinski; Portugal, by J. C. de Brito-Capello; Roumania, by Dr. Hepites; Russia, by Profs. Wild and Woeikof; South Africa, by Dr. Gamble; Sweden, by C. G. Fineman and C. Annerstedt; Victoria, by R. L. J. Ellery.

All the meteorological libraries of the world are represented, including, as worthy of special mention, those of the Meteorological office and Royal Meteorological Society, of London; the Société météorologique de France, Paris; the large manuscript collection of Prof. Poey, the Ronald's, Poulkova, and Brussels catalogues, all contained in the catalogue of Prof. Symons; the Deutsche Seewarte, Hamburg (including the library of the late Prof. Dove), and the k. k. Central-Anstalt, of Vienna (with that of Prof. Hann), added by the Signal office. The number of scientific and general libraries represented is very large.

Letters, requesting lists of their works, were sent to about 400 writers (exclusive of those in Germany, where this method had been employed by Dr. Hellmann), and the replies received have been of the greatest value in the representation of living authors.

The desirability of securing as great completeness as possible, the expectation of an early publication, and the fact that the Symons and Hellmann catalogues ceased with 1881, led to the adoption of this date as the close of the bibliography, and the following state-

ment of the titles on hand includes only those of works published before January 1, 1882. A large amount of material for subsequent years has been collected but has not been submitted to classification. It may be included in supplementary volumes, or incorporated with the bibliography if publication be delayed.

The chief sources of material and approximate number of titles added to the bibliography, after the rejection of duplicates, are as follows:

Prof. Symons' catalogue	18,000
Royal Society catalogue, i-viii	11,000
Hellmann, Repertorium	5,000
Printed catalogues and bibliographies, including Reuss, Poggendorff, &c. (400 vols.)	4,000
Manuscript catalogues and bibliographies	3,000
Periodicals indexed (6,400 vols.)	12,000
	<hr/>
Total number before final revision	53,000
Number of independent titles after final revision, about	50,000

The duplication of titles by double classification will increase the number of entries to about 55,000.

The form adopted for the work is that of a classed subject catalogue, with full author index. The general plan of the subject catalogue is similar to that of the Poulkova catalogue and that adopted by Drs. Houzeau and Lancaster for their *Bibliographie générale de l'astronomie*, the arrangement being chronological under each subject. The classification is based upon a scheme submitted by Dr. Lancaster, at the request of the Signal office, some minor modifications having been made after careful study and consultation with other meteorologists and bibliographers.

The general divisions of the classification are shown by the following outlines:

- | | | | | | | | | | | | |
|-------------------------------------|---|--|-------------------------------|---|--|---------------------------------|---|--|-------------------------------------|---|--|
| I. General meteorology. | { | <ul style="list-style-type: none"> A. History and bibliography. B. General and collected works. C. Organization and methods. D. Instruments. | | | | | | | | | |
| II. Theoretical meteorology. | { | <table> <tbody> <tr> <td style="vertical-align: middle;">A. Physics of the atmosphere.</td> <td style="font-size: 3em; vertical-align: middle;">{</td> <td style="vertical-align: middle;"> <ul style="list-style-type: none"> 1. Temperature. 2. Moisture. 3. Pressure. 4. Optical phenomena. 5. Electrical phenomena. </td> </tr> <tr> <td style="vertical-align: middle;">B. Mechanics of the atmosphere.</td> <td style="font-size: 3em; vertical-align: middle;">{</td> <td style="vertical-align: middle;"> <ul style="list-style-type: none"> 1. General circulation. 2. Winds. 3. Storms. </td> </tr> <tr> <td style="vertical-align: middle;">C. Cosmic relations of meteorology.</td> <td style="font-size: 3em; vertical-align: middle;">{</td> <td style="vertical-align: middle;"> <ul style="list-style-type: none"> 1. General circulation. 2. Winds. 3. Storms. </td> </tr> </tbody> </table> | A. Physics of the atmosphere. | { | <ul style="list-style-type: none"> 1. Temperature. 2. Moisture. 3. Pressure. 4. Optical phenomena. 5. Electrical phenomena. | B. Mechanics of the atmosphere. | { | <ul style="list-style-type: none"> 1. General circulation. 2. Winds. 3. Storms. | C. Cosmic relations of meteorology. | { | <ul style="list-style-type: none"> 1. General circulation. 2. Winds. 3. Storms. |
| A. Physics of the atmosphere. | { | <ul style="list-style-type: none"> 1. Temperature. 2. Moisture. 3. Pressure. 4. Optical phenomena. 5. Electrical phenomena. | | | | | | | | | |
| B. Mechanics of the atmosphere. | { | <ul style="list-style-type: none"> 1. General circulation. 2. Winds. 3. Storms. | | | | | | | | | |
| C. Cosmic relations of meteorology. | { | <ul style="list-style-type: none"> 1. General circulation. 2. Winds. 3. Storms. | | | | | | | | | |

- | | | |
|----------------------------|---|--|
| III. Applied meteorology. | { | A. Weather prediction.
B. Agricultural meteorology.
C. Medical meteorology.
D. Climatology. |
| IV. Terrestrial magnetism. | { | A. General.
B. Observations, instruments, and
methods.
C. Variation.
D. Distribution.
E. Connection with meteorology. |

V. Observations (meteorological and magnetic) classed geographically.

These have been largely subdivided, the number of divisions employed in the preliminary classification being 169. This number will be varied somewhat in revision, the final classification depending largely on the number and character of the titles in each class.

The following example will indicate the character of the subdivision :

- | | | |
|----------------------|---|---|
| II. A. 5. f. Aurora. | { | 1. General.
2. Description.
3. Height.
4. Frequency.
5. Periodicity.
6. Connection with meteorological phenomena.
7. Connection with terrestrial magnetism. |
|----------------------|---|---|

The classification has been from originals, where possible, and all resources of the libraries available have been used for this purpose. Where access to the work or article was not possible, correspondence was maintained for the explanation of doubtful titles. The assignment of cards to their subjects has been completed, but they are not yet arranged under their respective heads. Consequently, no statement of the number of titles under each class can yet be made, but a rough estimate shows that of the 50,000 titles about 5,000 will be under observations and 3,000 under terrestrial magnetism, leaving about 42,000 entries for meteorological discussions.

The author index is similar to that adopted by Drs. Houzeau and Lancaster, giving under the full name of the author, and for each title, an abbreviation of the subject under which it is classed, the date of publication, and the reference. The index, as completed, contains about 12,500 authors, or an average of four independent titles for each author. A biographical note may be included under each author.

The bibliography will be completed early in 1888, the only work now remaining being arrangement by subjects, revision, sub-class-

ification of observations, preparation of subject index and periodical list. The technical preparation of copy will follow when the appropriation for publication is made.

This communication was discussed by Messrs. MANN, FLETCHER, MARCUS BAKER, GILBERT, and the author.

Mr. LESTER F. WARD made a communication

ON THE GEOGRAPHICAL DISTRIBUTION OF FOSSIL PLANTS,

illustrated by a map.

[This paper will appear in full in the Eighth Annual Report of the U. S. Geological Survey, for the fiscal year 1886-'87.]

307TH MEETING.

NOVEMBER 12, 1887.

The President in the Chair.

Fifty-two members and guests present.

Announcement was made by the President of the election to and acceptance of membership of WILLIAM HENRY BABCOCK.

Mr. C. E. DUTTON presented a communication which had been jointly prepared by himself and Mr. S. NEWCOMB on

THE SPEED OF PROPAGATION OF THE CHARLESTON EARTHQUAKE.

[This paper appeared in full in The American Journal of Science, 3d series, 8°, New Haven, 1888, January, vol. 35, pp. 1-15.]

This paper was briefly discussed by Mr. CLARK and Mr. DUTTON.

Mr. HARKNESS read a paper

ON THE REPRESENTATION OF COMET ORBITS BY MODELS,

illustrated by card-board models.

[This paper appeared in The Sidereal Messenger; conducted by Wm. W. Payne. 8°. Northfield, Minn., Carleton College observatory, 1887, December, vol. 6, No. 10, pp. 329-349.]

308TH MEETING.

NOVEMBER 26, 1887.

The President in the Chair.

Fifty members and guests present.

A circular letter from the New York Academy of Sciences, requesting co-operation in erecting a monument to the memory of the ornithologist Audubon, was laid before the Society by the Secretary.

Mr. G. K. GILBERT presented a communication entitled

STATISTICS OF THE PHILOSOPHICAL SOCIETY FROM ITS
FOUNDATION.

[Abstract.]

The following data, except when otherwise noted, are compiled from the published records of the Society.*

The Society was organized March 13, 1871, with a membership of 44, and this was increased during the same year by the election of 17. In each succeeding year new members were elected, the smallest number being 8, in 1876, and the largest 35, in 1884. From time to time members have been dropped from the list for non-payment of dues, others have died, and others resigned. The average annual number of new members has been 18. The total number of resignations has been 24. The membership has always been classified as resident and non-resident, or "active" and "absent." From time to time a list of the members has been published in the Bulletin, and since 1879 these lists have been annual. The following table shows the number of active members at each of the indicated dates. It also shows the gross annual accession to membership, and likewise the average attendance at ordinary meetings for each year, beginning with 1875, previous to which time the attendance is not noted in the published minutes. The year 1882 had the minimum attendance, 34, and 1887 the maximum, 49. The general average of attendance at meetings for the reading of papers is 40; at meetings for the election of officers, 36.

*The paper, as read, did not include the statistics for 1887, which were necessarily imperfect at that time. The abstract for printing was brought down to December 21, 1887, the date of the annual meeting. Certain indicated data on membership were brought only to December 1, 1887.

TABLE I.

Membership and Attendance of the Philosophical Society, by Years.

Year.	New members.	Net active membership and date of same.	Average attendance at ordinary meetings.	Ratio of attendance to membership.	New societies or ganized.
1871----	17	44, Mar. 13 ..			
1872----	14	-----			
1873----	23	-----			
1874----	33	114, June			
1875----	22	124, Dec.	35	.29	
1876----	8	-----	37	--	
1877----	10	-----	40	--	
1878----	9	-----	40	--	
1879----	22	135, Apr. 2 ..	40	.29	Anth. Soc., Feb. 17.
1880----	19	154, July 20..	41	.27	Biol. Soc., Dec. 3.
1881----	13	152, July 18..	38	.25	
1882----	16	149, May	34	.23	
1883----	17	149, Dec. 31..	38	.26	Math. Sec., Mar. 29.
1884----	35	173, Dec. 20..	42	.26	Chem. Soc., Jan. 31.
1885----	22	179, Jan. 16..	47	.27	
1886----	18	183, Dec. 18..	47	.26	
1887----	15	191, Dec. 1...	49	.26	
Mean----	18	-----	40	.265	

In a general way there has been a continuous growth of the Society as regards membership, and the rate of growth, whether considered as a geometric ratio or as an arithmetic increment, has progressively diminished. The average attendance has likewise increased, but its law is not evident. The ratio of attendance to membership has ranged in ten recorded years from .23 to .29, the mean being .265.

The total active membership passed through a secondary maximum in 1880 and a minimum in 1882-'83. The current attendance exhibits a subsidiary maximum from 1877-'80 and a minimum in 1882. The curve of accessions shows maxima in 1874, 1879, and 1884. While there are many series of contemporaneous events with which these might be compared, one only will be considered, namely, the formation of other scientific societies in Washington and the formation of the Mathematical Section within our Society.

The Anthropological Society was organized February 17, 1879, and has now a membership of 154. The Biological Society was organized December 3, 1880, and has a membership of 174. The Mathematical Section of the Philosophical Society held its first meeting March 29, 1883. The Chemical Society was organized January 31, 1884, and now numbers 44 members. During the two years following the institution of the Anthropological Society our Society witnessed maxima in the accession to membership, in the total membership, in the attendance, and in the ratio of attendance to membership. During the two years following the foundation of the Biological Society each of these quantities reached or passed a minimum. The year of the organization of the Mathematical Section was characterized by an increase of attendance, but not of membership. In the four years elapsed since the beginning of the Chemical Society our membership and attendance have steadily increased, their ratio remaining constant. If the relation of our record to the Biological Society only were considered, it would be easy to infer that our Society suffered from the formation of another scientific society, but a contrary inference would be drawn from a comparison of our record with the histories of the Anthropological and Chemical Societies, and in view of all the facts it appears proper to conclude that our membership and attendance have not been materially influenced by the organization of the other societies.

The data of attendance have been classified by months likewise and finally by half-months, with the result which appears in Table II. The data cover a period of 12 years, but are somewhat imperfect. To diminish the error from imperfection of record, a general correction for annual phase was applied to all the observations—that is to say, they were all reduced to consistency with a mean attendance of 40. Only ordinary meetings for the reading of papers were included, and the year 1887 was omitted because the attendance appeared to be greatly affected by the change of quarters (March 26) from the Army Medical Museum to the Assembly Hall of the Cosmos Club.

TABLE II.

*Average Attendance at Ordinary Meetings for Each Half-Month,
Compiled from Records for 11 Years, 1875-1886.*

October, first half -----	39.8	March, first half -----	40.0
“ second half -----	40.5	“ second half -----	40.3
November, first half -----	45.0	April, first half -----	48.0
“ second half -----	43.9	“ second half -----	40.3
December, first half -----	43.2	May, first half -----	37.5
“ second half -----	40.8	“ second half -----	37.3
January, first half -----	31.5	June, first half -----	33.7
“ second half -----	45.9	“ second half -----	28.6
February, first half -----	41.3		
“ second half -----	41.0		

In compiling the statistics of papers or communications before the Society, everything has been included which was prepared or announced beforehand, whether offered independently or as part of a symposium, but the remarks of one member upon the communication of another have not been included. The impossibility of otherwise making a consistent distinction has led to the inclusion of every exhibition of apparatus and every reading of a letter upon a scientific subject. The biographical memoirs of deceased members which have from time to time been read are included, but not the commemorative resolutions.

The Society has listened in 17 years to 713 papers, as thus defined, an average of 42 per year. Six hundred and ninety-two of these have been presented before ordinary meetings, an average of 41 per year. There have been in the same period 277 ordinary meetings, and the average number of papers per meeting has been 2.5. The number of ordinary meetings and the total number of meetings per year were both somewhat greater in the earlier history of the Society than in the later, a tendency having developed to omit one or two meetings in June. There were also more papers read in the earlier years than in the later, and the diminution in papers has been slightly greater than the diminution in the number of meetings, so that the average number of papers per meeting has fallen off from 2.8 to 2.4.

For the purpose of exhibiting the subjects which have received the attention of the Society, the entire series of papers has been grouped in ten classes, the discrimination being based on the titles and abstracts, and, to some extent, in the absence of abstract, on the memory of the compiler. Papers belonging properly to two or

more of the selected classes have been entered in each, and such duplicate entries have been treated as integers and not as fractions. To an extent dependent on this treatment the deduced ratios are inaccurate.

It should be observed that the selection of classes has depended largely on the nature of the material to classify. As the statistics grew out of the work of indexing the Bulletin, the selection was affected by the needs of the indexer, and as it was desired to learn the influence of the organization of other societies on the scope of our proceedings, the selection was affected by the classification of subjects among the other societies. The following is the classification: Group 1, Mathematics; Group 2, Astronomy, including calendars; Group 3, Physics, including molecular physics, electricity, acoustics, optics, and microscopy, which last subject happens in the literature of the Society to be almost entirely optical; Group 4, Chemistry and mineralogy; Group 5, Meteorology and thermometry; Group 6, Geology; Group 7, Geography, including physical geography, surveying, and travel and exploration; Group 8, Biology, including zoology, botany, and human anatomy and physiology; Group 9, Anthropology, including ethnology, archæology, psychology, anthropometry, political economy, and social science and statistics; Group 10, Miscellaneous, chiefly technology, but including also biography and general philosophy. It will be seen that chemistry, biology, and anthropology are defined so as to include the scopes of the Chemical, Biological, and Anthropological Societies.

For convenience of discussion, the period of 17 years covered by the statistics has been divided into five unequal parts, such that three of the lines of separation correspond with the epochs of commencement of the three sister societies. The time divisions begin on the years 1871, 1875, 1879, 1881, and 1884, and contain, respectively, 4, 4, 2, 3, and 4 years. At the end of the second the Anthropological Society was established, at the end of the third the Biological, at the end of the fourth the Chemical. The Mathematical Section was organized one year before the Chemical Society. For each time division the number of papers of each class was ascertained, and from these numbers were computed the percentages which appear in Table III.

TABLE III.

Percentages of Papers on Different Subjects for Different Periods.

Subjects.	Periods.					1871 to 1887.
	1871- 1874.	1875- 1878.	1879- 1880.	1881- 1883.	1884- 1887.	
1. Mathematics -----	6	5	2	9	2	5
2. Astronomy -----	23	18	18	7	6	16
3. Physics -----	10	14	12	12	9	11
4. Chemistry -----	4	2	6	1	4	3
5. Meteorology -----	9	5	4	13	11	8
6. Geology -----	6	8	9	14	27	13
7. Geography -----	15	13	7	7	10	11
8. Biology -----	9	9	10	9	6	8
9. Anthropology -----	6	15	19	11	13	12
10. Miscellaneous -----	12	11	13	17	12	13
	100	100	100	100	100	100

It appears from this table that in the two periods previous to the organization of the Anthropological Society the subject of anthropology furnished first 6 and then 15 per cent. of our material, and in the following periods it furnished 19, 11, and 13 per cents. Biology furnished in the first three periods 9, 9, and 10 per cents., and after the beginning of the Biological Society 9 per cent. and 6 per cent. The percentages of chemistry for the first four periods are 4, 2, 6, and 1, and for the single period of four years since the organization of the Chemical Society, 4. These figures show that the organization of scientific societies devoting themselves to the cultivation of special scientific fields has not materially affected the interest of our Society in the same sciences, so far as that interest may be judged by the number of communications presented.

The table is not arranged to exhibit the effect upon our general meeting of the institution of the Mathematical Section, but an independent computation has been made with the following result: In 12 years previous to the Mathematical Section the Society listened to 28 mathematical papers, an average of 2.3 per year. In the five years following the general meeting listened to six mathematical papers, an average of 1.2 per year. While the amount of mathe-

matics before the Society in general meeting has been greatly diminished, the subject has not been entirely eliminated.

The general fact appears to be that the Philosophical Society, being composed partly of men with a wide interest in scientific matters and partly of specialists in many scientific branches, affords a fitting arena for the discussion of subjects of general scientific interest, but is not equally adapted to the presentation of highly specialized researches. By a process of natural and unconscious selection it has discountenanced those papers which from their nature can interest only the devotees of a single science, and it, therefore, has not fully met the needs of the scientific community of Washington. The natural and proper result has been the institution, without and within the Society, of organizations undertaking the cultivation of narrower fields, and these have found material of their own without detraction of material which naturally came to us. In anthropology, in biology, in chemistry, and in mathematics we still receive the communications which have a broad interest, and, as such papers are largely written from a philosophic point of view, it may well be that we are gainers by the multiplication of organizations.

But while the modifications which have occurred in the ratios in which various subjects have been represented on the floor of the Society do not indicate an important yielding of our program to outside influence, they do indicate progressive tendencies in other directions. Astronomy, which during the first period was the leading theme, with a percentage of 23, has fallen, through 18, 18, and 7, to 6 per cent.; geography, with 15 per cent. and 13 per cent. for the first two periods, has 7, 7, and 10 for the last three. Geology, on the other hand, with 6 per cent. at first, has increased steadily, through 8, 9, and 14, to 27 per cent., and anthropology and meteorology, while exhibiting fluctuations, have on the whole increased their percentages. During the first period astronomy and geography together gave 5 times as many papers as geology; during the last period their combined volume is only two-thirds that of geology. The general explanation is not far to seek. Geology has gained in importance on the floor of the Society because of the rapid growth of the Geological Survey, which has brought to the city and to the Society a large number of geologists. The increased attention of the Society to meteorology is traceable to the establishment of the Study Room of the Weather Bureau, and the increase in anthro-

pology is correlated with the growth of the Bureau of Ethnology. The great modification in the relative attention given to different subjects is due to the large amount of new blood acquired by the Society.

The statistics of the Mathematical Section are exhibited in the following table:

TABLE IV.

Statistics of the Mathematical Section from its Establishment to 1887.

Year -----	1883.	1884.	1885.	1886.	1887.
Number of meetings -----	9	6	6	2	12
Number of communications -----	18	11	14	3	20
Average attendance -----	15	15	15	16	17
Number of members -----	35	38	41	40	44

The whole number of papers presented to the Society, including those addressed to ordinary and special meetings and to the Mathematical Section, has been 786, and they have been communicated by 184 persons. Fifty-seven guests and correspondents of the Society have furnished 67 papers, and 127 members have furnished 719. The total number of persons who have at various times been elected to the Society is 312, and two-fifths of these have contributed something more than remarks to the proceedings.

The following numerical data concerning the membership and common membership of the Philosophical and three other scientific societies were derived from what is known as the "Consolidated List of the Philosophical Society," a list containing the names of the active members of the four societies and the resident members of the Cosmos Club. The list had been corrected to December 1, 1887. In Table V the Anthropological, Biological, Chemical, and Philosophical Societies are indicated by the initial letters of their names.

Mr. M. H. DOOLITTLE read a paper

ON NEWTON'S VIS,

and was followed by

Mr. B. PICKMAN MANN, who read a paper

ON REFERENCE INDEXING.

[Abstract.]

The author described in part the systems of indexing the literature of science which he had practised for many years, with illustrative examples and an argument to show their general applicability and value.

He commented upon the extent and variety of the literature of science as a whole, and the impossibility of obtaining a knowledge of the literature relating to special departments of research without the aid of indices prepared for the purpose. He then dwelt upon the multitude of separate, partial indices now in existence, upon the difficulties experienced in making use of these indices, and the waste of labor expended in disconnected attempts to obviate these difficulties. He adverted to the advantages which would accrue to all students through co-operative effort to obviate the difficulties described, and remarked upon the necessity, in case such co-operation were to take place, of determining upon a system of carrying it out. He considered the advantages which would be gained for temporary purposes by the combination of existing indices into one index to be the property of the co-operators and accessible either directly or mediately to all persons interested. He then passed to a consideration of systems by which indices have been constructed hitherto, and those which should obtain in the formation of such an index as was contemplated here.

309TH MEETING.

DECEMBER 10, 1887.

By courtesy of the trustees of the Columbian University the meeting was held in the law lecture-room of the University building.

Invitations to "yourself and friends" to attend the meeting had been mailed to all members of the Anthropological, Biological, and

Chemical Societies, and of the Cosmos Club. About one hundred persons were present.

Vice-President MALLERY presided.

President HARKNESS then presented his annual address, the subject being

THE PROGRESS OF SCIENCE AS EXEMPLIFIED IN THE ART OF
WEIGHING AND MEASURING.

[Printed in full on page XXXVII of this volume.]

A vote of thanks for the address was passed by the audience.

310TH MEETING.

DECEMBER 21, 1887.

THE SEVENTEENTH ANNUAL MEETING.

The President in the Chair.

Thirty-eight members present.

The minutes of the 294th, 308th, and 309th meetings were read and approved.

The President announced the election to and acceptance of membership of Mr. JOSEPH WILLIAM SPENCER.

The annual report of the Secretaries was read and accepted.

[Printed in full on pp. XXXII, XXXIII of this volume.]

The annual report of the Treasurer was read and referred to an auditing committee consisting of Messrs. J. S. Billings, J. C. Well-
ing, and C. O. Boutelle.

[Treasurer's report printed in full on pp. XXXIV, XXXV of this volume.]

The Treasurer read the list of members entitled, under Standing Rule 14, to vote at the annual meeting.

The constitutional amendment proposed by Mr. DALL at the last annual meeting was adopted by a vote of 26 for to 3 against it.

Election of officers was then held.

[The result is printed on page xv of this volume.]

The rough minutes of the meeting were then read and the Society adjourned.





Spencer F. Baird.

PROCEEDINGS

AT A MEETING COMMEMORATIVE OF

THE LIFE AND SCIENTIFIC WORK

OF

SPENCER FULLERTON BAIRD,

HELD JANUARY 11, 1888,

UNDER THE JOINT AUSPICES OF THE

ANTHROPOLOGICAL, BIOLOGICAL, AND PHILOSOPHICAL SOCIETIES
OF WASHINGTON.



INTRODUCTION.

On August 19, 1887, SPENCER FULLERTON BAIRD, Secretary of the Smithsonian Institution, Director of the U. S. National Museum, and U. S. Commissioner of Fish and Fisheries, died at Wood's Holl, Massachusetts, his post of duty in the last named office. His death at once excited throughout the world feelings and expressions of profound regret. At that time nearly all of his Washington associates in scientific pursuits were absent from the city, on field duty or in vacation, and were thus unable to jointly testify to the affection and respect in which he was held by them.

And especially the scientific societies of Washington, none of which meet during the summer months, were unable to immediately take any action in the matter or to give organized expression to the sentiments of their members.

With the resumption of meetings, however, it was determined that such expression should be given with all ceremonial completeness, and as the senior of the Washington scientific societies, and the one with which Professor Baird had been most closely connected, the Philosophical Society took the initial steps in arranging a joint meeting with the Anthropological and Biological Societies, a meeting which might enable the members and their friends to testify not only their profound respect for this foremost scientific leader, but also their affectionate regard for the man.

The appended invitation and programme, which was mailed to all members of the Philosophical, Anthropological, Biological, and Chemical Societies, and of the Cosmos Club, sets forth the form taken in those arrangements :

WASHINGTON, *January 4, 1888.*

SIR:

The Philosophical Society in conjunction with the other scientific societies of the city will hold a meeting on Wednesday evening, January the eleventh, in commemoration of the life and services to science of the late SPENCER FULLERTON BAIRD, Secretary of the Smithsonian Institution, Director of the National Museum, and United States Commissioner of Fish and Fisheries.

Members of the societies, and ladies and gentlemen whom they may desire to invite, will assemble in the lecture-room of the Columbian University, on the southeast corner of H and Fifteenth streets, at a quarter past eight o'clock.

Your presence on this occasion is earnestly desired.

C. E. DUTTON,
ROBERT FLETCHER,
J. H. KIDDER,
Committee of Management.

Opening of the meeting, by the President of the Philosophical Society.

Professor Baird as Administrator, Mr. W. B. TAYLOR, of the Smithsonian Institution.

Professor Baird in Science, Mr. W. H. DALL, President of the Biological Society.

The Personal Characteristics of Professor Baird, Mr. J. W. POWELL, President of the Anthropological Society.

Mr. GARRICK MALLERY, President of the Philosophical Society, called the meeting to order at the time and place above named.

RELATIONS BETWEEN PROFESSOR BAIRD AND PARTICIPATING SOCIETIES.

By MR. GARRICK MALLERY, President of the Philosophical Society.

LADIES AND GENTLEMEN :

During several winters before 1871, a club, with commingled social and scientific purposes, used to meet in this city at the houses of its members. A single paper on some scientific subject was read, usually by the host of the evening, following which was a discussion. Supper was always provided. The title of the club only related to the night of meeting, Saturday, and the organization was so loose that several of the survivors among the regular participants at the meetings do not now remember whether they were actual members, or indeed that there was a definite membership. As the city of Washington emerged from the condition of a Southern village, and the benign policy of the Government increased the number and force of the scientific institutions at the Capital, the need of an organization which should bring scientific men together on an equal footing and give more time to papers and their discussion became manifest. To meet this want the attendants of the Saturday-Night Club, on March 13th, 1871, formed the Philosophical Society of Washington, its object, in the words of the call, being "the free exchange of views on scientific subjects and the promotion of scientific inquiry among its members."

The term "Philosophical," as the first president of the Society, Joseph Henry, stated in his first address, was chosen after considerable deliberation, "not to denote, as it generally does in the present day, the unbounded field of speculative thought, which embraces the possible as well as the actual of existence, but to be used in its restricted sense to indicate those branches of knowledge that relate to the positive facts and laws of the physical and moral universe."

Of the forty-three gentlemen who signed the call twenty-one are now dead. Professor Baird was prominent among the founders, and served continuously as a member of the General Committee from the organization to November 10th, 1877, and from that date until

his death, on August 19th last, he was a member of the Committee on Publications.

The first communication of a scientific paper to the Society was made by him on March 18th, 1871. The most important and extended original papers communicated by him were "On the decrease of fish on the southern coast of New England," presented March 23d, 1872, and "On the artificial propagation of the cod, describing the measures and process adopted at Gloucester, Mass., and the success thus far obtained," presented March 1st, 1879.

The last-mentioned occasion is memorable to me, and some account of it will be interesting to the younger members of the Society, few of whom ever heard Professor Baird's voice raised in its hall. I happened to join him on his way to the meeting, and during the walk he spoke of the struggle at that moment between the sense of duty requiring him to take his part in the proceedings of the Society and his repugnance to making any formal address. This modesty—indeed, timidity—in an eminent writer and thinker, whose lightest words were sure of eager attention in a society composed mainly of his personal friends and wholly of his admirers, was the more remarkable because his address, presented a few minutes later, was most pleasing in its delivery as well as instructive in its substance. He spoke without notes, and, though his style was conversational and in no degree oratorical, his appropriate words in their rapid flow expressed his thoughts clearly, completely, and in orderly sequence.

During the same walk, Professor Baird mentioned with earnest commendation the usage of the Society by which the perfect equality of members is recognized through the omission of all official and professional titles. This was not a merely unwritten custom but was founded on a binding resolution, appearing in the minutes of June 6th, 1874. The Society is probably the only non-esoteric body in the United States in which the titles of Judge and General, Professor and Doctor, Governor, Senator, and even Honorable Member are forbidden; the simple and dignified Mr., the modern form of Magister, being the only address allowed. Perhaps the plethora of titles and the burdensome hierarchal gradations in Washington compelled this measure of relief.

The Anthropological Society was founded February 17th, 1879, its defined object being "to encourage the study of the natural history of man, especially with reference to America." Professor Baird warmly approved of the organization of this Society, took constant

interest in it, and, at the time of his death, was the only honorary member residing in the United States on its rolls.

The Biological Society was organized December 3d, 1880, "to encourage the study of the biological sciences," and Professor Baird was the only honorary member ever elected by it. He did not take an active part in the proceedings of either of the last-mentioned societies but gave them material assistance. Both of them met at first in the Regents' Room of the Smithsonian Institution, placed by him at their disposal, and he provided for the stereotyping and circulation of their volumes of Transactions, a benefaction which the Philosophical Society had earlier enjoyed.

President Henry, in his address before mentioned, stated that in no other city in the United States was there, in proportion to the number of its inhabitants, so many men actively engaged in pursuits connected with science as in Washington. In the seven following years the number of persons in the city engaged in scientific work was nearly doubled, and most of them joined the Philosophical Society, so that in the year 1878 it had become recognized as the most efficient scientific body on this continent with a membership confined to a single locality. The criteria of this superiority were not only the large membership and regular attendance of members, but the number, quality, and variety of the papers presented and discussed. This abundance and, as was proved by the later successful establishment of differentiated societies as an overflow, this superabundance of scientific papers occupied every moment of the meetings, so that the members, as such, had no opportunity to become acquainted with one another or to interchange views, except in the formal discussions following the papers announced in the printed programs. There was no provision for social introduction or intercourse. This appreciated want, the converse of the inadequacy of the Saturday-Night Club, resulted in the foundation of the Cosmos Club, on December 13th, 1878, in the organization of which all the members of the Philosophical Society were invited to join. It is needless to descant upon the unique character of the Cosmos Club in its membership and objects, its vital connection with science, literature, and art, and its immediate but enduring success. The remark, however, is pertinent that, in the winter of 1878, an unprecedented agitation, excited by impending national legislation, perturbed the scientific circles of the Capital, during which the proposition to form the Club was attacked

with virulence as a scheme in the selfish interest of a few individuals, and one fraught with machiavelian political designs; but when Professor Baird manifested his approval of the plan by accepting the first presidency of the Club after its formal organization, confidence in him was so dominant that suspicion was allayed and opposition disappeared. To him profound thanks are due for the timely establishment of the most important institution in the conjoint social and scientific life of Washington.

But by his work in the organization of these several societies and of the Cosmos Club, Professor Baird was, as in his other fields of labor, a benefactor and not a participant in the benefits secured to others. He was imbued with the cardinal principle of the Smithsonian Institution not only to establish and assist all useful agencies for the promotion of the well-being of man, but afterwards, when they had attained to successful operation, to leave them to themselves and explore new fields of beneficence. It was also his own character, apart from any formulated maxim of the Institution, that he could not rest in the personal enjoyment of accomplished results. He was one of the ceaseless workers, born

“ To scorn delights, and live laborious days,”

until

“ Comes the blind Fury with th' abhorred shears
And slits the thin-spun life. But not the praise !”

It is for us now, repressing sorrow, to join in tributes of praise to our benefactor.

PROFESSOR BAIRD AS ADMINISTRATOR.

By Mr. WM. B. TAYLOR, of the Smithsonian Institution.

We are met this evening to express in a memorial service our respect for an honored fellow-member of our several societies, lately deceased, and to indulge as well in an interchange of affectionate reminiscence of a departed friend.

Spencer Fullerton Baird was born at Reading, Pa., February 3, 1823. He was graduated at Dickinson College, in Carlisle, Pa., in 1840, at the age of seventeen, and with an original fondness for natural history and the study of the out-door world he spent several years in his favorite pursuits and in collecting animal specimens for preservation. In 1845, at the youthful age of twenty-two, he was elected Professor of Natural History in his *alma mater*—Dickinson College.

Three years later, in 1848, while still pursuing with ardor the study of nature, he applied for and obtained from the Smithsonian Institution (then recently established) its first modest grant for the promotion of original research. This was to be applied to the exploration of bone caves, and to the development of the local natural history of southeastern Pennsylvania. The transaction appears to have been the occasion of first bringing the young professor to the favorable notice of the Smithsonian Director, Professor Henry, and of initiating between the two a mutual respect and friendship that continued throughout their several lives.

The early history of the Smithsonian Institution was signalized by a long struggle—both in the Board of its Regents and in the Halls of Congress—between the votaries of literature and those of science for the disposal of the Smithson fund. During this period, in 1850, when it was seen that the income of this institution was not to be absorbed in the building up of a great National Library, Professor Henry asked of the Regents authority to appoint an Assistant Secretary in the department of natural history to take charge of the Museum and to aid in the publications and other interests of the establishment. A resolution authorizing such an appointment being adopted, Henry selected Professor Baird, of

Dickinson College, as the one well fitted for the place. The appointment was unanimously confirmed by the Board July 5, 1850, and Professor Baird being notified at once accepted and entered upon his new duties. He deposited in the Museum his own valuable collections, comprising an extensive series of the skins of various mammals (European as well as American), a large number of bird skins (unmounted), representing about 500 American species and half as many European species, a rich variety of birds' nests and birds' eggs, more than 500 glass jars, tin vessels, and kegs containing alcoholic specimens of reptiles and fishes, and a number of vertebrate skeletons and of fossil remains.

The new Assistant Secretary was truly in his element, and showed himself pre-eminently "the right man in the right place." In Henry's Fourth Annual Report (that for 1850), after recording the appointment of his Assistant, he adds: "He entered on his duties in July last and, besides being actively engaged in organizing the department of natural history, he has rendered important service in conducting our foreign exchanges and attending to the business of the press."

The Smithsonian system of exchanges was instituted for the purpose of facilitating the reciprocal transmission between the Old World and the New of the memoirs of learned societies, and this system has become an essential agency in the interchange and diffusion of knowledge, and in the more rapid advancement of scientific discovery, by a wider and prompter co-operation. Previous to this inauguration such distant scientific information was so rarely and inconveniently accessible, largely through the delays and harassments of customs exactions, that important principles had not unfrequently been re-discovered abroad or at home, and sometimes with a considerable interval of time, to subsequently disturb and dispute a coveted and settled priority.

By the urgent zeal of the Smithsonian Director, representing to foreign powers that only gratuitous distribution of the literary and scientific memoirs of societies or of individuals (not usually found on sale) was undertaken by the Institution, and that no commercial enterprise calculated in any way to interfere with the legitimate operations of trade was attempted—one port after another was opened to its packages, until, in the course of a few years, the announcement was made that the Smithsonian exchanges were allowed

to pass through every custom-house on earth, unopened and unquestioned.

Creditable as this special liberality is, it has not yet, unfortunately, been applied to the customary channels of book lore, and the quest for knowledge is still held by a majority of civilized nations as an indulgence very proper to be taxed. Our own legislators have also made our higher education a source of revenue; possibly with a view to the "incidental protection" of American science by the heavy tariff laid on the foreign and imported article.

The advantage to the cause of science from this Smithsonian system of international exchange of intellectual products, free of duty, and with the freight expenses assumed by the Institution, can scarcely be too highly appreciated. In the early promotion of this beneficent scheme, Professor Baird became an energetic agent and sympathetic co-adjutor of the Smithsonian Secretary. The remarkable development of this service may be sufficiently indicated by a glance at the amount of material transmitted through this Institution, on each tenth year for thirty years, showing something like a geometrical ratio of increase. The total weight of books, pamphlets, and charts distributed in 1855 was about six tons; in 1865, about nine tons; in 1875, about twenty tons; and in 1885, about eighty-five tons. With the rapid growth of the exchange operations, the active and comprehensive faculties of Professor Baird seemed but to find a better field of exercise.

At the same time, the accumulating collections of the museum—increased in 1858 by the transfer from the Patent Office to the Smithsonian building of the interesting contributions from the earlier national exploring expeditions—demanded a large share of attention for their proper arrangement, exposition, and superintendence.* To say that this important work of organization was zealously and judiciously carried out, is to characterize but imperfectly the directive skill and energy of the museum curator.

Of Professor Baird's work in original biologic research,—of his contributions to various scientific journals and society proceedings,—of his English translation of the popular "Iconographic Encyclo-

* This accession of the Government deposit of ethnological and natural history specimens was estimated by Professor Baird, in his report for 1858, as comprising not more than a fourth of the material already in the Smithsonian Museum or a fifth of the aggregate amount.

pædia," of his editorship of the "Annual Record of Science and Industry" for eight years,—and of his other publications,—it is not proposed here to speak. This aspect of his intellectual life will be discussed by one in every respect far more competent to a just and discriminating presentation of the theme. The present remarks will be confined to a cursory review of Professor Baird's varied administrative work.

For a number of years a notable decline in the productiveness of our extended fisheries had been with anxiety observed, the annual yield of this important element of our food supply having in many cases fallen off one-half of its amount a quarter of a century earlier. So serious a diminution and consequent enhancement of cost of subsistence was becoming a menacing problem. Were our leading food-fishes undergoing a process of slow but certain extinction? Several of the States (especially those of New England) appointed commissions of inquiry into the causes and remedies of the threatening evil, but with little result.

In the stern competitive struggle that from the dawn of terrestrial palæontology has been ordained by nature as the feudal tenure of all existence, and from which service man himself is not exempted, the feebleness of early youth in the individuals of every race would speedily terminate the biology of our planet were not provisions made for bridging over these cross lines of weakness to preserve the continuity of species. In the lower classes of being we find the crude expedient of a fertility so enormous as to allow of the wholesale destruction of the unprotected eggs or of their brood, and yet leave a remnant to spare for the chances of reaching adult age. In numerous other classes, a marvellous sagacity is displayed by the mother in depositing her eggs where they will be least exposed to accident or voracious attack, and where the progeny (that she shall never see) will meet with their appropriate sustenance. In insects this peculiar instinct—so difficult of explanation as "inherited experience"—is perhaps most strikingly displayed. And lastly, when we ascend to the higher classes of birds and mammals, we find the parental sentiment developed to an untiring vigilance for the protection, and provident care for the nutrition, of the new generation until it is able to take up for itself the battle of life.

As an illustration of the reckless prodigality of productiveness in some of the lower families of the vertebrate branch it may be recalled that a single salmon will lay five thousand eggs; a trout, fifteen thou-

sand eggs; a perch, a herring, or a shad, thirty thousand eggs; a pike, one hundred thousand eggs; a carp, four hundred thousand eggs; a mackerel, five hundred thousand eggs; a flounder, one million eggs; a haddock, one million and a half of eggs; a halibut, two and a half millions of eggs; a pollock, four million eggs; a cod-fish of medium size, five million eggs; a large-sized cod, nine million eggs, and a turbot, nine million eggs. Such numbers are simply astounding; they cannot be realized. And how great the marvel when we consider that each of these nine million units is a potential fish, capable of development into all the perfected attributes and functions of the parent form! Among the lower *invertebrates* may be simply instanced the oyster—capable of producing the incredible number of twenty or thirty million eggs, and if of large size as many as forty or fifty million eggs.

If with this amazing fertility the various kinds of fish just named are not rapidly increasing, but are stationary or even decreasing in numbers, how overwhelming must be their early destruction. Even after allowing for the many millions of adult fish taken by man it is obvious that of many species not one in a thousand or in ten thousand of eggs or of the newly hatched can survive to maturity. Professor Möbius estimates that for every grown oyster upon the beds of Schleswig-Holstein more than a million have died.

To avert, if possible, the menace of increasing scarcity of fish supply the attention of Congress was directed to the subject;—the more properly since in our National Government resided the jurisdiction over our extended sea coasts. By a joint resolution, approved February 9, 1871, the President was authorized and required to appoint a person of proved scientific and practical acquaintance with the fishes of the coast to be Commissioner of Fishes and Fisheries, with the duty to prosecute investigations into the causes of diminution, if any, in numbers of the food-fishes of the coast and the lakes of the United States, and to report whether any and what protective, prohibitory, or precautionary measures should be adopted in the premises.

No man more suitable for this important and responsible position than Professor Baird could have been selected. He was at once appointed by President Grant and confirmed by the Senate as the Commissioner. In his first report he announced, as the result of a most careful and thorough examination, that the decrease of the shore fishes of the New England waters during the preceding twenty

years was fully substantiated, and that it had been much more rapid since the year 1865.

In furtherance of his great work, the resources of the Smithsonian Institution were freely placed at the disposal of the Commissioner; and, in the same report, he gratefully acknowledges this hearty co-operation by saying: "I am indebted to Professor Henry for permission to use the extensive collection of apparatus belonging to the Smithsonian Institution, in the way of nets, dredges, tanks, &c., and thus saving the considerable outlay which would otherwise have been necessary."

The new studies into the life-history of the principal shore fishes,—into the character and range of their enemies, and into their appropriate means of subsistence, requisite to an intelligent consideration of the conditions most favorable to their propagation,—involved investigations embracing the entire marine fauna of the coast, vertebrate and invertebrate. These extensive and varied researches necessarily demanded the aid of skilled assistants—of a corps of eminent specialists in marine biology, and a corresponding division of labor.

The results of these investigations have been given to the world in hundreds of memoirs, published in the Reports and Bulletins of the Commission, and in the Proceedings and Bulletins of the National Museum. And it is quite within bounds to say that in importance, in variety, and in extent of original information thus communicated, no such quantity of contribution to our knowledge of zoology has ever emanated from any other organization within the same interval of time. Many species of fishes entirely new to science have been discovered and carefully described; and the number of invertebrate forms known to inhabit the waters explored, has probably been fully doubled.

It was found, from the abundance of the lower forms of life, that the decline of the useful fishes had not resulted from any lack of their accustomed food-supply; nor had it resulted apparently from any less favorable conditions of environment, nor from the prevalence of any epidemic diseases. It was therefore a consequence of excess in their destruction.

Among all the ravages of predaceous fishes it was found that the "bluefish" was the most voracious and devastating pirate of the coast. In the report it is stated: "Sometimes among a school of herring or menhaden thousands of bluefish will be seen biting off

the tail of one and then another, destroying ten times as many fish as they really need for food, and leaving in their track the surface of the water covered with the blood and fragments of the mangled fish." Fortunately this fish is itself valuable for food, and it is accordingly taken in large numbers.*

But by far the most rapacious and destructive scourge of the waters is man himself. By reckless extravagance in his methods of capture he would soon consume the capital of his abundant patrimony were no restraints imposed upon the thoughtless improvidence of his greed. With the growth of population and demand and the improved facilities for rapid transportation, the stimulus to inventive ingenuity occasioned the establishing of fish-traps and fish-pounds on a large scale that gathered thousands in their confines, with little regard to the probable supply of the future. As these traps and pounds were placed directly in the way of the fish to their spawning beds, it resulted that a very large proportion of spawn fishes were taken by them, thus greatly reducing the prospects of the succeeding generation.

Whatever protective measures might be deemed expedient to check this spendthrift waste, it was seen that the most immediate and promising work of the Commissioner would be to promote the rapid multiplication of fish; and to this dominant interest the annual appropriations by Congress have been more and more largely directed.

Pisciculture is by no means a recent art, it having been extensively practiced by the Chinese for a number of centuries; and even the artificial fecundation of fish-spawn is nearly a century and a third old, having been apparently first introduced by Jacobi, a German, of Westphalia. Most of the European nations had already given attention to the practical application of fish-culture, and in different parts of our own country enterprising individuals had undertaken the operation with gratifying results.

Under the organizing direction of Professor Baird a careful study was made of existing methods, extended experiments on artificial propagation were conducted, and successive improvements in the various stages of incubation, hatching, and development intro-

* In his first report, Professor Baird says: "I am myself cognizant of the capture of no less than 20,000 bluefish, representing a weight of at least one hundred thousand pounds, in one weir in the course of a single night."

duced,—each detail receiving a scientific treatment,—until a scale of success has been effected far more complete and satisfactory than ever before attained. While under natural conditions but a small proportion of the spawn deposited is hatched (the greater mass being eagerly devoured by various aquatic tribes), and of the portion hatched but a small percentage escapes to reach maturity, under the careful breeding of art fully ninety per cent. of all the eggs secured are fertilized and successfully developed.

Of the practical results of this great national enterprise it is unnecessary to speak. A dozen varieties of our best food-fishes have been disseminated throughout the inland waters and the seaboard of our country in increasing quantities; transported in the form of the young fry, or in that of fertilized eggs to other hatching stations; and while an accurate estimate is, perhaps, at present not easily attainable, it will hardly be held an exaggeration to say that these productions are to be numbered by thousands of millions. Of these, many millions (by a most praiseworthy public courtesy) have been distributed to foreign countries—to Australia, to Brazil, to Canada, to England, to France, to Germany, to Mexico, to The Netherlands, to Scotland, and to Switzerland.

In the great International Fisheries Exhibition at Berlin in 1880 our national commission was authorized by Congress to participate. Professor Baird appointed as his deputy to personally superintend this movement Professor Goode, the present Fish Commissioner, under whose energetic direction, in a remarkably short space of time, the marvellous American exhibit was organized, transported, and installed, to the wonder and admiration of every visitor. The head of the American Commission was hailed by the President of the German Fisheries Association as the “chief fish-culturist in the world,” and to him was awarded for the most complete and imposing display of all the details and accessories of his scientific art the unique first-honor prize of the exhibition, the gift of the Emperor of Germany.

But time fails to permit more than a passing glance at other fields of activity no less important in which Professor Baird employed his remarkable powers of executive management. The Smithsonian Institution from its inception had given great encouragement to explorations, and its director had zealously labored to enlist, as far as practicable, the various expeditions undertaken by the Government, in the extension of scientific research. These efforts were lib-

erally responded to by the Executive Departments, and trained experimentalists and observers were given every facility for physical, physiographical, and biological investigations at distant points. The Institution thus became almost the Government superintendent of scientific expeditions. In all that pertained to ethnology and natural history Professor Baird became of course the leading spirit, and the various circulars of direction and of inquiry issued by him show with what range and thoroughness he supervised this wide department, while the resulting memoirs and valuable museum accessions attest as their fruits the practical wisdom of the measures and methods adopted.

Congress having made provision for the representation by the Government in the National Centennial Exhibition to be held at Philadelphia, the President of the United States requested the Executive Departments, together with the Smithsonian Institution, to co-operate in a collection illustrative of our progress and resources. In his report for 1875, Professor Baird formulated (as requested by Professor Henry) his plans for the different details of the projected exhibit, and, these being adopted, were carried out to a result that made the Smithsonian display the leading attraction of the extensive Government building.

At the death of Professor Henry, in 1878, his faithful assistant and coadjutor was elected by the Regents as his successor, and his long familiarity with the different lines of active operations pursued by the Institution made him from the start an efficient director. Another grave responsibility was thus thrown entirely upon his shoulders, and he proved himself equal to the occasion.

In 1879, Congress made an appropriation (since continued annually) for the prosecution of North American ethnology, to be expended under the direction of the Smithsonian Institution. For the administration of this important trust, Professor Baird selected one whom he knew to be peculiarly fitted by training, by zeal, and by congenial tastes, to pursue successfully the anthropologic study of our waning aborigines, and the new Bureau of Ethnology was judiciously committed to the control of the distinguished director of the Geological Survey, Major Powell.

In the same year (that following Henry's death) an appropriation (for many years importunately besought of Congress) was made for the erection of a national museum building. In 1882 the completion of this building rendered necessary the re-organization of the

Museum, with a staff of expert curators, on a scale commensurate with its importance, and the abundance of its previously stored material.

Professor Baird had now become the manager of three great establishments—the Fisheries Commission, the Smithsonian Institution, and the National Museum; either one of which was a charge sufficient to fully task the energies of a vigorous man. No wonder, with the strain of unremitted though divided attention to these exacting duties, that while unconscious himself of any unaccustomed or undue exertions, he should find even his robust and stalwart strength was slowly failing under his accumulated labors.

Informed by his medical adviser that an entire and continued rest from all intellectual exertion was necessary to restore his nervous energies to their wonted tone, he reluctantly accepted the decision. A year ago he asked from the Smithsonian Regents authority to appoint two official assistants to relieve him from the greater portion of his responsibility, and in hearty compliance with his expressed desire, the eminent astronomer and physicist, Professor Langley, was appointed assistant in charge of the Smithsonian operations, and his well-trying friend and collaborator, Professor Goode, was appointed assistant in charge of the Museum affairs.

But the relaxation came too late. After a vigorous resistance of his strong constitution to the encroachments of internal organic derangements, he finally succumbed to the Destroyer, and quietly breathed his last on the 19th of August, 1887;—another example (far more frequent in the higher than in the lower fields of occupation) of sacrifice to over-work.

From even this hurried and imperfect sketch of Professor Baird's diversified administrative work it is at once apparent that he possessed, in a pre-eminent degree, two great capacities,—the faculty for successful organization, and the faculty for continuous labor. As a biologist he had made a study of the entire range of organic nature—vegetable and animal; and with the accuracy of the specialist, he combined the larger and fuller perception of the general zoologist as to the functional and genetic inter-relations of animated being. The tenor of his mind was rather synthetic than analytic. While he ever displayed a marvellous memory for particulars and a comprehensive grasp of details, these were apprehended more as the constituents of a general end or purpose, than as the residuals of a disjunctive conception. Clear-sighted and determined, he prevised

and compassed the result in the means. Simple and unostentatious, he received with ready affability a visitor, even when most pre-occupied. What young naturalist ever applied to him for the resolution of a difficulty or uncertainty without receiving cordial attention and satisfactory enlightenment?

Great as were his undoubted services in the original discovery of biologic truths, it may well be doubted whether his indirect influence in the advancement of science was not still greater, by the assistance and encouragement given to others and by his numerous official occasions of directing the efforts of the aspiring into channels of novel exploration whenever the opportunities of land or naval expeditions presented themselves.

Now that the first shock of bereavement at missing one who has occupied a prominent place in the public eye, as well as in our private regard, has somewhat subsided, we but the more clearly realize that in the lamented death of Spencer F. Baird the scientific world has lost an accomplished and illustrious naturalist, the institutions over which he presided an energetic and judicious administrator, and we, assembled here, an exalted associate, a faithful counsellor, an ever open-hearted friend.



PROFESSOR BAIRD IN SCIENCE.

By Mr. Wm. H. DALL, President of the Biological Society.

In accepting the honor of addressing you this evening on the biological work of Prof. Spencer F. Baird it is hardly necessary to state that I have felt keenly the inadequacy of my own equipment for the task. Not only does it happen that my own work has been almost entirely in departments of biology different from those which he adorned, but my early efforts were fostered by his wisdom and geniality, the period of my scientific studies has coincided with an acquaintance which ripened into affection and admiration, they have depended for their results upon opportunities largely due to the intervention of Professor Baird, and I feel that the best and truest of him is that which cannot be put in words. The sense of personal loss, as with many of you, is still so keen as to accentuate the difficulty of doing justice to the theme assigned me.

I should have almost despaired of myself on this occasion were it not that others have aided me in my endeavor to set forth the debt owed by the various departments of research to Professor Baird's original investigations. To naturalists so distinguished in their specialities as Ridgway, Stejneger, Goode, Coues, Allen, Merriam, and Yarrow, I am indebted either for direct contributions toward the substance of this address or for matter in their published works which has been similarly utilized.

Professor Baird's scientific activity was exhibited in three principal directions: First, in original investigation of the zoölogy of vertebrates; second, in the diffusion of scientific knowledge and methods through official documents, reports, cyclopedias, and records of progress; and lastly, in the organization and administration of scientific agencies such as the National Museum or the Fish Commission, which include in their scope not merely public education or economic applications of science, but the promotion of research. Behind all these and hardly less important for science was the personal influence of the man himself, which shone through all the planes of his activity as coruscations light the facets of a gem.

Although it is very difficult to separate the phases of his work, one from another, so closely were they inter-related, my theme tonight is restricted to the impress left upon zoölogical science by Baird's original investigations. So great has been his reputation as an organizer, so numerous have been the publications in which he has garnered for the public the precious grain of the annual scientific harvest, that the extent and importance of his original work, except by specialists, is in danger of being overlooked.

We owe an excellent bibliography of his publications to Professor Goode. From this we learn that, up to the end of 1882, the list comprises nearly eleven hundred titles, from which, after deduction of all notices, reviews, official reports, and works edited for others, some two hundred formal contributions to scientific literature remain, many of which are works of monographic character and extensive scope.

With the exception of a single early botanical paper these relate to the vertebrates of America and, in their several branches, cover nearly the entire field. Although descriptions of species in themselves afford a poor criterion of the value of the work containing them, it is interesting to note that, among the terrestrial vertebrates, the proportion of the fauna first made known by Baird to the total number recognized at the time as North American varied from twenty-two per cent. of the whole to forty per cent. in different groups.

His method of study of new material was as far removed as possible from bookishness. In the case of the collections from Hudson Bay or the Pacific Railroad Surveys, when birds, mammals, or reptiles sometimes came to hand by hundreds, each specimen having the collector's data attached, the whole collection was thrown together, each form to be sorted out on its merits and studied in the light of a multitude of specimens.

Professor Baird's early life had included so much of exercise in the shape of long pedestrian journeys with gun and gamebag, so much familiarity with the wood-life of his favorite birds and mammals, that it would have been in any case impossible to class him with the closet-naturalist, while to this knowledge he added a genius for thorough, patient, and exhaustive research into all which concerned the subject of his study, and a wonderful inventiveness in labor-saving devices for labelling, museum work, and registration.

He had a wonderful capacity for work. He undertook and carried out successfully tasks which it would seem nobody else would have dared to attempt, or, attempting, would have been physically unable to complete. In the case of the immense volume on the mammals of the Pacific Railroad Surveys he says in the preface, July 20, 1857 :

“ The examination of the material was actually commenced early in 1855 and many of the articles written in that year or 1856. With the continual accession of additional specimens it became finally necessary to rewrite, alter, or extend all that had been prepared prior to the present year (1857). It is to this that the frequent want of uniformity is due, the time allowed not being sufficient in many cases to permit the reworking of the whole matter. * * * It is, perhaps, unnecessary to state that the matter of the present report is entirely original throughout. * * * It is proper to state that, owing to various circumstances, the work was necessarily passed through the press with a rapidity probably unexampled in the history of natural-history printing, allowing very little opportunity for that critical and leisurely examination so necessary in correcting a work of the kind. For most of the time the proof has been furnished and read at the rate of twenty-four to thirty-two pages per day, nearly 400 pages having been set up, read, and printed during the first half of July alone. Owing to the urgent necessity for the speedy completion of the volume, no time was allowed for the revision of the manuscript as a complete work, nor, indeed, of its separate portions, and, for much of the time, the preparation of much of the manuscript was only a few hours in advance of its delivery to the compositor.”

The volume above referred to contains over 800 quarto pages and 42 plates. The manuscript was entirely prepared after six o'clock of working days which had been spent in the active administrative and executive work of the Assistant Secretary of the Smithsonian Institution, then unassisted by stenographer or other clerical supplement. Fortunately for science Baird did not always have to work under such circumstances, but the incident shows what he was capable of doing when the occasion seemed to him to warrant it. Probably no other work of equal importance, on any subject, was ever carried out under such pressure.

Mammals.—Professor Baird's contributions to a knowledge of North American Mammals, though less voluminous than those relating to birds, are not less important. Previous to this time but

one general work on the subject had been published, that of Audubon and Bachman on the Quadrupeds of North America, which was issued in three volumes, from 1846 to 1854.* Immediately after the completion of this great work collections began to pour into the Smithsonian Institution from the various exploring parties of the Pacific Railway Surveys. This material comprised so large a number of new species, and cast so much light upon many previously doubtful points concerning the relations of species already described, that a revision of the whole subject became necessary. Hence Professor Baird at once set about the preparation of the book commonly known as the Mammals of North America. I have already alluded to the manner in which it was prepared. This great work was rapidly pushed to completion and appeared in 1857, just three years after the publication of the last volume of Audubon and Bachman's Quadrupeds. It constitutes the eighth volume of the Pacific Railroad Reports, and is a ponderous quarto of more than 800 pages, accompanied by numerous excellent plates.

Though published thirty years ago, this work still remains the standard general treatise on North American mammals. It contains no biographical matter, but consists wholly of technical descriptions. It treats of all the mammals then known from the continent of North America north of Mexico, except the bats and the truly pelagic forms—whales, sea cows, and seals. The total number of known species was increased nearly twenty-five per cent.

In fullness of synonymy, and in the correct assignment of species previously described, Professor Baird was much in advance of previous workers. The descriptions, which are models of painstaking accuracy and precision, are taken from the specimens themselves, and are accompanied by long tables of measurements, the value of which more than justifies the enormous expenditure of time necessary in their preparation. Much more attention was paid to craniological characters than had been the custom with previous writers, which fact contributes largely to the permanent value of the work.

Professor Baird's long training as a careful observer, his power of concentrating his knowledge of matters under investigation, the

*The volume on Mammals of Richardson's *Fauna Boreali Americana* does not fall under this head, because it treats only of the northern portion of the continent.

wide scope of his information on nearly all departments of natural science, his clear perception of details, together with his excellent judgment, which was as marked in matters of minor detail as in those requiring great executive ability, enabled him to draw conclusions which subsequent accumulations of material have verified in a surprising manner; in fact, his pre-eminent superiority as a systematic zoölogist is everywhere apparent.

Birds.—When the great interest he took in birds is considered, and the long period over which his studies extended, it is somewhat surprising to find that the number of separate papers on ornithology published by Professor Baird sums up only some seventy-nine titles. It is less to their number that he owed his fame as an ornithologist than to their quality, combined with the fact that several of these publications covered practically the entire field of North American ornithology, and were of the nature of monographs.

“His reputation was, indeed, established,” says Ridgway, “by the first of his separate works, usually known and quoted as the “Birds of North America,” though not published under this title until two years after it had been printed by the Government as Volume IX of the Pacific Railroad Reports. With the publication of this great quarto volume, containing more than a thousand pages, in 1868, began what has been fitly termed by Dr. Elliott Coues the “Bairdian period” of American ornithology. This period, covering almost thirty years, was characterized by an activity in ornithological research and a rapidity of advancement without a parallel in the history of the science.

Of the “Birds of North America” Coues states* that “it represents the most important single step ever taken in the progress of American ornithology in all that relates to the technicalities.” The nomenclature was entirely remodeled from that previously in current use, and for the first time was brought abreast of the systematic acquirements of the time. The synonymy of the work, in which is embodied the history of investigation relating to each species, is more extensive, reliable, and elaborate than any before presented. With few exceptions, citations were original, and when, as occasionally happened, they were necessarily at second-hand the fact was

* Bibl. app. to the Birds of the Colorado Valley, p. 650.

always indicated. The text comprised not only diagnoses and descriptions of each species, but extended and elaborate commentary, comparisons and criticisms.

In this learned and sagacious work Professor Baird was aided by Cassin and Lawrence, two of the leading ornithologists of America. It exerted an influence perhaps stronger and more widely felt than any of its predecessors, Audubon and Wilson not excepted, and marked an epoch in the history of American ornithology. The data original to and embodied in this work have been used again and again by subsequent writers with various modifications. Such a monument of original research is likely to remain for an indefinite period a source of inspiration to other writers, while its authority as a work of reference will always endure.

The publication of this work rendered possible the studies and progress of a large number of persons, who without it would hardly have been able to enter the domain of scientific ornithology, but who, aided by the book as a standard of reference and by the genial correspondence and pregnant suggestions of its author, have made reputations of more or less distinction for valuable and permanent original investigation. The number of those who profited by this stimulation has been very large and in this way arose what has been called* the Bairdian School of Ornithologists, a school characterized by exactitude in matters of fact, conciseness in deductive statement, and careful analysis of the subject in all its various bearings. Its work is marked by a careful separation of the data from the conclusions derived from them, so that conclusions or arguments can be traced back to their sources and duly weighed, while the writings of the older European school afford little basis for analysis. In substance, according to Dr. Stejneger, the European method required an investigator to accept an author's statements and conclusions on his personal responsibility alone, while the method originated by Baird furnishes him with tangible facts from which to make his deductions.

These distinctive features were still further developed by the publication in 1864-'66 of the "Review of American Birds," a work of unequalled merit, displaying in their perfection Professor Baird's wonderful powers of analysis and synthesis, so strongly combined in his treatment of difficult problems. Although never

*Stejneger, Proc. U. S. Nat. Mus., VII, 1884, p. 76.

completed, this work has received unstinted praise from all competent to estimate it. It is said on excellent authority that no other single work on American birds has made so profound an impression on foreign ornithologists, notwithstanding the fact that circumstances prevented it from being made complete.

Although in his systematic work Professor Baird, like other naturalists, built partly on the scientific foundations laid by his predecessors and contemporaries, always with due acknowledgement, the high value of his work in this direction was largely due to an unerring instinct which enabled him to recognize and confirm the best features of the work of others and by adding material from his own lines of original research to combine the whole into a fabric which was a distinct advance on anything previously offered to the scientific world.

While the bent of his genius led him, in this as in other departments, to devote a main proportion of his work to the systematic biology which was the need of the time, and which, with the exploration and description upon which it is based, must always precede and lay the track for the theoretical biology more in vogue to-day, it must not be supposed that the work of Baird was confined to descriptive and systematic work. With the latter in his publications are combined a host of biographical data such as the field naturalist revels in. One of the earliest and most pregnant papers bearing on mutations of specific forms which have been contributed to the literature of evolution by American biologists is to be found in his article on the "Distribution and Migrations of North American Birds" published in the *American Journal of Science* in 1866.* In this paper, an abstract of a memoir presented to the National Academy of Sciences in 1865, are to be found the germs of much of the admirable work which has since been elaborated by other biologists on the correlation of geographical distribution and the peculiarities of the environment, with the modifications of color, size, and structure in the forms of animal life, called species.

Unlike some of his contemporaries twenty years ago, the views of Darwin excited in him no reaction of mind against the hypotheses then novel and revolutionary. His friendly reception of the new theories was so quiet and undisturbed that, to a novice seeking his

**Am. Jour. Sci. and Arts*, 2nd Series, XII, pp. 78-90, 184-92, 337-47, 1866.

inal. How well this work was done is shown by the fact that, in spite of the changes which are constant in zoölogical classification, nearly all the species still retain the names he applied to them. The descriptions were so carefully prepared that later students have never been troubled in making their identifications.

Notwithstanding his multifarious duties in later years, Professor Baird never lost his interest in these animals, and up to the last afforded every aid and encouragement to those studying them. Much of the work done in this country by such herpetologists as Girard, Kennicott, Hallowell, Cope, and others, found in his example and encouragement the stimulus which made it possible, was built on the foundations which he laid, and owes its publication to agencies which he promoted or controlled.

Fishes.—Professor Baird's contributions to ichthyological literature number some fourteen or fifteen papers, chiefly of a descriptive character, embodying the results of original research into the ichthyology of western and southwestern America and of the marine fishes of New Jersey and New York. Most of these papers were published jointly with Charles Girard.

Besides these, however, he added more than four hundred titles to the list of reviews, notices, reports, translations, and official documents relating to economic ichthyology, fish culture, and the general progress of the science. In this way he was instrumental in bringing together for the use and benefit of the English-speaking public the largest body of facts relating to fish and fisheries ever prepared and digested for such purposes by any individual or organization. Recognized by experts of foreign countries with one accord, as the most eminent living authority on economic ichthyology, America owes to his fostering care and unwearied labor the existence of a whole generation of ichthyologists, breeders of fishes, and inventors of appliances of all sorts for use in connection with the taking, preservation, and increase of these animals. So thoroughly is this understood by all who are in any way acquainted with American fish and fisheries, that to them this statement will appear a truism.

It does not enter into the purpose of this address to enumerate the economic results of the Commission which grew into such stately proportions under his skillful and progressive leadership, nor yet to enumerate the multitudinous researches in pure as well as eco-

advice and opinion amid the clatter of contending voices, it seemed almost as if the main features of the scientific gospel of the new era had existed in the mind of Baird from the very beginning. His thorough apprenticeship in the study of details of structure and their expression in systematic classification, as well as his cautious and judicial habit of mind, prevented him, notwithstanding his hearty recognition of evolutionary processes, from falling into those exuberancies of utterance and hypothesis characteristic of narrowness and immaturity which, within the memory of most of us, have enjoyed a sort of vogue now happily on the decline.

Batrachians and Serpents.—Professor Baird's contributions to herpetology began as early as 1849, his first paper being a revision of the North American tailed batrachians which appeared in the Journal of the Academy of Natural Sciences of Philadelphia. Excluding notices of the work of others in the Annual Record between 1849 and 1880, he published fourteen papers on this branch of science beside nine of which he was the joint author with Charles Girard. His activity in original work in this, as in some other directions, came to an end with the assumption of the burden of administrative work required by the organization and development of the Fish Commission.

Many of his herpetological papers were elaborate studies. One of the most important of the early memoirs was that on the reptiles of Stansbury's expedition to the valley of the Great Salt Lake, and another, that on those collected by the United States exploring expedition under Wilkes. The catalogue of North American Reptiles in the collection of the Smithsonian Institution is a classical work, serving to the present day as a text-book for students of herpetology. In 1859 appeared his great study of the reptiles collected by the parties engaged in the explorations for a Pacific railroad, a monument of patient research and discriminating analysis. After this his contributions to the subject were mostly short papers or announcements of new or interesting facts.

At the time Professor Baird began his studies of the amphibia little had been done for herpetology in America. The classical work of Holbrook contained little more than descriptions of Southern species and the work of Duméril and Bibron was equally meagre. Immense collections were placed in Baird's hands from the Western plains, and the work upon these was necessarily in great part orig-

onomic biology for which this organization has furnished material and means. No more emphatic object-lesson of the vital relations existing between research, as such, and the promotion of the material interests of mankind has ever been furnished to the so-called "practical man" than that afforded by the work of the United States Fish Commission as directed by Professor Baird.

Whether germane to the subject of scientific research or not, the most narrow specialist can hardly grudge an allusion to the grandeur of the methods by which the food supply of a nation was provided, hundreds of rivers stocked with fish, and the very depths of ocean were repopulated. Typically American we may call them in their audacity and their success. The Fishery boards of foreign countries, first quietly indifferent, then loudly incredulous, in due time became interested inquirers and enthusiastic followers. In a few years we may fairly expect to see the food supply of the entire civilized world materially increased, with all the benefits which that implies, and this result will in the main be owing to the unremunerated and devoted exertions of Spencer F. Baird.

THE PERSONAL CHARACTERISTICS OF PROFESSOR BAIRD.

By Mr. J. W. POWELL, President of the Anthropological Society.

Baird was one of the learned men of the world, and, to a degree perhaps unexampled in history, he was the discoverer of the knowledge he possessed. He knew the birds of the air, from the ptarmigan that lives among everlasting snows, to the humming-bird that revels among the orchids of the tropics; he knew the beasts of the forests and the prairies, and the reptiles that crawl through desert sands or slimy marshes; he knew the fishes that scale mountain torrents, that bask in quiet lakes, or that journey from zone to zone through the deep waters of the sea. In all this realm of nature he had a minute and comprehensive knowledge that no other man has ever acquired. What others have recorded in this field of research he knew, and to their discoveries he made a contribution of his own so bounteous, so stupendous, that he is recognized as the master of systematic zoölogists.

All of Baird's scientific work is an illustration of modern inductive or scientific reasoning. The inductions or general principles of modern science are reached by the accumulation of vast stores of facts. He knew how to accumulate facts; how to reject the trivial and select the significant. Modern science is almost buried under the *débris* of observation, the record of facts without meaning, the sands of fact that are ground from the rock of truth by the attrition of mind; but Baird could walk over the sands and see the diamonds. Then he knew how to marshal significant facts into systems, and to weld them into fundamental principles. In all his works there can be discovered no taint of *a priori* reasoning or syllogistic logic; for in his mind there was no room for controversy, and disputation fled before the light of his genius. Formal logic, a disease of modern thought,—the contagion of *Aristotleina*,—never

ravaged his brain. With healthful directness, he sought the truth guided by wise inference, and told the truth in its simplicity.

Baird was an organizer of the agencies of research. When a bold explorer essayed to penetrate the seas of ice by the path of peril and in quest of fame, Baird would ever so manage that a corps of quiet scholars should be attached to the expedition to study the climate of the Arctic zone, the geology of the Arctic rocks, the flora of the Arctic lands, or the fauna of the Arctic fields; and the best knowledge we have of the igloo-dwellers, the Eskimo whose home is on the ice of the North, has been brought to us by the quiet students he succeeded in attaching to Arctic exploring expeditions: and so the love of glory was made to serve the cause of truth.

When, in the interests of international commerce, expeditions were sent to explore and survey routes of travel and transportation across Central America from sea to sea, he managed to send with them corps of scientific men whose function it was to bring from the tropics all forms of its abundant life, vegetal and animal, and the relics of the arts of the people of Central America as they are exhibited in stone and clay and gold; and the National Museum has been enriched by the results of this labor, and the boundaries of human knowledge extended thereby: and so the greed of gain was made to serve the love of truth.

When our army was distributed on the frontiers of the land, he everywhere enlisted our scholarly officers into the service of science and he transformed the military post into a station of research, an Indian campaign into a scientific expedition. Scott, Marcy, McClellan, Thomas, and many other of the great generals of America, were students of natural history and collectors for Baird. When our navy cruised around our shores, its officers were inspired with that love of nature which made every voyage of military duty a voyage of discovery in the realms of natural science; when they journeyed among the islands of the sea they brought back stores of scientific materials, and when they sailed through the littoral waters of other continents they made voyages of scientific investigation. Many of these earlier naturalists of the Navy in subsequent times became commodores and admirals.

But time would fail me to tell of the exploring expeditions and the railroad surveys throughout America, and the travels throughout the world, which he utilized in the interest of science, or of which he was the immediate projector. Of the abundant material

thus gathered from all parts of the world, some has gone to enrich American institutions of learning, and some has been gathered into the National Museum—the outgrowth of Baird's organizing genius and a splendid monument to his memory.

The hills of the land stretch not so far as the billows of the sea; the heights of the mountains are not so great as the depths of the ocean; and so the world was unknown until this greater region was explored. The treasures of the land did not satisfy the desires of Baird; he must also have the treasures of the sea, and so he organized a fish commission, with its great laboratories and vessels of research.

“What hid'st thou in thy treasure-caves and cells,
 Thou hollow-sounding and mysterious main?
 Pale, glistening pearls and rainbow-colored shells,
 Bright things which gleam unreck'd of, and in vain.
 Keep, keep thy riches, melancholy sea!
 We ask not such from thee.”

What the scholar asked of the sea was all its forms of life, its organisms minute and lowly, its crawling articulates, its pearl-housed mollusks, its fishes that swim in armies, and its leviathans that prowl among the waves—the life of the reedy shore, the life of the ocean-current, and the life of the deep sea. So, with many ingenious appliances, he and his lieutenants sailed away to explore the ocean's mystery.

So the Fish Commission was an agency of research; but it was more; he made it an agency by which science is applied to the relief of the wants of mankind, by which a cheap, nutritious, healthful, and luxurious food is to be given to the millions of men. He affirmed that for the production of food an acre of water is more than equal to ten acres of land, thus giving to the gloomy doctrine of Malthus its ultimate refutation, and tearing away the veil of despair from the horizon of the poor; for, when the sea shall serve man with all the food that can be gathered from its broad expanse, the land cannot contain the millions whom it is thus possible to supply.

In the research thus organized the materials for the work of other scientific men were gathered. When a great genius reads to the world a chapter from the book of nature the story is so beautiful that many are stimulated to search in the same field for new chapters of the same story. Thus it was that the publication of

Baird's great works on natural history developed in America a great corps of naturalists, many of whom have become illustrious, and the stimulus of his work was felt throughout Europe. In the research which he organized the materials were furnished for this corps of naturalists; but his agency in the development of this body of workers was even more direct. He incited the men personally to undertake and continuously prosecute their investigations. He enlisted the men himself, he trained them himself, he himself furnished them with the materials and instruments of research, and, best of all, was their guide and great exemplar. Thus it was that the three institutions over which he presided—the Smithsonian Institution, the National Museum, and the Fish Commission—were woven into one great organization—an university of instruction in the methods of scientific research, including in its scope the entire field of biology and anthropology. Such is Baird the investigator, Baird the organizer, and Baird the instructor in the length, breadth, and thickness of his genius, the solidarity of a great man.

All that I have said is a part of the public record; it is found in the great libraries of the world; but, however exalted the feeling of admiration we may entertain for Baird as a scholar and administrator, it is to his attributes as a man, as disclosed in his personal relations with friends, associates, and contemporary men of affairs, that we most fondly turn. It is in these relations that he most clearly exhibited those kindly and modest traits of character which made him so universally beloved.

As a man of affairs, Professor Baird exhibited great sagacity. His plans for the organization of scientific work were of great magnitude, and had they been presented to the administrative officers of the Government or to legislative bodies with exaggeration, or even had they been presented with the glow of an enthusiastic missionary of science, they might well have encountered opposition. But Baird had a wonderful faculty of presenting his plans with extreme modesty, and with a degree of understatement, but suggestion of possibilities which speedily caused him to whom the appeal was made himself to become an advocate of the Professor's measure. He had traits of character in this respect which are hard to explain, and which seem at first to be contradictory. In the advocacy of measures his modesty amounted almost to timidity, and he avoided alike argumentation and ostentation, and he presented his measures with the directness of a child. Notwithstanding all this, there was

such a poise of faculties—such dignity of mien—that he impressed those with whom he came in contact as a venerable and wise patriarch. He seemed devoid of personal interest or feeling, and solicitous only for the welfare of those to whom he was in fact appealing, and he conveyed the impression that he was giving benignant advice. Thus the shrinking, sensitive man, who could not even stand before a public body, such as a committee of Congress or a scientific society and advocate a cause, could, from his seat by the fireside or at the desk, so illumine the subject with which he had to deal that men stood round him to gather his words, that nothing should be lost, for in the exposition of his subject he illumined everything with clear statement, arising from an exhaustive knowledge and full understanding of results.

As the director of the work of research in which other men were engaged, Professor Baird had marvelous insight and skill. The appliances of modern research, alike in the inorganic world and in biology, have come to be multifarious and diverse, and there is this peculiarity about their use: That once used, so that the secret of nature which they were planned to unlock has been revealed, they speedily become obsolete, and immediately new keys, new apparatus, new devices are necessary. Thus to a large extent skill in research is absorbed in the skill necessary for the development of the agencies of research. A continuous line of research, prosecuted by a corps of men so that the boundaries of knowledge are carried far forward, can result only from a continuous line of inventions in the apparatus of research, and it was here that Baird exhibited his skill. His own devices were many and constant, and ever he was fertile in suggestions to his assistants. No wonder, then, that so many of the secrets of nature were unlocked through his agency. It was in the direction of this work of research that the man Baird stood forth as a giant; it was where his vast knowledge of details was most apparent; it was where his marvellous skill was most shown; it was where his insight into human character was most exhibited. With clearness he formulated his interrogatories; with aptness he selected his course of procedure; with judgment he sought the aid of others, and with suggestiveness directed their work. And, lo! his questions were speedily answered. It was in this manner that his own good hands were supplemented by the hands of many, that his own great mind was re-enforced by

the best mental activity of many assistants; and thus the whole body of men under his control worked together as one organic integer for the increase and diffusion of knowledge among men.

In his work with his assistants he scrupulously provided that every one should receive the meed of honor due for successful research and treated all with generosity. Many an investigation begun by himself was turned over to assistants when he found that valuable conclusions could be reached; and these assistants, who were his warm friends, his younger brothers, reaped the reward; and he had more joy over every young man's success than over the triumphs and honors heaped upon himself from every quarter of the globe. He was the sympathetic counsellor of many men; into his ears were poured the sorrows and joys of others, and he mourned with the mourning and rejoiced with the rejoicing. To those in need his hand was ready and his purse was open, and many and many were the poor who called him "blessed." Though a man of great force of character, a man of great learning, a man upon whom had been showered the honors of the scientific world, in character he was as simple as a child. He had a fund of "folk-lore," and loved the books and papers written for children. In his later years, weakened with disease and burdened with many labors, he still read *St. Nicholas* from month to month, and kept the run of every little story, and was glad to be "a child again." His life at home was pure and sweet, and full of joys, for he gave and received love and trust and tender care. But the history of his home life is sacred. Its words and acts abide in the hearts of the wife and the daughter.

For many long months he contemplated the day of parting. Labor that knew no rest, responsibility that was never lifted from his shoulders, too soon brought his life to an end. In the summer of the past year he returned to his work by the seaside, that he might die in its midst. There at Wood's Holl he had created the greatest biologic laboratory of the world; and in that laboratory, with the best results of his life-work all about him, he calmly and philosophically waited for the time of times. Three days before he died he asked to be placed in a chair provided with wheels. On this he was moved around the pier, past the vessels which he had built for research, and through the laboratory, where many men were at work at their biologic investigations. For every one he had a word of good cheer, though he knew it was the last. At the same time,

along the pier and through the laboratory, a little child was wheeled. "We are rivals," he said, "but I think that I am the bigger baby." In this supreme hour he was playing with a child. Then he was carried to his chamber, where he soon became insensible, and remained so until he was no more.

"Blessed are the pure in heart, for they shall see God."



BULLETIN

OF THE

PHILOSOPHICAL SOCIETY OF WASHINGTON.

MATHEMATICAL SECTION.



STANDING RULES

OF THE

MATHEMATICAL SECTION.

1. The object of this Section is the consideration and discussion of papers relating to pure or applied mathematics.

2. The special officers of the Section shall be a Chairman and a Secretary, who shall be elected at the first meeting of the Section in each year, and discharge the duties usually attaching to those offices.

3. To bring a paper regularly before the Section it must be submitted to the Standing Committee on Communications for the stated meetings of the Society, with the statement that it is for the Mathematical Section.

4. Meetings shall be called by the Standing Committee on Communications whenever the extent or importance of the papers submitted and approved appear to justify it.

5. All members of the Philosophical Society who wish to do so may take part in the meetings of this Section.

6. To every member who shall have notified the Secretary of the General Committee of his desire to receive them, announcements of the meetings of the Section shall be sent by mail.

7. The Section shall have power to adopt such rules of procedure as it may find expedient.

LIST OF OFFICERS AND MEMBERS
OF THE
MATHEMATICAL SECTION OF THE PHILOSOPHICAL
SOCIETY FOR THE YEAR 1887.

Chairman, WM. B. TAYLOR. *Secretary*, R. S. WOODWARD.

ABBE, C.	HAZEN, H. A.
AVERY, R. S.	HILL, G. W.
BAKER, M.	HODGKINS, H. L.
BATES, H. H.	KING, A. F. A.
BILLINGS, J. S.	KUMMELL, C. H.
BURGESS, E. S.	MARTIN, A.
CHRISTIE, A. S.	MARVIN, C. F.
COFFIN, J. H. C.	MCADIE, A. G.
CURTIS, G. E.	MCGEE, W. J.
DELAND, T. L.	NEWCOMB, S.
DOOLITTLE, M. H.	PAUL, H. M.
DUTTON, C. E.	RITTER, W. F. M'K.
EASTMAN, J. R.	ROBINSON, T.
EIMBECK, W.	RUSSELL, T.
ELLIOTT, E. B.	SMILEY, C. W.
FARQUHAR, H.	STONE, O.
FLINT, A. S.	TAYLOR, W. B.
GILBERT, G. K.	UPTON, W. W.
GORE, J. H.	WILSON, H. C.
GREEN, B. R.	WINLOCK, W. C.
HALL, A.	WOODWARD, R. S.
HARKNESS, W.	ZIWET, ALEX.

BULLETIN
OF THE
MATHEMATICAL SECTION.

24TH MEETING.

FEBRUARY 16, 1887.

The Chairman, Mr. WM. B. TAYLOR, presided.

Present, eighteen members and one guest.

The Section proceeded to the election of officers for 1887 by appointing a Nominating Committee consisting of Messrs. FARQUHAR, BAKER, and HILL.

The Committee nominated Mr. WM. B. TAYLOR for Chairman and Mr. R. S. WOODWARD for Secretary; these nominees were elected by acclamation.

Mr. M. H. DOOLITTLE read a paper on

ASSOCIATION RATIOS.

[Abstract.]

The present communication is an effort in the direction of a science of statistics. It includes the principles involved in my communication* of December 3, 1884, but presents them in a more general manner.

Suppose that there are s occasions on which the presence or absence of the phenomena A and B are determined by observation. Suppose that there are a instances of the occurrence of A, and b instances of the occurrence of B, each including c instances in which A is associated with B. There remain $s - a - b + c$ instances in which A and B are both absent. If $a = b = c$, the two phenomena are always found associated, and the association may be regarded as perfect. If either A or B is ever found alone, the association is

* The verification of predictions. See Bulletin of Phil. Soc. for 1884, vol. 8, pp. 122-127.

imperfect. I assume that the extent of association is a quantity capable of numerical expression, and further assume it $= \frac{c^2}{ab}$. This is tantamount to the assumption that whenever either of the ratios $\frac{c}{a}$ or $\frac{c}{b}$ is constant, the extent of association varies directly as the other ratio, and $= 1$ when they each $= 1$.

Not-A and Not-B may also be regarded as phenomena whose presence is equivalent to the absence of A and B and *vice versa*. Not-A, therefore, occurs $s - a$ times; and Not-B $s - b$ times. The following table will hardly need further explanation:

Phenomena.	Both occur.	Neither occurs.	Extent of association.
A and B	c	$s - a - b + c$	$\frac{c^2}{ab}$
A and Not-B	$a - c$	$b - c$	$\frac{(a - c)^2}{a(s - b)}$
Not-A and B	$b - c$	$a - c$	$\frac{(b - c)^2}{(s - a)b}$
Not-A and Not-B	$s - a - b + c$	c	$\frac{(s - a - b + c)^2}{(s - a)(s - b)}$

For illustration, let blindness and deafness be the phenomena denoted respectively by A and B. Then the extent of association between blindness and deafness $= \frac{c^2}{ab}$; that between sight and deafness $= \frac{(b - c)^2}{(s - a)b}$, &c.

I call the above expressions for extent of association *indiscriminate association ratios*. It is important now to understand that the magnitude of each is determined both by general and special causes. In an ordinary community the indiscriminate association ratio between sight and hearing is very large, nearly $= 1$, for the general reason that most people can see whether they can hear or not, and most people can hear whether they can see or not. If there is a special reason why a larger proportion of men able to see than of blind men shall be able to hear, this special reason will tend to increase the indiscriminate association ratio, and a contrary special reason will tend to diminish it.

I now seek to obtain a *discriminate association ratio*, whose magnitude shall be affected by special causes only, and which may

therefore serve as a measure of their efficiency. The general problem may be stated as follows: Having given the number of instances respectively in which things are both thus and so, in which they are thus but not so, in which they are so but not thus, and in which they are neither thus nor so, it is required to eliminate the general quantitative relativity inhering in the mere thingness of the things, and to determine the special quantitative relativity subsisting between the thusness and the so-ness of the things.

If no special causes are in operation, the number of instances in which both A and B occur should be $= \frac{ab}{s}$ according to the general theory of probabilities. The operation of such causes is therefore indicated by a difference between the values of c and $\frac{ab}{s}$. Now, instead of the ratio $\frac{c}{a}$, which varies directly as c , let us form a ratio which shall vary directly as $c - \frac{ab}{s}$ and which shall $= 1$ when $c = a$. These conditions give us the ratio

$$\frac{c - \frac{ab}{s}}{a - \frac{ab}{s}} \text{ or } \frac{cs - ab}{a(s - b)}$$

In like manner, instead of the ratio $\frac{c}{b}$ we have $\frac{cs - ab}{b(s - a)}$. Now, assuming that whenever either of these derivative ratios is constant, the required discriminate association ratio varies directly as the other ratio varies, and that it equals unity when they each equal unity, it is found equal to their product $= \frac{(cs - ab)^2}{ab(s - a)(s - b)}$.

For the phenomena A and Not-B the number of concurrences probable from general causes $= \frac{a(s - b)}{s}$; and subtracting this quantity from $a - c$, from a , and from $s - b$, the indiscriminate association ratio $\frac{(a - c)^2}{a(s - b)}$ becomes $\frac{(ab - cs)^2}{ab(s - a)(s - b)}$, which differs from the discriminate association ratio for A and B merely in the algebraic sign of the quantity under the exponent. This is as it should be. Sight is precisely as favorable or unfavorable to hear-

ing as it is unfavorable or favorable to deafness. In like manner the same discriminate association ratio is obtained for the phenomena Not-A and B, and for Not-A and Not-B. The logical relation between sight and hearing is just as close as that between sight and deafness, as that between blindness and hearing, and as that between blindness and deafness. It is in fact the same relation stated in different words.

The sum of the four indiscriminate association ratios is

$$\frac{c^2}{ab} + \frac{(a-c)^2}{a(s-b)} + \frac{(b-c)^2}{(s-a)b} + \frac{(s-a-b+c)^2}{(s-a)(s-b)} = 1 + \frac{(cs-ab)^2}{ab(s-a)(s-b)}$$

Hence the discriminate association ratio = the sum of the indiscriminate association ratios - 1. Since every instance of A or of Not-A is necessarily associated with an instance of B or of Not-B and every instance of B or of Not-B is necessarily associated with an instance of A or of Not-A, this alternative association is perfect, and its extent = 1 whatever A and B may denote. The excess of the sum of the indiscriminate association ratios above unity may, therefore, be taken as a measure of that portion of the aggregate which is peculiar to any special signification of A and B. Such association as belongs necessarily to any two classes of phenomena whatever having been eliminated, the discriminate association ratio measures that residue which indicates special relations.

I call $c - \frac{ab}{s}$ the *concurrence residual*. If c is less than $\frac{ab}{s}$, the concurrence residual is negative and indicates that special causes prevent oftener than they produce positive association between A and B. If $c = 0$ and $a = s - b$, the negative association (or dissociation) is perfect, and the discriminate association ratio = 1. These conditions signify that the two phenomena are never both present and are never both absent.

Denoting the discriminate association ratio by y , the concurrence residual by x , and the class residuals $a - \frac{ab}{s}$ and $b - \frac{ab}{s}$ respectively by α and β , we have the equation

$$y = \frac{x^2}{\alpha\beta};$$

and regarding x and y as variables and α and β as constants this equation is represented in Cartesian co-ordinates by a parabola.

The value of the discriminate association ratio is not affected by interchange of a and b . It is assumed that association and reciprocal association are equal.

The concurrence residual is significant in proportion to its square; and this is in accordance with the general comparative importance of residuals in the theory of least squares.

When s is infinite, with a , b , and c each finite, the discriminate association ratio reduces to the indiscriminate $\frac{c^2}{ab}$. In this case the chances are as infinity to one against fortuitous concurrence; and the extent of association must be regarded as based wholly on special relations.

This paper was briefly discussed by Messrs. GILBERT, H. FARQUHAR, BAKER, and the author.

25TH MEETING.

MARCH 2, 1887.

The Chairman presided.

Present, twenty-one members and two guests.

A symposium was held on the following problem in probabilities:

ONE-THIRD OF THE APPLES ON A TREE ARE ROTTEN AND ONE-FOURTH ARE WORMY, WHAT IS THE PROBABILITY THAT AN APPLE TAKEN AT RANDOM FROM THE TREE WILL BE (1) ROTTEN ONLY; (2) WORMY ONLY; (3) BOTH ROTTEN AND WORMY; AND (4) SOUND?

The discussion was begun by Mr. M. BAKER who gave an analytical statement of the conditions of the problem and concluded that the problem was an indeterminate one until some assumptions were introduced. Without introducing anything additional to that stated he concluded that the four probabilities were respectively

$$p_1 = \frac{3}{4} - \frac{d}{s}; \quad p_2 = \frac{2}{3} - \frac{d}{s}; \quad p_3 = \frac{d}{s} - \frac{5}{12}; \quad p_4 = \frac{d}{s};$$

where d = the number of sound apples and s the total number of apples.

Mr. DOOLITTLE, proceeding on the hypothesis that the problem is indeterminate, gave an infinite series of possible values for the respective probabilities. But he thought the problem should be understood as determinate, and assigned $\frac{1}{2}$ as the proper value for the third probability.

Mr. HILL expressed the opinion that the probability $\frac{1}{2}$ for a rotten and wormy apple is the proper value, but gave a solution of the problem by means of double integrals which brought out a different result.

Messrs. CURTIS, ELLIOTT, and FARQUHAR gave different solutions leading to $\frac{1}{2}$ for the third probability.

Mr. FARQUHAR objected to the result $\frac{1}{2}$ as involving the absurdity that if one-fourth are wormy the probability of the combination is exactly the same for all values of the rotten between $\frac{1}{4}$ and $\frac{3}{4}$; and also further objected to calling a probability "indeterminate" because it was not a certainty.

Mr. MARTIN gave a brief history of the problem, which appeared originally in his *Mathematical Visitor*,* and of which he gave three solutions leading to $\frac{1}{2}$ for the third probability. He stated that the correctness of his solution depended on the correctness of the view that all possible values of any one of the probabilities are equally probable.

The subject was further discussed by Messrs. GILBERT, CHRISTIE, and WOODWARD.

Mr. HILL also read a letter from Prof. A. HALL relating to the problem.

The discussion was closed with some remarks by the Chairman on the language of the problem and its proper interpretation.

*The *Mathematical Visitor*; edited and published by A. Martin. 4^o. Erie, Pa. 1881. Vol. 1, No. 4, January, 1880, p. 115, problem 180; solutions pp. 180-181.

26TH MEETING.

MARCH 16, 1887.

The Chairman presided.

Present, sixteen members.

Mr. CHRISTIE read a paper on

A PROBLEM IN PROBABILITIES.

In this paper he reviewed the conditions of the question in probabilities discussed at the previous meeting. He considered it a question susceptible of a definite answer, dependent only on a logical and mandatory application of the elementary principles of probability. In his analysis he derived expressions for the possible combinations of the several events and deduced therefrom a function representing the probability of the compound event (rotteness and worminess), the variable in this function being the probability sought. The value of the variable making the function a maximum was taken as the required probability, the result being $\frac{1}{1\frac{1}{2}}$.

If n = total number of apples, r = number rotten, w = number wormy, x = number both rotten and wormy, then

$$\frac{(r+1)(w+1)}{n+2} > x > \frac{(r+1)(w+1)}{n+2} - 1, \text{ or } x' > x > x'',$$

and the chance of a particular apple being both rotten and wormy is $\frac{x}{n}$. When x' and x'' are integral the chance is *either* $\frac{x'}{n}$ *or* $\frac{x''}{n}$, that

is $\frac{x'+x''}{2n}$. When n, r, w are all infinite, the case of continuous

number, this chance is $\frac{rw}{n^2}$.

Mr. STONE took the ground that the problem is susceptible of but one interpretation, and gave a geometric solution leading to $\frac{1}{1\frac{1}{2}}$ for the probability of the compound event. He also gave some instances of allied questions in dependent probabilities.

An animated discussion, extending over the remaining time of the meeting, then followed. Of those who participated in the discussion, Messrs. CHRISTIE, CURTIS, DOOLITTLE, ELLIOTT, HILL, KUMMELL, STONE and ZIWET considered the problem determinate, while Messrs. BAKER, HARKNESS, and WOODWARD considered it indeterminate.

27TH MEETING.

MARCH 30, 1887.

The Chairman presided.

Present, twelve members and two guests.

Mr. R. S. WOODWARD read a paper on

THE FREE COOLING OF A HOMOGENEOUS SPHERE INITIALLY
HEATED TO A UNIFORM TEMPERATURE.

[This paper appeared in full in the *Annals of Mathematics*. 4°. Charlottesville, Va. 1887, June; vol. 3, no. 3, pp. 75-88. Also separately printed.]

Remarks were made on this paper by Messrs. KUMMELL, HILL, and the Chairman.

Mr. KUMMELL read a paper on

THE BRACHISTHODE ON THE HELICOID.

[Abstract.]

The characteristics of this class of curves and the methods of computing their lengths in the several cases were explained and discussed. Accurately constructed stereoscopic diagrams of several of these curves were exhibited.

[This paper is expected to appear in the *Mathematical Visitor*.]

28TH MEETING.

APRIL 13, 1887

The Chairman presided.

Present, nineteen members and one guest.

Mr. G. W. HILL read a paper on

THE MOTION OF HYPERION.

Although designed to meet the special case presented by Hyperion, Mr. HILL's paper treated the general problem of three bodies under the restrictions that they are all nearly in the same plane and that

the mass of the one whose motion is sought is negligible in comparison with the masses of the other two. The potential function for the disturbed body was put in a general form for the purpose of ascertaining the most advantageous variables for its development, and some of the particular forms were derived and discussed. Mr. HILL also indicated the methods which might be most advantageously followed in the application of his theory to Hyperion.

This paper was discussed by Mr. A. HALL, who alluded to the unique character of the motion of Hyperion, and stated some of the more interesting facts concerning the observations of this satellite and the failure of the theories thus far advanced to represent its motion.

Other remarks were made by the Chairman and Mr. WOODWARD.

[This paper appeared in full in the *Annals of Mathematics*. 4^o. Charlottesville, Va. 1887, June; vol. 3, no. 3, pp. 65-73. Also separately printed.]

Mr. A. HALL presented a paper on

THE PARALLAX OF α TAURI.

He gave a historical account of the early attempts at the determination of stellar parallax together with some of the results attained. He exhibited in tabular form the principal data on which his value for the parallax of α Tauri depends. In contrasting his result with the larger value for the same star determined by STRUVE he stated that his values for parallax are generally smaller than those of other observers.

The brief discussion which followed was participated in by Messrs. EASTMAN, PAUL, and others.

29TH MEETING.

APRIL 27, 1887.

The Chairman presided.

Present, thirteen members.

Mr. A. S. FLINT read a paper on

THE MOST PROBABLE VALUE OF THE LATITUDE AND ITS THEORETICAL WEIGHT FROM ENTANGLED OBSERVATIONS OCCURRING IN THE USE OF TALCOTT'S METHOD.

In this paper Mr. FLINT showed first how to express the weighted

mean value of the latitude and its weight in the most general case of entanglement in terms of the results from individual pairs of stars and their symbolical weights. To find the numerical values of these symbolical weights he made use of the principle that the weights of the individual results must be such as to make the probable error of the weighted mean a minimum. After treating the most general case he considered some of the special cases occurring most commonly, and deduced practical formulas for computing the weights of individual results. In illustration of his methods he gave the details of the numerical operations in one of the more complex cases presented in actual work.

In the discussion which followed, Mr. HARKNESS derived, by a different and less complex process, some of the formulas given by Mr. FLINT. Others participating in the discussion were Messrs. PAUL, FARQUHAR, STONE, and WOODWARD.

Mr. E. B. ELLIOTT began the presentation of a paper on

THE MUTUAL ACTION OF ELEMENTS OF ELECTRIC CURRENTS.

30TH MEETING.

MAY 11, 1887.

The Chairman presided.

Present, ten members and two guests.

Mr. E. B. ELLIOTT continued his paper on

THE MUTUAL ACTION OF ELEMENTS OF ELECTRIC CURRENTS.

He stated that Ampère's theory of such currents involves the assumption that the action between the elements is limited in direction to the line joining them. In conformity with this assumption the result reached by Ampère, and now usually given in text books, is that the action is proportional to

$$\frac{1}{2} \cos \theta \cos \theta' - \sin \theta \sin \theta' \cos \omega,$$

in which θ and θ' are respectively the angles between the directions of the elements and the line joining them, and ω is the angle between the two planes defined by the directions of the elements and the line joining them.

In his own investigation Mr. ELLIOTT makes no assumption or restriction with reference to the direction of the action of the elements and finds the action proportional to the following expression :

$$\begin{aligned}
 (\cos \theta + \sin \theta . i) (\cos \theta' + \sin \theta' \cos \omega . i + \sin \theta' \sin \omega . j) = \\
 \cos \theta \cos \theta' - \sin \theta \sin \theta' \cos \omega \\
 + (\sin \theta \cos \theta' + \cos \theta \sin \theta' \cos \omega) i \\
 + \cos \theta \sin \theta' \sin \omega . j \\
 + \sin \theta \sin \theta' \sin \omega . i j.
 \end{aligned}$$

In this expression θ , θ' and ω have the same signification as stated above, and i, j and ij (or its equivalent k) are quadrantal versors. The first term of this formula represents action in the line joining the elements; the second term represents action in the plane of the connecting line and one of the elements and perpendicular to the connecting line; the third term represents action in a direction at right angles to the plane just mentioned; and the fourth term represents torsion in a plane perpendicular to the connecting line. The actions resulting in some special cases, as when the elements lie in one plane, etc., were explained and discussed.

[This paper was presented to the American Association for the Advancement of Science at its New York meeting, August, 1887, and appeared in the *Electrical World*; a weekly review, etc. fol. New York, 1887, August 27; vol. 10, no. 9, p. 116. Also separately printed.]

Mr. HILL, following Maxwell, gave some of the principal steps in the process which leads to Ampère's result, indicating that that process differs from Mr. ELLIOTT's in leaving out of account certain couples and in assuming a certain undetermined quantity to be zero.

The paper was further discussed by Mr. HARKNESS, the Chairman, and others.

Mr. DOOLITTLE began the presentation of a paper on

ASSOCIATION RATIOS.

31ST MEETING.

MAY 25, 1887.

The Chairman presided.

Present, sixteen members and one guest.

Mr. M. H. DOOLITTLE continued his paper on

ASSOCIATION RATIOS,

which consisted chiefly in a review and criticism of an article* by Mr. G. K. GILBERT on Finley's Tornado Predictions. The following is an abstract of Mr. DOOLITTLE's paper :

By Mr. GILBERT's notation :

 s = whole number of predictions. p = number of positive predictions. o = number of occurrences. c = number of verifications of positive predictions. $p' = s - p$ = number of negative predictions. $o' = s - o$ = number of non-occurrences. $o - c$ = "measure of the failure in inclusion." $p - c$ = "measure of the failure in exclusion."

We should also have for consistency

 c = measure of success in inclusion. $c' = s - o - p + c$ = measure of success in exclusion.

He says, "If inclusion and exclusion are equally important their measures bear the same weights." This is as true for success as for failure, but Mr. GILBERT gives to the measure of success in exclusion no weight whatever, and entirely disregards it.

He has

 $o + p - 2c$ = measure of the general failure of prediction.

We should also have

 $s - o - p + 2c$ = measure of the general success in prediction.

The latter measure consists of the "favorable cases;" the former

* American Meteorological Journal. 8°. Detroit, Mich., 1884, September; vol. 1, no. 5, pp. 166-172.

of the "unfavorable;" and the "ratio of verification (the favorable cases divided by the sum of the favorable and unfavorable," becomes

$$v = \frac{s - o - p + 2c}{s} = \frac{c + c'}{s}.$$

And this is Mr. FINLEY'S method of computation.

Mr. GILBERT then employs a process to which he gives no name, but which may be called the elimination of hypothetical chance.

He estimates that $\frac{op}{s}$ verifications of positive predictions might have been expected if the same number of positive predictions had been made at random, and sets these cases aside as proving neither discrimination nor want of it. In effect, he subtracts $\frac{op}{s}$ from each of the quantities o , p , and c , and proceeds with the residuals. This portion of his reasoning is regarded as sound, and the process may be applied with great utility to properly formed ratios.

The ratio v is

$$\frac{c + c'}{s} = \frac{c + c'}{p + p'}.$$

To eliminate hypothetical chance, $\frac{op}{s}$ should be subtracted from each of the quantities c and p , and $\frac{o'p'}{s}$ from c' and p' . Denoting the result by i ,

$$i = \frac{c - \frac{op}{s} + c' - \frac{o'p'}{s}}{p - \frac{op}{s} + p' - \frac{o'p'}{s}} = \frac{2(cs - op)}{p(s - o) + o(s - p)}.$$

When

$$p = 100, o = 51, c = 28, s = 2803;$$

then

$$p' = 2703, o' = 2752, c' = 2680;$$

and

$$i = \frac{26 \cdot 18 + 26 \cdot 18}{98 \cdot 18 + 49 \cdot 18} = 0.355.$$

The above formula, like many others, successfully passes all the tests which Mr. Gilbert devised for his own formula, but it fails

under others, and it is not maintained that it has any scientific value.

Mr. Gilbert says that he hopes "to show that Mr. Finley's method involves a serious fallacy. This fallacy consists in the assumption that verifications of a rare event may be classed with verifications of the predictions of frequent events without any system of weighting." It is not perceived that Mr. Gilbert has furnished any such system. The fallacy, perhaps, consists rather in the supposition that any valuable result can be obtained by averaging the percentages of verification of heterogeneous classes of predictions. Mr. Finley correctly computed his indiscriminate percentage of verification, and thereby furnished a striking and, perhaps, much-needed illustration of the worthlessness of such computations. The elimination of hypothetical chance from such mixed percentages merely renders their worthlessness less apparent.

This paper was briefly discussed by Messrs. CURTIS, FARQUHAR HILL, BAKER, and WOODWARD.

Mr. H. FARQUHAR presented a solution and generalization of a problem, proposed in *Science*,* requiring the division of a rectangle, by a single step-cut, into two parts which when put together will form a square.

Mr. MARCUS BAKER presented a communication on

A COLLECTION OF SOLUTIONS OF THE TRISECTION PROBLEM.

[Abstract.]

The communication consisted of an informal statement from notes and memoranda of progress in the direction of an exhaustive collection of real solutions of the problem to trisect an angle. It was pointed out that, though the problem was a very old and very famous one, energy is constantly wasted in its study by those ignorant of what has been done, and that this misdirected energy might, in large part, be due to the want of any satisfactory digest of results hitherto attained. The author had himself felt the need of such a digest, and, finding none, had some years ago begun a collection of

* See *Science*. 4°. New York, 1887, May 20; vol. 9, no. 224, p. 488, query 5.

notes and memoranda, with a view to the preparation of a fairly complete collection of solutions of the problem and the preparation of a bibliography.

Progress in the work had been slow, and the results are still very incomplete, especially the bibliographic part, which was deemed the most important.

The present collection of notes contained about a dozen different solutions of the problem and a suggested classification for a digest of the subject as follows:

1. Historical Introduction.
2. Trisection by the conic sections.
3. Trisection by special or higher curves.
4. Trisection by mechanical devices.
5. Trisection by approximation.
6. False trisections.
7. Bibliography.

Of the trisections by the conic sections five were enumerated, viz:

1. By parabola and circle.
2. By parabola and parabola.
3. By parabola and hyperbola.
4. By the equilateral hyperbola.
5. By the hyperbola, whose asymptotes form an angle of 120° .

Trisections by the following curves were also enumerated:

1. Conchoid of Nicomedes.
2. Conchoid on circular base = trisectrix = planetary curve of Ptolemy = special case of limaçon of Pascal.
3. Cycloid.
4. Epicycloid or trochoid.
5. Quadratrix of Dinostratus or Hippias of Elis.
6. Quadratrix of Tschirnhausen.
7. Spiral of Archimedes.

Respecting the cissoid of Diocles, it was remarked that no solution of the trisection problem, by its aid, had been found. Also respecting the cycloid, which Sir Isaac Newton is said to state may be used to trisect an angle, no solution by means of it had been found, but the author had himself made one recently.

Of the various mechanical devices used for trisection the linkage of Thomas of Ceva was given, others being referred to only.

Of false trisections, the number was stated to be very large and of unequal value, some giving close approximations and others failing ignominiously. Finally, in the bibliography, now containing some fifty references, and believed to be only the beginning of a reasonably full list, it was proposed to make an authors' catalogue of entries, and to follow each reference with a very brief characterization of the contents of the article.

The foregoing scheme had been laid out but latterly had made no progress, and the opinion of the section was sought as to the desirability or advisability of carrying the work on.

Mr. CURTIS made the following remarks:

Six or eight years ago I began a similar collection of trisection methods, in looking over which I find a number of solutions additional to those presented by Mr. BAKER.

The following six belong to the class in which an angle is trisected by means of curves:

$$(1) \quad y^3 + x^2y - axy + bx^2 = 0;$$

the ophiuride of Dietrich Uhlhorn (1764-1837).

$$(2) \quad x^2 = \frac{(2a^2 - y^2)^2}{4a^2 - y^2};$$

the polyode of Dr. Wm. Hillhouse,* Prof. J. W. Nicholson,† J. Bruen Miller.‡

$$(3) \quad 4x^2 + 12y^2 = (\sqrt{1-x^2} + y)^4 - 8y\sqrt{1-x^2} + 4.$$

Dr. Wm. Hillhouse.

(4) [Curve drawn, but equation not given.]

Ibid.

*The Analyst; edited and published by J. E. Hendricks. 8°. Des Moines, Iowa. 1882, November, vol. 9, no. 6, pp. 181-184. See also same, 1876, September, vol. 3, no. 5, p. 151.

†*Same.* 1883, March, vol. 10, no. 2, pp. 41-43. See also The Multisector and Polyode. By Prof. J. W. Nicholson, M. A., Professor of Mathematics. Louisiana State University. 8°. New Orleans; published at the Times-Democrat. 14 pp.

‡Van Nostrand's Engineering Magazine. 8°. New York, D. Van Nostrand, 1880, March, vol. 22, no. 135, pp. 206-209.

$$(5) \frac{x^2}{x^2 + \left(\sqrt{1-4x^2} + \frac{\sqrt{3}}{2} - y \right)^2} + \left(\frac{\sqrt{3}}{2} - y + \frac{\sqrt{1-4x^2}}{2} \right)^2 = 1$$

Ibid.

$$(6) \quad x^2 + (3y - 4y^3)^2 = r^2$$

Ibid.

Dr. William Hillhouse, of New Haven, has not only shown that the last five curves may be used for trisecting an angle, but has devised instruments for describing them. This latter step, as I view the problem of trisection, is a necessary part of any real solution by means of curves. The simple determination of the equations that will satisfy the analytical conditions of trisection, without the instrumental means for describing the curves, does not constitute a solution of the problem. It is essentially something to be *done*, not something merely to be proved, and its fame arises from the impossibility of making the trisection of an angle by means of a ruler and pair of compasses. Any proposed solution, therefore, must indicate a geometrical instrument for accomplishing it, and the nature of the motion applied therein determines the character of the solution.

A class of solutions, regarded the most elegant of all, is that in which link machines trisect the angle directly, without the aid of interposed curves. Of this class I have found three instruments, invented respectively by the Marquis de l'Hôpital (1661-1704), A. B. Kempe, and Professor Sylvester. That of l'Hôpital is a combination of link and sliding motion; those of Kempe and Sylvester are pure linkages. With respect to the two latter, I wish to call attention to the elementary character of the solution. Euclid's postulates require us to be able to draw a straight line and a circle, and it is frequently assumed that they imply the use of a straight-edge and a pair of compasses. But, manifestly, any other instruments that can describe the circle and the straight line satisfy equally the requirements of the postulates. Moreover, the use of a straight edge assumes as accomplished the very thing proposed to be done; whence the straight-edge is not an original instrument for describing a straight line. Such an instrument is given by the linkage of Peaucellier. More originally, therefore, than by the straight-edge, the postulates of Euclid may be assumed to imply the use of pure link motion. Wherefore, if pure link motion be considered as postulated by Euclidian geometry, the trisection of an angle becomes one of the simplest of geometrical problems.

Mr. KUMMELL remarked that the supposed analogy between the duplication of a cube and the trisection of an angle does not exist, since the latter requires a cubic with three real roots, while the former requires a cubic having one real and two imaginary roots.

The subject was further discussed briefly by the Chairman and Mr. BATES.

32D MEETING.

OCTOBER 19, 1887.

The Chairman presided.

Present, sixteen members and one guest.

Mr. G. W. HILL read a paper on

THE INTEGRATION OF DIFFERENTIAL EQUATIONS ADMITTING PERIODIC INTEGRALS.

[Abstract.]

The independent variable being conceived as time, a system of ordinary differential equations may be said to admit periodic integrals when the values of the dependent variables, either exactly or with an approximate tendency, after a certain lapse of time, repeat their series of values. In the latter case the longer the lapse is made the more nearly is the repetition brought about. Strange as it may seem, this subject, except in the case of simply periodic integrals, is, at present, not completely understood. The text-books on differential equations are almost wholly engaged with the cases, which, by certain artifices, can be integrated in finite terms or reduced to quadratures. In the treatment of physical problems, however, we seldom meet with equations of this class. Far more frequently it is found that methods of approximation must be resorted to. Cauchy appears to be the author who has done the most for the elucidation of this part of the subject. His memoirs are in his later *Exercises* and in the volumes of the *Comptes Rendus* for 1856 and 1857.

In this paper the mode in which simply periodic integrals arise was discussed, and the theory afterwards illustrated by treating the following problem:

Find the conditions of motion of any number of material points mov-

ing about a centre under the action of central forces whose potential is a function of the sum of the squares of the radii vectores.

The differential equations of this problem, in the case where the radii are supposed to describe no areas, were first integrated by Binet.* But the addition to the forces of the terms arising from centrifugal action much enhances the interest of the problem.

The chief point of interest brought out by the solution was that while the directions of the points, whether as seen from the centre or from each other, all return to the same values after the lapse of a certain time, as do also the ratios of the radii vectores, the absolute values of the latter have all a factor whose period is generally different from the former. Thus the movement of the system may be conceived as taking place under the operation of two distinct causes, viz: the *first* producing a revolution of all the points about the centre in closed curves in the same time, while the *second*, having a different period, changes the scale of representation of the system in space.

[This paper appeared in full in the Annals of Mathematics. 4°. Charlottesville, Va. 1887, October; vol. 3, no. 5, pp. 145-153.]

Mr. HILL's paper was briefly discussed by Mr. A. HALL and the Chairman.

Mr. A. HALL read a paper on

EULER'S THEOREM (GENERALLY CALLED LAMBERT'S).

[Abstract.]

This theorem is well known to astronomers and is very useful in computing the orbits of comets. The time of the passage of the comet from one point to another of its orbit is expressed by means of the two radii vectores drawn to the points, and the chord joining these points. For many years, and by many writers even of the present time, this theorem is attributed to Lambert. Mr. HALL stated that it was first given by Euler about 1743. He gives two proofs for the parabola, and then extends the theorem to the ellipse. For this case Euler gives first an expression for the perihelion distance in terms of the sum of the two radii vectores and the chord. He then gives an approximate expression for the time of describing the arc in terms of the perihelion distance, the radii

* Journal de mathématiques; par J. Liouville. 4°. Paris, 1837. 1st series, vol. 2, p. 457.

vectores and the eccentricity of the ellipse, and directs us to substitute the value of the perihelion distance. Euler does not, therefore, give an explicit expression for the time in terms of the radii vectores and the chord, although he points out how this may be done. Considering the results that he obtained, Mr. HALL thinks that this theorem, with respect to all the conic sections, should be known by the name of *Euler*.

Remarks on this communication were made by Messrs. HILL, STONE, and WINLOCK.

33D MEETING.

NOVEMBER 2, 1887.

The Chairman presided.

Present, fifteen members and one guest.

Mr. E. B. ELLIOTT gave a brief description of a new form of computing machine, which prints and arranges in the usual form for addition any series of numbers and then prints their sum, the work of the operator being merely mechanical as in the use of the typewriter. Although designed especially for performing and printing work in addition, the machine may also be used for multiplication and division.

Mr. WM. HARKNESS presented a paper on

THE CONSTANT P IN OBSERVATIONS OF TERRESTRIAL MAGNETISM.

It was explained that this paper arose from a correspondence in *Nature* concerning the modes of computing the constant. In a letter published in the number of that journal for August 18th, 1887, Mr. HARKNESS referred to an expression for P given in Stewart and Gee's Practical Physics, and suggested a more convenient form for logarithmic computation. In the number for September 8th, Mr. William Ellis gave another but somewhat less accurate expression for the computation of P ; and in the number for September 29th, Prof. Arthur W. Rücker gave what he considered a more accurate expression than either of the others.

Starting from the fundamental equations of Gauss, Mr. HARKNESS derived a formula for P correct to terms of the second order inclusive. He then showed that Rücker's formula, which pur-

ported to give terms of the second order, was incorrect, and pointed out that the error in Rucker's process consisted in expanding to terms of the second order an expression which included only terms of the first order.

This paper was briefly discussed by Messrs. HALL, ABBE, KUMMELL, and HARKNESS.

This and other related papers appeared in *Nature*.*

Mr. R. S. WOODWARD read a paper on

THE CONDITIONED COOLING OF A HOMOGENEOUS SPHERE.

The salient features only of this paper were presented. The fundamental assumptions and analytical conditions of the problem were indicated, and especial attention was directed to the distinction between the case of "conditioned cooling" and that of "free cooling," which latter was discussed by the author, at the 27th meeting of the section. It was shown that the solution for the more complex case of "conditioned cooling" is derivable by a comparatively simple process from the solution for "free cooling." The probable discrepancy between the data presented by the earth as a cooling sphere and those assumed in the solution of the problem, and the additional data requisite for a more complete solution were pointed out.

The presentation of the paper was followed by an informal discussion participated in by nearly all present. This discussion referred chiefly to the physical features of the earth as a cooling sphere, and served to disclose a diversity of opinion concerning the conductive and convective properties of such large masses.

[This paper appeared in full in the *Annals of Mathematics*. 4°. Charlottesville, Va. 1887, October; vol. 3, no. 5, pp. 129-144.]

* *Nature*, a weekly illustrated journal of science. 4°. London, 1887-1888. 1887, Aug. 18, vol. 36, no. 929, p. 366. On the constant P ; by Wm. Harkness.

Sept. 8, vol. 36, no. 932, p. 436. Same; by Wm. Ellis.

Sept. 29, vol. 36, no. 935, p. 508. Same; by A. W. Rucker.

Dec. 8, vol. 37, no. 945, pp. 127-128. Same; by Harkness and rejoinder by Rucker.

1888, Jan. 19, vol. 37, no. 951, pp. 272-273. Same; by Harkness and rejoinder by Rucker.

34TH MEETING.

NOVEMBER 16, 1887.

The Chairman presided.

Present, ten members.

Mr. ORMOND STONE read a paper on

THE ORBIT OF HYPERION.

[Abstract.]

The principal difficulty in the integration of the equations of motion in the case of the problem of three bodies arises in the integration of terms involving the inverse powers of the distances between the disturbed and disturbing bodies. When the ratio between the radius vectors is not too near unity, the inverse powers referred to can be developed in rapidly converging series in terms of cosines of multiples of the elongation. When, however, these ratios do not differ greatly from unity the convergence of the series mentioned is very slow. If, in addition, the mean motions of the two bodies are nearly commensurate, the ordinary methods of solving the problem become inapplicable.

Such a case presents itself in the determination of the perturbations of Hyperion produced by Titan. On the other hand the mutual inclination of the orbits of these satellites is so small as to have eluded detection; the eccentricity of the orbit of Titan is less than 0.03, and the position of the aposaturnium of Hyperion so nearly coincides, at least at present, with the point of conjunction of the two satellites as to give rise to a suspicion that the eccentricity of its orbit is, in reality, small, and that the apparent eccentricity is principally due to the perturbations produced by Titan.

In view of these circumstances, that part of the disturbance has been investigated, which may be determined by neglecting the mutual inclination and the eccentricities of the orbits of both bodies, reserving a discussion of the remaining portion for another paper. It was accordingly assumed that

$$r = a(1 + a_1 \cos \theta + a_2 \cos 2\theta + \dots),$$

$$\frac{dw}{dt} = n(1 + n_1 \cos \theta + n_2 \cos 2\theta + \dots);$$

where r and w are the radius vector and longitude in orbit of Hyperion, θ is the mean angular distance between the radius vectors of

Titan and Hyperion, a and n are the mean values of r and w , and α_1, n_1 , etc., are constants to be determined. In the differential equations of motion for r and w , those terms not containing explicitly the mass of Titan were expanded by Taylor's theorem into series of sums of terms containing cosines of multiples of θ affected with constant coefficients; while the terms containing the mass of Titan explicitly were expanded *mechanically* into a series of cosines of multiples of θ by means of assumed values of the coefficients. Equating the coefficients of the cosines of equal multiples of θ , a number of equations were obtained from which to derive a corresponding number of the quantities α_1, n_1 , etc. With these new values were obtained and the process repeated. Instead, however, of considering m' (the mass of Titan) as known, α_3 was assumed to be given and m' was considered as one of the unknowns.

[This paper appeared in full in the *Annals of Mathematics*. 4°. Charlottesville, Va., 1887. Vol. 3, No. 6, p. 161.]

Brief remarks on Mr. STONE'S communication were made by the Chairman and by Messrs. BAKER, HILL, and KUMMELL.

Mr. E. B. ELLIOTT presented a paper on

THE QUOTIENTS OF SPACE-DIRECTED LINES.

He wrote down some of the fundamental relations of this analysis and explained the nature and properties of the special symbols employed. He called attention to the lectures of Hamilton on quaternions, and to his "letters" on the same subject, as they appear in Nichol's *Cyclopædia*;* and commented on the transition from Hamilton's primary conception of a *quarternion* as a quotient of two directed right lines in space to his secondary conception of a quaternion as the sum of a directed right line and a number.

The presentation of this paper was followed by a discussion, in which Messrs. BAKER, HILL, STONE, WOODWARD, and the Chairman participated.

* See *A cyclopædia of the physical sciences, etc.*, by J. P. Nichol. * * 8°. London and Glasgow, 1857. pp. 625-628.

35TH MEETING.

NOVEMBER 30, 1887.

The Chairman presided.

Eleven members present.

Mr. E. B. ELLIOTT continued his remarks, begun at the last meeting, on

THE QUOTIENTS OF SPACE-DIRECTED LINES.

[Abstract.]

Mr. ELLIOTT said that the quotient of two space-directed lines is not a line, but is abstract. It is a quantity which applied as a multiplier to one of the space-directed lines will produce the other.

He then gave as an illustration of this principle its application to the problem of the mutual action of the elements of electric currents.

Let μ and μ' represent, respectively, in length, current strength, and direction, two elements of electric currents.

ρ and ρ' represent, respectively, in length and direction, the lines connecting the centers of the elements.

θ represent the angle made by the element μ with the line connecting the elements μ and μ' ; that is, with ρ .

ψ represent the angle made by the element μ' with its rectangular projection in the primary plane; that is, the plane determined by the element μ and the connecting line ρ .

φ represent the angle made in the primary plane by the rectangular projection of the element μ' and the connecting line ρ' .

The effect of the action of μ on μ' will be as the product of the current strength, the length, and the direction of the elements, and inversely as the square of the distance, and the direction of the action will be expressed by the following formula:

$$\begin{aligned} U \frac{\mu}{\rho} \times U \frac{\mu'}{\rho'} &= \cos \theta \cos \psi \cos \varphi - \sin \theta \cos \psi \sin \varphi \\ &+ [\cos \theta \cos \psi \sin \varphi + \sin \theta \cos \psi \cos \varphi] i \\ &+ \cos \theta \sin \psi \cdot j \\ &+ \sin \theta \sin \psi \cdot ij; \end{aligned}$$

in which the *first* line denotes action (transference) in the direction of the line connecting the centers of the elements; the *second* line

denotes action (transference) in the primary plane, but perpendicular to the direction of the connecting line; the *third* line denotes the action (transference) perpendicular to the connecting line in a plane perpendicular to the primary plane; the *fourth* line denotes action (torsion) in a plane perpendicular to the primary plane.

If instead of the angles ψ and φ the angles θ' and ω are used, θ' denoting the angle made by μ' , with the line connecting the centers of the elements, that is, with ρ' ; and ω denoting the angle which the plane of μ' and ρ' makes with the plane of μ and ρ , the direction of the resulting action will be expressed by the following formula:

$$\begin{aligned} U_{\rho}^{\mu} \times U_{\rho'}^{\mu'} &= \cos \theta \cos \theta' - \sin \theta \sin \theta' \cos \omega \\ &+ [\sin \theta \cos \theta' + \cos \theta \sin \theta' \cos \omega] i \\ &+ \cos \theta \sin \theta' \sin \omega . j \\ &+ \sin \theta \sin \theta' \sin \omega . ij. \end{aligned}$$

The values of the four parts of this formula are identical, respectively, with the corresponding parts of the former one.

The mutual action of the unit-right-quotients (or quadrantal versors) i, j and ij are such that $i^2 = -1$; $j^2 = -1$; and \overline{ij}^2 (or its substitute k^2) = -1 , from which it readily appears that $ij = k = -ji$; $jk = i = -ki$; and $ki = j = -ik$.

Brief remarks on Mr. ELLIOTT'S paper were made by the Chairman and by Mr. CHRISTIE.

Mr. ARTEMAS MARTIN presented a paper on

METHODS OF FINDING NTH-POWER NUMBERS WHOSE SUM IS AN NTH-POWER; WITH EXAMPLES.

[Abstract.]

First method:

Let $1^n + 2^n + 3^n + 4^n + \dots + x^n = S_{x,n}$

and assume the auxiliary formula

$$(p + q)^n - p^n = a; \quad . \quad . \quad . \quad (1)$$

also assume d such that

$$S_{x,n} - a = d,$$

whence

$$S_{x,n} - d + p^n = (p + q)^n. \quad . \quad . \quad (2)$$

The solution now consists in determining by trial whether d can be separated into n^{th} -power numbers, all different.

Second method:

In equation (1) a may sometimes be separated by trial into n^{th} -power numbers, all different.

Third method:

Assuming b^n nearly equal to but less than $S_{x,n}$, and putting r for the difference, we have

$$S_{x,n} - r = b^n. \quad (3)$$

In formula (1) p and q may be any numbers chosen at pleasure. In formula (2) x should be chosen equal to or greater than the number of powers sought, and p and q any numbers that will give d positive, provided p be not less than x .

In formula (3) b must be greater than x .

Formulæ (1) and (2) are taken from Dr. Hart* who has treated the cases of squares and cubes at some length. Formula (3) is found to be especially serviceable if a large number of powers is sought.

Examples.—The values of $S_{x,n}$ for $n = 2, 3, 4,$ and $5,$ respectively, are here set down for reference as follows:

$$S_{x,2} = \frac{1}{6} x(x+1)(2x+1);$$

$$S_{x,3} = \frac{1}{4} x^2(x+1)^2;$$

$$S_{x,4} = \frac{1}{30} x(6x^4 + 15x^3 + 10x^2 - 1);$$

$$S_{x,5} = \frac{1}{12} x^2(x+1)^2(2x^2 + 2x - 1).$$

I. $n = 2:$

Ex. 1. Using formula (2) assume $x = 5,$ $p = 6,$ and $q = 1.$

Then $d = 42,$ which by trial is found equal to $1^2 + 4^2 + 5^2,$ whence

$$2^2 + 3^2 + 6^2 = 7^2.$$

*See *The Mathematical Magazine.* Edited and published by Artemas Martin. 4^o. Erie, Pa. 1882-1884. Vol. 1, No. 1 [January, 1882], pp. 8-9, and No. 11 [July, 1884], pp. 173-176.

Ex. 2. Using formula (1) assume $p = 8$ and $q = 3$; whence $a = 57$, which is by trial found equal to $1^2 + 2^2 + 4^2 + 6^2$ and

$$1^2 + 2^2 + 4^2 + 6^2 + 8^2 = 11^2.$$

Ex. 3. Using formula (3) assume $x = 50$ and $b = 206$; then $r = 489$, which by trial is found equal to

$$1^2 + 2^2 + 22^2 \text{ or } 5^2 + 8^2 + 20^2, \text{ etc.};$$

whence we have two sets of 47 numbers, the sum of whose squares is a square.

Ex. 4. Using formula (3) assume $x = 100$ and $b = 1750$; then $r = 2850$, which by trial is found to equal $4^2 + 5^2 + 53^2$; whence

$$1^2 + 2^2 + 3^2 + 6^2 + 7^2 + \dots \\ + 52^2 + 54^2 + \dots + 100^2 = 1750^2$$

II. $n = 3$:

Ex. 1. Using formula (2) assume $x = 5$, $p = 5$, $q = 1$, whence $d = 134$, which by trial is found equal to $1^3 + 2^3 + 5^3$, whence

$$3^3 + 4^3 + 5^3 = 6^3.$$

Ex. 2. Using formula (1) assume $p = 8$, $q = 1$, whence $a = 217$, which by trial is found to equal $1^3 + 6^3$; hence

$$1^3 + 3^3 + 4^3 + 5^3 + 8^3 = 9^3.$$

Ex. 3. Using formula (3) assume $x = 100$ and $b = 294$; whence $r = 90316$, which by trial is found to equal $1^3 + 6^3 + 11^3 + 21^3 + 43^3$, whence

$$2^3 + \dots 5^3 + 7^3 + \dots 10^3 + 12^3 + \dots \\ 20^3 + 22^3 + \dots 42^3 + 44^3 \dots + 100^3 = 294^3.$$

Ex. 4. Using formula (3) assume $x = 1000$ and $b = 6303$; whence $r = 5869873$, which by trial is found to equal $1^3 + 2^3 + 10^3 + 16^3 + 32^3 + 180^3$; hence,

$$3^3 + \dots 9^3 + 11^3 + \dots 15^3 + 17^3 + \dots \\ 31^3 + 33^3 + \dots 179^3 + 181^3 + \dots 1000^3 = 6303^3.$$

III. $n = 4$:

Ex. 1. Using formula (2) assume $x = 10$, $p = 14$, and $q = 1$; whence $d = 13124$, which by trial is found equal to $1^4 + 2^4 + 3^4 + 5^4 + 7^4 + 10^4$, whence

$$4^4 + 6^4 + 8^4 + 9^4 + 14^4 = 15^4.$$

Ex. 2. Using formula (3) assume $x = 100$ and $b = 212$; whence $r = 30\,370\,194$, which by trial is found equal to

$$1^4 + 2^4 + 3^4 + 4^4 + 8^4 + 10^4 + 14^4 + 24^4 + 42^4 + 72^4;$$

hence if all the natural numbers from 1 to 100, except the ten above given, be raised to the fourth power and added, their sum equals 212^4 .

IV. $n = 5$:

Ex. 1. Using formula (2) assume $x = 10$, $p = 11$, and $q = 1$; whence $d = 133\,044$, which by trial is found to equal $1^5 + 2^5 + 3^5 + 8^5 + 10^5$, and therefore

$$4^5 + 5^5 + 6^5 + 7^5 + 9^5 + 11^5 = 12^5.$$

Ex. 2. Using formula (1) assume $p = 29$ and $q = 1$; whence $a = 3\,788\,851$, which by trial is found equal to $5^5 + 10^5 + 11^5 + 16^5 + 19^5$; hence

$$5^5 + 10^5 + 11^5 + 16^5 + 19^5 + 29^5 = 30^5.$$

Ex. 3. Using formula (2) assume $x = 18$, $p = 31$, $q = 1$; whence $d = 1\,731\,920$, which by trial is found to equal $1^5 + 2^5 + 4^5 + 5^5 + 9^5 + 12^5 + 17^5$, and therefore

$$3^5 + 6^5 + 7^5 + 8^5 + 10^5 + 11^5 + 13^5 + 14^5 + 15^5 + 16^5 + 18^5 + 31^5 = 32^5.$$

In finding these numbers, use has been made of Barlow's tables of fourth and fifth powers. To further facilitate the work the values of $S_{x,n}$ for $n = 4$ and $n = 5$ were tabulated.

This paper was discussed briefly by the Chairman and by Messrs. DOOLITTLE, HILL, BAKER, and KUMMELL.



NOTE ON THE PUBLICATIONS OF THE SOCIETY.

The ten volumes of the bulletin now issued cover the proceedings of the Society from its organization in March, 1871, to the end of December, 1887, a period of 17 years. Volumes 1 to 3 of the Bulletin apply to irregular periods; volume 4 gives the proceedings for a Society's year, beginning in October of one calendar year and ending in June of the next. In 1882, the Society's year was changed to coincidence with the calendar year, and volume 5 contains the minutes from October, 1881, to December, 1882, inclusive. Volumes 6 to 10 cover, respectively, the calendar years 1883-1887.

The pages of all the volumes have been stereotyped at the expense of the Smithsonian Institution, and after the Society's edition, usually of 500 copies, has been printed, the plates have gone into the custody of the Institution, which has subsequently issued an edition of its own, constituting a paper of its Miscellaneous Collections. In the Smithsonian edition, volumes 1, 2, and 3 of the Bulletin constitute volume 20 of the Miscellaneous Collections, and volumes 4 and 5 constitute part of volume 25 of the Miscellaneous Collections. Volumes 6 to 8 have been reprinted by the Institution, but not yet gathered into a Collections volume for binding. Their numbers in the Smithsonian list are as follows:

Vol. 6	No. 543
Vol. 7	No. 592
Vol. 8	No. 636

The Smithsonian edition is in the main typographically identical with the Society's edition, but the following differences are to be noted.

Volume 20 of the Smithsonian Collections contains, in addition, the following title page and contents:

Smithsonian Miscellaneous Collections. Vol. XX. (Vignette and motto.) Washington: Published by the Smithsonian Institution. 1881.

Contents. Article I. Bulletin of the Philosophical Society of Washington. Vol. I, March, 1871, to June, 1874. Pp. 218.

Article II. Bulletin of the Philosophical Society of Washington. Vol. II, October 10, 1874, to November 2, 1878. Pp. 452.

Article III. Bulletin of the Philosophical Society of Washington. Vol. III, November 9, 1878, to June 19, 1880. Pp. 169.

The plates for this volume were changed by way of correction in a number of details, and the following list of differences may be regarded as corrigenda for volumes 1, 2, and 3 of the Society's edition.

DIFFERENCES IN VOLUME I OF BULLETIN.

<i>Page.</i>	<i>Line.</i>	<i>Society's edition.</i>	<i>Smithsonian edition.</i>
31	17	Benj. F. Pierce	Benj. Pierce
38	12	34, 35	36, 37
54	38	B. F. Taylor	W. B. Taylor
57	11	erosions	erosion
57	13	particles,	particles
57	14	is a minimum	is at a minimum
85	9	marl-gravel	marl, gravel
85	22	sufficed,	sufficed
85	23	west,	west
85	23	water,	water
91	24	o. London	of London
107	42	Glaishen	Glaisher
109	5	J. K. Gilbert	G. K. Gilbert
109	13	Division	division
109	16	Raibal Plateau	Kaibab Plateau
44*	24	Sandstones	Sandstone
47*	10	87	89

DIFFERENCES IN VOLUME II OF BULLETIN.

<i>Page.</i>	<i>Line.</i>	<i>Society's edition.</i>	<i>Smithsonian edition.</i>
X	31	Carl	Karl
XIII	15	Cripsey	Crissey
21	21	.00279	.00729
28	28	among the Esquimaux tribes by	resulting from grammatical
42	7	A. H. Spofford	A. R. Spofford

* Appendix.

<i>Page.</i>	<i>Line.</i>	<i>Society's edition.</i>	<i>Smithsonian edition.</i>
42	22	Dalton	Dutton
64	16	Meyer	Mayer
67	2	E. K. Gilbert	G. K. Gilbert
67	7	September	September.
69	2	E. K. Gilbert	G. K. Gilbert
69	18	E. K. Gilbert	G. K. Gilbert
87	2	Charles C. Boerner	Charles G. Boerner
95	7	Whyte	White
104	15	B. A. Alvord	B. Alvord
105	8	Espy	Espy
110	30	Whyte	White
111	6	M. B. Meek	F. B. Meek
113	16	"The Henry Mountains,"	The Henry Mountains,
123	22	B. F. Green	B. F. Greene
123	30	Greene	Green
126	15	Woodward	Woodward
130	27	Henry Parker	Henry, Parker
131	last	great, that	great that
133	38	Martin	Martyn
189	9	Cox	Coues
190	3	J. W. Clark	F. W. Clark
196	24	Gallandet	Gallaudet
199	10	La Verrier's	Le Verrier's
313	2	Observations	Observatories
380	12	Esquimaux	the extension of

DIFFERENCES IN VOLUME III OF BULLETIN.

<i>Page.</i>	<i>Line.</i>	<i>Society's edition.</i>	<i>Smithsonian edition.</i>
1	2	I-XV	i-xv
18	4	David B. Todd	David P. Todd
18	8	Ichthys	Tethys
33	12	Phosphorescent	Phosphorescent
34	37	base	bases
44	36	G. W. Osborne	J. W. Osborne
56	foot note		In the above diagram, the symbol α should be a , and $\alpha\sqrt{2}$ should be $a\sqrt{2}$.

<i>Page.</i>	<i>Line.</i>	<i>Society's edition.</i>	<i>Smithsonian edition.</i>
57	17	0.49788, 15817, 54736.	0.49788 15817 54736.
58	9	$+\frac{b^2}{a}$	$+\frac{b^2}{a^2}$
58	14	m	in
59	foot note		In this page and the following, the symbol γ (for radius) should read r .
117	3	Nevada	Wyoming
120	23	Michaelson	Michelson
124	27	Alfred	Albert
125	16	G. W. Osborne	J. W. Osborne
126	9	carboniferous	Carboniferous
126	26	to and in consequence of	streams, which result from
127	31	when known	as far as known
127	37	miocene	Miocene
156	52	Nicholas	Nichols
159	6	Instition	Institution
164	21	Hoarlem	Haarlem
165	26	R. Craig	T. Craig
168	5	Aztic	Aztec
168	12	A. Michelson	A. A. Michelson
168	14	119 and 147	119 and 148
168	26	G. W. Osborne	J. W. Osborne
168	36	S. W. Powell	J. W. Powell
169	7	C. S. Schott	C. A. Schott
169	30	L. L. Woodward	J. J. Woodward

Volume 25 of the Smithsonian Collections has the following title-page and contents.

Smithsonian Miscellaneous Collections. Vol. XXV. (Vignette and motto.) Washington: Published by the Smithsonian Institution. 1883.

Table of Contents.

Article I. (498.) Bulletin of the Philosophical Society of Washington. Vol. IV. October 9, 1880, to June 11, 1881. 1883. Pp. 189.

Article II. (503.) Bulletin of the Philosophical Society of Washington. Vol. V. October 8, 1881, to December 16, 1882. 1883. Pp. 189.

INDEX TO VOLUMES I-X.

Volume, Roman pagination, Arabic pagination, and pagination of appendix are distinguished thus: **ix**, xvi, 23, (17).

The pages of appendices are differently numbered at top and at bottom; the index refers to the pagination at bottom.

The titles of all papers read to the Society are entered (with some duplication) under the following words: Acoustics, Anatomy, Anthropology, Archæology, Astronomy, Biography, Biology, Botany, Calendars, Chemistry, Electricity, Geography, Geology, Mathematics, Meteorology, Microscopy, Mineralogy, Miscellaneous, Oceanography, Optics, Physics, Political Economy, Psychology, Seismology, Social Science, Thermometry, Zoology.

	Page.		Page.
Abbe, Cleveland, communication on the aerial currents observed in balloon ascensions. <i>Abstract</i>	i 38	Achromatic objectives, Corrections of.....	iii 39
the laws governing the movement of storm centers. <i>Abstract</i>	i 99	Acoustic investigations by Joseph Henry..	ii 344
the position of the planes of certain nebulae. <i>Abstract and reference</i>	i 109	Acoustics , List of papers on:	
report of the committee to collect information relative to the meteor of December 24th, 1873. <i>In full</i> . 2 figures.....	ii 123, 139	on phenomena of sound and experiments with tuning forks. J. Henry. <i>Title only</i>	i 22
the aurora. <i>Abstract</i>	iv 21	on sound in relation to fog-signals, from investigations under the direction of the U. S. Light House Board. J. Henry <i>In full</i>	i 65, ii (45)
determining the temperature of the air. <i>Abstract</i>	vi 24	recent experimental researches in acoustics, by Prof. A. M. Mayer. J. E. Hilgard. <i>Title only</i>	i 90
methods of verifying weather predictions. <i>Abstract</i>	viii 8	experiments on fog signals during the past summer. J. Henry. <i>Title only</i> ..	i 90
Signal Service bibliography of meteorology. <i>In full</i>	x 20	[letter on fog-signals.] J. Tyndall. <i>Communicated by J. Henry. No abstract</i> ..	i 91
remarks on auroras.....	i 45	on audition. J. Henry. <i>Title only</i>	ii 22
Stone Mountain earthquake.....	i 102	on fog-signals and abnormal conditions of sound. J. Henry. <i>Reference</i>	ii 37
land and sea breezes.....	ii 18	sound in connection with fog signals. J. Henry. <i>Reference</i>	ii 57
the mean terrestrial ellipsoid, the geoid, and levelling.....	ii 24	acoustic refraction. W. B. Taylor. <i>Abstract</i>	ii 57
Dakota calendar.....	ii 93	an account of researches on sound in its application to fog-signals. <i>Annual address</i> , 1875. J. Henry. <i>Reference</i>	ii 60
polarization of light by a narrow slit.....	iii 124	exhibition of a telaphon. E. Gray. <i>Abstract</i>	ii 67
Benjamin Peirce.....	iv 25	[fog-signals.] J. Henry. <i>Abstract</i>	ii 85
anomalies of sound.....	v 37	the telephone. A. G. Bell. <i>Abstract</i>	ii 103
deflection of rivers.....	vii 23	comments on the telephone. E. B. Elliott. <i>Title only</i>	ii 111
report as treasurer..v 176, 180, vi xxii, vii xxiv		[scientific method and its application to acoustic researches in connection with fog signals.] <i>Annual address</i> , 1877. J. Henry. <i>In full</i>	ii 162
Abbe de l'Epee's instruction of the dumb..	vi 63		
Abbe, Prof. E., Apertometer of.....	iii 18		
cited on microscopy.....	iii 26		
Abbey, Westminster S., letter on a fish found on the Florida coast. <i>Read by C. Abbe. No abstract</i>	ii 202		
Abel's researches in elliptic integrals.....	vii 106		
Achromatic objective.....	iii 65		

	Page.		Page.
Acoustics , List of papers on—Continued.		Air, Contamination of.....	iv 37
the telephoto. E. B. Elliott. <i>Abstract</i>	ii 192	Alaska, Discoveries in.....	iv 163
musical intervals. E. B. Elliott. <i>Abstract</i>	ii 199	Glaciation in.....	vi 33, x 15
binaural audition. A. G. Bell. <i>Abstract</i>	iii 68, 69	Results of travels in.....	i 23
the spectrophone. A. G. Bell. <i>In full</i>		Value to the United States of.....	i 25
<i>Plate</i>	iv 142	Alaska-Siberia boundary.....	iv 123
upon a modification of Wheatstone's microphone and its applicability to radiophonic researches. A. G. Bell. <i>In full</i>		Albertype process of photo-engraving.....	i 42
<i>Plate</i>	iv 183	Aleutian Islands, Shell heaps of.....	ii 65
recent investigations by the Light House Board on the anomalies of sound from fog-signals. A. B. Johnson. <i>In full</i>		Alexander, Stephen, communication on the zodiacal light. <i>Read by J. E. Hilgard</i>	
2 maps, 1 figure.....	v 23	<i>In full</i> , 9 figures.....	i 105, (10)
anomalies of sound signals. J. C. Welling. <i>In full</i>	v 39	Algebra, Logical.....	i 88
the difficulty in determining the direction of sound. A. B. Johnson. <i>Abstract</i>	viii 11, 12	Algorithm of the arithmetico-geometric mean.....	vii 102
A. G. Bell. <i>Title only</i>	viii 18	Alignment curves on any surface.....	vi 123
Action at a distance.....	v 156	Allard, M. E., cited on the light-house service of the United States.....	iv 138
Adams, Prof. Carl, cited on Malfatti's problem.....	ii 118	Alluvial basin of the Mississippi.....	i (10)
Adams, Prof. W. G., cited on electric resistance.....	iv 154	Alphabet, Phonetic.....	ix 17
Address of chairman of Mathematical Section.....	vi 117	Altitude of the Caspian and Aral seas.....	ii 34
of President Henry, 1871.....	i v, 34	Altitudes deduced from combination of railroad levellings.....	ii 23
Henry, 1875.....	ii 60	Alvord, Benjamin, cited on gravitation formula.....	viii 40
Henry, 1877.....	ii 162	communication on the habitability of the elevated plateaus of the west. <i>Title only</i>	i 74
Newcomb, 1879.....	iii 52	the recent earthquakes in North Carolina. <i>Abstract</i>	i 101
Newcomb, 1880.....	iv 40	the mortality among army officers. <i>Reference</i>	ii 49
Woodward, 1881.....	v 49	proposed governmental insurance. <i>No abstract</i>	ii 49
Taylor, 1882.....	v 126	a trigonometrical formula. <i>Title only</i>	ii 104
Powell, 1883.....	vi xxvii, 110	the intersection of circles and the intersection of spheres. <i>Title only</i>	ii 198
Welling, 1884.....	viii xxix, 81	new points respecting the intersections of circles and the intersections of spheres. <i>Title only</i>	ii 201
Hall, 1885.....	viii xxxiii, 30	life and work of Joseph Henry. <i>In full</i>	ii 370
Billings, 1886.....	ix xxxv, 46	a curious fallacy as to the theory of gravitation. <i>In full</i>	v 85
Harkness, 1887.....	x xxxvii, 39	some of the properties of Steiner's power circle. <i>Title only</i>	v 89
of retiring president, Resolution concerning.....	iv 30	the compass plant. <i>Reference</i>	v 106
on the life and character of Joseph Henry, ii 203, 368, 370		a special case in maxima and minima. <i>Abstract</i>	vi 149
Adhesion and cohesion.....	v 136	Death of.....	vii 72, 127
Adirondack region, Proposed reservoirs in the.....	ii 67, 82	List of mathematical papers by.....	vii 128
Adjustment of conditioned observations, viii 41		Memorial to.....	vii 127
of the calendar.....	xi 59	remarks on Lake Bonneville.....	ii 103
Administration of scientific work.....	ix xliii	Benjamin Peirce.....	iv 23, 24
Adulteration of food.....	iv 39	Arkansas bonds.....	vi 105
Aerolite. See <i>Meteor</i> .		agricultural colleges.....	vi 106
Agassiz, Louis, Announcement of death of.....	i 93	Amendment to constitution.....	ix 47, x 39
Resolutions on death of.....	i 95		
Agricola, Georg, cited on mineralogy.....	i 77		
Ague, Conservative function of.....	vi 5		

	Page.
Amendment to standing rules.....	iii 149, iv xi, 38, viii x, xi
American Academy of Arts and Sci- ences	viii xxxvi
American Association for the Advancement of Science.....	viii xxxix
American Philosophical Society.....	viii xxxiv
American scientific societies.....	viii xxxiii
Ampère, Law of.....	v 139
Anal notch in Pleurotomaria.....	iii 76
Analysis of meteorite.....	vii 32
Anatomy and Physiology, List of papers on:	
on the alleged hermaphrodite described by Drs. Acely, Blackman, and Jackson. J. J. Woodward. <i>Abstract and reference.</i>	i 24
on the fluctuations of the temperature of the human body. B. F. Craig. <i>Ref- erence</i>	i 31
on fractures of the inner table of the cran- ium. G. A. Otis. <i>Title only</i>	i 73
[letter on autopsy of Agassiz.] Dr. Jack- son. <i>Communicated by J. J. Woodward. No abstract</i>	i 93
on the similarity between the red blood- corpuscles of man and those of certain other mammals, especially the dog; considered in connection with the di- agnosis of blood-stains in criminal cases. J. J. Woodward. <i>Abstract and reference</i>	i 20
explanatory note in regard to the diagnosis of blood-stains. J. G. Richardson. <i>Communicated by J. J. Woodward. Ref- erence</i>	i 41
the conservative element in disease. A. F. A. King. <i>Abstract</i>	i 111
the conservative influence of disease as illustrated in the phenomena of pul- monary phthisis. A. F. A. King. <i>Ab- stract</i>	i 124
the influence of the cardiac and respiratory movements upon the motion of the lymph. S. C. Busey. <i>Abstract and ref- erence</i>	i 133
asymmetry in the form of the human cran- ium. C. A. White. <i>Title only</i>	i 190
the physiology of civilization. H. Reed. <i>Title only</i>	i 20
color perception and color blindness. S. M. Burnett. <i>Abstract and reference</i>	iv 54
on the influence of the constant use of high-heeled shoes upon the health and form of the female, and upon the rela- tion of the pelvic organs. S. C. Busey. <i>Abstract</i>	v 117

	Page.
Anatomy and Physiology, List of papers on—Continued.	
modern ideas of brain mechanism. F. Baker. <i>Title only</i>	viii 17
Anaxagoras' philosophy	vii xxxii
Andromeda, New star in.....	ix 14
Animal population of the globe.....	iv 27
Annual address. See <i>Address</i> .	
Annual meeting. See <i>Election of officers and Address</i> .	
Anomalies of sound from fog-signals	v 23, 39
Anthropological Society of Washington	x 46
Invitation from.....	viii 5, ix 15, x 6
Anthropological work of the Smithsonian Institution.....	i 299
Anthropology, List of papers on. (See, also, <i>Archæology</i>.)	
on the characteristics and zoological rela- tions of man. T. Gill. <i>Abstract</i>	i 24
on the mythology of the Numas. J. W. Powell. <i>Reference</i>	i 96
on the genesis and demonology of the Numa tribe of Indians. J. W. Powell. <i>Reference</i>	i 104
a calendar of the Dakota Indians. G. Mal- lery. <i>Abstract and reference</i>	i 90
the philosophy of the North American In- dians. J. W. Powell. <i>Title only</i>	i 109, 110
some common errors respecting the North American Indians. G. Mallery. <i>Ab- stract and reference</i>	i 175
poisons among the North American In- dians. J. W. Powell. <i>Abstract</i>	i 182
the use of poisoned arrows by North Amer- ican Indians. E. Coues and W. J. Hoff- man. <i>Title only</i>	i 183
the evolution of language. J. W. Powell. <i>Title only</i>	i 199
the progressive dispersion of mankind over the surface of the earth. A. Win- chell. <i>Title only</i>	i 33
the future of the human race regarded from the standpoint of evolution. S. Newcomb. <i>Presidential address. Title only</i>	i 52
on the gentile system of the Omahas. J. O. Dorsey. <i>In full; 3 figures</i>	i 128
comparison of written language, with that which is spoken only. O. T. Mason. <i>Abstract</i>	i 139
limitations to the use of some anthropo- logic data. J. W. Powell. <i>Refer- ence</i>	iv 134
the three methods of evolution. J. W. Powell. <i>Presidential address. In full</i> vi xxvii, 110	

	Page.		Page.
Anthropology , List of papers on—Cont'd.		Applied science. Plea for	vii 11
composite photography applied to crani-		Approximate quadratures.....	ii 48
ology. J. S. Billings. <i>Abstract</i>	vii 25	Aral sea, Altitude of.....	ii 34
natural naturalists. W. Matthews. <i>Read</i>		Archæology , List of papers on:	
<i>by J. S. Billings. Abstract</i>	vii 73	[exhibition of] archæological specimens.	
mythological dry paintings of the Navajos.		O. T. Mason. <i>Title only</i>	ii 48
W. Matthews. <i>Abstract</i>	viii 14	the classification of objects of archæology.	
anthropometric and reaction-time appa-		O. T. Mason. <i>Title only</i>	ii 50
ratus. J. S. Billings and W. Matthews.		remarks on the Papyrus Ebers. J. J. Wood-	
<i>Abstract</i>	viii 25	ward. <i>Abstract</i>	ii 64
two examples of similar inventions in areas		the succession of the strata of the shell-	
widely apart. O. T. Mason. <i>Abstract</i>	ix 12	heaps of the Aleutian Islands. W. H.	
customs of every-day life. G. Mallery.		Dall. <i>Abstract</i>	ii 65
<i>Abstract</i>	ix 19	the international symbols for charts of pre-	
bowyers and fletchers. O. T. Mason. <i>Ab-</i>		historic archæology. O. T. Mason.	
<i>stract</i>	ix 44	<i>Abstract</i>	ii 71, 72
counting out rhymes of children; their		prehistoric copper. J. D. Butler. <i>Title</i>	
antiquity, origin and wide distribu-		<i>only</i>	ii 185
tion. H. C. Bolton. <i>Reference</i>	x 13	the fresh-water shell-heaps of the interior	
Anticlinal and synclinal axes.....	ii (22)	rivers of North America. C. A. White.	
Antisell, Thomas, communication on dust		<i>Title only</i>	iii 32
from Armenia. <i>No abstract</i>	i 25	the decipherment of some Aztec monu-	
meteorology of Japan. <i>Title only</i>	i 70	ments lately discovered in Guatemala.	
visit to Japan. <i>No abstract</i>	ii 84	O. T. Mason. <i>Title only</i>	iii 37
terrestrial geogony. <i>Title only</i>	ii 132, 133, 134	Arctic exploration.....	i 89, ix 8
temperatures of the Pacific Ocean. <i>Ab-</i>		Argentine coinage.....	ii 65, iii 38
<i>stract</i>	ii 192	Aristotle cited on atoms.....	vii xxxii
chemical molecular changes. <i>Title</i>		mineralogy.....	i 77
<i>only</i>	iii 28	Arithmetic, Binary.....	vi 3, 38
the building up of organic matter. <i>Title</i>		Arizona, Physical features of.....	i 54
<i>only</i>	v 97	Volcanic activity in.....	i 99
remarks on waterspouts.....	ii 104	Army and Navy officers as scientific admin-	
faunal accommodation.....	ii 181	istrators.....	ix xlix
poisoned arrows.....	ii 183	officers, Mortality among.....	ii 49
vegetation and environment.....	ii 183	Medical Museum.....	ix 35
Wasatch fault.....	ii 196	Medical Museum building.....	x 10, 31
ravages of teredo.....	v 98	Arrow, Sir F., cited on phenomena of sound.	
artesian water on the Plains.....	v 101		ii (49), (50)
thermometer exposure.....	vi 47	Arrows, Poisoned.....	ii 180, 182
dissociation.....	vii 16	Artesian well with geyser action.....	i 103
volcanic dust.....	vii 20, 25, 26	wells on the Great Plains.....	v 101
cause of thunderstorms.....	viii 11	Arts, Evolution of.....	vi xlviii
odor.....	viii 27	Assembly Hall of Cosmos Club.....	x 10, 31
Antlers, Morphology of.....	ii 135	Association ratios.....	x 83, 94
Apertometers.....	iii 18	Astigmatism.....	vi 4
Aphakia.....	vi 5	Focal lines in.....	vi 45
Appalachian mountains.....	iv 60	Astronomy , List of papers on. (See also	
topography.....	ix 22	<i>Calendars</i>):	
Apparatus, Base-line.....	iii 35	on the elements of the Comet I, 1871. A.	
for examination of the eye.....	iii 53	Hall. <i>Communicated by B. F. Sands.</i>	
for exhibiting local time at all points of		<i>Abstract</i>	i 23
the globe.....	iii 107	on two immense meteorites at Conception	
for viewing the sun by light of any desired		and San Gregorio, Mexico. H. B.	
wave length.....	x 13	Butcher. <i>Reference</i>	i 24
to facilitate "sweeping".....	iii 142	on astronomical photography. A. Hall.	
Apples, Problem of rotten and wormy.....	x 87, 89	<i>Abstract and reference</i>	i 23

	Page.
Astronomy , List of papers on—Cont'd.	
on the transits of Venus, past and future. S. Newcomb. <i>Title only</i>	29
on the heat of the sun. B. Peirce. <i>Abstract</i>	31
on the physical constitution of the corona of the sun. W. Harkness. <i>Reference</i>	31
on the spectrum of Encke's comet and the appearance of Tuttle's comet. W. Harkness. <i>Reference</i>	34
on the astronomical proof of the existence of a resisting medium in space. A. Hall. <i>Reference</i>	34
[on the spectrum of Encke's comet.] W. Harkness. <i>Reference</i>	34
on the appearance of Encke's comet as seen at Harvard College observatory. C. S. Peirce. <i>Reference</i>	35
on the density of the hypothetical resisting medium in space. W. Harkness. <i>Reference</i>	39
on the possibility of a universal atmosphere. S. Newcomb. <i>Title only</i>	52
on the discovery of new planets having especial reference to the asteroids. J. C. Watson. <i>Title only</i>	53
[letter on solar eclipse.] Capt. Tupman. <i>Communicated by W. Harkness. No abstract</i>	56
[letters on Cordoba Observatory.] B. A. Gould. <i>Communicated by J. H. C. Coffin and J. J. Woodward. No abstract</i>	57
on the determination of the errors of a provisory catalogue of fundamental stars. O. Stone. <i>Title only</i>	62
on the progress of the construction of the new telescope for the Naval Observatory. S. Newcomb. <i>Reference</i>	62, 63
on our present knowledge of the planet Jupiter. W. B. Taylor. <i>Title only</i>	62
maps prepared by G. W. Hill for use in connection with the transit of Venus in December, 1874. J. H. C. Coffin. <i>Reference</i>	63
on stellar photometry. C. S. Peirce. <i>Reference</i>	63
the proceedings of the commission to arrange for the observation of the next transit of Venus. S. Newcomb. <i>Title only</i>	65
a comparison of the thermometers used to determine the correction for atmospheric refraction at the U. S. Naval Observatory. J. R. Eastman. <i>Abstract</i>	68

	Page.
Astronomy , List of papers on—Cont'd.	
on the results of astronomical observations at Sherman Station, Wyoming Terr. R. D. Cutts. <i>Abstract and reference</i>	70
on the theories of the nature of comets' tails. B. Peirce. <i>Reference</i>	74
on the general star catalogue prepared from the observations at the Naval Observatory since 1845. M. Yarnall. <i>Reference</i>	74
on the power necessary to drive the pendulum of an astronomical clock. W. Harkness. <i>Title only</i>	74
on a proposed method of observing astronomical transits. E. Foote. <i>Title only</i>	75
the frequency of the occurrence of the zero and the nine digits in the tenths of seconds from the chronographic record of transit observations. J. R. Eastman. <i>Abstract</i>	85
[letter on the Cordoba Observatory.] B. A. Gould. <i>Communicated by J. J. Woodward. No abstract</i>	88
[letter on proposed observatory.] J. Lick. <i>Communicated by J. Henry. No abstract</i>	91
a detailed account of the construction of the lenses and other interesting portions of the large telescope now established at the Naval Observatory. A. Clark. <i>Title only</i>	92
on the determination of the personal errors in the observation of astronomical transits. J. E. Hilgard. <i>Title only</i>	92
on comets and meteors. A. Hall. <i>Reference</i>	94
[the meteor of December 24, 1873.] P. Parker. <i>No abstract</i>	94
[letter on the meteor of December 24, 1873.] B. Hallowell. <i>Communicated by J. Henry. No abstract</i>	95
on the adopted value of the sun's apparent diameter. E. S. Holden. <i>In full</i> , 1 95, (3)	
on various hypotheses in reference to space. C. S. Peirce. <i>Title only</i>	97
on specimens of meteoric iron from Chihuahua, Mexico, and the structure of meteorites in general. F. M. Endlich. <i>Title only</i>	98
on meteor trains, and the upper atmospheric currents. J. Henry. <i>Title only</i>	98
on the apparatus to be used in the observations of the approaching transit of Venus. W. Harkness. <i>Title only</i>	102

	Page.
Astronomy , List of papers on—Cont'd.	
on the zodiacal light. S. Alexander. <i>Communicated by J. E. Hilgard. In full; 9 figures</i>	105, (19)
on Sir William Herschel's observations of the satellites of Uranus. E. S. Holden. <i>In full</i>	106, (30)
a new apparatus for the investigation of personal error in astronomical transit observations. J. E. Hilgard. <i>Title only</i>	106
on the position of the planes of certain nebulae. C. Abbe. <i>Abstract and reference</i>	109
on the correction of a comet's orbit. O. Stone. <i>Reference</i>	11 22
[letter on transit of Venus, 1874.] C. H. F. Peters. <i>Communicated by A. Hall. Abstract</i>	11 31
[letter on transit of Venus, 1874.] C. W. Raymond. <i>Communicated by A. Hall. Abstract</i>	11 31
[letters] on the operations of the several parties sent from the United States to observe the transit of Venus on the 8th of Dec'r, 1874. A. Hall. <i>Abstract</i>	11 31, 33
[letter on transit of Venus, 1874.] W. Harkness. <i>Communicated by A. Hall. Abstract</i>	11 32
[letter on transit of Venus, 1874.] G. Davidson. <i>Communicated by A. Hall. Abstract</i>	11 32
the expedition to Pekin for observing the late transit of Venus [1874]. C. A. Young. <i>Abstract</i>	11 33
on the transit of Venus [1874]. S. Newcomb. <i>Title only</i>	11 41
two drawings of nebulae, made with the XXVI-inch telescope of the U. S. Naval Observatory, by Mr. L. Trouvelot, of Cambridge, Mass. E. S. Holden. <i>Abstract</i>	11 51
the methods of measuring the inequalities of the pivots of a transit instrument. W. Harkness. <i>Title only</i>	11 68
the temperature of space. W. B. Taylor. <i>Abstract</i>	11 73
[search for Vulcan.] E. S. Holden. <i>Abstract</i>	11 85
the appearance of Saturn's rings. A. Hall. <i>Abstract</i>	11 94
on reference catalogues of astronomical papers and memoirs. E. S. Holden. <i>Abstract</i>	11 95
the shadow of the ball of Saturn projected on the rings. E. S. Holden. <i>Abstract</i>	11 101

	Page.
Astronomy , List of papers on—Cont'd.	
a bright spot which [has] recently become visible on the ball of Saturn. A. Hall. <i>Abstract</i>	11 102
the cosmogony. S. Newcomb. <i>Title only</i>	11 113
report of the committee to collect information relative to the meteor of December 24th, 1873. <i>Read by C. Abbe. In full; 2 figures, 1 map</i>	11 123, 139
the position of the centre of gravity of the apparent disk of a planet. A. Hall. <i>Reference</i>	11 181
the results of [a] search for satellites of Mars. A. Hall. <i>Abstract and reference</i>	11 186
the nebular hypothesis and the inner moon of Mars. M. H. Doolittle. <i>Abstract</i>	11 188, 190
aerolithic disturbance of planetary motions. M. H. Doolittle. <i>Abstract</i>	11 190
the recent transit of Mercury [1878]. S. Newcomb. <i>Abstract</i>	11 199
a new eye-piece for observing personal equations. A. Schott. <i>Title only</i>	11 200
the velocity of light and determination of the solar parallax. W. Harkness. <i>Title only</i>	11 201
observations of the total solar eclipse, July 29, 1878. S. Newcomb. <i>Abstract</i>	11 202
notes on the brightness and the stellar magnitude of the third Saturnian satellite, Tethys. E. S. Holden. <i>Read by A. N. Skinner. Title only</i>	11 18
on the supposed discovery of a trans-Neptunian planet at the U. S. Naval Observatory in 1850. A. Hall. <i>Abstract</i>	11 20
a note on the precession of stars in right ascension. A. N. Skinner. <i>Title only</i>	11 21
on the satellites of Saturn. A. Hall. <i>Abstract</i>	11 26
a personal equation instrument. J. R. Eastman. <i>Abstract</i>	11 33, 37
the recurrence of eclipses. S. Newcomb. <i>Title only</i>	11 33
notes on the orbits of Titan and Hyperion. A. Hall. <i>Abstract</i>	11 40
some results from the discussion of the observations of the transit of Mercury of May 6, 1878. J. R. Eastman. <i>Abstract</i>	11 43
a recent visit to California to inspect a site for the new Lick Observatory. S. Newcomb. <i>Title only</i>	11 45
solar parallax from the velocity of light. D. P. Todd. <i>Reference</i>	11 74

	Page.
Astronomy , List of papers on—Cont'd.	
a pile of balls. M. H. Doolittle. <i>Abstract</i> ,	iii 76
on the solar corona. W. Harkness. <i>Abstract</i>	iii 116
review of B. A. Gould's Uranometria Argentina. E. S. Holden. <i>Reference</i> ,	iii 119, 122
remarks on the total solar eclipse of January 11th, 1880. E. Frisby. <i>Abstract</i> ,	iii 121
on a mechanical attachment for equatorial mountings to facilitate sweeping in right ascension. D. P. Todd. <i>Abstract and reference</i>	iii 142
on a simple method of deriving some equations used in the theory of the moon and of the planets. W. F. McK. Ritter. <i>In full</i>	iv 57
on the orbit of Swift's comet. E. Frisby. <i>Abstract</i>	iv 59
the solar parallax as derived from the American photographs of the transit of Venus, 1874, December 8-9. D. P. Todd. <i>Abstract and reference</i>	iv 168
the relative accuracy of different methods of determining the solar parallax. W. Harkness. <i>Reference</i>	v 39
on the total lunar eclipse of June 11, 1881. W. B. Taylor. <i>Abstract</i>	v 90
the Florida expedition for observation of the transit of Venus [1882]. J. R. Eastman. <i>Abstract</i>	vi 21
note on the rings of Saturn. W. B. Taylor. <i>Abstract</i>	vi 41
the determination of the mass of a planet from observation of two satellites. A. Hall. <i>Abstract</i>	vi 132
certain possible abbreviations in the computation of the long-period perturbations of the moon's motion due to the direct action of the planets. G. W. Hill. <i>Abstract and reference</i>	vi 136
a new meteorite. J. R. Eastman. <i>Abstract</i>	vii 32
the formulæ for computing the position of a satellite. A. Hall. <i>In full</i> . 1 figure.	vii 93
a case of discontinuity in elliptic orbits. W. B. Taylor. <i>Abstract</i>	vii 122
variations of latitude. A. Hall. <i>Abstract and reference</i>	viii 10
comets II and III, 1884. W. C. Winlock. <i>Title only</i>	viii 16
the asteroids. G. L. Ravené. <i>Title only</i> ,	viii 18, 54

	Page.
Astronomy , List of papers on—Cont'd.	
flexures of transit instruments. W. Harkness. <i>Abstract</i>	viii 27
physical observations of Wolf's comet (1884 II). W. C. Winlock. <i>Abstract</i> ,	viii 37
the theory of Mercury. G. L. Ravené. <i>Abstract</i>	viii 41
secular perturbations of Polyhymnia by Jupiter. W. F. McK. Ritter. <i>Abstract</i> ,	viii 54
the new star in the nebula of Andromeda. A. Hall. <i>Reference</i>	ix 14
the images of stars. A. Hall. <i>Reference</i>	ix 15
a comparison of the Boss and Auwers' declination standards. H. Farquhar. <i>Abstract and reference</i>	ix 53
on a device for viewing the sun by light of any desired wave length. W. Harkness. <i>Abstract</i>	x 13
on the representation of comet orbits by models. W. Harkness. <i>Reference</i>	x 28
The motion of Hyperion. G. W. Hill. <i>Abstract and reference</i>	x 90
the parallax of a Tauri. A. Hall. <i>Abstract</i>	x 91
the most probable value of the latitude and its theoretical weight from entangled observations occurring in the use of Talcott's method. <i>Abstract</i>	x 91
Euler's theorem (generally called Lambert's). A. Hall. <i>Abstract</i>	x 101
the orbit of Hyperion. O. Stone. <i>Abstract and reference</i>	x 104
Atmospheric temperature determination.	vi 24
Atomic motions.....	v 143
philosophy, physical and metaphysical,	vii xxix
volume curve.....	vii 15
volumes of crystallized and double salts.....	i 103
weights.....	vii xlvii
Atoms.....	vii 45
and molecules.....	v 141
molecules and waves.....	i 66
Attracting centre, Motion of a particle toward.....	i 88, ii 19, vii 122
Attraction, Infinite, of a finite mass.....	ii 19, viii 58
Auditing Committee. See <i>Committee</i> .	
Audition, Binaural.....	iii 69
Aurora, Height of.....	iv 21
of February 4th, 1872.....	i 47
Theories of.....	i 43
Auwers' declination standards.....	ix 53
Avicenna, cited on mineralogy.....	i 77
Avogadro, Law of.....	v 139

	Page.		Page.
Babcock, O. E., Death of.....	vii 72	Barker, Prof. G. F., cited on diatomic molecules.....	v 150
Bacillus malariae.....	iv 39	vital principle.....	v 50
Bache, A. D., Eulogy on.....	i 35	nerve currents.....	v 61
Bacteria.....	i 43	Barnard, Gen., cited on precession and terrestrial rigidity.....	ii 78
and spontaneous generation.....	ii 109	Barnes, J. K., Death of.....	vi xvi
Baer's law.....	vii 21	Barometric gradient as related to velocity and direction of wind.....	i 106
Baeyer, cited on corrections to levelling for deflection of the plumb line.....	ii 25	hypsonetry.....	v 48
Bagehot, cited on occult force.....	vi xxxiii	New method of.....	ii 131
Bailey, T., Death of.....	ii 109, 111	observations modified by wind.....	v 91
Baird, S. F., and scientific societies.....	x 45	pressure and wind velocity.....	x 10
as an administrator.....	x 49	and winds in relation to tides.....	i 53
communication on the decrease of fish on the southern coast of New England.		Bartholin, cited on mineralogy.....	i 77
<i>Reference</i>	i 52	Basaltic columns.....	viii 19
the artificial propagation of the cod.		Basch's experiments on the circulation of the blood.....	v 77
<i>Abstract</i>	iii 29	Base-line apparatus.....	iii 35
Death of.....	x 17, 20, 76	at Kanab, Utah.....	iii 34
Meeting commemorative of.....	x 41	measurement near Atlanta.....	i 50
Personal characteristics of.....	x 71	Basketry.....	ix 13
remarks on archæological collection by G. Latimer.....	ii 48	Bates, H. H., cited on gravitation formula, communication on the motion of a particle towards an attracting centre. <i>Title only</i>	viii 39, 40
Scientific work of.....	x 61	movement of a particle attracted towards a point. <i>Abstract</i>	ii 19
Bairdian school of ornithologists.....	x 66	the nature of matter. <i>Reference</i>	vi 5
Baker, Frank, communication on modern ideas of brain mechanism. <i>Title only</i> , remarks on audition.....	viii 17	the physical basis of phenomena. <i>In full</i> , 2 figures.....	vii 40
Baker, Marcus, communication on the history of Malfatti's problem. <i>In full</i> , 2 figures.....	viii 13	remarks on wind-vane formula.....	x 9
a geometric problem, with bibliographical notes. <i>In full</i> , 4 figures.....	iii 53, 55	Bates, N. L., communication on organic cells of unknown origin and form found in human feces (two cases). <i>Title only</i>	ix 35
the boundary line between Alaska and Siberia. <i>In full</i> . <i>Map</i>	iv 123	Baudin's method in thermometry.....	ix 29
a geometrical question relating to spheres. <i>In full</i>	v 107	Bayma, Prof. J., cited on action at a distance.....	v 158
Benjamin Alvord. <i>Read by E. B. Elliott</i> . <i>In full</i>	vii 127	Bay's Mountains, Tenn.....	x 7
a collection of formulae for the area of a plane triangle. <i>Reference</i>	viii 37	Bean, T. H., communication on the distribution of fishes in the oceanic abysses and middle strata. <i>Title only</i>	ix 22
a group of circles related to Feuerbach's circle. <i>In full</i> , 4 figures.....	viii 45	Bebb, M. S., cited on salices.....	iv 110
What is a topographic map? <i>Abstract</i>	x 11	Becquerel, A. E., cited on chemical rays.....	v 135
a problem in probabilities. <i>Abstract</i>	x 87	Bede, cited on cure of dumbness.....	vi 53
a collection of solutions of the trisection problem. <i>Abstract</i>	x 96	Behring's Strait.....	iv 123
remarks on Alaskan glaciers.....	x 15	Bell, A. G., communication on the telephone. <i>Abstract</i>	ii 103
a geometrical problem.....	v 88	binaural audition. <i>Abstract</i>	iii 68, 69
graphics.....	x 5	the spectrophone. <i>In full</i> . <i>Plate</i>	iv 142
Benjamin Alvord.....	vii 123	a modification of Wheatstone's microphone and its applicability to radiophonic researches. <i>In full</i> . <i>Plate</i> ,.....	iv 183
Balloon ascensions and air currents.....	i 35		
Bancroft, H. H., cited on diminution of Indians.....	ii 175		
Bank loans, Distribution of.....	iv 31		

	Page.		Page.
Bell, A. G., communications on—Cont'd.		Billings, J. S., communications on—Cont'd.	
fallacies concerning the deaf, and the influence of such fallacies in preventing the amelioration of their condition. <i>In full</i>	vi 48	the scientific work carried on under the direction of the National Board of Health. <i>Abstract</i>	iv 37
the mechanism of "clicks" and "clucks." <i>Title only</i>	viii 18	mortality statistics of the Tenth Census. <i>Abstract</i>	iv 163, 164
remarks on temperature observations.....	vi 47	the ventilation of the House of Representatives. <i>Abstract</i>	v 99
earthquake waves and sound waves.....	ix 42, 43	composite photography applied to cranialogy. <i>Abstract</i>	vii 25
Bellroth, cited on microscopic organisms,	ii 110	a collection of microscopes. <i>No abstract</i>	vii 73
Boman, Prof. W. W., Solution of a geometrical problem by.....	iii 65	the vital statistics of the Tenth U. S. Census. <i>Reference</i>	viii 4
Benedict, Prof. F. N., Survey by.....	ii 67	anthropometric and reaction-time apparatus. <i>Abstract</i>	viii 25
Benoit's coefficient of expansion of glass,	ix 32	germ cultures. <i>Abstract</i>	viii 30
Bentham and Hooker, cited on classification of plants.....	iv 108, 110, 113	museum specimens illustrating biology. <i>Abstract</i>	ix 35
Bergman, cited on mineralogy.....	i 78	scientific men and their duties. <i>Presidential address. In full</i>	ix xxxv, 46
Bernstein, cited on muscular contraction, nerve action.....	v 58, 61	remarks on mosquito inoculation.....	vi 10
Berzelius, cited on mineralogy.....	i 78, 79	bibliography.....	vii 72
Bessel's method for computing positions of satellites.....	vii 94	smell.....	viii 28
Bessels, Emil, communication on some of the results of the Polaris north pole expedition. <i>Title only</i>	i 92	care of pamphlets.....	viii 29
the hygrometrical condition of the air in high latitudes. <i>Title only</i>	ii 66	Charleston earthquake.....	ix 42
the late English polar expedition. <i>Abstract</i>	ii 89	Bi-metallism.....	iii 78, 107, iv 141
remarks on Arctic glaciers.....	ii 36	Binary arithmetic, Experiments in.....	vi 3, 38
Bibliographic notes on a geometrical problem.....	iii 64	Binaural audition.....	iii 69
Bibliography of astronomy.....	ii 95	Binocular microscopes.....	iv 35
Benjamin Alvord.....	vii 128	Biogen.....	v 102
S. F. Baird.....	x 62	Biography , List of papers on:	
Great Basin ranges.....	ix 6	on the life and scientific labors of the late Alexander Dallas Bache. J. Henry. <i>Reference</i>	i 35
Joseph Henry.....	ii 360	biographical notice of Archibald Robertson Marvine. J. W. Powell. <i>In full</i> ,	ii 83, (53)
Malfatti's problem.....	ii 120	life and character of Joseph Henry. J. C. Welling. <i>In full</i>	ii 203
medical medals.....	vi 40	a memoir of Joseph Henry. A sketch of his scientific work. W. B. Taylor. <i>In full</i>	ii 203, 230
meteorology.....	x 20, 23	address commemorative of Joseph Henry. P. Parker. <i>In full</i>	ii 368
North American geology.....	vii 71	[address commemorative of] Joseph Henry. B. Alvord. <i>In full</i>	ii 370
G. A. Otis.....	iv 181	[remarks commemorative of Jonathan Homer Lane.] J. E. Hilgard. <i>In full</i>	iii 122
science.....	ii 302, x 38	a biographical sketch of the late Dr. [G. A.] Otis. J. J. Woodward. <i>In full</i>	iv 171
trisection problem.....	x 97, 98	[eulogy on A. A. Humphreys.] J. C. Welling. <i>Abstract</i>	vii 4
Bigelow, Dr., cited on gaseous disinfection.....	iv 38	memorial [to Benjamin Alvord.] M. Baker and E. B. Elliott. <i>In full</i>	vii 127
Billings, J. S., communication on some minute fungi. <i>Abstract</i>	i 42		
the collection of a large library. <i>Abstract</i>	ii 92		
bacteria and spontaneous generation. <i>Abstract</i>	ii 109		
the work of the National Board of Health. <i>Title only</i>	iii 50		

	Page.		Page.
Biography , List of papers on—Cont'd.		Boss' declination standards.....	ix 53
relations between Professor Baird and participating societies. G. Mallory. <i>In full</i>	x 45	Botany , List of papers on. (See also <i>Botany</i> :)	
Professor Baird as an administrator. W. B. Taylor. <i>In full</i>	x 49	on some minute fungi. J. S. Billings. <i>Abstract</i>	i 42
Professor Baird in science. W. H. Dall. <i>In full</i>	x 61	descriptions of new species of fossil plants from Alleghany Co., Virginia; with some remarks on the rock seen along the Chesapeake and Ohio Railroad, near the White Sulphur Springs of Greenbrier County, West Virginia. F. B. Meek. <i>Read by T. Gill. In full. 2 plates</i>	i 62, ii (26)
the personal characteristics of Professor Baird. J. W. Powell. <i>In full</i>	x 71	on the cause and remedy of the potato rot. L. D. Gale. <i>Title only</i>	i 97
Biological Society, Invitation from.....	viii 5, viii 4	[plants common to Japan and eastern America.] A. Gray. <i>Abstract</i>	ii 42
Biological Society of Washington.....	x 47	the climate of plants. L. D. Gale. <i>Abstract</i>	ii 183
Biology , List of papers on. (See also <i>Zoology and Botany</i> :)		the natural system of plants. L. F. Ward. <i>Title only</i>	ii 186, 187
bacteria and spontaneous generation. J. S. Billings. <i>Abstract</i>	ii 109	field and closet notes on the flora of Washington and vicinity. L. F. Ward. <i>Abstract</i>	iv 64
principles of morphology. T. Gill. <i>Reference</i>	iv 123	on the compass plant. B. Alvord. <i>Reference</i>	v 106
modern philosophical conceptions of life. J. J. Woodward. <i>Presidential address. In full</i>	v 49	the flora of the Laramie group. L. F. Ward. <i>Reference</i>	viii 17
on the organic compounds in their relations to life. L. F. Ward. <i>Title only</i>	v 91	our city shade-trees, their foes and their future. C. V. Riley. <i>Reference</i>	x 7
on the building up of organic matter. T. Antisell. <i>Title only</i>	v 97	on the geographical distribution of fossil plants. L. F. Ward. <i>Reference</i>	x 28
on the possibilities of protoplasm. E. Coues. <i>Abstract and reference</i>	v 102	Boundary line between Alaska and Siberia.....	iv 123
the three methods of evolution. J. W. Powell. <i>Presidential address. In full</i>	vi xxvii, 110	Boutelle, C. O., remarks on deflection of rivers.....	vii 24
germ cultures. J. S. Billings. <i>Abstract</i>	viii 30	Bowditch, N., and the Mecanique Celeste.....	viii xxxvi
organic cells of unknown origin and form found in human faeces (two cases). N. L. Bates. <i>Title only</i>	ix 35	Bowyers and fletchers.....	ix 44
on museum specimens illustrating biology. <i>Symposium. Abstract</i>	ix 35	Boyle, R., cited on atomic philosophy.....	vii xlv
Black drop.....	ii 199, vi 23	Boyle's law.....	v 139
Black Hills of Dakota.....	iii 125	Brachisthode.....	vi 124
Blair, H. W., Death of.....	vii 81	on the helicoid.....	x 90
Blindness, Color.....	iv 54	Brain and phosphorus.....	v 75
Blood corpuscles of man and other animals compared.....	ii 20, 41	temperatures.....	v 75
Blue Ridge, Fault in.....	vi 30	Brainard's Arctic exploration.....	ix 11
Board of Health, National.....	iv 37	Bremiker, Dr., cited on alignment curves.....	vi 124, 126
Boerner, C. G., letter on a shower of the Rocky Mountain grasshoppers. <i>Communicated by J. Henry. Abstract</i>	ii 87	Brewer, Prof. W. H., remarks on the potato rot.....	i 97
Bogosloff crater.....	vii 34	Brianchon, cited on Feuerbach's circle.....	viii 45
Bolton, Prof. H. C., communication on counting-out rhymes of children, their antiquity, origin, and wide distribution. <i>Reference</i>	x 13	Brooks, W. K., communication on the embryology of <i>Lingula</i> and the systematic relations of the Brachiopods. <i>Title only</i>	iii 33
Bonneville, Lake.....	i 84, ii 103		
Boscovich's philosophy of matter.....	vii xlv, 49		

	Page.
Brown, Judge A., cited on difficulty of determination of sound direction.....	viii 12
Brown, W. R., cited on conservation of energy.....	vii 62
force and matter.....	vii 31
Buccinum undatum.....	iii 75
Buchan, cited on barometric pressures.....	i 108
Bulletin, Cost of printing.....	v 177
Distribution list of.....	iii 159
of the Mathematical Section.....	vi 121, vii 87, viii 37, ix 53, x 79
of the Society, Function of the.....	i x
Rules for publication of.....	i ii, ii vii, iii vii, iv 13, v 13, vi xxxiii, 135, vii xiii, viii xiii, ix xiii, x xiii
Bulletins, Note on.....	x 113
Bulwer, J., cited on visible speech.....	vi 54
Buoys, Drifting.....	vii 14
Burchard, H. N., communication on the silver question. <i>Abstract</i>	iii 109
remarks on agricultural production.....	vii 20
Burdon, W., Solution of a geometrical problem by.....	iii 64
Bureau of Ethnology.....	x 57
Burger, Franz, Electric investigations by.....	v 47
Burnett, S. M., communication on color perception and color blindness. <i>Abstract and reference</i>	iv 54
refraction in the principal meridians of a triaxial ellipsoid; regular astigmatism and cylindrical lenses. <i>Reference</i>	vi 4
the character of the focal lines in astigmatism. <i>Abstract</i>	vi 45
why the eyes of animals shine in the dark. <i>Abstract and reference</i>	vii 13
Are there separate centres for light, form-, and color-perception? <i>Abstract and reference</i>	vii 72
the Javal and Schiötz ophthalmometer. <i>Title only</i>	viii 11
Busey, S. C., communication on the gathering, packing, transportation, and exposure of fruits for sale. <i>Title only</i>	ii 16
the influence of the cardiac and respiratory movements upon the motion of the lymph. <i>Abstract and reference</i>	ii 133
the relation of the meteorological conditions to the summer diarrhoeal diseases. <i>Abstract and reference</i>	iv 165
the influence of the constant use of high-heeled shoes upon the health and form of the female, and upon the relation of the pelvic organs. <i>Abstract</i>	v 117
Butcher, H. B., communication on two immense meteorites at Conception and San Gregorio, Mexico. <i>Reference</i>	i 24

	Page.
Butler, J. D., communication on prehistoric copper. <i>Title only</i>	ii 185
Byasson, H., cited on phosphorus and cerebral activity.....	v 75
By-Laws. See <i>Standing Rules</i> .	
Calcium sulphide, Clock faces coated with,.....	iii 33
Calendar of the Society.....	vii xxii, viii xxx, ix xxvii, x xxxi
Calendars and Time Standards, List of papers on:	
on a Gregorian calendar. E. Frisby. <i>Abstract</i>	i 75
on a proposed reformation of the Gregorian calendar. J. E. Hilgard. <i>Abstract</i>	ii 29, 30
calendar formulæ. E. B. Elliott. <i>Abstract</i> ,.....	ii 37
a calendar proposed by a Persian astronomer in 1079. W. B. Taylor. <i>Abstract</i>	ii 38
adjustment of the calendar. E. B. Elliott. <i>Abstract</i>	ii 59
standards of time—international, sectional, and local. E. B. Elliott. <i>Abstract</i>	ii 137
meridional time for railway and telegraphic purposes. E. B. Elliott. <i>Abstract</i>	ii 202
on a system of standard time. A. S. Christie. <i>Abstract</i>	v 112
the action of the International Geodetic Association as to an initial meridian and universal time. R. D. CUTTS. <i>Abstract</i>	vi 106
California, Geology of northern.....	ix 4
Latest volcano in.....	ix 46
Cambrian system in the United States and Canada.....	vi 98
Campagna, Eucalyptus on the.....	vi 36
Capron, Horace, communication on Japan. <i>Title only</i>	ii 79
Death of.....	viii 8
Carbonate deposits of Leadville, Colo.....	vi 32
Care of pamphlets.....	viii 29
Carpenter, Dr. W. B., cited on binocular microscopes.....	iv 35
Cartesian philosophy.....	vii xli
Caspian Sea, Altitude of.....	ii 34
Catalogue of astronomical papers.....	ii 95
of stars prepared at U. S. Naval Observatory.....	i 74
Catlin, cited on color, number, and theology of Indians.....	ii 175
Cells found in human feces.....	ix 35
Census, Mortality statistics of the Tenth,.....	iv 164

	Page.		Page.
Census, Vital statistics of the Tenth.....	viii 4	Chemistry, List of papers on—Cont'd.	
Centre of population of United States.....	i 35	observations on chemical molecular	
United States.....	i 22	changes. T. Antisell. <i>Title only</i>	iii 28
Centres for light-, form-, and color-percep-		the origin of the chemical elements. L.	
tion.....	vii 72	F. Ward. <i>Title only</i>	iii 33
Ceremonial institutions, Origin of certain.....	ix 19	a case of peculiar corrosive action on me-	
Cernuschi, cited on bi-metallism.....	iii 108	tallic tin. J. W. Osborne. <i>Title only</i>	iii 44
Chadwick, Lt. Com'd'r F. E., cited on sound		determination of the specific gravity of	
anomalies.....	v 34	solids by the common hydrometer.	
Challis, Prof. J., cited on elasticity.....	v 152, 154	C. E. Munroe. <i>In full</i>	vi 26
force.....	v 128	the periodic law of chemical elements. F.	
Chamberlin, T. C., communication on What		W. Clarke. <i>Abstract</i>	vii 15
is a glacier? <i>Abstract</i>	vii 38	music and the chemical elements. M. H.	
the varying attitudes of former level		Doolittle. <i>Abstract</i>	vii 26, 27
surfaces in the Great Lake region and		an attempt at a theory of odor. F. W.	
the applicability of proposed explana-		Clarke. <i>Abstract</i>	vii 27
tions. <i>Title only</i>	ix 15, 16	Chickering, J. W., communication on the	
remarks on the loess of Iowa and Ne-		correlation of the winds and the tem-	
braska.....	iv 121	peratures of the surface waters of the	
Champlain, Ice on Lake.....	ii (22)	ocean along the coast of New Hamp-	
Changes of terrestrial level surfaces due to		shire. <i>Abstract</i>	ii 17
variations in the distribution of super-		Luray cave. <i>Title only</i>	ii 65
ficial matter.....	vii 92, 101, ix 15, 53	Roan Mountain, N. C. <i>In full</i>	iv 60
Chapman's Flora of the Southern States,		the thermal belts of North Carolina. <i>Ab-</i>	
iv 99		stract.....	vi 11
Charles, Law of.....	v 139	the Muir glacier, Alaska. <i>Title only</i>	x 15
Charleston earthquake.....	ix 37, 38, x 17, 28	Chesapeake and Ohio Railroad, Geology	
Charts of archæology.....	ii 72	along.....	ii (26)
Chase, Salmon P., Resolutions on death of.....	87	Chesapeake Bay geology.....	x 16
Chatard, T. M., remarks on earth tremors,		Chico group in Northern California.....	ix 4
viii 28		Chimæra, New species of.....	ii 182
Chemical equivalency.....	vii xlvii	Chinese language.....	ii 28
rays.....	v 135	Chitonidæ.....	ii 103
side of vitality.....	v 53	Chlamydoconcha Orcuttii.....	viii 5
Society, Invitation from.....	viii 29, ix 46	Chorography.....	x 14
theory of volcanism.....	vi 90, 93	Christie, A. S., communication on a system	
Chemistry, List of papers on:		of standard time. <i>Abstract</i>	v 112
[exhibition of apparatus for the genera-		a quasi general differentiation. <i>Title</i>	
tion of ozone.] H. F. Craig. <i>No ab-</i>		only.....	vi 122
stract.....	i 52	contact of plane curves. <i>Abstract</i>	vi 157
on the cause and remedy of the potato rot.		a form of the multinomial theorem.	
L. D. Gale. <i>Title only</i>	i 97	<i>Title only</i>	vii 101
on the chemistry of the Bessemer pro-		a problem in probabilities. <i>Abstract</i>	x 89
cess. C. E. Dutton. <i>Title only</i>	i 98	remark on infinitesimals.....	vi 135
on the atomic volumes of crystallized and		Christmas eve meteor.....	ii 139
double salts. F. W. Clarke. <i>Refer-</i>		Chronograph readings, Relative frequency	
ence.....	i 103	of digits in.....	i 85
on the molecular heats of similar com-		Circle, Quadrature of.....	i 57
pounds. F. W. Clarke. <i>Abstract</i>	i 104	Circles related to Feuerbach's circle.....	viii 45
on the coloring agent of gems. F. M. End-		Circular on the meteor of Dec. 24, 1873.....	ii 139
lich. <i>Abstract</i>	ii 31	Circumference, Ratio of, to diameter.....	i 57
the estimation of manganese as pyrophos-		Clark, Alvan, communication on the con-	
phate. C. E. Munroe. <i>Communicated</i>		struction of the lenses and other inter-	
by T. Antisell. <i>Reference</i>	ii 132	esting portions of the large telescope	
chemical remarks on terrestrial geogony.		now established at the Naval Observa-	
T. Antisell. <i>Title only</i>	ii 132, 133, 134	tory. <i>Title only</i>	i 92

	Page.
Clarke, F. W., communication on the atomic volumes of crystallized and double salts. <i>Reference</i>	103
the molecular heats of similar compounds. <i>Abstract</i>	104
the periodic law of the elements. <i>Abstract</i>	15
topaz from Stoneham, Maine. <i>Abstract and reference</i>	5
an attempt at a theory of odor. <i>Abstract</i>	27
the Flood Rock explosion. <i>Abstract</i>	28
the present status of mineralogy. <i>Title only</i>	6
the Manchester meeting of the British Association for the Advancement of Science, 1887. <i>Title only</i>	19
remarks on chemical theories of volcanism.....	93
Classification of insectivorous mammals ...	118
literature of meteorology.....	26
plants.....	108
Clausen, cited on computation of π	58
Clausius' researches in molecular physics,	138, 140
Clerk-Maxwell. See <i>Maxwell</i> .	
Clifford's philosophy.....	liii
Climate and variations in solar radiation.....	10
of plants.....	183
of Roan Mountain.....	62
Quaternary, of the Great Basin.....	21
Climatic influence of land areas.....	46
Clingman, T. L., communication on the earthquake phenomena recently experienced in North Carolina. <i>Abstract and reference</i>	104
the falling of waterspouts in North Carolina. <i>Abstract</i>	104
Cloud bursts in North Carolina.....	104
Coal, Formation of.....	28
Coastal plains.....	23
Coffin, J. H. C., cited on cyclonic motion... communication on maps prepared by G. W. Hill for use in connection with the transit of Venus in December, 1874. <i>Reference</i>	108
Sumner's method in navigation. <i>In full</i>	105
remarks on calendars.....	29, 60
standard time.....	202, 115
Cohesion.....	127
and adhesion.....	136
Coin, Amount of subsidiary silver.....	14
Coinage, International.....	38
of the Argentine Republic.....	65
Coincidences.....	8

	Page.
Coins, Exhibition of.....	22
Collier, Peter, communication on sugar from sorghum. <i>Abstract</i>	140
Color of Indians.....	175
perception and color blindness.....	54
tests.....	54
Colorado of the West, Valley of the.....	48
Coloring agent of gems.....	31
Columnar structure in the diabase of Orange Mt., N. J.....	19
Comet, Barnard's.....	17
Encke's.....	34, 35
I, 1871, Elements of.....	23
III, 1834, (Wolf's).....	37
Orbit of Swift's.....	59
orbits illustrated by models.....	23
Spectrum of Encke's.....	34
Tuttle's.....	34
Comets and meteors.....	94
Comet's orbit, Correction of.....	22
Comets' tails.....	74
Committee, auditing, Appointment of.....	84, 174, vi 111, vii 82, viii 31, ix 47, x 39.
Report of.....	89, vi 5, vii 15, viii 3, ix 3, x 3.
Resolution on.....	84
on communications.....	21, ii viii, 161, iii 151, iv 31, 39, v 14, 175, vi xiv, xv, vii xiv, xv, viii xiv, xv, ix xiv, xv, x xiv, xv.
on mathematical papers.....	135, 161, vii 129, viii 63, x 111
on mathematical papers, Resolution on.....	135
on the meteor of December 24, 1873.....	94, 98, ii 139
on papers and essays. See <i>Committee on Communications</i> .	
on publications.....	21, ii viii, 161, iii 151, v 14, 175, vi xiv, xv, vii xiv, xv, viii xiv, xv, ix xiv, xv, x xiv, xv.
to draft resolutions on the death of	
L. Agassiz.....	93, 94
F. B. Meek.....	111
A. B. Eaton.....	111
C. H. Davis.....	111
T. Bailey.....	111
J. Henry.....	196
A. R. Marvin.....	83
B. Peirce.....	21, 23
A. J. Myer.....	23, 31
G. A. Otis.....	120, 134
to draft resolutions on the discovery of the satellites of Mars.....	186
to nominate officers of Mathematical Section.....	x 83
Communications, List of. See <i>Acoustics, Anatomy, Anthropology, Archæology, Astronomy, Biography, Biology, Botany,</i>	

	Page.		Page
<i>Calendars, Chemistry, Electricity, Geography, Geology, Mathematics, Meteorology, Microscopy, Mineralogy, Miscellaneous, Oceanography, Optics, Physics, Political Economy, Psychology, Seismology, Social Science, Thermometry, Zoology.</i>			
Statistics of.....	x 32	Craig, B. F., communication on—Cont'd.	
Compass plant.....	v 106	apothecaries' weights and measures.	
Composite photography applied to cran-		<i>Title only</i>	i 34
iology.....	vii 25	thermometers. <i>Title only</i>	i 42
Composition of error.....	v 106	a method of verifying with exactness the	
Computation by method of least squares.....	i 62,	indications of a thermometer. <i>Title</i>	
	vi 160, viii 41	<i>only</i>	i 43
of a comet's orbit.....	ii 22	apparatus for the generation of ozone.	
planetary perturbations of the moon		<i>No abstract</i>	i 52
	vi 136	the water supply of cities. <i>Title only</i>	i 65
Computing the position of a satellite.....	vii 93	Resolutions on the death of.....	ii 130
machine.....	x 102	Craig, Thomas, communication on vortex	
Comte, Auguste, cited on forces.....	v 127	motion in ordinary fluids. <i>Reference,</i>	
Conditioned observations, Adjustment of,			iii 143
	viii 41	Crane, C. H., Death of.....	vi 41
Conservation of energy.....	vii 62	Craniology.....	vii 25
force.....	i 27	Crelle, Dr. A. L., cited on Malfatti's prob-	
Conservative element in disease.....	ii 111, 124	lem.....	ii 115
Consolidated list.....	x 36	Croll, Prof. J., cited on action at a distance	
Constant <i>P</i> in terrestrial magnetism.....	x 102		v 156
Constitution... i xv, ii lii, iii lii, iv 5, v 6, vi vii,		Croll's theory.....	ii 43, 45
vii vii, viii vii, ix vii, x vii		Crookes, W., cited on matter.....	v 129
Adoption of.....	i 20, 21	Crookes' radiometer.....	ii 80
Amendment to.....	ix 47, x 39	Cross Timbers of Texas.....	x 6
Contact of plane curves.....	vi 157	Crumpling of the earth's crust.....	viii 18
Contraction hypothesis.....	vi 90, viii 18	Crystalline state of matter.....	iii 39
Corona of the sun.....	i 31, iii 116, 121	Culture media.....	viii 30
Corrections to normal thermometers.....	ix 28	Cumberland plateau.....	ix 24
Corrigenda... ii p. 4 of cover, iii 148, vi 162, x 114		Currents shown by drifting buoys.....	vii 14
Coseismic map.....	ix 39	Curtis, G. E., communication on the rela-	
Cosmos assembly hall.....	x xxxi, 10, 31	tions between northers and magnetic	
Cosmos Club, Organization of.....	x 47	disturbances at Havana. <i>Reference,</i>	
Cotes, Roger, cited on ultimate causes.....	v 163		vii 25
Cones, Elliott, cited on Baird's "Birds of		Lieutenant Lockwood's expedition to	
North America".....	i 65	farthest north. <i>Abstract</i>	ix 8
poisoned wounds from arrows.....	ii 182	the theory of the wind-vane. <i>Refer-</i>	
communication on the structure and		<i>ence</i>	x 0
homologies of the limbs, especially in		a problem in probabilities. <i>No ab-</i>	
Aves. <i>Title only</i>	i 96	<i>stract</i>	x 88
the use of poisoned arrows by North		solutions of the trisection problem. <i>Ab-</i>	
American Indians. <i>Title only</i>	ii 183	<i>stract</i>	x 98
the possibilities of protoplasm. <i>Abstract</i>		remarks on verification of weather pre-	
<i>and reference</i>	v 102	dictions.....	viii 9
remarks on poisoned arrows.....	ii 183	Curtis, Josiah, letter on Hayden's Survey.	
Counting-out rhymes.....	x 13	<i>Communicated by E. B. Elliott. No ab-</i>	
Cracks in ice on Lake Champlain.....	ii (22)	<i>stract</i>	i 63
Craig, B. F., communication on the fluctua-		Death of.....	vi 41
tions of the temperature of the human		Curve of the fourth degree.....	i 30
body. <i>Reference</i>	i 31	Curves, Alignment.....	i 123
		Contact of plane.....	vi 157
		similar to their evolutes.....	vi 87
		Customs of every day life.....	ix 19
		Cutts, R. D., communication on the misap-	
		plication of geographical terms, as	
		bearing especially on the question of	
		the fishery right treaties. <i>Abstract</i> ... i 39	

	Page.
Cutts, R. D., communication on—Cont'd.	
the results of astronomical observations at Sherman Station, Wyoming Terr.	
<i>Abstract and reference</i>	70
the action of the International Geodetic Association as to an initial meridian and universal time. <i>Abstract</i>	106
Death of.....	111
Cyclones, Movement of.....	99
Retardation of.....	103
Cyclonic storms, Laws of.....	106
Dakota, Black Hills of.....	125
calendar.....	90
Dall, W. H., communication on the relative value of Alaska to the United States, as compared with that of other territorial acquisitions. <i>Abstract and reference</i>	25
elevations and depressions in Alaska. <i>No abstract</i>	27
the succession of the strata of the shell heaps of the Aleutian islands. <i>Abstract</i>	65
the results of recent investigations into the natural history of the Chitonidæ. <i>Abstract</i>	193
the museums and zoological gardens of Northern Europe. <i>Title only</i>	19, 21
the muscles of the oyster. <i>Abstract</i>	36
the deep sea dredgings in the Gulf of Mexico and the West Indies in 1873-1878, by Professors Louis and Alexander Agassiz and the officers of the U. S. Coast Survey. <i>Title only</i>	45
some recent observations on mollusks. <i>Abstract</i>	75
the boundary line between Alaska and British America. <i>Title only</i>	77
recent discoveries in Alaska north of Behring Strait. <i>Abstract</i>	163
some peculiar features of mollusks found at great depths. <i>Abstract</i>	90
glaciation in Alaska. <i>Abstract</i>	33
recent advances in our knowledge of the limpets. <i>Abstract</i>	4
certain appendages of the mollusca. <i>Reference</i>	32
What is a glacier? <i>Abstract</i>	38
two remarkable forms of mollusks. <i>Abstract and reference</i>	5
South Florida notes. <i>Title only</i>	x
Professor Baird in science. <i>In full</i>	x
remarks on the glacial period.....	36
Arctic tides.....	89
teredo borings.....	98
glaciation and climate.....	11

	Page.
Dall, W. H., remarks on—Cont'd.	
tornadoes.....	vii 3
drifting buoys.....	vii 15
deflection of rivers.....	vii 24
the Bogosloff eruption.....	vii 34
Arctic exploration.....	ix 12
Dalton's atomic philosophy.....	vii xvii
law.....	v 139
Dana, J. D., cited on mineralogy.....	1 78, 79
Darton, N. H., communication on the occurrence of copper ore in the Trias of the Eastern United States. <i>Title only</i>	ix 46
Darwin's doctrine of gemmules.....	vii liii
law of the distribution of volcanoes.....	ii 89, 91
Dase, cited on computation of π	i 53
Davidson, George, letter on transit of Venus, 1874. <i>Communicated by Asaph Hall. Abstract</i>	ii 32
Davidson, Lieut., cited on the co-ordinates of Bald Head, Alaska.....	iv 126
Davis, C. H., Death of.....	ii 111
Dawson, Prof. J. W., cited on fossil plants from Virginia.....	ii (38), (42)
Deaf mutes, Fallacies concerning.....	vi 48
Languages of.....	iv 55
Death of L. Agassiz.....	i 93
B. Alvord.....	vii 72, 127
O. E. Babcock.....	vii 72
S. F. Baird.....	x 17, 20 43, 76
T. Bailey.....	ii 109, 111
H. W. Blair.....	vii 81
H. Capron.....	viii 8
S. P. Chase.....	i 87
B. F. Craig.....	ii 130
C. H. Crane.....	vi 41
J. Curtis.....	vi 41
R. D. Cutts.....	vi 111
C. H. Davis.....	ii 111
A. B. Eaton.....	ii 111
E. Foote.....	vi 48
L. D. Gale.....	vi 48
W. R. Hazen.....	x 6
J. Henry.....	ii 196, 203, 214, 358, 370
Mrs. J. Henry.....	v 97
F. B. Hough.....	viii 25
A. A. Humphreys.....	vii 3, 4
F. Kampff.....	ii 189
W. C. Kerr.....	viii 25
J. H. Lane.....	iii 122
E. P. Lull.....	x 8
A. R. Marvinne.....	ii 83, (53)
F. B. Meek.....	ii 111
A. J. Myer.....	iv 23, 31
G. A. Otis.....	iv 120, 134, 171
T. R. Peale.....	viii 10
B. Peirce.....	iv 21, 23

	Page.		Page.
Death of—Cont'd.		Discontinuity in elliptic orbits.....	vii 122
J. C. Riley.....	iii 28	Discovery of the satellites of Mars.....	ii 186
J. Rodgers.....	v 102	Disease and climate.....	iv 164
B. F. Sands.....	vi 41	Conservative element in.....	ii 111, 125
G. C. Shaeffer.....	i 90	Disinfection by gases.....	iv 38
W. J. Twining.....	v 102	of ships.....	iii 51
J. J. Woodward.....	vii 72, 75	Dismal Swamp, Geology of.....	vi 28
M. Yarnall.....	iii 28	Displacement, Geologic.....	ii 75
Declination standards.....	ix 53	of the middle Atlantic slope.....	x 16
Deep sea mollusks.....	v 90	Dissipation of energy.....	vii 63
Definitions.....	vii 46	Distances on any spheroid.....	viii 52
Degradation. See <i>Erosion</i> .		Distribution of fossil plants.....	x 28
Delgarno, G., cited on instruction of the dumb.....	vi 71	mammals.....	ii 26
Delta of the Mississippi river.....	i (10)	scientific men and institutions.....	x 7
Democritus' philosophy.....	vii xxxiv	the surplus money of the United States among the States.....	vi 103
<i>De nihilo nihil fit</i>	vii xxx, xxxiii	District of Columbia, Flora of.....	iv 64
Denver, Altitude of.....	ii 24	Diurnal variation of magnetic declination,	iii 46
Department of science.....	ix xlv	Dixwell, G. B., communication on cylinder condensation, steam jackets, and super- heated steam. <i>Title only</i>	ii 64
Depauperation of Limnæa.....	iii 75	Doane, G. C., report of the Yellowstone ex- pedition of 1870. <i>Communicated by S.</i> <i>F. Baird. Reference</i>	i 21
Derham, Dr. W., cited on echoes.....	v 41	Dobson, Surgeon-Major, cited on insectivorous mammals.....	v 118, 120
De Tocqueville, cited on destruction of In- dians.....	ii 175	Dog, Malformed.....	ii 185
Device for viewing the sun by light of any desired wave length.....	x 13	Doolittle, M. H., communication on the ne- bulular hypothesis and the inner moon of Mars. <i>Abstract</i>	ii 188, 190
Devonian strata near Sulphur Springs, W. Va.....	ii (27)	the influence of aerolites on planetary motion. <i>Abstract</i>	ii 190
Dewar, Prof., cited on the radiometer.....	ii 81	aerolithic disturbance of planetary mo- tions. <i>Abstract</i>	ii 190
Diagnosis of blood-stains.....	ii 20, 41	a pile of balls. <i>Abstract</i>	iii 76
Diarrhoeal diseases and weather.....	iv 165	the silver question. <i>Abstract</i>	iii 103, 112
Diatonic scale.....	vii 26	the geometrical problem to determine a circle equally distant from four points. <i>Abstract</i>	v 88
Differential equations admitting periodic integrals.....	x 100	substance, matter, motion, and force. <i>Title only</i>	vi 14
Diffraction fringes.....	iii 119	infinite and infinitesimal quantities. <i>Abstract</i>	vi 133
phenomena in the field of the micro- scope.....	ii 60	the rejection of doubtful observations. <i>Abstract</i>	vi 152
Diller, J. S., communication on the volcanic sand which fell at Unalashka October 20, 1883, and some considerations con- cerning its composition. <i>Abstract</i>	vii 33	music and the chemical elements. <i>Abstract</i>	vii 26, 27
topaz from Stoneham, Maine. <i>Abstract</i> and reference.....	viii 5	the verification of predictions. <i>Ab-</i> <i>stract</i>	vii 122
the geology of northern California. <i>Ab-</i> <i>stract</i>	ix 4	cause and chance in the concurrence of phenomena. <i>Title only</i>	viii 54
the latest volcanic eruption in northern California and its peculiar lava. <i>Refer-</i> <i>ence</i>	ix 46	What is topography? <i>Abstract</i>	x 14
Mount Shasta contrasted with Mount Rainier. <i>No abstract</i>	x 11	Newton's vis. <i>Title only</i>	x 38
remarks on geology of Cascade Moun- tains.....	ix 8	association ratios. <i>Abstract</i>	x 83
Kraakatoan dust.....	vii 35	a problem in probabilities. <i>Abstract</i>	x 88
Diorthode.....	vi 123		
Diphtheria, Inoculation of.....	iv 38		
Direction of sound, Determination of.....	iii 69, viii 12, ix 43		

- | | Page. | | Page. |
|--|------------------|---|------------|
| Doolittle, M. H., communication on—Cont'd. | | Dutton, C. E., communication on—Cont'd. | |
| association ratios. <i>Abstract</i> | x 93, 94 | the geological character of the Colorado | |
| remarks on sesquisection..... | viii 52 | river. <i>Title only</i> | iii 28 |
| gravitation formula..... | viii 40 | the succession of volcanic eruptions. | |
| phonetic alphabet..... | ix 19 | <i>Title only</i> | iii 36, 37 |
| bi-metallism..... | iii 103 | the Permian formation of North Amer- | |
| the need of a biometer..... | v 105 | ica. <i>Abstract</i> | iii 65, 67 |
| binary arithmetic..... | vi 39 | the silver question. <i>In full</i> | iii 78 |
| Dorsey, J. Owen, communication on the | | the scenery of the Grand Cañon district. | |
| gentile system of the Omahas. <i>In full</i> . | | <i>Title only</i> | iv 120 |
| 3 figures..... | iii 128 | the Vermilion cliffs and the valley of | |
| Drainage system and loess of eastern Iowa, | | the Virgen in southern Utah. C. E. | |
| | vi 93 | Dutton. <i>Title only</i> | iv 122 |
| of the Black Hills..... | iii 125 | the geology of the Hawaiian islands. | |
| systems..... | i 49 | <i>Abstract</i> | vi 13 |
| Draper, Prof. J. W., cited on photography...i | 47 | the volcanic problem stated. <i>Abstract</i> , | |
| radiant energy..... | v 135 | | vi 87 |
| Dreams in their relation with psychology...vi | 37 | What is a glacier? <i>Abstract</i> | vii 39 |
| Driftless region. | vi 94 | the volcanoes and lava fields of New | |
| Drift of Iowa and Nebraska..... | iv 120 | Mexico. <i>Abstract</i> | vii 76 |
| Dry painting of the Navajos..... | viii 14 | practical geology <i>versus</i> speculative | |
| Duane, Gen., cited on fog signals..... | v 32, 43 | physics. <i>Title only</i> | viii 4, 5 |
| phenomena of sound..... | ii (49), (50) | a recent visit to the scene of the Charles- | |
| Du Bois-Raymond, Experiments in animal | | ton earthquake and resulting conclu- | |
| electricity by..... | v 57, 60, 61, 62 | sions. <i>Title only</i> | x 16 |
| Dudley, P. H., communication on the uses | | the depth of earthquake foci. <i>Abstract</i> , | |
| of the dynagraph, and the work per- | | 1 figure..... | x 17 |
| formed in determining the resistance | | the speed of propagation of the Charles- | |
| of trains, etc. <i>Abstract</i> | iii 29 | ton earthquake. <i>Reference</i> | x 28 |
| Dulong and Petit, Law of..... | v 139 | remarks on distribution of volcanic ac- | |
| Thermometric experiments of..... | v 91, 93 | tion..... | i 102 |
| Dumbness of deaf children..... | vi 43 | wind and temperature observations.... | ii 18 |
| Du Pré, Warren, cited on earthquakes.....i | 101 | refraction of sound..... | ii 58 |
| Dutton, C. E., communication on the meas- | | geology of the Colorado region..... | ii 76 |
| urement of the pressure developed by | | the earth's interior..... | ii 77 |
| the explosion of gunpowder in fire- | | charcoal in the drift..... | iv 122 |
| arms. <i>Title only</i> | i 52 | separation of minerals by density..... | vi 27 |
| some recent experiments on different | | nebular hypothesis..... | vi 45 |
| kinds of gunpowder at Fortress Mon- | | temperature observation..... | vi 43 |
| roe. <i>Title only</i> | i 54 | outlines of continents..... | vii 24 |
| the causes of the elevations and subsi- | | sun glows..... | vii 35 |
| dences of the earth's surface. <i>Title</i> | | Indian observation of nature..... | vii 74 |
| <i>only</i> | i 74 | earthquake detonations..... | viii 28 |
| geological time. <i>Title only</i> | i 89 | Charleston earthquake..... | ix 42 |
| Mallet's theory of the formation of the | | Dynagraph, The..... | iii 29 |
| physical features of the earth. <i>Title</i> | | Dyaamic hypothesis..... | vi xxx |
| <i>only</i> | i 90 | theories of force..... | v 126 |
| recent improvements in the economy of | | | |
| fuel. <i>Title only</i> | i 96 | Eastman, J. R., cited on individual vocabu- | |
| recent improvements in the manufact- | | laries..... | ii (21) |
| ure of steel. <i>Title only</i> | i 97 | communication on a comparison of the | |
| the chemistry of the Bessemer process. | | thermometers used to determine the | |
| <i>Title only</i> | i 98 | correction for atmospheric refraction | |
| the glacial period. <i>Title only</i> | i 26 | at the U. S. Naval Observatory. <i>Ab-</i> | |
| the causes of glacial climate. <i>Abstract</i> , | | <i>stract</i> | i 68 |
| | ii 43, 45 | | |

	Page.		Page.
Eastman, J. R., communication on—Cont'd.		Electricity , List of papers on (See also	
the frequency of the occurrence of the		<i>Acoustics</i>):	
zero and the nine digits in the tenths		on the recording systems of the trans-	
of seconds as obtained from the chro-		atlantic cables. J. E. Hilgard. <i>Title</i>	
nographic record of transit observa-		<i>only</i>	53
tions. <i>Abstract</i>	85	[a method of lighting gas jets by electric-	
the comparison of rain-gauges at differ-		ity.] Dr. Van Sant. <i>No abstract</i>	56
ent elevations. <i>Abstract</i>	49	on electricity engendered by the driving	
a personal equation instrument. <i>Ab-</i>		belt of the machinery for ventilating	
<i>stract</i>	33, 37	the Capitol at Washington. J. Henry.	
some results from the discussion of the		<i>Abstract</i>	40
observations of the transit of Mercury		Jablokoff's electric candle. J. E. Hilgard.	
of May 6, 1878. <i>Abstract</i>	43	<i>Title only</i>	19
the Florida expedition for observation		large area illumination by electricity. E.	
of the transit of Venus [1882]. <i>Ab-</i>		B. Elliott. <i>Title only</i>	45
<i>stract</i>	21	the storage of electric energy. C. H. Koyl.	
the Rochester (Minnesota) tornado. <i>Ab-</i>		<i>Abstract</i>	46
<i>stract</i>	3	units of force and energy, including elec-	
a new meteorite. <i>Abstract</i>	32	tric units. E. B. Elliott. <i>Title only</i> ,	
remarks on vocabularies.....	28	<i>vi</i>	137
Eaton, A. B., communication on the preser-		electric lighting. E. B. Elliott. <i>Title only</i> ,	
vation of foods. <i>Title only</i>	22	<i>vii</i>	80
Death of.....	111	[exhibition of a volt-meter.] T. C. Men-	
Eaton, Prof., cited on classification of ferns,		denhall. <i>Abstract</i>	26
<i>iv</i>	110	the electrometer as used in observations	
Earth, Interior of.....	76	of atmospheric electricity. C. F. Mar-	
tremors as shown by astronomical obser-		vin. <i>Title only</i>	9
vations.....	120	the mutual action of elements of electric	
at Niagara Falls.....	186	currents. E. B. Elliott. <i>Abstract and</i>	
Velocity of.....	28	<i>reference</i>	92
Earthquake. See <i>Seismology</i> .		the quotients of space-directed lines. E.	
Earth's crust, Crumpling of.....	18	B. Elliott. <i>Abstract</i>	105, 106
interior, Condition of.....	7	Elements, Periodic law of.....	15
Easter, Computation of.....	15	Elevation. See <i>Altitude</i> .	
Echo from surface of ocean.....	171	Eliot and Storer, cited on atoms.....	128
Echoes, Tyndall on.....	41	Elliott, E. B., calendar of the Society... <i>vii</i>	xxii,
Eclipse of the moon, June 11, 1881.....	90	<i>viii</i> xxx, <i>ix</i> xxvii, <i>x</i> xxxi	
sun, January 11, 1880.....	121	communication on the statistics of the	
sun, July 29, 1878.....	202, 111	borrowing power of the United States.	
Economic phase of the English sparrow		<i>Title only</i>	29
question.....	16	the new coinage of Japan. <i>Title only</i> ... <i>i</i>	31
Economics. See <i>Political Economy</i> .		the locus of the point of equal illumina-	
Education in Japan.....	69	tion by two unequal lights treated	
Edwards, W. H., cited on the pupation of the		by the quaternion analysis. <i>Title only</i> ,	
Nymphalidæ.....	42	<i>i</i>	35
Eidocenter.....	47	the adjustment of census returns. <i>Title</i>	
Eimbeck, Wm., cited on the diorthode.....	132	<i>only</i>	63
Elasticity.....	130	life and annuity tables, based on the	
Election of officers.....	20, 32, 64, 91, 116, 59,	census of 1870. <i>Title only</i>	74
86, 161, <i>iii</i> 17, 51, <i>iv</i> 29, <i>v</i> 84, 174, <i>vi</i> 111		international coinage. <i>Title only</i>	75
<i>vii</i> 81, <i>viii</i> 80, <i>ix</i> 47, <i>x</i> 39.		change in value of dollar. <i>No abstract</i> ,	
officers of the Mathematical Section... <i>vi</i>	122,	<i>i</i>	91
<i>vii</i> 87, <i>viii</i> 37, <i>ix</i> 53, <i>x</i> 83		the credit of the United States, as shown	
Electric receivers.....	153	by the value of its securities. <i>Title</i>	
researches by Joseph Henry.....	236	<i>only</i>	109
Electricity as a primitive force.....	168		

	Page.
Elliott, E. B., communication on—Cont'd.	
the use of metric weights and balances for postal purposes in the United States. <i>Abstract</i>	11 15
further remarks on metric weights and balances for the postal service. <i>Abstract</i>	11 19
the transition in Germany, and the Scandinavian nations of Sweden, Norway, and Denmark, from the silver standard of coinage and money of account to a gold standard.....	11 25
calendar formulæ. <i>Abstract</i>	11 37
affected quantities of the first order. <i>Title only</i>	11 42
the mutual relations as to price of gold, silver bullion, silver coin, and greenbacks. <i>Title only</i>	11 50
the mutual relation as to price of gold, greenbacks, silver bullion, and silver coin. <i>In full</i>	11 52
adjustment of the calendar. <i>Abstract</i>	11 59
two propositions, now before Congress, for changing the coin of the United States. <i>Title only</i>	11 68
force and momentum. <i>Title only</i>	11 84
monetary standards. <i>Title only</i>	11 85
mutual relations of gold and silver, and of prices of commodities. <i>Abstract</i>	11 87
the telephone. <i>Title only</i>	11 111
a statistical diagram. <i>No abstract</i>	11 134
optional money standards. <i>Title only</i>	11 135
standards of time—international, sectional, and local. <i>Abstract</i>	11 137
the telephote. <i>Abstract</i>	11 192
musical intervals. <i>Abstract</i>	11 199
the adjustment of the Carlisle tables of reversions and annuities. <i>Title only</i>	11 201
meridional time for railway and telegraphic purposes. <i>Abstract</i>	11 202
the progress of international coinage in France and America. <i>Title only</i>	11 27
the subject of international coinage. <i>Abstract</i>	11 38
large area illumination by electricity. <i>Title only</i>	11 45
the silver question. <i>Abstract</i>	11 103, 107
the construction of the Government sinking fund. <i>Abstract</i>	11 113
bi-metallism. <i>Abstract</i>	iv 141
accrued interest on Government securities. <i>Title only</i>	v 21
the credit of the United States, past, present, and prospective. <i>Title only</i>	v 102
some formulæ relating to Government securities. <i>Title only</i>	v 106

	Page.
Elliott, E. B., communication on—Cont'd.	
survivorships, with tables and formulas of construction. <i>Title only</i>	v 122
formulas for the computation of Easter. <i>In full</i>	vi 14
units of force and energy, including electric units. <i>Title only</i>	vi 137
a financial problem. <i>Title only</i>	vi 149
electric lighting. <i>Title only</i>	vii 80
Benjamin Alvord. <i>In full</i>	vii 127
example illustrating the use of a certain symbol in the calculus of affected quantity. <i>Title only</i>	viii 37
quantity of United States subsidiary silver coin existing and in circulation. <i>Title only</i>	ix 14
annual profit to banks of national bank note circulation. <i>Title only</i>	ix 14
a problem in probabilities. <i>No abstract</i> ,	x 88
the mutual action of elements of electric currents. <i>Abstract and reference</i>	x 92
a new computing machine. <i>Abstract</i>	x 102
the quibtiens of space-directed lines. <i>Abstract</i>	x 105, 106
remarks on auroras.....	i 45, iv 22
calendar reform.....	ii 30
bi-metallism.....	iii 103
Benjamin Peirce.....	iv 24
small loans by banks.....	iv 34
the metric system.....	vi 4
standard time.....	vi 110
infinitesimals.....	vi 135
theory of errors.....	vi 148
tornado.....	vii 3
sun glows.....	vii 17
irrigation.....	vii 20
Poole's euharmonic organ.....	vii 28
Elliott, H. W., communication on the habits of the fur-bearing seals of the islands of St. Paul and St. George, Behring Sea. <i>Reference</i>	i 91
Elliptic integral of the third species.....	ix 54
integrals.....	vii 102
Ellis, William, cited on the constant <i>P</i>	x 102
Emmons, S. F., communication on ore deposition by replacement. <i>Abstract and reference</i>	vi 32
What is a glacier? <i>Abstract</i>	vii 37
remarks on glaciers.....	vii 9
Emmons' Taconic system.....	x 5
Encke's comet.....	i 34, 35
Endlich, F. M., communication on mineral systems. <i>In full</i>	i 77
electrical phenomena in the Rocky Mountains. <i>Title only</i>	i 95

Page.	Page.
Endlich, F. M., communication on—Cont'd.	Falconiæ, Natural arrangement of..... ii 41
two bricks from the great wall of China.	Fall line..... ix 23
<i>Title only</i> i 98	Fallacies concerning the deaf..... vi 43
specimens of meteoric iron from Chi-	Fallacy as to the theory of gravitation..... v 85
huahua, Mexico, and the structure of	Faraday, cited on matter..... vii 43
meteorites in general. <i>Title only</i> i 98	Farquhar, Edward, cited on personal vocab-
the occurrence of pure tellurium in cer-	ulary..... ii (18)
tain gold mines of Colorado. <i>Title</i>	communication on certain remarkable
<i>only</i> i 101	effects of lightning. <i>Read by Joseph</i>
the coloring agent of gems. <i>Abstract,</i>	<i>Henry. Title only</i> i 42
ii 31	dreams in their relation with psychol-
some interesting cases of metamor-	ogy. <i>Abstract</i> vi 37
phism. <i>Title only</i> iii 27	remarks on the aurora..... iv 22
remarks on the glacial period..... ii 36	tornadoes..... vii 3
Endowment of research..... viii xli	thunder storms..... viii 11
Energy..... vii 61	determining the direction of sound..... viii 13
Conservation and dissipation of..... i 27	Farquhar, Henry, communication on experi-
Engelman, Dr. G., cited on <i>Quercus</i> iv 110	ments in binary arithmetic. <i>Abstract,</i>
English sparrow question..... x 16	v 125, vi 3
Entomology. See <i>Zoology</i> .	further experiments in binary arith-
Eotvos, cited on sounds produced by me-	metic. <i>Abstract</i> vi 38
teors..... ii 157	form of least-square computation. <i>In</i>
Epicurus cited on philosophy..... vii xxx	<i>full</i> vi 150
Erie, Altitude of Lake..... ii 23	the problem discussed by Mr. Alvord.
Erosion as related to displacement..... ii 75	<i>Abstract</i> vi 152
by drifting sand..... i 57	the theoretical discussion in Prof. P. G.
Errata..... ii p. 4 of cover, iii 148, vi 162, x 114	Tait's "Encyclopedia Britannica"
Errors, Composition of..... v 106	article on mechanics. <i>Abstract</i> vii 29
respecting the North American Indians. i 175	empirical formulæ for the diminution
Theory of..... vi 138, 152	of amplitude of a freely-oscillating
Eruption, Latest, in Northern California,	pendulum. <i>Abstract</i> vii 89
ix 46	a Fonetic Eifabet. <i>Abstract</i> ix 17
Theories of..... vi 87	a comparison of the Boss and Auwers
Eskimo shell heaps..... ii 65	declination standards. <i>Abstract and</i>
Estimation of manganese as pyrophosphate,	<i>reference</i> ix 53
ii 132	a problem in probabilities. <i>Abstract</i> x 88
Ether, Hypothesis of an..... vi xxix	a solution and generalization of a prob-
Ethnology. See <i>Anthropology</i> .	lem requiring the division of a rec-
Eucalyptus on the Roman campagna..... vi 36	tangle into parts which form a square.
Euler ignored by Am. Phil. Soc..... viii xxxvii	<i>No abstract</i> x 96
Euler's theorem..... x 101	remarks on standard time..... v 114
Eulogy on A. D. Bache..... i 35	Infinitesimals..... vi 135
A. A. Humphreys..... vii 4	drifting buoys..... vii 15
Evolutes..... vii 87	earth tremors..... viii 23
Evolution and phthisis..... ii 125	Fault at the base of the Wasatch Moun-
Methods of..... vi xxvii	tains..... ii 103
of the bow and arrow..... ix 44	near Harper's Ferry..... vi 30
elements..... vii 16	scarps..... ii 195
Expansion and buckling of ice fields..... ii (22)	Faults, Geologic..... ii 75, 76
Experimentation..... ii 163, vii li	in the Sierra Nevada..... ix 4, 5
Explosion at Flood Rock..... viii 28	of the Great Basin..... ix 5
"Explosion" of meteor explained..... ii 143	Ferguson, J., observation of supposed trans-
Exposure of thermometers..... vi 46, vii 80	Neptunian planet..... iii 20
Eye, Optical defects of..... i 22	Ferrel, William, cited on deflection of rivers
Eyes, Apparatus for testing..... iii 53	by rotation..... vii 22
shining in the dark..... vii 13	law of storms..... i 100

	Page.
Ferrel, William, cited on—Cont'd.	
thermometry.....	vi 25
communication on the effects of winds and barometric pressure on the tides of Boston, and on the mean level of the sea. <i>Abstract and reference</i>	i 53
the law connecting the velocity and direction of the wind with the barometric gradient. <i>Abstract</i>	i 106
the conditions determining temperature. <i>In full</i>	v 90, 91
solar radiation at Shermau, Wyoming. <i>Title only</i>	v 101
Feuerbach's circle.....	viii 45
Finance. See <i>Political Economy</i> .	
Financial problem.....	vi 149
Fish, Decrease of, on the southern coast of New England.....	i 52
fauna of Massachusetts.....	i 29
New species of.....	ii 182
Remarkable ingestion of.....	iii 116
Fishes, Shoulder girdle of.....	i 64
Fisheries exhibitions.....	vii 26, x 56
of the world.....	v 117
Fishery Commission's work.....	x 52, 69
right treaties, Interpretation of.....	i 39
Fletcher, Robert, communication on recent experiments on serpent venom. <i>Reference</i>	vi 38
report as treasurer.....	vii 82, viii xxviii, 31, ix xxx, 47, x xxxiv, 39
Fletchers and bowyers.....	ix 44
Flexures of transit instruments.....	viii 27
Flint, A. S., communication on the most probable value of the latitude and its theoretical weight from entangled observations occurring in the use of Talcott's method. <i>Abstract</i>	x 91
Flora of Laramie group.....	viii 17
Roan Mountain.....	iv 63
Washington and vicinity.....	iv 64
Floras of America and Japan.....	i 42
different regions compared.....	iv 99
Florida expedition for observation of the transit of Venus.....	vi 21
Submergence of.....	iv 53
Flood Rock explosion.....	viii 28
Focal lines in astigmatism.....	vi 45
Fog signals and acoustics.....	ii 37, 57, 60, 167, 345, (45), iv 135, v 23, 39
Food adulteration.....	iv 39
Foote, Elisha, communication on the laws of condensation of aqueous vapor in the atmosphere. <i>Title only</i>	i 74
a proposed method of observing astronomical transits. <i>Title only</i>	i 75

	Page.
Foote, Elisha, communication on—Cont'd.	
some causes that produce rain. <i>Title only</i>	i 98
the causes of electrical developments in thunder storms. <i>Abstract</i>	ii 189
Death of.....	vi 48
Force of.....	i 27, v 126, vi xxviii, vii 47
and life.....	v 57
matter.....	viii 30
Forecasts, verification of.....	vii 8
Formula for the length of a seconds-pendulum.....	vii 101
Formula for area of a plane triangle.....	viii 37
diminution of pendulum swing.....	vii 89
Fort Yukon, Determination of position of.....	i 22
Fossil plants, Distribution of.....	x 28
from Alleghany Co., Va.....	ii (26)
Fossils in aerolites.....	v 66
Foster, M., cited on muscular contraction.....	v 60
nerve currents.....	v 62
Fourier, cited on the temperature of space.....	i 73
Forshey, C. G., communication on the alluvial basin of the Mississippi river styled the delta. <i>In full</i>	i 93, (10)
Frank, F., cited on brain temperatures.....	v 76
Franklin's scientific work.....	viii xxxv
Free will.....	iv 46
Fremont, Dr. H. F., Researches on inoculation of diphtheria by.....	iv 38
Frisby, E., communication on a series for the determination of the number expressing the ratio of the circumference to the diameter. <i>In full</i>	i 57
a Gregorian calendar. <i>Abstract</i>	i 75
series. <i>Title only</i>	ii 193
the total solar eclipse of January 11th, 1880. <i>Abstract</i>	iii 121
magic squares. <i>Abstract</i> . 6 figures.....	iii 143
the orbit of Swift's comet. <i>Abstract</i>	iv 59
remarks on calendars.....	ii 38
Frost limits in North Carolina.....	vi 11
Fundamental distance in thermometry.....	ix 27
Fungi, Microscopic.....	i 42
Gale, L. D., communication on the cause and remedy of the potato rot. <i>Title only</i>	i 97
the geology of the lignite formation, and on a hitherto undescribed deposit discovered in 1834 in New York bay. <i>Title only</i>	i 106
the failure of the wooden pavements of Washington City. <i>Abstract</i>	ii 26
the climate of plants. <i>Abstract</i>	ii 183
remarks on the bowlders of Long Island.....	ii 27
Death of.....	vi 48

	Page.
Galen, cited on life.....	v 51
Galileo, cited on Saturn's rings.....	vi 44
Gallaudet, E. M., communication on unconscious cerebration. <i>Title only</i>	ii 48
the international convention of the teachers of the deaf and dumb, at Milan. <i>Abstract</i>	iv 55
remarks on gesture language and visible speech.....	vi 77
Gamgee, A., cited on muscular contraction.....	v 59, 60
nerve currents.....	v 62
Gardner, J. T., communication on the use of railroad levellings in determining elevations on the great lakes and rivers in the United States and in the Rocky Mountains. <i>Abstract and reference</i>	ii 23
Gases, Theory of.....	v 138
Gauss, cited on computation of π	i 59
Gauss' algorithm.....	vii 102
method for computing variation of elements of an orbit.....	viii 41
transformation.....	vii 110
Gay-Lussac, Law of.....	v 139
Gems, Coloring agent of.....	ii 31
General committee rules. See <i>Standing Rules</i> .	
Gentile system of the Omahas.....	iii 128
Geographical distribution of mammals.....	ii 26
terms and fishery treaties.....	i 39
Geography , List of papers on (see also <i>Oceanography and Seismology</i>):	
official report of the Yellowstone expedition of 1870. G. C. Doane. <i>Communicated by S. F. Baird</i> . <i>Reference</i>	i 21
[exhibition of map of the headwaters of the Yellowstone and Lewis rivers.] M. C. Meigs. <i>No abstract</i>	i 21
[geographical centre of the United States.] J. E. Hilgard. <i>Abstract</i>	i 22
on the results of travels in Alaska and the determination of the position of Fort Yukon. C. W. Raymond. <i>Communicated by T. L. Casey</i> . <i>Reference</i>	i 22
[exhibition of dust from Armenia.] T. Antisell. <i>No abstract</i>	i 25
on the relative value of Alaska to the United States, as compared with that of other territorial acquisitions. W. H. Dall. <i>Abstract and reference</i>	i 25
on the distribution of the population of the United States. J. E. Hilgard. <i>Title only</i>	i 29
on observations made on a journey to California. J. Henry. <i>Title only</i>	i 31

	Page.
Geography , List of papers on—Cont'd.	
on the westward movement of the population of the United States. J. E. Hilgard. <i>Reference</i>	i 35
on the misapplication of geographical terms, as bearing especially on the question of the fishery right treaties. R. D. Cutts. <i>Abstract</i>	i 39
recent explorations in Syria under the auspices of the Palestine exploration fund. Prof. Porter. <i>Title only</i>	i 54
on certain recent geological and geographical researches in Arizona and Nevada. G. K. Gilbert. <i>Abstract</i>	i 54
[a visit to Egypt.] W. T. Sherman. <i>No abstract</i>	i 63
on the fluctuations of the river Nile. J. Henry. <i>Title only</i>	i 63
[letter on the Hayden Survey.] J. Curtis. <i>Communicated by E. B. Elliott</i> . <i>No abstract</i>	i 63
on some measurements of heights by a pocket aneroid. W. Harkness. <i>Title only</i>	i 64
[on the Goldschmidt aneroid barometer.] J. E. Hilgard. <i>No abstract</i>	i 65
[travels in Turkey and the Caucasus.] W. T. Sherman. <i>No abstract</i>	i 65
on the proceedings of the International Metrological Commission. J. E. Hilgard. <i>Title only</i>	i 68
on the habitability of the elevated plateaus of the West. B. Alvord. <i>Title only</i>	i 74
on the use of the cañons of the Colorado for weighing the earth. G. K. Gilbert. <i>Title only</i>	i 88
on the recent determination of the longitude between Paris and Greenwich. J. E. Hilgard. <i>Title only</i>	i 89
on some of the results of the Polaris North Pole Expedition. E. Bessels. <i>Reference</i>	i 92
a method of describing and locating with ease the approximate positions of geographical regions. J. M. Toner. <i>Title only</i>	i 97
on two bricks from the great wall of China. F. M. Endlich. <i>Title only</i>	i 98
on the alluvial basin of the Mississippi river styled the delta. C. G. Forshey. <i>In full</i>	i 98 (10)
on the use of railroad levellings in determining elevations on the great lakes and rivers in the United States and in the Rocky Mountains. J. T. Gardner. <i>Abstract and reference</i>	ii 23

	Page.
Geography , List of papers on—Cont'd.	
on the geographical distribution of mammals. T. Gill. <i>Abstract</i>	11 26
on the movements caused in large ice-fields by expansion and contraction, as illustrative of the formation of anticlinal and synclinal axes in geological formations. M. C. Meigs. <i>In full</i> . 4 figures.....	11 33, (22)
on the Uintah Mountains. J. W. Powell. <i>Title only</i>	11 34
the results of a recent determination of the elevation of the Caspian and Aral seas. A. Woelkoff. <i>Abstract</i>	11 34
account of progress of the International Metrical Commission. J. E. Hilgard. <i>Title only</i>	11 41
the measurement of a base-line for the primary triangulation of the United States Coast Survey near Atlanta, Georgia. J. E. Hilgard. <i>Abstract and reference</i>	11 50
the watershed of the Adirondack region. F. F. Judd. <i>Abstract</i>	11 67
[voyage of the U. S. S. Swatara.] W. Harkness. <i>No abstract</i>	11 68, 69
Japan. H. Capron. <i>Title only</i>	11 79
the Adirondack watershed. F. F. Judd. <i>Abstract</i>	11 82
the deviations of the plumb-line as determined in the survey of the 49th parallel of latitude. F. V. Greene. <i>Abstract and reference</i>	11 82
[route for] the interoceanic canal through Nicaragua. F. P. Lull. <i>Title only</i>	11 83
[visit to Japan.] T. Antisell. <i>No abstract</i> ,	11 84
the late English polar expedition. E. Bessels. <i>Abstract</i>	11 89
a special method of barometric hypsometry. G. K. Gilbert. <i>Abstract</i>	11 131
standard scales or measures of length. J. E. Hilgard. <i>Abstract</i>	11 136
a proposed new leveling instrument. G. K. Gilbert. <i>Abstract</i>	11 184
the recent history of Great Salt Lake. G. K. Gilbert. <i>Abstract</i>	11 187
the lands of the arid region of the United States. J. W. Powell. <i>Abstract</i>	11 189
on the Kanab base-line, and a proposed new method of base measurement. G. K. Gilbert. <i>Abstract</i>	11 34
the secular change in the magnetic declination in the United States and at some foreign stations. C. A. Schott. <i>Abstract</i>	11 45

	Page.
Geography , List of papers on—Cont'd.	
[Luray cave.] J. W. Chickering. <i>Title only</i>	111 65
on the boundary line between Alaska and British America. W. H. Dall. <i>Title only</i>	111 77
a model of the basin of the Gulf of Mexico. J. E. Hilgard. <i>Abstract</i>	iv 52
notes on Roan Mountain, North Carolina. J. W. Chickering. <i>In full</i>	iv 60
the scenery of the Grand Cañon district. C. E. Dutton. <i>Title only</i>	iv 120
the Vermilion Cliffs and the valley of the Virgen, in Southern Utah. C. E. Dutton. <i>Title only</i>	iv 122
boundary line between Alaska and Siberia. M. Baker. <i>In full. Map</i>	iv 123
recent discoveries in Alaska north of Behring strait. W. H. Dall. <i>Abstract</i>	iv 163
on barometric hypsometry. G. K. Gilbert. <i>Reference</i>	v 48
alignment curves on any surface, with special application to the ellipsoid. C. H. Kummell. <i>Abstract. 1 figure</i>	vi 123
graphic tables for computing altitudes from barometric data. G. K. Gilbert. <i>Reference</i>	vi 136
the existing glaciers of the High Sierra of California. I. C. Russell. <i>Abstract and reference. 2 figures</i>	vii 5
some physical and economic features of the Upper Missourian system. L. F. Ward. <i>Reference</i>	vii 20
the diversion of water courses by the rotation of the earth. G. K. Gilbert. <i>Abstract and reference</i>	vii 21
What is a glacier? <i>Symposium. Abstract</i>	vii 37
a concrete problem in hydrostatics. G. K. Gilbert. <i>Abstract</i>	vii 92
a formula for the length of a seconds-pendulum. G. W. Hill. <i>Reference</i> ,	vii 101
discussion of a concrete problem in hydrostatics proposed by Mr. G. K. Gilbert. R. S. Woodward. <i>Title only</i>	vii 101
variations of latitude. A. Hall. <i>Abstract and reference</i>	viii 10
distances on any spheroid. C. H. Kummell. <i>Abstract and reference</i>	viii 52
some practical features of a field time determination with a meridian transit. R. S. Woodward. <i>Abstract</i>	viii 55
Lieutenant Lockwood's expedition to farthest north. G. E. Curtis. <i>Abstract</i>	ix 8

	Page.
Geography , List of papers on—Cont'd.	
on the changes of terrestrial level surfaces due to variations in distribution of superficial matter. R. S. Woodward. <i>Reference</i>	ix 15
the physical-geographical divisions of the southeastern portion of the United States and their corresponding topographical types. G. Thompson. <i>Abstract</i>	ix 22
on the position and shape of the geoid as dependent on local masses. R. S. Woodward. <i>Reference</i>	ix 53, 54
the topography and geology of the Cross Timbers of Texas. R. T. Hill. <i>Read by W J McGee. Reference</i>	x 6
the topography and structure in the Bays Mountains, Tennessee. B. Willis. <i>Reference</i>	x 7
development of a perspective map from a contour map. B. Willis. <i>Title only</i>	x 9
[exhibition of a new plane table.] W. D. Johnson. <i>No abstract</i>	x 9
Mt. Rainier and its glaciers. B. Willis. <i>Abstract</i>	x 10
What is a topographical map? M. Baker. <i>Abstract</i>	x 11
What is topography? <i>Symposium. Abstract</i>	x 14
the Muir glacier, Alaska. J. W. Ohicker- ing. <i>Title only</i>	x 15
South Florida notes. W. H. Dall. <i>Title only</i>	x 16
the progress of science as exemplified in the art of weighing and measuring. W. Harkness. <i>Presidential address. In full</i>	x xxxvii, 39
the most probable value of the latitude and its theoretical weight from entangled observations occurring in the use of Talcott's method. A. S. Flint. <i>Abstract</i>	x 91
Geoidal deformation by local masses vii 92, 101, ix 15, 53	
Geology , List of papers on. (See also <i>Seis- mology</i> .)	
remarks on the structural geology of the valley of the Colorado of the West. J. W. Powell. <i>Abstract</i>	i 48
on certain recent geological and geograph- ical researches in Arizona and Ne- vada. G. K. Gilbert. <i>Abstract</i>	i 54
on sand sculpture in the West. G. K. Gil- bert. <i>Abstract</i>	i 57
descriptions of new species of fossil plants from Alleghany County, Virginia; with	

	Page.
Geology , List of papers on—Cont'd.	
some remarks on the rock seen along the Chesapeake and Ohio railroad, near the White Sulphur Springs of Greenbrier County, West Virginia. F. B. Meek. <i>In full 2 plates</i>	i 62, ii (26)
on the causes of the elevations and sub- sidences of the earth's surface. C. E. Dutton. <i>Title only</i>	i 74
on the glacial epoch in Utah and Nevada. G. K. Gilbert. <i>Abstract</i>	i 84
on geological time. C. E. Dutton. <i>Title only</i>	i 89
on Mallet's theory of the formation of the physical features of the earth. C. E. Dutton. <i>Title only</i>	i 90
on the recent earthquakes in North Caro- lina. B. Alvord. <i>Abstract</i>	i 101
on a cold geyser or intermittent artesian well in Ohio. G. K. Gilbert. <i>Abstract</i> , i 103	
on the geology of the lignite formation, and on a hitherto undescribed deposit discovered in 1834 in New York bay. L. D. Gale. <i>Title only</i>	i 106
on the age of the Tonto sand-tones. G. K. Gilbert. <i>Abstract and reference</i>	i 109
on the glacial period. C. E. Dutton. <i>Title only</i>	ii 26
[geological history of Lake Winnipeg.] G. K. Warren. <i>Abstract</i>	ii 27
[elevations and depressions in Alaska.] W. H. Dall. <i>No abstract</i>	ii 27
on the movements caused in large ice- fields by expansion and contraction, as illustrative of the formation of anti- clinal and synclinal axes in geological formations. M. C. Meigs. <i>In full. 4 figures</i>	ii 33, (22)
on the Uintah Mountains. J. W. Powell. <i>Title only</i>	ii 34
the glacial theory. J. Henry. <i>Abstract</i>	ii 35
the causes of glacial climate. <i>Symposium. Abstract</i>	ii 43, 45
ripple-marks. G. K. Gilbert. <i>Abstract</i>	ii 61
some types of mountain building. J. W. Powell. <i>Title only</i>	ii 65
landslips and lakelets. G. K. Gilbert. <i>Ab- stract</i>	ii 69
monoclinical ridges. J. W. Powell. <i>Ab- stract</i>	ii 74
the distribution of thermal springs in the United States. G. K. Gilbert. <i>Title only</i>	ii 80
[geologists versus physicists.] J. W. Pow- ell. <i>No abstract</i>	ii 85

	Page.
Geology , List of papers on—Cont'd.	
Lake Bonneville. G. K. Gilbert. <i>Abstract and reference</i>	ii 103
the structure of the Henry Mountains. G. K. Gilbert. <i>Abstract and reference</i> , ii 112, 113	113
chemical remarks on terrestrial geogony. T. Antisell. <i>Title only</i>	ii 132, 133, 134
the Wasatch a growing mountain. G. K. Gilbert. <i>Abstract</i>	ii 195
on some interesting cases of metamorphism. F. M. Endlich. <i>Title only</i>	iii 27
the geological character of the Colorado river. C. E. Dutton. <i>Title only</i>	iii 28
the succession of volcanic eruptions. C. E. Dutton. <i>Title only</i>	iii 36, 37
on the Permian formation of North America. C. E. Dutton. <i>Abstract</i>	iii 65, 67
the subject of the Permian formation in North America. C. A. White. <i>Abstract</i>	iii 104
on the oscillations of Lake Bonneville. G. K. Gilbert. <i>Title only</i>	iii 113
the drainage system of the Black Hills. G. K. Gilbert. <i>Abstract</i>	iii 125
quaternary deposits of western Iowa and eastern Nebraska. J. E. Todd. <i>Abstract</i>	iv 120
the Vermilion cliffs and the valley of the Virgin in southern Utah. C. E. Dutton. <i>Title only</i>	iv 122
the origin of the topographical features of lakeshores. G. K. Gilbert. <i>Title only</i>	iv 170
the quaternary climate of the Great Basin. G. K. Gilbert. <i>Reference</i>	v 21
on artesian wells on the Great Plains. C. A. White. <i>Reference</i>	v 101
geology of the Hawaiian islands. C. E. Dutton. <i>Abstract</i>	vi 13
the geology of Hatteras and the neighboring coast. W. C. Kerr. <i>Abstract</i>	vi 28
topographical indications of a fault near Harper's Ferry. H. F. Walling. <i>Abstract</i>	vi 30
ore deposition by replacement. S. F. Emmons. <i>Abstract and reference</i>	vi 32
glaciation in Alaska. W. H. Dall. <i>Abstract</i>	vi 33
the volcanic problem, stated. C. E. Dutton. <i>Abstract</i>	vi 87
the drainage system and the distribution of the loess of eastern Iowa. W. J. McGee. <i>Abstract</i>	vi 93
the Cambrian system in the United States and Canada. C. D. Walcott. <i>Abstract</i> , 1 figure.....	vi 98

	Page.
Geology , List of papers on—Cont'd.	
the existing glaciers of the High Sierra of California. I. C. Russell. <i>Abstract and reference</i> . 2 figures.....	vii 8
the mica mines of North Carolina. W. C. Kerr. <i>Abstract</i>	vii 9
deposits of volcanic dust in the Great Basin. I. C. Russell. <i>Abstract</i>	vii 18
the diversion of water courses by the rotation of the earth. G. K. Gilbert. <i>Abstract and reference</i>	vii 21
the volcanic sand which fell at Unalashka October 20, 1883, and some considerations concerning its composition. J. S. Diller. <i>Abstract</i>	vii 33
the methods of modern petrography. G. H. Williams. <i>Abstract</i>	vii 36
What is a glacier? <i>Symposium. Abstract</i> , vii 37	37
the strata exposed in the east shaft of the water-works extension. T. Robinson. <i>Abstract</i>	vii 69
plan for the subject bibliography of North American geologic literature. G. K. Gilbert. <i>Title only</i>	vii 71
plan for the subject bibliography of North American geologic literature. J. W. Powell. <i>Title only</i>	vii 71
the volcanoes and lava fields of New Mexico. C. E. Dutton. <i>Abstract</i>	vii 76
a concrete problem in hydrostatics. G. K. Gilbert. <i>Abstract</i>	vii 92
discussion of a concrete problem in hydrostatics proposed by Mr. G. K. Gilbert. R. S. Woodward. <i>Title only</i>	vii 101
practical geology versus speculative physics. C. E. Dutton. <i>Title only</i>	viii 4, 5
geological and physical theories. W. B. Taylor. <i>Abstract</i>	viii 6
variations of latitude. A. Hall. <i>Abstract and reference</i>	viii 10
the flora of the Laramie group. L. F. Ward. <i>Reference</i>	viii 17
problems connected with the physics of the earth's crust. H. M. Paul. <i>Title only</i>	viii 17, 18
the crumpling of the earth's crust. W. B. Taylor. <i>Abstract and reference</i>	viii 18
the columnar structure in the diabase of Orange Mountain, N. J. J. P. Iddings. <i>Abstract</i> . 4 figures.....	viii 19
the terraces of the Potomac valley. W. J. McGee. <i>Title only</i>	viii 24
notes on the geology of northern California. J. S. Diller. <i>Abstract</i>	ix 4

	Page.
Geology, List of papers on—Cont'd.	
notes on the faults of the Great Basin and of the eastern base of the Sierra Nevada. I. C. Russell. <i>Abstract</i>	ix 5
recent changes of level in the basin of Lake Ontario. G. K. Gilbert. <i>Reference</i>	ix 8
on the changes of terrestrial level surfaces due to variations in distribution of superficial matter. R. S. Woodward. <i>Reference</i>	ix 15
on the observed changes of level surfaces in the Bonneville area, and their explanation. G. K. Gilbert. <i>Title only</i> ,	ix 15
on the varying attitudes of former level surfaces in the Great Lake region and the applicability of proposed explanations. T. C. Chamberlin. <i>Title only</i>	ix 15, 16
the enlargement of mineral fragments as a factor in rock alteration. R. D. Irving. <i>Title only</i>	ix 16
the subaerial decay of rocks and the origin of the red clay of certain formations. I. C. Russell. <i>Title only</i>	ix 16
on geological museums. G. P. Merrill. <i>Title only</i>	ix 36
certain new and small mountain ranges. G. K. Gilbert. <i>Title only</i>	ix 45
on the occurrence of copper ore in the Trias of the Eastern United States. N. H. Darton. <i>Title only</i>	ix 46
the latest volcanic eruption in northern California and its peculiar lava. J. S. Diller. <i>Reference</i>	ix 46
on the position and shape of the geoid as dependent on local masses. R. S. Woodward. <i>Reference</i>	ix 53, 54
the geologic age of the lowest formation of Emmons' Taconic system. C. D. Walcott. <i>Reference</i>	x 5
the topography and geology of the Cross Timbers of Texas. R. T. Hill. <i>Read by W J McGee. Reference</i>	x 6
the topography and structure in the Bays Mountains, Tennessee. B. Willis. <i>Title only</i>	x 7
Mt. Rainier and its glaciers. B. Willis. <i>Abstract</i>	x 10
[Mt. Shasta, contrasted with Mt. Rainier.] J. S. Diller. <i>No abstract</i>	x 11
the Muir glacier, Alaska. J. W. Chickering. <i>Title only</i>	x 15
the quaternary deposits and the great displacement of the Middle Atlantic slope. W J McGee. <i>Reference</i>	x 16

	Page.
Geology, List of papers on—Cont'd.	
South Florida notes. W. H. Dall. <i>Title only</i>	x 16
on the geographical distribution of fossil plants. L. F. Ward. <i>Reference</i>	x 28
Geometrical problems.....	iii 53, 64, v 88, 107, vi 157, viii 45
Geometry, Graßmann's.....	viii 53
Germ culture.....	i 42, viii 30
Gesture language.....	vi 63, 84
Geyser, A cold.....	i 103
Gilbert, G. K., cited on wind and barometric observation.....	v 108
verification of predictions.....	vii 122, x 94, 96
communication on certain recent geological and geographical researches in Arizona and Nevada. <i>Abstract</i>	i 54
sand sculpture in the West. <i>Abstract</i> .	i 57
the glacial epoch in Utah and Nevada. <i>Abstract</i>	i 84
the use of the cañons of the Colorado for weighing the earth. <i>Title only</i>	i 88
a cold geyser or intermittent artesian well in Ohio. <i>Abstract</i>	i 103
the age of the Tonto sand-stones. <i>Abstract and reference</i>	i 109
ripple-marks. <i>Abstract</i>	ii 61
the horary oscillations of the temperature of the atmosphere. <i>Abstract</i>	ii 67
horary oscillations of the atmosphere. <i>Abstract</i>	ii 69
landslips and lakelets. <i>Abstract</i>	ii 69
the distribution of thermal springs in the United States. <i>Title only</i>	ii 80
Lake Bonneville. <i>Abstract and reference</i>	ii 103
the structure of the Henry Mountains. <i>Abstract and reference</i>	ii 112, 113
a special method of barometric hypsometry. <i>Abstract</i>	ii 131
a proposed new leveling instrument. <i>Abstract</i>	ii 184
the recent history of Great Salt Lake. <i>Abstract</i>	ii 187
the Wasatch a growing mountain. <i>Abstract</i>	ii 195
the Kanab base-line, and a proposed new method of base measurement. <i>Abstract</i>	iii 34
air currents on mountain slopes. <i>Abstract</i>	iii 38
the oscillations of Lake Bonneville. <i>Title only</i>	iii 113
the drainage system of the Black Hills. <i>Abstract</i>	iii 125

	Page.		Page.
Glaciers of the High Sierra.....	vii 5	Great Basin, Quaternary climate of.....	v 21
Mt. Rainier.....	x 10	ranges, Bibliography of.....	ix 6
Glaisher, cited on barometric gradient.....	i 107	volcanic dust in.....	vii 18
Gley, E., cited on the pulse.....	v 78	Great Salt Lake, Fluctuations of.....	ii 187, 188
Goethe, cited on applied science.....	vii 12	Great Spirit, The, a mistake.....	ii 176
Gold and silver and the prices of commodities.....	ii 87	Grecian atomic philosophy.....	vii xxix
and silver coinage.....	iii 78, 107	Greely, A. W., cited on bibliography of meteorology.....	x 22
Gold-silver ratio.....	iv 141	Green, H. J., cited on thermometry.....	ix 25
Goode, G. B., Bibliography of S. F. Baird by.....	x 62	Greene, B. F., communication on the Navy compass. <i>Title only</i>	ii 123
communication on the swordfish and its allies. <i>Reference</i>	iv 162	an adjustable binnacle for the correction of a ship's compass. <i>Title only</i>	ii 134
the fisheries of the world. <i>Reference</i>	v 117	Greene, F. V., communication on the deviations of the plumb-line as determined in the survey of the 49th parallel of latitude. <i>Abstract and reference</i>	ii 82
fisheries exhibitions. <i>Reference</i>	vii 26	Gregorian calendar, A.....	i 75
the systematic care of pamphlets. <i>Abstract and reference</i>	viii 29	Proposed reformation of.....	i 29
the distribution of fishes in the oceanic abysses and middle strata. <i>Title only</i> ,	ix 22	Growth of stones and organisms.....	v 67
museum specimens illustrating biology. <i>Title only</i>	ix 36	Grunmach, Dr., cited on thermometry.....	ix 30, 32
the geographical distribution of scientific men and institutions in the United States. <i>Reference</i>	x 7	Gudermann's notation.....	vii 103
Goodfellow, E., remarks commemorative of Benjamin Peirce.....	iv 25	Gulf of Mexico, Model of.....	iv 52
Gould, R. A., letters on Cordoba Observatory. <i>Communicated by J. H. C. Coffin and J. J. Woodward. No abstract</i>	i 57	Gulf stream, Channel of.....	iv 53
letter on Cordoba Observatory. <i>Communicated by J. J. Woodward. No abstract</i>	i 88	Gunnell, F. M., communication on yellow fever disinfection. <i>Abstract</i>	iii 51
communication on scientific culture in the Argentine Republic. <i>No abstract</i>	ii 15	Guthrie, Prof. F., cited on attraction.....	v 150
the coinage of the Argentine Republic. <i>Read by E. B. Elliott. Abstract</i>	ii 65	Guyot, Arnold, cited on the Appalachians,	iv 61
Governmental endowment of research.....	viii xli	distribution of mountains and plains,	viii 19
Graham, Law of.....	v 138	Habits of fur-bearing seals.....	i 91
Graphic methods in research.....	x 4	Hahn, O., cited on fossils in aerolites.....	v 66
table for computation.....	v 120, vi 136	Hall, Asaph, communication on the elements of the Comet I, 1871. <i>Read by B. F. Sands. Abstract</i>	i 23
Grasshoppers, Shower of.....	ii 87	astronomical photography. <i>Abstract and reference</i>	i 25
Grassmann's system of geometry.....	viii 53	a curve of the fourth degree. <i>Abstract and reference</i>	i 30
Gravitation.....	vii 43, 47	the astronomical proof of the existence of a resisting medium in space. <i>Reference</i>	i 34
Fallacy concerning.....	v 85	an historical note on the method of least squares. <i>Reference</i>	i 62
Modification of formula of.....	viii 39	the experimental determination of the ratio of the circumference to the diameter, based on the principles of the calculus of probabilities. <i>Title only</i>	i 62
Gray, Asa, cited on the classification of plants.....	iv 108, 109, 110	the rectilinear motion of a particle toward an attracting centre. <i>Reference</i>	i 88
communication on plants common to Japan and eastern America. <i>Abstract</i>	ii 42	comets and meteors. <i>Reference</i>	i 94
Gray, Elisha, communication on a telophon. <i>Abstract</i>	ii 67		
Gray, L. C., cited on brain temperatures.....	v 76		
Great Basin, Faults of.....	ix 5		
Later geology of.....	i 84		

	Page.
Hall, Asaph, communication on—Cont'd.	
the method adopted in writing the international scientific telegrams. <i>Abstract</i>	1 101
the operations of the several parties sent from the United States to observe the transit of Venus on the 8th of December, 1874. <i>Abstract</i>	ii 31, 32
approximate quadratures. <i>Abstract</i> , ii 48	
the appearance of Saturn's rings. <i>Abstract</i>	ii 94
a bright spot which has recently become visible on the ball of Saturn. <i>Abstract</i>	ii 102
the position of the centre of gravity of the apparent disk of a planet. <i>Reference</i>	ii 181
the results of a search for satellites of Mars. <i>Abstract and reference</i>	ii 186
the supposed discovery of a trans-Nep- tunian planet at the U. S. Naval Ob- servatory in 1850. <i>Abstract</i>	iii 20
the satellites of Saturn. <i>Abstract</i>	iii 26
the orbits of Titan and Hyperion. <i>Abstract</i>	iii 40
inaugural address as chairman of the Mathematical Section. <i>In full</i>	vi 117
the determination of the mass of a planet from observation of two satel- lites. <i>Abstract</i>	vi 132
the formulæ for computing the position of a satellite. <i>In full</i> . 1 figure.....	vii 93
American scientific societies. <i>Presiden- tial address</i> . <i>In full</i>	viii xxxiii, 30
variations of latitude. <i>Abstract and ref- erence</i>	viii 10
the new star in the nebula of Andro- meda. <i>Reference</i>	ix 14
the images of stars. <i>Reference</i>	ix 15
a problem in probabilities. <i>Read by G. W. Hill</i> . <i>No abstract</i>	x 88
the parallax of a Tauri. <i>Abstract</i>	x 91
Euler's theorem (generally called Lam- bert's). <i>Abstract</i>	x 101
Longitude of Plover Bay by.....	iv 124, 126
remarks on planetary motions...ii 188, 189, 192	
transit of Mercury.....	ii 199
criteria for the rejection of observa- tions.....	vi 155
Grassmann's geometry.....	viii 53
time determinations.....	viii 58
Hall, G. S., communication on recent expe- riments on reaction time and the time sense. <i>Title only</i>	viii 4
Haller, A. von, cited on nerve currents....	v 61

	Page.
Hallowell, Benjamin, letter on the meteor of December 24, 1873. <i>Communicated by J. Henry</i> . <i>No abstract</i>	i 95
Halo, A remarkable solar.....	v 112
Hamilton, Sir W., cited on ultimate causes, v 163, 166	
Harkness, William, communication on the physical constitution of the corona of the sun. <i>Reference</i>	i 31
the spectrum of Encke's comet. <i>Refer- ence</i>	i 34
the spectrum of Encke's comet, and the appearance of Tuttle's comet. <i>Refer- ence</i>	i 34
the density of the hypothetical resisting medium in space. <i>Title and refer- ence</i>	i 39
some measurements of heights by a pocket aneroid. <i>Title only</i>	i 64
the power necessary to drive the pendu- lum of an astronomical clock. <i>Title only</i>	i 74
the distribution of temperature over the surface of the globe. <i>Reference</i>	i 96
the apparatus to be used in the observa- tions of the approaching transit of Venus. <i>Title only</i>	i 102
the transit of Venus in 1874. <i>Communi- cated by A. Hall</i> . <i>Abstract</i>	ii 32
the methods of measuring the inequali- ties of the pivots of the transit instru- ment. <i>Title only</i>	ii 68
the voyage of the U. S. S. Swatara. <i>No abstract</i>	ii 68, 69
the velocity of light and determination of the solar parallax. <i>Title only</i>	ii 201
the color corrections of achromatic ob- jectives. <i>Abstract</i>	iii 39
the number of lenses required in an achromatic objective, consisting of in- finitely thin lenses in contact, in order that, with any given law of dispersion whatever, the greatest possible number of light-rays of different degrees of refrangibility may be brought to a common focus. <i>In full</i>	iii 65
the solar corona. <i>Abstract</i>	iii 116
the relative accuracy of different meth- ods of determining the solar parallax. <i>Reference</i>	v 39
the monochromatic aberration of the human eye in aphakia. <i>Reference</i> , vi 5	
flexures of transit instruments. <i>Ab- stract</i>	viii 27

	Page.		Page.
Harkness, William, communication on—Cont'd.		Hazen, H. A., remarks on—Cont'd.	
the progress of science as exemplified		weather prediction.....	viii 9
in the art of weighing and measuring.		care of pamphlets.....	viii 29
<i>Presidential address. In full.....</i>	x xxxvii, 39	graphics.....	x 5
a device for viewing the sun by light of		wind vanes.....	x 9
any desired wave length. <i>Abstract.....</i>	x 13	the sparrow question	x 16
the representation of comet orbits by		Hazen, W. B., bibliography of meteorology	
models. <i>Reference.....</i>	x 28	x 21
the constant <i>P</i> in observations of terres-		Death of.....	x 6
trial magnetism.....	x 102	Heat of the sun.....	i 31
remarks on the black drop.....	ii 199	Theory of.....	v 133
results from photographs of the transit		Heats, Molecular.....	i 104
of Venus.....	iv 169	Hell Gate explosion.....	viii 28
vital force.....	v 105	Hellmann, Dr. G., bibliographic work in	
temperature observations.....	vi 26	meteorology.....	x 20, 21, 23, 25
hygrometry.....	vi 36	Helmert, cited on alignment curves.....	vi 124, 126
postulated continents.....	vi 93	Henry, Joseph, Address on the life and char-	
accidental and constant errors.....	vi 133	acter of.....	ii 203, 368, 370
glaciers.....	vii 9	cited on a telephonic experiment.....	ii 104
vision.....	vii 13	adhesion and cohesion.....	v 137
problem in probabilities.....	x 89	land and sea breezes.....	v 29
Harper's Ferry, Fault near	vi 30	sound anomalies.....	ii 58, iv 135, v 33, 40, 43
Hart, A. S., cited on Malfatti's problem.....	ii 117, 119	the Philosophical Society.....	x 45
Harting, cited on mineral aggregates.....	iii 39	Washington as a scientific center.....	x 47
Hartley, J., Solution of a geometrical prob-		communication on phenomena of sound	
lem by.....	iii 64	and experiments with tuning forks.	
Hattersas, Geology of Cape	vi 28	<i>Title only.....</i>	i 22
Hausen, C. A., cited on nerve currents.....	v 60	observations made on a journey to Cali-	
Hauy, cited on mineralogy.....	i 77, 78	fornia. <i>Title only.....</i>	i 31
Havana magnetic disturbance and north-		the organization and objects of the So-	
ers	vii 25	ciety. <i>Presidential address. In full,</i>	
Hawaiian geology.....	vi 13	i v, 34
Hayden, Everett, communication on the		the life and scientific labors of the late	
Charleston earthquake. <i>Abstract.</i>		Alexander Dallas Bache. <i>Reference.....</i>	i 35
<i>Map.....</i>	ix 38	the expenditure of the income of the	
Hayden, F. V., cited on base-line methods.....	iii 34	Bache fund for 1872. <i>Title only.....</i>	i 53
Hazen, H. A., communication on the retarda-		the fluctuations of the river Nile. <i>Title</i>	
tion of storm centres at elevated sta-		only.....	i 63
tions and high wind as a probable		the condition of the Society. <i>No ab-</i>	
cause. <i>In full.....</i>	v 108	stract.....	i 64
the coming winter of 1882-'83. <i>Ab-</i>		sound in relation to fog-signals, from in-	
stract.....	v 122	vestigations under the direction of the	
hygrometric observations. <i>Abstract.....</i>	vi 36	U. S. Light House Board. <i>In full.....</i>	i 65,
thermometer exposure. <i>Abstract.....</i>	vi 46	ii (45)
the sun glows. <i>Abstract and reference.....</i>	vii 17	atmospheric electricity. <i>Title only.....</i>	i 75, 87
thermometer exposure. <i>Abstract.....</i>	vii 80	experiments on fog signals during the	
thunderstorms of 1884. <i>Abstract.....</i>	viii 10	past summer. <i>Title only.....</i>	i 90
the condensing hygrometer and sling		a method of developing magnetism in	
psychrometer. <i>Abstract.....</i>	viii 25	bars of steel. <i>Title only.....</i>	i 97
effects of solar radiation upon thermom-		eteor trains, and the upper atmos-	
eter bulbs having different metallic		pheric currents. <i>Title only.....</i>	i 98
coverings. <i>Abstract.....</i>	ix 33	Giffard's injector. <i>Title only.....</i>	i 99
the sky glows of 1883. <i>Title only.....</i>	x 6	audition. <i>Title only.....</i>	i 22
relation between wind velocity and		the glacial theory. <i>Abstract.....</i>	ii 35
pressure. <i>Reference.....</i>	x 10	fog signals and abnormal conditions of	
remarks on deflection of rivers.....	vii 24	sound. <i>Reference.....</i>	ii 37

	Page.
Henry, Joseph, communication on—Cont'd. electricity engendered by the driving belt of the machinery for ventilating the Capitol at Washington. <i>Abstract.</i>	40
<i>Reference.</i>	57
half-vision. <i>Title only.</i>	60
researches on sound in its application to fog signals. <i>Presidential address.</i> <i>Reference.</i>	60
illuminating materials. <i>Title only.</i>	71
Crookes' radiometers. <i>Abstract.</i>	80
[fog signals.] <i>Abstract.</i>	85
paper made of asbestos. <i>Title only.</i>	86
scientific method and its application to acoustic researches in connection with fog signals. <i>Presidential address. In full.</i>	162
Memoir on the scientific work of.	230
Memorial services of.	27
Portrait of..... <i>i</i> frontispiece-	
remarks on auroras..... <i>i</i> 46, 48	
Japan..... <i>i</i> 71	
waterspouts..... <i>i</i> 105	
Resolutions on the death of..... <i>i</i> 196	
Henry, Mrs. Joseph, Death of..... <i>v</i> 97	
Henry Mountains..... <i>i</i> 113	
Heraclitus, cited on philosophy..... <i>vii</i> <i>xxxi</i>	
Hera path, J., cited on elasticity..... <i>v</i> 130	
Hering's theory of color..... <i>iv</i> 54	
Hermann, cited on muscular contraction <i>v</i> 58, 59	
nerve currents..... <i>v</i> 61	
Hermaphrodite, Alleged..... <i>i</i> 24	
Herschel, Sir John, cited on cohesion..... <i>v</i> 129	
force..... <i>v</i> 151, 153	
laws..... <i>v</i> 169	
standard time..... <i>v</i> 115	
satellites of Uranus..... <i>i</i> (30), (34)	
temperature of space..... <i>i</i> 73	
theory of errors..... <i>vi</i> 138, 140	
Herschel, Sir William, cited on relation of light to heat..... <i>v</i> 135	
satellites of Uranus..... <i>i</i> (30)	
Saturn..... <i>i</i> 102	
Saturn's rings..... <i>vi</i> 43	
High-heeled shoes..... <i>v</i> 117	
High power definition..... <i>i</i> 47	
High Sierra glaciers..... <i>vii</i> 5	
Hilgard, J. E., cited on earthquake tides... <i>v</i> 144	
communication on the distance trav- ersed by approaching the North Pole on a loxodromic curve. <i>Title only.</i>	21
a chronograph. <i>No abstract.</i>	22
the geographical centre of the United States. <i>Abstract.</i>	22

	Page.
Hilgard, J. E., communication on—Cont'd. a chronoscope. <i>No abstract.</i>	23
the distribution of the population in the United States. <i>Title only.</i>	29
an exponential formula having reference to the tolerance allowed at the U. S. mint. <i>Title only.</i>	31
the westward movement of the popula- tion of the United States. <i>Reference.</i>	35
the aurora of February 4th. <i>Abstract.</i>	47
Hindoo arithmetic. <i>Title only.</i>	53
the recording systems of the trans-At- lantic cables. <i>Title only.</i>	53
the Goldschmidt aneroid barometer. <i>No abstract.</i>	65
the proceedings of the International Metrological Commission. <i>Title only.</i>	68
an inquiry into the law of probability. <i>Title only.</i>	84
the air thermometer of Prof. Jolly. <i>Title only.</i>	89
the recent determination of the longi- tude between Paris and Greenwich. <i>Title only.</i>	89
recent experimental researches in acoustics, by Prof. A. M. Mayer. <i>Title only.</i>	90
the determination of the personal errors in the observation of astronomical transits. <i>Title only.</i>	92
a new apparatus for the investigation of personal error in astronomical transit observations. <i>Title only.</i>	106
a proposed reformation of the Gregorian calendar. <i>Abstract.</i>	29, 30
the proceedings of the International Metrical Commission. <i>Title only.</i>	41
iron facing copper plates. <i>Abstract.</i>	42
the measurement of a base-line for the primary triangulation of the United States Coast Survey near Atlanta, Georgia. <i>Abstract and reference.</i>	50
standard scales, or measures of length. <i>Abstract.</i>	136
an optical salinometer. <i>Abstract.</i>	185
Jablokoff's electric candle. <i>Title only.</i>	19
phosphorescent clocks. <i>Abstract.</i>	33
remarks commemorative of Jonathan Homer Lane. <i>In full.</i>	122
a model of the basin of the Gulf of Mex- ico. <i>Abstract.</i>	52
Siemens' deep sea thermometer and Carré's ice machine. <i>Title only.</i>	100
remarks on auroras..... <i>i</i> 46, 48	

Page.	Page.
Hilgard, J. E., remarks on—Cont'd.	Hoffman, W. J., cited on the poisoning of
persistent observation of phenomena..... ii 19	arrows..... ii 182
vocabularies..... ii 28	communication on the use of poisoned
calendar reform..... ii 30	arrows by North American Indians.
photographs of the sun..... ii 33	<i>Title only</i> ii 183
cause of glacial climate..... ii 36	Holden, E. S., communication on the adopted
a new meteorological instrument..... ii 64	value of the sun's apparent diameter.
Dakota calendar..... ii 92	<i>In full</i> i 95, (3)
Peiree's Linear Associative Algebra..... iv 24	Sir William Herschel's observations of
unification of longitudes and time..... vi 109	the satellites of Uranus. <i>In full</i> i 106, (30)
Hilgard, Theodore, communication on the	the number of words used in speaking
number of the cephalic vertebrae.	and writing. <i>In full</i> ii 28, (16)
<i>Reference</i> i 26	two drawings of nebulae, made with the
Hill, G. W., communication on certain possible	xxvi-inch telescope of the U. S. Naval
abbreviations in the computation	Observatory, by Mr. L. Trouvelot, of
of the long-period perturbations of	Cambridge, Mass. <i>Abstract</i> ii 51
the moon's motion due to the direct	search for Vulcan. <i>Abstract</i> ii 85
action of the planets. <i>Abstract and</i>	reference catalogues of astronomical
<i>reference</i> vi 136	papers and memoirs. <i>Abstract</i> ii 95
a formula for the length of a seconds-	the shadow of the ball of Saturn pro-
pendulum. <i>Reference</i> vii 101	jected on the rings. <i>Abstract</i> ii 101
a problem in probabilities. <i>Abstract</i> x 88	the brightness and the stellar magni-
the motion of Hyperion. <i>Abstract and</i>	tude of the third Saturnian satellite,
<i>reference</i> x 90	Tethys. <i>Read by A. N. Skinner. Title</i>
the integration of differential equations	<i>only</i> iii 18
admitting periodic integrals. <i>Abstract</i>	B. A. Gould's Uranometria Argentina.
and <i>reference</i> x 100	<i>Reference</i> iii 119, 122
remarks on infinitesimals..... vi 135	Holmes, W. H., remarks on glaciers..... vii 8
gravitation formula..... viii 40	Homologies of the shoulder girdle of fishes..... i 64
adjustment of conditioned observations,	Homophenes..... vi 58, 76
..... viii 41	Hooker, Thermometric observations by..... v 94
Grassmann's geometry..... viii 53	Hooker, R., cited on natural law..... v 173
density of Mercury..... viii 45	Hoosac tunnel, Acoustic features of..... ii 172
problem in probabilities..... x 89	Hopkins, cited on the liquidity of the earth's
electric currents..... x 93	interior..... ii 76, 78
Hill, M., cited on visible speech..... vi 78, 80	temperature of space..... ii 73
Hill, R. T., communication on the topography	Hough, F. B., communication on the culti-
and geology of the Cross Timbers of	vation of Eucalyptus on the Roman
Texas. <i>Read by W J McGee. Reference,</i>	Campagna. <i>Reference</i> vi 36
..... x 6	Death of..... viii 25
Hillhouse, Dr. William, cited on trisection of	House of Representatives, Ventilation of,
angles..... x 99 v 99
Hind, cited on supposed trans-Neptunian	Howland, Dr. E. P., remarks on Charleston
planet..... iii 20	earthquake..... ix 42
Historical note on binocular microscopes,	Hubbard, G. G., remarks on visible speech,
..... iv 35 vi 82
on the method of least squares..... i 62	Hughes' microphone..... iv 184
History of a geometrical problem..... iii 64	Humboldt, Baron von, cited on transmission
Malfatti's problem..... ii 113	of sound..... v 41
Hitchcock, Romyn, communication on recent	Humidity observations..... vi 36
improvements in microscopic ob-	Humphreys, A. A., Eulogy on..... vii 4
jectives, with demonstration of the	Death of..... vii 3, 4
resolving power of a new 1-16th inch.	Humphreys and Abbot, cited on the delta
<i>Title only</i> ix 16	of the Mississippi..... i (10), (12), (13)
Hoffman, Dr. A. W., cited on ultimate	Huron, Altitude of Lake..... ii 23
causes..... v 166	Huxley, T. H., cited on vital principle..... v 78

	Page.		Page.
Hydrometer employed to determine specific gravity.....	vi 26	Irving, R. D., communication on the enlargement of mineral fragments as a factor in rock alteration. <i>Title only.</i>	ix 16
Hygrometers.....	viii 25	Isogram.....	x 4
Hygrometric observations.....	vi 36	Isoselsmal map.....	ix 37, 39
Hymers, J., cited on Malfatti's problem.....	ii 118	Ivory, James, cited on action at no distance.....	v 161
Hyperion, Orbit of.....	iii 26, 40, x 90, 104	Jacobi's method for removing side-coefficients.....	viii 41
Hypothesis, Use of.....	ii 164, vi xxxiii	notation.....	vii 103
Hypsometry, Barometric.....	v 48	Jackson, President, cited on the distribution of surplus among the States.....	vi 103
New method of.....	ii 131	Jackson, Dr., letter on autopsy of Agassiz. <i>Communicated by J. J. Woodward. No abstract.</i>	i 93
Ice fields, Anticlinal and synclinal axes in (22)	ii (22)	Japan, Education in.....	ii 69
pyramids.....	vii 6	Japanese coinage.....	iii 38
Iddings, J. P., communication on the columnar structure in the diabase of Orange Mountain, N. J. <i>Abstract.</i>	4	dry painting.....	viii 16
<i>figures.</i>	viii 19	Jenkins, T. A., remarks on drifting buoy.....	vii 15
Illinois, Flora of.....	iv 99	Johnson, A. B., communication on the history of the light house establishment of the United States. <i>Abstract and reference.</i>	iv 135
Illiteracy and rainfall.....	i 68	recent investigations by the Light House Board on the anomalies of sound from fog-signals. <i>In full. 2 maps. 1 figure.</i>	v 23
Illumination of objects for examination with certain immersion objectives.....	ii 126	some peculiar ravages of the Teredo navalis. <i>Title only.</i>	v 98
Images of stars.....	ix 15	some eccentricities of ocean currents. <i>Abstract.</i>	vii 14
Impressions on polished glass.....	ii 39	the difficulty in determining the direction of sound. <i>Abstract.</i>	viii 11, 12
Indexing scientific literature.....	x 38	Johnson, W. D., communication on a new plane table. <i>No abstract.</i>	x 9
Indian explanation of gravitation.....	vi xxxi	What is topography? <i>Abstract.</i>	x 15
Indians as observers of nature.....	vii 73	Johnston, Gen., cited on the phenomena of sound.....	ii (48)
Errors respecting.....	ii 175	Jones, B., cited on phosphorus and brain disease.....	v 75
(See also <i>Anthropology.</i>)		Jones, Rev. George, cited on zodiacal light.....	i (19), (20), (21), (26)
Inductive reasoning.....	vii lii	Journals of mathematics.....	vi 117
Inertia.....	vii 48	Judd, F. F., communication on the watershed of the Adirondack region. <i>Abstract.</i>	ii 67
Infinite and infinitesimal quantities.....	vi 133	the Adirondack watershed. <i>Abstract.</i>	ii 82
attraction.....	ii 19, viii 58	Jukes, cited on ripple marks.....	ii 61, 62
Ingestion among fishes.....	iii 116	Juvet, —, communication on a time globe. <i>Abstract.</i>	iii 106
Initial meridian, Proposed.....	vi 106	Kampf, Ferdinand, Death of.....	ii 189
Inoculation of diphtheria.....	iv 38	Kanab base line.....	iii 34
through mosquitoes.....	vi 5	Keith, Reuel, communication on achromatic object glasses. <i>Title only.</i>	i 73
Insecticides.....	vii 10		
Insectivorous mammals.....	v 118		
Institutions, Evolution of.....	vi xlviii		
Integrals, Elliptic.....	vii 102, ix 54		
Integration of differential equations admitting periodic integrals.....	x 100		
Interior angle of objective.....	iii 19		
Intermarriage of the deaf.....	vi 83		
International coinage.....	iii 38		
convention of teachers of the deaf and dumb.....	iv 55		
Geodetic Association on standard time.....	vi 106		
scientific telegrams.....	i 101		
symbols for archeologic charts.....	ii 72		
Intervals, Musical.....	ii 199		
Investigation, Methods of.....	ii 163		
Iowa, Loess and drainage system of.....	vi 93		
Quaternary of.....	iv 120		
Irby, J. R. M., communication on the crystalline state of matter. <i>Abstract.</i>	iii 39		

	Page.
Keith, Reuel, communication on—Cont'd. the nature of the force of gravitation. <i>Title only</i>	89
Kempe, A. B., Trisection linkage of.....	92
Kerosene oil tests.....	11
Kerr, M. B., remarks on glaciers.....	8
Kerr, W. C., communication on the geology of Hatteras and the neighboring coast. <i>Abstract</i>	28
the mica mines of North Carolina. <i>Ab- stract</i>	9
Death of.....	viii
Kidder, J. H., communication on deep sea temperature observations. <i>Title only</i> , <i>ix</i>	14
the gilding of thermometer bulbs. <i>Title only</i>	ix
Kilauca.....	13
Kinematic theories of force.....	v 126, vi xxviii
King, A. F. A., communication on the con- servative element in disease. <i>Ab- stract</i>	111
the conservative influence of disease as illustrated in the phenomena of pul- monary phthisis. <i>Abstract</i>	124
the prevention of malarial diseases, illus- trating, <i>inter alia</i> , the conservative function of ague. <i>Abstract</i>	5
King, C., cited on geology of Great Basin.....	56
King, Major, communication on the con- struction of the bridge across East River between Brooklyn and New York. <i>Title only</i>	23
the fatigue of metals. <i>Title only</i>	1
King, S. A., communication on the aerial currents observed in fifty balloon as- censions. <i>Read by C. Abbe. In full</i>	35
Klaproth, cited on mineralogy.....	1
Knight's tour.....	78
Knox, J. J., communication on the distribu- tion of loans in the Bank of France, the national banks of the United States, and the Imperial Bank of Ger- many. <i>Abstract</i>	31
the distribution of the surplus money of the United States among the States.....	103
Kolb, Baron, cited on population.....	iv
Koyle, C. H., communication on the storage of electric energy. <i>Abstract</i>	46
Krakatoa and sun glows.....	vii
Kummell, C. H., communication on compo- sition of error from single causes of error. <i>Reference</i>	v
alignment curves on any surface, with special application to the ellipsoid. <i>Abstract. 1 figure</i>	vi

	Page.
Kummell, C. H., communication on—Cont'd. the theory of errors practically tested by target-shooting. <i>Abstract. 2 figures</i> , <i>vi</i>	138
curves similar to their evolutes. <i>Ab- stract</i>	vii
the quadric transformation of elliptic integrals, combined with the algo- rithm of the arithmetico-geometric mean. <i>Abstract</i>	vii 101, 102
an artifice sometimes useful for the ad- justment of conditioned observations. <i>Abstract</i>	viii
distances on any spheroid. <i>Abstract and reference</i>	viii
Can the attraction of a finite mass be in- finite? <i>In full</i>	viii
the use of Somoff's theorem for evalua- tion of the elliptic integral of the third species. <i>Reference</i>	ix
the brachisthode on the helicoid. <i>Ref- erence</i>	x
remarks on temperature readings.....	vi
infinitesimals.....	vi
conic sections.....	vi
music and the elements.....	viii
Fenerbach's circle.....	viii
time determinations.....	viii
problem in probabilities.....	x
trisection of angles.....	x
Lagrange ignored by the Am. Phil. Soc., <i>viii xxxviii</i>	
Lagrange's method.....	vii
Lake Bonneville.....	i 84, ii 103
and the geoid.....	vii 92, 101, ix 15
Lake Champlain, Ice phenomena on.....	ii (22)
Lake Erie, Altitude of.....	ii
Lake, Great Salt.....	ii 187, 188
Lake Lahontan.....	vii
Lake Michigan, Altitude of.....	ii
Lake Ontario, Changes of level in the basin of.....	ix
Lakelets and landslips.....	ii
Lancaster's classification of meteorological literature.....	x
Landen's transformation.....	vii
Lands of the arid region.....	ii
Landslips and lakelets.....	ii
Lane, J. H., cited on solar physics.....	i
Eulogy of.....	iii
Resolution on the death of.....	iii
Language, Evolution of.....	vi
written and spoken.....	vii
Laplace cited on the solar atmosphere and zodiacal light.....	i (19), (27)

	Page.		Page.
Laplace ignored by the Am. Phil. Soc.,	viii xxxviii	Light-house establishment of the United States.....	iv 135
Laramie flora.....	viii 17	Lightning, Cause of.....	ii 189
Lassell cited on the satellites of Uranus,	i (30), (34)	Limnæa megasoma, Depauperation of.....	ii 75
Observations of Hyperion by.....	iii 40	Limpets.....	vii 4
Latent heat.....	v 137	Linnaeus, cited on growth of stones.....	v 67
impressions on glass.....	ii 39	mineralogy.....	i 77
Latimer, George, Legacy by.....	ii 48	Lippman, G., cited on electricity.....	v 168
Latitude, A method of determining.....	ii 105	List of deceased members.....	iii xiv, viii xxv, ix xxvi, x xxviii
computations.....	x 91	members.....	i 19, (37), ii ix, iii ix, 153, iv 15, v 15, vi xvi, vii xvi, viii xvi, ix xvi, x xvi
of Lockwood's farthest north.....	ix 9	members of the Mathematical Section.	vi 116, vii 86, viii 36, ix 52, x 82
variations of.....	viii 10	recipients of the Bulletin.....	iii 159
Lava fields of New Mexico.....	vii 76	The consolidated.....	x 36
Leadville ores.....	vi 32	Lister, Prof. J., cited on germ culture.....	ii 109
Least square computation.....	vi 150, viii 41	Lithology. See <i>Geology</i> .	
squares.....	i 62, 89	Littrow's telegraphic system.....	i 101
Le Conte, John, communication on the microscopical structure of wool.....	ii 62	Loans by banks in France, Germany, and the United States.....	iv 31
Lee, W., communication on medallie medical history. <i>Abstract</i>	vi 39	Lockwood's expedition to farthest north.....	ix 8
Lefavour, E. B., remarks on infinitesimals,	vi 135	Locusts, Shower of.....	ii 87
music and the elements.....	vii 28	Lodge, Dr. O. J., cited on electricity.....	v 168
Lefroy, letter on changes of sea-level at Bermuda. <i>Communicated by J. Henry.</i>		Loess of eastern Iowa.....	vi 93
<i>No abstract</i>	i 75	Origin of the.....	iv 121
Legendre ignored by the Am. Phil. Soc.,	viii xxxviii	Logical algebra.....	ii 88
Lehmus, Prof. D. C. L., cited on Malfatti's problem.....	i 115	Lombard, J. S., cited on brain temperatures,	v 75
Leibnitz cited on Newton's philosophy.....	v 162	Longitude computation.....	viii 52
Leibnitz's philosophy.....	vii xlii	Loomis, Elias, cited on cyclonic motion,	i 107, 108
Lenses, Achromatic combination of.....	iii 65	retardation of storm centres.....	v 108
Cylindrical.....	vi 4	Lovering, Prof., cited on auroras.....	i 44
Le Sage's theory of cohesion.....	v 129	Loxodrome.....	vi 124
Lesquereux, Prof. L., cited on fossil plants from Virginia.....	ii (38), (40)	Lucas, F. A., communication on museum specimens illustrating biology. <i>Title only</i>	ix 36
Levees of the Mississippi delta.....	i (14)	Lucretius' philosophy.....	vii xxxvii
Levelling instrument, Proposed.....	ii 184	Lull, E. P., communication on the inter-oceanic canal through Nicaragua. <i>Title only</i>	ii 83
Lewes, G. H., cited on action at a distance.....	v 157	Death of.....	x 8
L'Epee's instruction of the dumb.....	vi 63	Lunar theory.....	iv 57, vi 136
Ley cited on cyclonic motion.....	i 107	variation of magnetic declination.....	iii 47
L'Hospital's trisection instrument.....	x 99	Lymph, Motion of the.....	ii 133
Liagre's theory of target shooting.....	vi 138	McClellan, Gen., cited on phenomena of sound.....	ii (48)
Library of the Surgeon General's Office.....	i 92	McCullough, Hon. H., remarks on U. S. surplus given to the State of Indiana.....	vi 106
Lick, James, letter on proposed observatory. <i>Communicated by J. Henry. No abstract</i>	i 91	McDowell, S., cited on thermal belts.....	vi 11
Life.....	i 27, v 49, 102	McGee, W J, communication on the drainage system and the distribution of the loess of eastern Iowa. <i>Abstract</i>	vi 93
and electricity.....	v 57		
force.....	v 57		
Modern philosophical conceptions of.....	v 49		
Light and sound.....	iv 143		
of the sun, passed through a narrow slit,	iii 119		

Page.	Page.
McGee, W J, communication on—Cont'd.	Mars, Satellites of..... ii 181, 186, 189, 190, vi 45
What is a glacier? <i>Abstract</i> vii 38	Marsh, Hon. G. P., cited on individual vocabularies..... ii (16), (19), (21)
the terraces of the Potomac valley.	Marth's method..... vii 98
<i>Title only</i> vii 24	Martin, Artemas, communication on a problem in probabilities. <i>Abstract</i> x 80
the Charleston earthquake. <i>Abstract</i> . ix 37	methods of finding <i>n</i> th -power numbers whose sum is an <i>n</i> th -power. <i>Abstract</i> . x 107
the quaternary deposits and the great displacement of the middle Atlantic slope. <i>Reference</i> x 16	Letter from..... vii 87
remarks on earthquakes..... ix 42	Marvin, C. F., communication on the Flood Rock explosion. <i>Title only</i> viii 28
Machin, cited on computation of π i 53	the electrometer as used in observations of atmospheric electricity. <i>Title only</i> . x 9
McKenney and Hall, cited on diminution of Indians..... ii 175	Marvine, A. R., Biographical notice of..... ii (53)
McMurtrie, William, communication on the meteorological conditions affecting the culture of the sugar beet. <i>Reference</i> , iii 142	Resolutions on the death of..... ii 84
Magic squares..... iii 143	Mass of a planet determined from observations on two satellites..... vi 132
Magnetic declination, Secular change in. iii 45	Mason, O. T., communication on archaeological specimens. <i>Title only</i> ii 48
disturbance and northers..... vii 25	the classification of objects of archaeology. <i>Title only</i> ii 50
storms..... iii 47	international symbols for charts of pre-historical archaeology. <i>Title only</i> ... ii 71, 72
Magnetism. See <i>Electricity</i> .	the decipherment of some Aztec monuments lately discovered in Guatemala. <i>Title only</i> iii 37
Main, R., cited on Saturn's rings..... vi 42	comparison of written language with that which is spoken only. <i>Abstract</i> , iii 139
Mairan, cited on auroras..... i 44	two examples of similar inventions in areas widely apart. <i>Abstract</i> ix 12
Malarial diseases, Prevention of..... vi 5	bowyers and fletchers. <i>Abstract</i> ix 44
Malfatti's problem..... ii 113	remarks on implements of Australia, Aleutian Islands, and North America..... ii 66
Mallery, Garrick, communication on a calendar of the Dakota Indians. <i>Abstract and reference</i> ii 90	the telephone..... ii 104
some common errors respecting the North American Indians. <i>Abstract and reference</i> ii 175	ancient Indian population..... ii 130
customs of every-day life. <i>Abstract</i> ... ix 19	charcoal in the drift..... iv 122
relations between Professor Baird and participating societies..... x 45	Indian observation of nature..... vii 74
remarks on phonetic alphabets..... ix 18	origin of customs..... ix 21
Mallet's contraction hypothesis..... vi 90	Mason, —, communication on kerosene oil tests. <i>Abstract</i> ii 72
method of determining earthquake foci, x 17, 19	Mathematical Journals..... vi 117
Maloney, J. A., Electric investigations by.. v 47	Mathematical Section, Minutes of... vi 121, vii 87, viii 37, ix 53, x 83
Mammals, Classification of..... ii (3)	Organization of..... vi 23, 121
Distribution of..... ii 26	place of meeting..... vii 81
Insectivorous..... v 118	Statistics of..... x 34, 36
Manganese, Estimation of..... ii 132	Mathematics , List of papers on (See also <i>Astronomy</i>):
Man, Zoological relations of..... i 24	on the distance traversed by approaching the North Pole on a loxodromic curve.
Mann, B. P., communication on reference indexing. <i>Abstract</i> x 38	J. E. Hilgard. <i>Title only</i> i 21
remarks on care of pamphlets..... viii 29	[exhibition of chronograph.] J. E. Hilgard. <i>No abstract</i> i 22
throwing-sticks..... ix 14	on a curve of the fourth degree. A. Hall. <i>Abstract and reference</i> i 30
Map of Charleston earthquake..... ix 37, 39	
Gulf of Mexico..... iv 52	
path of meteor of December 24, 1873... ii 160	
Topographic..... x 11	
Maps for use in connection with the transit of Venus, 1874..... i 63	
Marcou, J., cited on paleozoic rocks..... vi 102	
Mariotte, Law of..... v 139	

	Page.
Mathematics, List of papers on—Cont'd.	
on an exponential formula having refer- ence to the tolerance allowed at the U. S. Mint. J. E. Hilgard. <i>Title only</i> ,	1 31
on the locus of the point of equal illu- mination by two unequal lights treated by the quaternion analysis. E. B. Elliott. <i>Title only</i>	1 35
on Hindoo arithmetic. J. E. Hilgard. <i>Title only</i>	1 53
on a series for the determination of the number expressing the ratio of the circumference to the diameter. E. Frisby. <i>In full</i>	1 57
on the experimental determination of the ratio of the circumference to the di- ameter, based on the principles of the calculus of probabilities. A. Hall. <i>Title only</i>	1 62
an historical note on the method of least squares. A. Hall. <i>Reference</i>	1 62
an inquiry into the law of probability. J. E. Hilgard. <i>Title only</i>	1 84
on logical algebra. C. S. Peirce. <i>Refer- ence</i>	1 88
on the mechanical representation of a problem in least squares. S. New- comb. <i>Reference</i>	1 89
on quaternions, as developed from the gen- eral theory of the logic of relatives. C. S. Peirce. <i>Title only</i>	1 94
on affected quantities of the first order. E. B. Elliott. <i>Title only</i>	1 42
approximate quadratures. A. Hall. <i>Ab- stract</i>	1 43
some recent investigations on the theory of invariants. J. J. Sylvester. <i>Title only</i>	1 95
a trigonometrical formula. B. Alvord. <i>Title only</i>	1 104
the history of Malfatti's problem. M. Baker. <i>In full</i> . 2 figures.....	1 113
series. E. Frisby. <i>Title only</i>	1 193
the intersection of circles and the inter- section of spheres. B. Alvord. <i>Title only</i>	1 198
an adjustment of the Carlisle tables of re- versions and annuities. E. B. Elliott. <i>Title only</i>	1 201
new points respecting the intersections of circles and the intersections of spheres. B. Alvord. <i>Title only</i>	1 201
discussion of a geometrical problem, with bibliographical notes. M. Baker. <i>In full</i> . 4 figures.....	111 53, 55

	Page.
Mathematics, List of papers on—Cont'd.	
on magic squares. E. Frisby. <i>Abstract</i> . 6 figures.....	111 143
on the geometrical problem to determine a circle equally distant from four points. M. H. Doolittle. <i>Abstract</i>	v 88
on some of the properties of Steiner's power-circle. B. Alvord. <i>Title only</i> ..	v 89
on composition of error from single causes of error. C. H. Kummell. <i>Reference</i> ,	v 106
on a geometrical question relating to spheres. M. Baker. <i>In full</i>	v 107
on a graphic table for computation. G. K. Gilbert. <i>Abstract</i>	v 120
experiments in binary arithmetic. H. Farquhar. <i>Abstract</i>	v 125, v1 3
formulas for the computation of Easter. E. B. Elliott. <i>In full</i>	v1 14
further experiments in binary arithmetic. H. Farquhar. <i>Abstract</i>	v1 38
inaugural address of the chairman of the Mathematical Section. A. Hall. <i>In full</i>	v1 117
a quasi general differentiation. A. S. Christie. <i>Title only</i>	v1 122
infinite and infinitesimal quantities. M. H. Doolittle. <i>Abstract</i>	v1 133
certain possible abbreviations in the com- putation of the long-period perturba- tions of the moon's motion due to the direct action of the planets. G. W. Hill. <i>Abstract and reference</i>	v1 136
the theory of errors practically tested by target-shooting. C. H. Kummell. <i>Ab- stract</i> . 2 figures.....	v1 138
a special case in maxima and minima. B. Alvord. <i>Abstract</i>	v1 149
form of least-square computation. H. Far- quhar. <i>In full</i>	v1 150
note on the problem discussed by Mr. Al- vord. H. Farquhar. <i>Abstract</i>	v1 152
the rejection of doubtful observations. M. H. Doolittle. <i>Abstract</i>	v1 152
the special treatment of certain forms of observation-equations. R. S. Wood- ward. <i>Abstract</i>	v1 156
contact of plane curves. A. S. Christie. <i>Abstract</i>	v1 157
curves similar to their evolutes. C. H. Kummell. <i>Abstract</i>	v1 87
the problem of the knight's tour. G. K. Gilbert. <i>Abstract</i>	v1 88
empirical formulæ for the diminution of amplitude of a freely-oscillating pen- dulum. H. Farquhar. <i>Abstract</i>	v1 89

	Page.
Mathematics, List of papers on—Cont'd.	
the formulæ for computing the position of a satellite. A. Hall. <i>In full</i>	vii 93
a form of the multinomial theorem. A. S. Christie. <i>Title only</i>	vii 101
the quadric transformation of elliptic integrals, combined with the algorithm of the arithmetico-geometric mean. C. H. Kummell. <i>Abstract</i>	vii 101, 102
a case of discontinuity in elliptic orbits. W. B. Taylor. <i>Abstract</i>	vii 122
the verification of predictions. M. H. Doolittle. <i>Abstract</i>	vii 122
methods of verifying weather predictions. C. Abbe. <i>Abstract</i>	viii 8
example illustrating the use of a certain symbol in the calculus of affected quantity. E. B. Elliott. <i>Title only</i>	viii 37
a collection of formulæ for the area of a plane triangle. M. Baker. <i>Reference</i> , viii 37	viii 37
an artifice sometimes useful for the adjustment of conditioned observations. C. H. Kummell. <i>Abstract</i>	viii 41
a group of circles related to Feuerbach's circle. M. Baker. <i>In full</i> . 4 figures, viii 45	viii 45
distances on any spheroid. C. H. Kummell. <i>Abstract and reference</i>	viii 52
on Grassmann's system of geometry. A. Ziwet. <i>Reference</i>	viii 53
cause and chance in the concurrence of phenomena. M. H. Doolittle. <i>Title only</i>	viii 54
Can the attraction of a finite mass be infinite? C. H. Kummell. <i>In full</i>	viii 58
on the use of Somoff's theorem for the evaluation of the elliptic integral of the third species. C. H. Kummell. <i>Reference</i>	ix 54
graphic methods in research. G. K. Gilbert. <i>Abstract</i>	x 4
association ratios. M. H. Doolittle. <i>Abstract</i>	x 83
a problem in probabilities. <i>Symposium</i> . <i>Abstract</i>	x 87, 89
on the free cooling of a homogeneous sphere initially heated to a uniform temperature. R. S. Woodward. <i>Reference</i>	x 90
on the brachisthode on the helicoid. C. H. Kummell. <i>Reference</i>	x 90
the motion of Hyperion. G. W. Hill. <i>Abstract and reference</i>	x 90
the parallax of a Tauri. A. Hall. <i>Abstract</i>	x 91

	Page.
Mathematics, List of papers on—Cont'd.	
the most probable value of the latitude and its theoretical weight from entangled observations occurring in the use of Talcott's method. A. S. Flint. <i>Abstract</i>	x 91
association ratios. M. H. Doolittle. <i>Abstract</i>	x 93, 94
[solution and generalization of a problem requiring the division of a rectangle into parts which form a square.] H. Farquhar. <i>No abstract</i>	x 96
a collection of solutions of the trisection problem. M. Baker. <i>Abstract</i>	x 96
[on the trisection problem.] G. E. Curtis. <i>Abstract</i>	x 98
the integration of differential equations admitting periodic integrals. G. W. Hill. <i>Abstract and reference</i>	x 100
Euler's theorem (generally called Lambert's). A. Hall. <i>Abstract</i>	x 101
[a new computing machine.] E. B. Elliott. <i>Abstract</i>	x 102
on the constant <i>P</i> in observations of terrestrial magnetism. W. Harkness. <i>Abstract and reference</i>	x 102
the conditioned cooling of a homogeneous sphere. R. S. Woodward. <i>Reference</i>	x 103
the orbit of Hyperion. O. Stone. <i>Abstract and reference</i>	x 104
the quotients of space-directed lines. E. B. Elliott. <i>Abstract</i>	x 105, 106
methods of finding <i>n</i> th -power numbers whose sum is an <i>n</i> th -power. A. Martin. <i>Abstract</i>	x 107
Matter and force.....	xi 30
Combination of.....	vi xxxv
Properties of.....	i 27, v 127, vi 5, vii 40
Three states of.....	v 136
Matteucci cited on muscular contraction...v	59
Matthews, Washington, communication on natural naturalists. <i>Read by J. S. Billings</i> . <i>Abstract</i>	vii 73
mythological dry paintings of the Navajos. <i>Abstract</i>	viii 14
anthropometric and reaction-time apparatus. <i>Abstract</i>	viii 25
Mauna Loa.....	vi 13
Maxima and minima, Special case in...vi	149, 152
Maxwell, Prof. J. C., cited on matter.....v	128
on elasticity.....	v 132
theories of heat.....	v 134
radiant energy.....	v 136
Boyle's law.....	v 139
molecular orbits.....	v 140, 147, 149

	Page.		Page.
Maxwell, Prof. J. C., cited on—Cont'd.		Merrill, G. P., communication on geological museums. <i>Title only</i>	ix 36
dissipation of molecular energy.....	v 153	Metaphysic philosophy.....	vi xxx
surface repulsion.....	v 155	Metaphysics.....	vii xxix
vortex rings.....	vii liv	Metcalf, Capt. H., cited on theory of target practice.....	vi 145
matter.....	vii 44	Meteor, Explanation of explosion of.....	ii 143
Mayer, A. M., communication on a method of determining a definite interval of time, and its application to measuring the number of vibrations of solid bodies. <i>Title only</i>	ii 64	of December 24, 1873.....	i 94, ii 123, 139
Mayer's topophone.....	viii 13	(See also <i>Meteors</i> .)	
Mechanical representation of a problem in least squares	i 89	Meteoric matter and planetary motions,	ii 188, 190
Medallic medical history.....	vi 39	Meteorite, A new.....	vii 32
Medals, Exhibition of.....	v 22	Meteorites at Concepcion and San Gregorio, New Mexico.....	i 24
Meehan, Thos., cited on the common names of plants.....	iv 113	Meteorological work by Joseph Henry.....	ii 236
Meek, F. B., communication on new species of fossil plants from Alleghany Co., Virginia; with some remarks on the rock seen along the Chesapeake and Ohio railroad, near the White Sulphur Springs of Greenbrier county, West Virginia. <i>Read by T. Gill. In full. 2 plates</i>	i 62, ii (26)	of the Smithsonian Institution.....	ii 295
Death of.....	ii 111	Meteorology , List of papers on (See also <i>Thermometry</i>):	
Meigs, M. C., communication on a map of the head waters of the Yellowstone and Lewis rivers. <i>No abstract</i>	i 21	on the aerial currents observed in fifty balloon ascensions. S. A. King. <i>Communicated by C. Abbe. In full</i>	i 35
the movements caused in large ice-fields by expansion and contraction, as illustrative of the formation of anticlinal and synclinal axes in geological formations. <i>In full. 4 figures</i>	ii 33, (22)	[on aerial currents observed in balloon ascensions.] C. Abbe. <i>Abstract</i>	i 38
remarks on glacial period.....	ii 37	on certain remarkable effects of lightning. E. J. Farquhar. <i>Communicated by J. Henry. Title only</i>	i 42
Members. See <i>List of Members</i> .		on the aurora. W. B. Taylor. <i>Abstract</i>	i 43
Membership statistics of scientific societies.....	x 29	on the aurora of February 4th [1872]. J. E. Hilgard. <i>Abstract</i>	i 47
Memoir on the scientific work of Joseph Henry.....	ii 203	on the effects of winds and barometric pressure on the tides of Boston, and on the mean level of the sea. W. Ferrel. <i>Abstract and reference</i>	i 53
Memorial to B. Alvord.....	vii 127	on the meteorology of Japan. T. Antisell. <i>Title only</i>	i 70
(See also <i>Biography</i> .)		on the results of astronomical observations at Sherman Station, Wyoming Terr. R. D. Cutts. <i>Abstract and reference</i>	i 70
Mendenhall, T. C., communication on the measurement of temperature at distant points. <i>Title only</i>	viii 18	on the laws of condensation of aqueous vapor in the atmosphere. E. Foote. <i>Title only</i>	i 74
the Charleston earthquake. <i>Abstract</i> ,	ix 37	on the meteorology of Russia. A. Woeikof. <i>Reference</i>	i 75
remarks on Japanese customs.....	ix 21	on atmospheric electricity. (3 papers.) J. Henry. <i>Title only</i>	i 75, 87
Mercadier, M., cited on radiophony.....	iv 158	on electrical phenomena in the Rocky Mountains. F. M. Endlich. <i>Title only</i> ,	i 95
Mercury, Theory of.....	viii 41	on the distribution of temperature over the surface of the globe. W. Harkness. <i>Reference</i>	i 96
Transit of.....	ii 199, iii 43	on some causes that produce rain. E. Foote. <i>Title only</i>	i 98
Meridian, Proposed initial.....	vi 106	on the laws governing the movement of storm centres. C. Abbe. <i>Abstract</i>	i 99
Meridian transit time determinations.....	viii 55		
Merriam, C. H., communication on the economic phase of the English sparrow question. <i>Reference</i>	x 16		

	Page.
Meteorology , List of papers on—Cont'd.	
on the law connecting the velocity and direction of the wind with the barometric gradient. W. Ferrel. <i>Abstract</i>	106
on the correlation of the winds and the temperatures of the surface waters of the ocean along the coast of New Hampshire. J. W. Chickering. <i>Abstract</i>	17
meteorological observations in Peru, and some of the meteorological conditions of that country. A. Woeikof. <i>Title only</i>	35
the glacial theory. J. Henry. <i>Abstract</i>	35
the causes of glacial climate. <i>Symposium</i> . <i>Abstract</i>	43, 45
the comparison of rain-gauges at different elevations. J. R. Eastman. <i>Abstract</i>	49
a new meteorological instrument. J. W. Osborne. <i>Abstract</i>	63
the hygrometrical condition of the air in high latitudes. E. Bessels. <i>Title only</i> ,	66
the horary oscillations of the temperature of the atmosphere. G. K. Gilbert. <i>Abstract</i>	67
horary oscillations of the atmosphere. G. K. Gilbert. <i>Abstract</i>	69
facts relating to the falling of waterspouts in North Carolina. T. L. Clingman. <i>Abstract</i>	104
the causes of electrical developments in thunderstorms. E. Foote. <i>Abstract</i>	139
suggestions respecting the study of meteorology in regard to the causes of yellow fever. J. W. Osborne. <i>Title only</i> ,	21, 27
a curious manifestation of force by the wind. J. W. Osborne. <i>Title only</i>	27
air currents on mountain slopes. G. K. Gilbert. <i>Abstract</i>	33
on the meteorological conditions affecting the culture of the sugar beet. W. McMurtrie. <i>Reference</i>	142
[the aurora borealis.] C. Abbe. <i>Abstract</i>	21
on the conditions determining temperature. W. Ferrel. <i>In full</i>	90, 91
on errors of barometric observations produced by wind. G. K. Gilbert. <i>Reference</i>	91
on solar radiation at Sherman, Wyoming. W. Ferrel. <i>Title only</i>	101
on the retardation of storm centres at elevated stations, and high wind as a probable cause. H. A. Hazen. <i>In full</i>	103

	Page.
Meteorology , List of papers on—Cont'd.	
[a remarkable halo.] W. B. Taylor. <i>Abstract</i>	112
on a graphic table for computation. G. K. Gilbert. <i>Abstract</i>	120
on the coming winter of 1832-'83. H. A. Hazen. <i>Abstract</i>	122
the response of terrestrial climate to secular variations in solar radiation. G. K. Gilbert. <i>Abstract</i>	10
the thermal belts of North Carolina. J. W. Chickering. <i>Abstract</i>	11
hygrometric observations. H. A. Hazen. <i>Abstract</i>	36
the Rochester (Minnesota) tornado. J. R. Eastman. <i>Abstract</i>	3
the sun-glow. H. A. Hazen. <i>Abstract and reference</i>	17
the relations between northers and magnetic disturbances at Havana. G. E. Curtis. <i>Reference</i>	25
methods of verifying weather predictions. C. Abbe. <i>Abstract</i>	8
thunderstorms of 1884. H. A. Hazen. <i>Abstract</i>	10
the condensing hygrometer and sling psychrometer. H. A. Hazen. <i>Abstract</i> ,	25
normal barometers. T. Russell. <i>Title only</i>	46
the sky-glow of 1883. H. A. Hazen. <i>Title only</i>	6
the theory of the wind-vane. G. E. Curtis. <i>Reference</i>	9
the electrometer as used in observations of atmospheric electricity. C. F. Marvin. <i>Title only</i>	9
relation between wind velocity and pressure. H. A. Hazen. <i>Reference</i>	10
the Signal Service bibliography of meteorology. C. Abbe. <i>In full</i>	20
memorandum on the Signal Service bibliography of meteorology and terrestrial magnetism. C. J. Sawyer. <i>Read by C. Abbe. In full</i>	23
Meteors and comets.....	94
Method of least squares.....	62, 89, 150, 111
research.....	163, 111, 111
Methods of evolution.....	11, 11
modern petrography.....	11, 36
verifying predictions.....	11, 122
verifying weather predictions.....	11, 8
Metric system.....	4
advocated by Geodetic Commission.....	11, 109
for postal purposes.....	11, 15, 19
in microscopy.....	11, 22

	Page.
Mexico, Gulf of.....	iv 52
Meyer's atomic volume curve.....	vii 15
Mica mines of North Carolina.....	vii 9
Michelson, A. A., communication on the modifications suffered by light in passing through a very narrow slit. <i>Abstract</i>	iii 119
Michigan, Altitude of Lake.....	ii 23
Micrometry, Standard for.....	iii 22
Micron.....	iii 23
Microphone, Hughes'.....	iv 184
Modification of Wheatstone's.....	iv 183
Microscopy , List of papers on (See also <i>Optics</i>):	
on the desirability of reproducing photographs of scientific objects and especially of magnified microscopical preparations in a permanent form by some photo-mechanical method. J. J. Woodward. <i>Abstract</i>	i 41
on the use of monochromatic sunlight as an aid to high power definition. J. J. Woodward. <i>Abstract and reference</i>	i 47
on micrometric writing on glass. J. J. Woodward. <i>Title only</i>	i 93
on the modern microscope, Nobert's lines, and the attempts of others to construct them. J. J. Woodward. <i>Title only</i>	ii 25
diffraction phenomena in the field of the microscope. J. J. Woodward. <i>Abstract and reference</i>	ii 60
the microscopical structure of wool. J. J. Woodward and John Leconte. <i>Title only</i>	ii 62
the use of photography in connection with the micrometer measurement of blood corpuscles. J. J. Woodward. <i>Title only</i>	ii 79
a simple device for the illumination of balsam-mounted objects for examination with certain immersion objectives whose "balsam angle" is 90° or upwards. J. J. Woodward. <i>In full</i> . <i>1 figure</i>	ii 126
on the apertometer of Prof. E. Abbe, of Jena, Germany. J. J. Woodward. <i>Abstract</i>	iii 18
on a standard for micrometry. J. J. Woodward. <i>Abstract</i>	iii 22
on the oil-immersion objectives of Zeiss, and on convenient methods of obtaining oblique illumination for these and similar objectives. J. J. Woodward. <i>Abstract</i>	iii 25
a new apertometer for microscopic objectives. J. J. Woodward. <i>Title only</i>	iii 37

	Page.
Microscopy , List of papers on—Cont'd.	
Riddell's binocular microscopes—an historical notice. J. J. Woodward. <i>Abstract and reference</i>	iv 35
[exhibition of a collection of microscopes.] J. S. Billings. <i>No abstract</i>	vii 73
recent improvements in microscopic objectives, with demonstration of the resolving power of a new 1-16th inch. R. Hitchcock. <i>Title only</i>	ix 16
Milneria minima.....	viii 5
Mills, cited on thermometry.....	ix 30
Mind and body.....	v 72
Mineralogy , List of papers on :	
on mineralogical systems. F. M. Endlich. <i>In full</i>	i 77
on specimens of meteoric iron from Chihuahua, Mexico, and the structure of meteorites in general. F. M. Endlich. <i>Title only</i>	i 98
on the occurrence of pure tellurium in certain gold mines of Colorado. F. M. Endlich. <i>Title only</i>	i 101
on some interesting cases of metamorphism. F. M. Endlich. <i>Title only</i>	ii 27
some observations on the crystalline state of matter. J. R. M. Irby. <i>Abstract</i>	iii 39
topaz from Stoneham, Maine. F. W. Clarke and J. S. Diller. <i>Abstract and reference</i>	viii 5
the enlargement of mineral fragments as a factor in rock alteration. R. D. Irving. <i>Title only</i>	ix 16
the present status of mineralogy. F. W. Clarke. <i>Title only</i>	x 6
Misapplication of geographical terms.....	i 39
Miscellaneous Papers , List of :	
anniversary address, Nov. 18, 1871; [on the organization and objects of the Society.] J. Henry. <i>In full</i>	i v, 34
on the preservation of foods. A. B. Eaton. <i>Title only</i>	i 22
[exhibition of a chronoscope.] J. E. Hilgard. <i>No abstract</i>	i 23
on the construction of the bridge across East River between Brooklyn and New York. Major King. <i>Title only</i>	i 23
on the new coinage of Japan. E. B. Elliott. <i>Title only</i>	i 31
on apothecaries' weights and measures. B. F. Craig. <i>Title only</i>	i 34
on the measurement of the pressure developed by the explosion of gunpowder in firearms. C. E. Dutton. <i>Title only</i>	i 52

	Page.
Miscellaneous Papers, List of—Cont'd.	
on the expenditure of the income of the Bache fund for 1872. J. Henry. <i>Title only</i>	i 53
an account of some recent experiments on different kinds of gunpowder at Fortress Monroe. C. E. Dutton. <i>Title only</i>	i 54
[the Woodbury photo-relief process.] J. J. Woodward. <i>Abstract</i>	i 57
[the condition of the Society.] J. Henry. <i>No abstract</i>	i 64
on the water supply of cities. B. F. Craig. <i>Title only</i>	i 65
on the collection of a large library. J. S. Billings. <i>Abstract</i>	i 92
a description of a new spirometer. G. A. Otis. <i>Title only</i>	i 94
on recent improvements in the economy of fuel. C. E. Dutton. <i>Title only</i>	i 96
on recent improvements in the manufacture of steel. C. E. Dutton. <i>Title only</i> , i 97	i 97
on Giffard's injector. J. Henry. <i>Title only</i>	i 99
on the method adopted in writing the international scientific telegrams. A. Hall. <i>Abstract</i>	i 101
[on scientific culture in the Argentine Republic.] B. A. Gould. <i>No abstract</i>	i 15
on the present state of the sciences. C. W. Shields. <i>Abstract and references</i>	i 16
on the gathering, packing, transportation, and exposure of fruits for sale. S. C. Busey. <i>Title only</i>	i 16
on the failure of the wooden pavements of Washington City. L. D. Gale. <i>Abstract</i>	i 26
on latent impressions on polished glass plates produced by heating the plates in close connection with engraved metallic plates. A. C. Ross. <i>Abstract</i>	i 39
iron facing copper plates. J. E. Hilgard. <i>Abstract</i>	i 42
the progress of the natural sciences during the past century. T. N. Gill. <i>Reference</i>	i 56
cylinder condensation, steam jackets, and superheated steam. G. B. Dixwell. <i>Title only</i>	i 64
the coinage of the Argentine Republic. B. A. Gould. <i>Communicated by E. B. Elliott. Abstract</i>	i 65
the progress which [has] been made in educational matters in [Japan.] D. Murray. <i>Abstract</i>	i 69

	Page.
Miscellaneous Papers, List of—Cont'd.	
illuminating materials. J. Henry. <i>Title only</i>	ii 71
[kerosene oil tests.] ——— Mason. <i>Abstract</i>	ii 72
paper made of asbestos. J. Henry. <i>Title only</i>	ii 86
the burning of theatres and public halls. J. M. Toner. <i>Reference</i>	ii 95
the rulings on glass by Mr. Rogers, of Cambridge. J. J. Woodward. <i>Abstract</i> , ii 130	ii 130
the uses of [the] dynagraph, and the work performed in determining the resistance of trains, etc. P. H. Dudley. <i>Abstract</i>	ii 29
phosphorescent clocks. J. E. Hilgard. <i>Abstract</i>	ii 33
the work of the National Board of Health. J. S. Billings. <i>Title only</i>	ii 50
[yellow fever disinfection.] F. M. Gunnell. <i>Abstract</i>	ii 51
[exhibition of a time globe.] ——— Juvet. <i>Abstract</i>	ii 106
sugar from sorghum. P. Collier. <i>Abstract</i> , ii 140	ii 140
the scientific work carried on under the direction of the National Board of Health. J. S. Billings. <i>Abstract</i> , iv 37	iv 37
the history of the light house establishment of the United States. A. B. Johnson. <i>Abstract and reference</i>	iv 135
relation of meteorological conditions to the summer diarrhoeal diseases. S. C. Bnsey. <i>Abstract and reference</i>	iv 165
[exhibition of a panoramic photograph.] W. B. Taylor. <i>Abstract</i>	v 21
[exhibition of coins and medals.] J. M. Toner. <i>Abstract</i>	v 22
on the ventilation of the House of Representatives. J. S. Billings. <i>Abstract</i> , v 99	v 99
on the philosophical order of the sciences. C. W. Shields. <i>Reference</i>	v 105
on the fisheries of the world. G. B. Goode. <i>Reference</i>	v 117
the cultivation of eucalyptus on the Roman Campagna. F. B. Hough. <i>Reference</i>	vi 36
sketches from medallic medical history. W. Lee. <i>Abstract</i>	vi 39
fisheries exhibitions. G. B. Goode. <i>Reference</i>	vii 26
American scientific societies. A. Hall. <i>Presidential address. In full</i> , viii xxxiii, 30	viii xxxiii, 30

	Page.
Miscellaneous Papers, List of—Cont'd.	
the systematic care of pamphlets. G. Brown Goode. <i>Abstract and reference.</i>	viii 29
the systematic care of pamphlets. C. V. Riley. <i>Abstract.</i>	viii 29
scientific men and their duties. J. S. Billings. <i>Presidential address. In full.</i>	ix xxxv, 46
when I first saw the cholera bacillus. R. D. Mussey. <i>Title only.</i>	ix 22
the frequency of coincidences. L. F. Ward. <i>Abstract.</i>	x 8
Manchester meeting of the British Association for the Advancement of Science, 1887. F. W. Clarke. <i>Title only.</i>	x 19
on reference indexing. B. P. Mann. <i>Abstract.</i>	x 38
Mississippi delta.	i (10)
Missouri, Valley of the Upper.	vii 20
Mivart, St. G., cited on life.	v 52
Model of the basin of the Gulf of Mexico.	iv 52
Mohs, cited on mineralogy.	i 78, 79
Molecular excursions.	v 140, 141
heats of similar compounds.	i 104
kinetics.	v 133
physics. See <i>Physics</i> .	
Molecules, atoms, and waves.	i 66
size of.	v 141
complexity of.	v 147
Mollusks, Appendages of.	vii 32
found at great depths.	v 90
Observations on.	iii 75
Two remarkable.	viii 5
Moore, Commander, cited on Plover Bay.	iv 124
Moon, Theory of.	iv 57, vi 136
Moon's eclipse of June 11, 1881.	v 90
motion, Computation of.	vi 136
Money, Gold and silver.	iii 78, 107
Mono craters.	vii 19
Monochromatic aberration in aphakia.	vi 5
sunlight as an aid to high definition.	i 47
Monoclinical ridges.	ii 74
More, Henry, cited on matter.	vii xlij
Morphology, Biologic.	iv 123
of the antlers of the Cervidæ.	i 135
Morse, E. S., cited on disparity of sexes in Buccinum.	iii 75
Mortality among army officers.	ii 49
statistics of the tenth census.	iv 164
Mosher, Experiments of.	ii 40
Mosler, cited on phosphorus and cerebral activity.	v 75
Mosquito inoculation.	vi 5
Mosso, Pletysmograph of.	v 77
Motion, Laws of.	vii 56

	Page.
Motion, Modes of.	vi xxxviii
of a particle toward an attracting centre.	i 88, ii 19, vii 122
Transmutation of.	vi xxviii
Mount Dana glacier.	vii 5
Mount Lyell glacier.	vii 6
Mount Rainier and its glaciers.	x 10
Mount Taylor, Geology of.	vii 77
Mount Washington meteorological observations.	v 108
Movement of storm centres.	i 99
Muir's glacier observations.	vii 8
Munroe, C. E., communication on the estimation of manganese as pyrophosphate. <i>Read by T. Antisell. Reference.</i>	ii 132
the determination of the specific gravity of solids by the common hydrometer. <i>In full.</i>	vi 26
Murdoch, John, remarks on throwing-sticks.	ix 13
Murray, David, communication on the progress which has been made in educational matters in Japan. <i>Abstract.</i>	ii 69
Muscular contraction.	v 58
Museum, National.	ii 292
Museum specimens illustrating biology.	ix 35
Music and the chemical elements.	vii 26
Musical intervals.	ii 199
Mussey, R. D., communication on the application of physical methods to intellectual science. <i>Abstract.</i>	vii 18
when I first saw the cholera bacillus. <i>Title only.</i>	ix 22
remarks on artesian wells.	v 101
phonetic alphabets.	ix 18
Myer, A. J., Death of.	iv 236
Resolution on the death of.	iv 31
Mythological dry painting of the Navajos.	viii 14
Mythology of the Numas.	i 96
National Academy of Sciences.	viii xl
National Board of Health, Scientific work by the.	iv 37
National Museum.	ii 292, x 57
Natural naturalists.	vii 73
Navajo dry painting.	viii 14
Naval Observatory, New telescope of.	i 62, 63
star catalogue.	i 74
Navigation, Sumner's method in.	ii 105
Nebraska, Quaternary of.	iv 120
Nebula of Andromeda.	ix 14
Nebulæ, Drawings of.	ii 51
Planes of certain.	ii 109
Nebular hypothesis and the satellites of Mars.	ii 186, 188, 190, vi 45

Page.	Page.
Necks of volcanoes.....vii	78
Nerve currents.....v	60
Névé and glacier defined.....vii	37
Nevada, Glacial epoch in.....i	84
Physical features of.....i	54
Volcanic activity in.....i	99
New Hampshire, Relation of winds to sea temperature on the coast of.....ii	17
New Mexican volcanoes and lava-fields.....vii	76
New star.....ix	14
Newberry, Dr. J. S., cited on fossil plants from Virginia.....ii (38), (42)	
Newcomb, Simon, communication on the transits of Venus, past and future. <i>Title only</i>i	29
the possibility of a universal atmosphere. <i>Title only</i>i	52
the progress of the construction of the new telescope for the Naval Observatory. <i>Reference</i>i	62, 63
the proceedings of the commission to arrange for the observation of the next transit of Venus. <i>Title only</i>i	65
the mechanical representation of a problem in least squares. <i>Reference</i>i	89
the transit of Venus. <i>Title only</i>ii	41
a thermodynamic theory of the spectrum. <i>Title only</i>iii	41, 43
the cosmogony. <i>Title only</i>ii	113
the recent transit of Mercury [1878]. <i>Abstract</i>i	199
observations of the total solar eclipse, July 29, 1878. <i>Abstract</i>ii	202
the recurrence of eclipses. <i>Title only</i>iii	33
a recent visit to California to inspect a site for the new Lick observatory. <i>Title only</i>iii	45
the future of the human race regarded from the standpoint of evolution. <i>Presidential address, 1879. Title only</i>iii	52
the principles of taxation. <i>Title only</i> , iii	119
the relation of scientific method to social progress. <i>Presidential address, 1880. In full</i>iv	40
the speed of propagation of the Charleston earthquake. <i>Reference</i>x	28
remarks on auroras.....i	46
the radiometer.....ii	81
passage of light through a narrow slit, iii	120
auroras.....iv	22
Benjamin Peirce.....iv	26
Newton, Henry, Researches in the Black Hills by.....iii	125
Newton, Prof. H. A., cited on the aurora.....iv	22
Newton, Sir Isaac, cited on action at a distance.....v	159
atoms.....vii	xliv
elasticity.....v	130
laws of orbits.....v	146
the spectrum.....v	142
the ultimate.....v	165, 167
trisection of angles.....x	97
Newton's rings.....v	155
Newtonian formula of gravitation, Modification of.....viii	39
philosophy.....vii	45
Niagara Falls, Earth tremors at.....iv	186
Nichol, J. P., Thermometric experiments of.....v	93
Nicholson, W. L., report of the committee to collect information relative to the meteor of December 24th, 1873. <i>In full. Map and 2 figures</i>ii	139
remarks on the effect of magnetism on the length of magnetic bars.....ii	373
Nomogram.....x	4
Normal section in geodesy.....vi	123
North American Indians, Errors respecting, ii	175
North Carolina coast, Geology of.....vi	28
earthquakes.....i	101, 104
mica mines.....vii	9
thermal belts.....vi	11
waterspouts.....ii	104
Norther and magnetic disturbance.....vii	25
Nth-power numbers whose sum is an nth-power.....x	107
Numas, Genesis and demonology of.....i	104
Mythology of.....i	96
Nymphalidae, Pupation of.....iii	41
Objective, Interior angle of.....iii	19
Achromatic.....iii	65
Objectives, Color corrections to achromatic, iii	39
Oil-immersion.....iii	25
Oblateness of the earth, Change in.....viii	19
Oblique illumination in microscopy.....iii	23
Observation and experimentation, Principles of.....ii	163, vii
Observation equations, Special treatment of certain.....vi	156, viii
Observations of the meteor of Dec. 24, 1873.....ii	144
Occult force.....vi	xxxiii
qualities.....v	126
Oceanography , List of papers on: on the effects of winds and barometric pressure on the tides of Boston, and on the mean level of the sea. W. Ferrel. <i>Abstract and reference</i>i	53

	Page.
Oceanography , List of papers on—Cont'd.	
[letter on changes of sea-level at Bermuda.] J. H. Lefroy. <i>Communicated by J. Henry. No abstract.</i>	1 75
on the tides of the Bay of Fundy. Mr. Ramsay. <i>Communicated by J. J. Woodward. Title only</i>	1 94
Sumner's method in navigation. J. H. C. Coffin. <i>In full</i>	1 105
the navy compass. B. F. Greene. <i>Title only</i>	1 123
an adjustable binnacle for the correction of a ship's compass. B. F. Greene. <i>Title only</i>	1 134
optical salinometer. J. E. Hilgard. <i>Abstract</i>	1 185
temperatures of the Pacific Ocean. T. Antisell. <i>Abstract</i>	1 192
the deep sea dredgings in the Gulf of Mexico and the West Indies in 1873-1878, by Professors Louis and Alexander Agassiz and the officers of the U. S. Coast Survey. W. H. Dall. <i>Title only</i> ,	iii 45
on Siemens' deep sea thermometer and Carré's ice machine. J. E. Hilgard. <i>Title only</i>	v 100
some eccentricities of ocean currents. A. B. Johnson. <i>Abstract</i>	vii 14
historical sketch of deep sea temperature observations. J. H. Kidder. <i>Title only</i>	ix 14
Odor, Theory of.....	viii 27
Office, Rotation in.....	v 49
Officers, Duties of. (See <i>Standing Rules</i> .)	
for 1871.....	i 20
1872.....	i 32, 33
1873.....	i 64
1874.....	i 91
1875.....	i 16
1876.....	i x, 59, 84
1877.....	i 86
1878.....	i 161
1879.....	iii 17
1880.....	iii 51, 53, 151
1881.....	iv 30
1882.....	v 14, 85, 112
1883.....	v 175, vi xiv, 41, 122
1884.....	vi xv, vii xiv, 36, 85
1885.....	vii xv, viii xiv, 36
1886.....	viii xv, ix xiv, 52
1887.....	ix xv, x xiv, 82
1888.....	x xv
of the Army and Navy as scientific administrators.....	ix xlix

	Page.
Ogden, H. G., communication on What is topography? <i>Abstract</i>	x 15
Oil-immersion objectives.....	iii 25
Oldberg, R., The Flora Columbiana of.....	iv 65
Omaha Indians, Gentle system of.....	iii 128
Omar Cheyam, Calendar proposed by.....	i 38
Onatsevich, Lt. M. S., Co ordinates of Plover Bay by.....	iv 128
Ontario Basin, Changes of level in.....	ix 8
Ophthalmology. (See <i>Optics</i> .)	
Optical salinometer.....	i 185
Optics , List of papers on (see also <i>Microscopy</i>):	
on a new method for detecting and measuring the optical defects of the eye. W. Thomson. <i>Reference</i>	i 22
on achromatic object glasses. R. Keith. <i>Title only</i>	i 73
[exhibition of spectra and spectroscopes.] J. J. Woodward. <i>No abstract</i>	i 89
half-vision. J. Henry. <i>Title only</i>	i 60
the markings on <i>Navicula rhomboides</i> . J. J. Woodward. <i>Title only</i>	i 69
the color corrections of achromatic objectives. W. Harkness. <i>Abstract</i>	iii 39
a thermodynamic theory of the spectrum. S. Newcomb. <i>Title only</i>	iii 41, 43
some apparatus recently brought into use by the medical department of the Army for the examination of the eye. J. J. Woodward, <i>Abstract</i>	iii 53
the number of lenses required in an achromatic objective, consisting of infinitely thin lenses in contact, in order that, with any given law of dispersion whatever, the greatest possible number of light-rays of different degrees of refrangibility may be brought to a common focus. W. Harkness. <i>In full</i>	iii 65
the modifications suffered by light in passing through a very narrow slit. A. A. Michelson. <i>Abstract</i>	iii 119
color perception and color blindness. S. M. Burnett. <i>Abstract and reference</i> ,	iv 54
refraction in the principal meridians of a triaxial ellipsoid, regular astigmatism and cylindrical lenses. S. M. Burnett. <i>Reference</i>	vi 4
the monochromatic aberration of the human eye in aphakia. W. Harkness. <i>Reference</i>	vi 5
the character of the focal lines in astigmatism. S. M. Burnett. <i>Abstract</i> ,	vi 45

	Page.
Peirce, C. S., communication on—Cont'd.	
the coincidence of the geographical distribution of rain fall and illiteracy, as shown by the statistical maps of the ninth census reports. <i>Abstract</i>	i 68
logical algebra. <i>Reference</i>	i 88
quaternions, as developed from the general theory of the logic of relatives. <i>Title only</i>	i 94
various hypotheses in reference to space. <i>Title only</i>	i 97
Peirce's criterion.....	vi 155
Pendulum formulæ	vii 89, 101
Perception of color, form, and light.....	vii 72
Periodic integrals.....	x 100
law of the chemical elements.....	vii 15
Permian formation of North America.....	iii 67, 104
Persian calendar.....	i 38
Perturbations of moon's motion, Computation of.....	vi 136
Polyhymnia by Jupiter.....	viii 54
Peru, Meteorology of.....	i 35
Peters, Prof. C. H. F., cited on supposed trans-Neptunian planet.....	iii 20
letter on transit of Venus, 1874. <i>Communicated by A. Hall. Abstract</i>	i 31
Petrographic methods.....	vii 36
Phenomena, Physical basis of.....	vii 40
Philosophical Society of Washington.....	viii xlv
Growth of.....	x 47
why this name was chosen.....	i v, x 45
Phonetic alphabet.....	ix 17
Phosphorescent clocks.....	iii 33
Phosphorus and cerebral activity.....	v 75
Photo-engraving.....	i 41
Photographic panorama.....	v 21
Photographing the sun's corona.....	iii 117
transit of Venus, 1882.....	vi 21
Photographs of transit of Venus, 1874.....	i 31
Photography as an aid to astronomy.....	i 28
an aid to research.....	i 41
Composite.....	vii 25
Photometry, Stellar.....	i 63
Photophone.....	iv 143
Phthisis.....	i 124
Physical geography. (See <i>Geography and Geology</i> .)	
Physical-geographical divisions of the southeastern portion of the United States,	ix 22
Physical investigations by Joseph Henry.....	i 271
method in intellectual sciences.....	vii 18
Physics, List of papers on (see also <i>Acoustics, Optics, Electricity</i>):	
on the nature and origin of force. W. B. Taylor. <i>Abstract and reference</i>	i 27

	Page.
Physics, List of papers on—Cont'd.	
on the fatigue of metals. Major King. <i>Title only</i>	i 53
on waves, molecules, and atoms. W. B. Taylor. <i>Abstract</i>	i 66
on the rectilinear motion of a particle toward an attracting centre. A. Hall. <i>Reference</i>	i 88
on the motion of a particle towards an attracting centre. H. H. Bates. <i>Title only</i>	i 89
on the nature of the force of gravitation. R. Keith. <i>Title only</i>	i 89
on a method of developing magnetism in bars of steel. J. Henry. <i>Title only</i> ,	i 97
on the movement of a particle attracted towards a point. H. H. Bates. <i>Abstract</i>	i 19
a method of determining a definite interval of time, and its application to measuring the number of vibrations of solid bodies. A. M. Mayer. <i>Title only</i>	i 64
Crookes' radiometers. J. Henry. <i>Abstract</i>	i 80
force and momentum. E. B. Elliott. <i>Title only</i>	i 84
a thermodynamic theory of the spectrum. S. Newcomb. <i>Title only</i>	iii 41, 43
vortex motion in ordinary fluids. T. Craig. <i>Reference</i>	iii 143
curious fallacy as to the theory of gravitation. B. Alvord. <i>In full</i>	v 85
on physics and occult qualities. W. B. Taylor. <i>Presidential address. In full</i> ,	v 125, 126
the three methods of evolution. J. W. Powell. <i>Presidential address. In full</i> ,	vi xxvii, 110
the nature of matter. H. H. Bates. <i>Reference</i>	vi 5
substance, matter, motion, and force. M. H. Doolittle. <i>Title only</i>	vi 14
the atomic philosophy, physical and metaphysical. J. C. Welling. <i>Presidential address. In full</i>	vii xxix, 81
music and the chemical elements. M. H. Doolittle. <i>Abstract</i>	vii 26, 27
review of the theoretical discussion in Prof. P. G. Tait's "Encyclopædia Britannica" article on mechanics. H. Farquhar. <i>Abstract</i>	vii 29
the physical basis of phenomena. H. H. Bates. <i>In full</i>	vii 40
a formula for the length of a seconds-pendulum. G. W. Hill. <i>Reference</i>	vii 101

	Page.		Page.
Physics, List of papers on—Cont'd.		Political Economy, List of papers on—	
a slight modification of the Newtonian formula of gravitation. W. B. Taylor. <i>Abstract</i>	viii 39	Cont'd.	
Can the attraction of a finite mass be infinite? C. H. Kummell. <i>In full</i>	viii 58	[change in value of dollar.] E. B. Elliott. <i>No abstract</i>	1 91
Newton's vis. M. H. Doolittle. <i>Title only</i> , x	38	on the credit of the United States, as shown by the value of its securities. E. B. Elliott. <i>Title only</i>	1 109
the free cooling of a homogeneous sphere initially heated to a uniform temperature. R. S. Woodward. <i>Reference</i>	x 90	on the transition in Germany, and the Scandinavian nations of Sweden, Norway, and Denmark, from the silver standard of coinage and money of account to a gold standard. E. B. Elliott.....	11 25
the conditioned cooling of a homogeneous sphere. R. S. Woodward. <i>Reference</i>	x 103	the mutual relations as to price of gold, silver bullion, silver coin, and greenbacks. E. B. Elliott. <i>Title only</i>	11 50
Physics of the Mississippi river.....	1 (13)	mutual relation as to price of gold, greenbacks, silver bullion, and silver coin. E. B. Elliott. <i>In full</i>	11 52
Piedmont region.....	ix 24	two propositions, now before Congress, for changing the coin of the United States. E. B. Elliott. <i>Title only</i>	11 68
Pile of balls.....	111 76	monetary standards. E. B. Elliott. <i>Title only</i>	11 85
Piles bored by teredo.....	v 98	mutual relations of gold and silver, and of prices of commodities. E. B. Elliott. <i>Abstract</i>	11 87
Pisciculture.....	x 55	optional monetary standards. E. B. Elliott. <i>Title only</i>	11 135
Plains, Artesian wells on the.....	v 101	the progress of international coinage in France and America. E. B. Elliott. <i>Title only</i>	11 27
Plane curves, Contact of.....	v 157	the subject of international coinage. E. B. Elliott. <i>Abstract</i>	11 38
Planet, Centre of apparent disk of.....	11 181	the silver question. C. E. Dutton. <i>In full</i>	11 78
search for intra-Mercurial.....	11 85	the silver question. <i>Symposium. Abstract</i>	11 107
supposed discovery of a trans-Neptunian, 111	20	the construction of the Government sinking fund. E. R. Elliott. <i>Abstract</i>	11 113
Planetary mass determined from two satellites.....	vi 132	the principles of taxation. S. Newcomb. <i>Title only</i>	11 119
motion as affected by meteoric matter, 11 188, 189, 190	vi 41	the distribution of loans in the Bank of France, the national banks of the United States, and the Imperial Bank of Germany. J. J. Knox. <i>Abstract</i> , iv	31
motions.....	11 26, vi 41	[bi-metallism.] E. B. Elliott. <i>Abstract</i> , iv	141
perturbations of the moon.....	vi 136	accrued interest on Government securities. E. B. Elliott. <i>Title only</i>	v 21
Planets, Theory of.....	iv 57	on the credit of the United States, past, present and prospective. E. B. Elliott. <i>Title only</i>	v 102
Plants, Climate of.....	11 183	on some formulæ relating to Government securities. E. B. Elliott. <i>Title only</i>	v 106
on Roan Mountain.....	iv 63		
Plateau region.....	1 55, vi 76		
Plato cited on philosophy.....	vii xxxvi		
Plethysmographs.....	v 77		
Pleurotomaria, Notch in shell of.....	111 76		
Plover Bay, Alaska.....	iv 124		
Plücker, Prof. J., cited on Malfatti's problem 11	118		
Plumb-line deflection.....	11 82, vi 92, 101, ix 15, 53		
Poggendorf corrections in thermometry.....	ix 29		
Poinsot, Louis, cited on impact of inelastic bodies.....	v 131		
Poisoned arrows.....	11 180, 182		
Poisson cited on temperature of space.....	11 73		
Polar expedition.....	11 89		
Polaris expedition.....	1 92		
Polarization of light by a narrow slit.....	111 119, 124		
Pole, Shifting of the earth's.....	viii 10		
Political Economy, List of papers on :			
on the statistics of the borrowing power of the United States. E. B. Elliott. <i>Title only</i>	1 29		
on international coinage. E. B. Elliott. <i>Title only</i>	1 75		

	Page.		Page.
Political Economy , List of papers on— Cont'd.		Powell, J. W., communication on—Cont'd.	
the distribution of the surplus money of the United States among the States. J. J. Knox. <i>Abstract</i>	vi 103	the three methods of evolution. <i>Presi- dential address. In full</i>	vi xxvii, 110
a financial problem. E. B. Elliott. <i>Title only</i>	vi 149	plan for the subject bibliography of North American geologic literature. <i>Title only</i>	vii 71
annual profit to banks of national bank note circulation. E. B. Elliott. <i>Title only</i>	ix 14	the personal characteristics of Professor Baird. <i>In full</i>	x 71
quantity of United States subsidiary silver coin existing and in circulation. E. B. Elliott. <i>Title only</i>	ix 14	remarks on auroras.....	i 48
Polyhymnia, Perturbations of.....	viii 54	volcanism in Arizona and Nevada.....	i 99
Poncelet, cited on Feuerbach's circle.....	viii 45	distribution of volcanic action.....	i 102
Population, Animal, of the globe.....	iv 27	the vocabulary of the Utes.....	i 28
of the earth.....	iv 28	ripple marks.....	ii 62
Westward movement of.....	i 35	khivas.....	ii 66
Porter, —, communication on recent ex- plorations in Syria under the auspices of the Palestine Exploration Fund. <i>Title only</i>	i 54	landslip lakes.....	ii 69
Porter, Miss S., cited on the instruction of the deaf.....	vi 81	interior of the earth.....	ii 79, 85
Porter, R. P., cited on statistics of sheep.....	iv 23	aboriginal historical charts.....	ii 93
Portrait of S. F. Baird.....	x 41	fallacies concerning Indians.....	ii 180
of Joseph Henry.....	ii frontispiece.	mounds as evidence of population.....	ii 181
Potato rot.....	i 97	western Permian strata.....	iii 106
Pouillet, cited on temperature of space.....	ii 73	organization of primitive society.....	iii 137
Pouillet's formula for rate of cooling.....	v 91	plants of Washington and vicinity.....	iv 119
Powell, J. W., communication on the struc- tural geology of the valley of the Colo- rado of the West. <i>Abstract</i>	i 48	auroras.....	iv 22
the mythology of the Numas. <i>Refer- ence</i>	i 96	uniformity of peak altitudes in the Ap- palachians.....	iv 64
the genesis and demonology of the Numa tribe of Indians. <i>Reference</i>	i 104	force and vital principle.....	v 104
the Uintah Mountains. <i>Title only</i>	ii 34	eruption and elevation.....	vi 92, 93
the causes of the glacial climate. <i>Ab- stract</i>	ii 44, 45	drainage system of Iowa.....	vi 97
some types of mountain building. <i>Title only</i>	ii 65	glaciers.....	vii 8
monoclinal ridges. <i>Abstract</i>	ii 74	distribution of volcanic eruption.....	vii 79
life of Archibald Robertson Marvine. <i>In full</i>	ii 83, (53)	Precession and terrestrial rigidity.....	ii 77, 78
geologists versus physicists. <i>No abstract</i> ,	ii 85	Precipitation measured at different heights,	ii 49
the philosophy of the North American Indians. <i>Title only</i>	ii 109, 110	Preece, cited on photophonic experiments,	iv 149
poisons among the North American In- dians. <i>Abstract</i>	ii 182	radiophony.....	iv 183
the lands of the arid region of the United States. <i>Abstract</i>	ii 189	Predictions of weather and their verifica- tion.....	vii 122, viii 8
the evolution of language. <i>Title only</i>	ii 199	Presidential address. See <i>Address</i> .	
limitations to the use of some anthro- pologic data. <i>Reference</i>	iv 134	Pressure and temperature, Diurnal changes of.....	ii 67, 69
		Prevost's theory of exchanges.....	v 140
		Price, cited on infinite attraction.....	viii 58
		Price-Edwards E., cited on refraction of sound.....	iv 137
		Prices of gold, greenbacks, and silver.....	ii 52
		Probabilities, Meteorologic.....	v 122
		Problem concerning spheres.....	v 107
		Financial.....	vi 149
		in hydrostatics.....	vii 92, 101, ix 15, 53
		probabilities.....	x 87, 89
		Problems in geometry.....	iii 55, 64, v 88, 107, vi 157, viii 45, x 96
		Proctor, Richard, cited on the zodiacal light,	i (20), (22)
		Prodromus Methodi Mammalium.....	ii (3)

Page.	Page.		
Prognostication for the winter of 1882-83.....v	122	Quimby, Prof., cited on the aurora of Feb.	
Proorthode.....v	123	14, 1872.....i	48
Protagon.....v	75	Quotients of space-directed lines.....x	105, 106
Protoplasm, Possibilities of.....v	102	Radcliffe, C. B., cited on muscular contrac-	
Psychical research.....x	8	tion.....v	59, 61
Psychology.....v	72	Radiometer.....ii	80
Psychology, List of papers on :		Radiophony.....iv	143, 183
on logical algebra. C. S. Peirce. <i>Refer-</i>		Railroad levellings and their hypsometric	
<i>ence</i>i	88	value.....ii	23
on the number of words used in speaking		trains, Resistance of.....iii	29
and writing. E. S. Holden. <i>In full,</i>		Rain-fall and illiteracy.....i	68
<i>ii</i> 28, (16)		Rain-gauges at different elevations.....ii	49
unconscious cerebration. E. M. Gallaudet.		Rainier and its glaciers.....x	10
<i>Title only</i>ii	48	Ramsey, —, letter on the tides of the Bay	
dreams in their relation with psychology.		of Fundy. <i>Communicated by J. J. Wood-</i>	
E. J. Farquhar. <i>Abstract</i>vi	37	<i>ward. Title only</i>i	94
the atomic philosophy, physical and meta-		Rankine, W. J. M., cited on reconcentration	
physical. J. C. Welling. <i>Presidential</i>		of energy.....v	172
<i>address. In full</i>vii	xxix, 81	Ratio of circumference to diameter.....i	57
the application of physical methods to in-		Ravené, Gustave, communication on the as-	
tellectual science. R. D. Mussey. <i>Ab-</i>		teroids. <i>Title only</i>viii	18, 54
<i>stract</i>vii	18	the theory of Mercury. <i>Abstract</i>viii	41
Are there separate centers for light, form,		Rayleigh, Lord, cited on sound produced by	
and color-perception? S. M. Burnett.		<i>heat</i>iv	150, 183
<i>Abstract and reference</i>vii	72	Raymond, C. W., communication on the re-	
recent experiments on reaction time and		sults of travels in Alaska and the de-	
the time sense. G. S. Hall. <i>Title</i>		termination of the position of Fort	
<i>only</i>viii	4	Yukon. <i>Communicated by T. L. Casey.</i>	
modern ideas of brain mechanism. F.		<i>Reference</i>i	22
Baker. <i>Title only</i>viii	17	letter on transit of Venus, 1874. <i>Commu-</i>	
anthropometric and reaction-time appa-		<i>nicated by A. Hall. Abstract</i>ii	31
ratus. J. S. Billings and W. Matthews.		Reaumur cited on the pupation of the Nym-	
<i>Abstract</i>viii	25	phalidæ.....iii	41
an attempt at a theory of odor. F. W.		Reed, Henry, communication on the physi-	
Clarke. <i>Abstract</i>viii	27	ology of civilization. <i>Title only</i>iii	20
the frequency of coincidences. L. F.		Reference indexing.....x	38
Ward. <i>Abstract</i>x	8	Refraction in the principal meridians of a	
Psychrometer, Sling.....viii	25	triaxial ellipsoid.....vi	4
Publication of mathematical papers.....vi	115, 135	of sound.....ii	57, 167 (48), v 35, 39, 44
of bulletin. See <i>Bulletin</i> .		Uncertainty of correction for atmos-	
Publications of scientific societies.....viii	xxxvii	pheric.....i	69
the Philosophical Society.....x	114	Rejection of doubtful observations.....vi	152
Pumpelly, Prof. R., Researches on sewage in		Religion and science.....ii	16, 224
soils by.....iv	38	Removal of place of meeting.....x	xxxii, 10, 31
Pupation of the Nymphalidæ.....iii	41	Remsen, Prof. Ira, Researches on impure air	
Pyrethrum powder.....vii	10	by.....iv	37
Pythagorean philosophy.....vii	xxxiii	Report of committee to collect information	
Quadrature of circlei	57	relative to the meteor of December	
Quadratures, Approximate.....ii	48	24th, 1873.....ii	139
Quadric transformation of elliptic integrals,		Representation of comet orbits by models,	
vii	102	x	28
Quaternary climate of the Great Basin.....v	21	Research, Endowment of.....viii	xli
deposits of western Iowa and eastern Ne-		Method of.....ii	163, iv 40, vii li, x 4
braska.....iv	120	Resistance of railway trains.....iii	29
of the middle Atlantic slope.....x	16	Resisting medium in space.....i	34, 39

	Page.		Page.
Resolution on acceptance of membership,	111 149	Ritter, W. F. McK., communication on a	
auditing committee.....	v 84	simple method of deriving some equations	
committees on mathematical papers.....	vi 135	used in the theory of the moon	
discovery of the satellites of Mars.....	ii 186	and of the planets. <i>In full</i>	iv 57
resigned and dropped members.....	v 84	secular perturbations of Polyhymnia by	
the title "Mr.".....	i 104, x 46	Jupiter. <i>Abstract</i>	viii 54
providing for presidential address.....	iv 30	Rivers and terrestrial rotation.....	vii 21
Resolutions of the International Geodetic		of Iowa.....	vi 93
Commission on unification of longi-		Roan Mountain.....	iv 60
tudes and time.....	vi 107	Robinson, J., Flora of Essex Co., Mass., by	
on the death of L. Agassiz.....	i 94	iv 95
B. Alvord.....	vii 127	Robinson, T., communication on the strata	
S. P. Chase.....	i 87	exposed in the east shaft of the water-	
B. F. Craig.....	ii 130	works extension. <i>Abstract</i>	vii 69
J. Henry.....	ii 196	Was the earthquake of September 19th	
J. H. Lane.....	iii 123	[1884] felt in the District of Columbia?	
A. R. Marvin.....	ii 83	<i>Abstract</i>	vii 73
A. J. Myer.....	iv 31	remarks on deflection of rivers.....	vii 24
G. A. Otis.....	iv 134	measuring earth tremors.....	viii 28
B. Peirce.....	iv 23	Robison, Prof. J., cited on elasticity.....	v 132
J. Rodgers.....	v 105	Newton's rings.....	v 155
G. C. Schaeffer.....	i 90	Rochester tornado.....	vii 3
J. J. Woodward.....	vii 75	Rockwood, C. G., communication on the	
Review of Tait's article on mechanics.....	vii 29	Charleston earthquake. <i>Abstract</i>	ix 37
Reynolds, Prof., cited on refraction of sound,		Rodgers, John, Death of.....	v 102, 105
.....	ii 58, v 40, 44	Rogers, Prof. H. D., cited on the Devonian	
Rhymes, Counting out.....	x 13	in Pennsylvania.....	ii (34), (38)
Richardson, J. G., communication in regard		Rogers, Prof. W. B., cited on geology at Sul-	
to the diagnosis of blood-stains. <i>Read</i>		phur Springs, W. Va.....	ii (27), (30)
by J. J. Woodward. <i>Reference</i>	ii 41	Rogers' rulings on glass.....	ii 130
Riddell, Dr. J. L., Discovery in microscopy		Ross, A. C., communication on latent im-	
by.....	iv 35	pressions on polished glass plates pro-	
Ridges, Monoclinical.....	ii 74	duced by heating the plates in close	
Ridgway, Robert, cited on Baird's "Birds		connection with engraved metallic	
of North America".....	x 65	plates. <i>Abstract</i>	ii 39
communication on a natural arrangement		Rotation and rivers.....	vii 21
of the Falconidae. <i>Read by T. Gill.</i>		in office.....	v 49
<i>Reference</i>	ii 41	Rowland, cited on thermometry.....	ix 30
Rigidity of the earth.....	ii 76	Rücker, Prof. A. W., cited on the constant <i>P</i> ,	
Riley, C. V., communication on the pupation		x 102
of the Nymphalidae. <i>Abstract</i>	ii 41	Rule on communications from sections.....	vi 38
the issuance of silk worms from their		Rules for Publication of Bulletin. See	
cocoon and some striking departures		<i>Bulletin</i> .	
from normal habits in insects. <i>Title</i>		Standing. See <i>Standing rules</i> .	
<i>only</i>	ii 44	Rulings on glass.....	ii 130
Recent advances in economic entomology.		Rumford, Count, cited on theories of heat.....	v 133
<i>Abstract</i>	vii 10	Russell, I. C., communication on the exist-	
the systematic care of pamphlets. <i>Ab-</i>		ing glaciers of the High Sierra of Cali-	
<i>stract</i>	viii 29	fornia. <i>Abstract and reference. 2 fig-</i>	
our city shade-trees, their foes and their		ures.....	vii 5
future. <i>Reference</i>	x 7	deposits of volcanic dust in the Great	
Riley, J. C., Death of.....	iii 28	Basin. <i>Abstract</i>	vii 18
Rings of Saturn.....	ii 94, 102, 188, vi 141	What is a glacier? <i>Abstract</i>	vii 37
Ripple marks.....	ii 61	the faults of the Great Basin and of the	
Ritter, J. W., cited on the chemical rays...v	135	eastern base of the Sierra Nevada.	
		<i>Abstract</i>	ix 5

	Page.		Page.
Russell, I. C., communication on—Cont'd.		Scientific men and their duties.....	ix xxxv
the subaerial decay of rocks and the		Distribution of.....	x 7
origin of the red clay of certain forma-		method.....	ii 163, vi xxxiii, vii 11
tions. <i>Title only</i>	ix 16	and social progress.....	iv 40
Russell, Thomas, communication on tem-		societies.....	i vi, viii xxxliii
peratures at which differences be-		of Washington, and Professor Baird.....	x 45
tween mercurial and air thermometers		of Washington, Proposed federation of,	
are greatest. <i>In full. 1 figure</i>	ix 25	v 102	
normal barometers. <i>Title only</i>	ix 46	of Washington, Statistics of.....	x 29
Russian meteorology.....	i 75	work by state aid.....	viii xli
Rutherford, cited on computation of π	i 53	Scrope, G. P., cited on columnar structure,	viii 24
Sabine, Gen., cited on Plover Bay.....	iv 125	Sea level influenced by winds and baro-	
St. George Island, Seals on.....	i 91	metric pressure..	i 53
St. Louis directrix, Altitude of.....	ii 24	Seals, Fur-bearing.....	i 91
St. Paul Island, Seals on.....	i 91	Secchi, Angelo, cited on elasticity.....	v 130
Salinometer.....	ii 185	Saturn's rings.....	vi 43
Sand sculpture.....	i 57	Seconds-pendulum formula.....	vii 101
Sanderson, Dr. Burden, cited on bacteria..	ii 109	Secretaries' report...vi 111, vii xxiii, viii xxvii,	
Sands, B. F., Death of.....	vi 41	ix xxix, x xxxii	
Sandwich Islands, Geology of.....	vi 13	Secular change in magnetic declination..	ii 45
Satellites, Computations concerning.....	vii 93	perturbations of Polyhymnia by Jupiter,	
of Mars.....	ii 181, 186, 188, 190, vi 45	viii 54	
Saturn.....	iii 26, 40	Seebach's method of determining earth-	
Uranus.....	i (30)	quake foci.....	x 17
Saturday-Night Club.....	x 45	Seitz, E. B., cited on Malfatti's problem..	ii 118
Saturn and its rings, Revolution of.....	ii 183	Seismology , List of papers on:	
Bright spot on.....	ii 102	on the earthquake phenomena recently	
Rings of.....	ii 94, 102, 188, vi 41	experienced in North Carolina. T. L.	
Satellites of.....	iii 26, 40	Clingman. <i>Abstract and reference</i>	i 104
Shadow of.....	ii 102	earth tremors as shown by astronomical	
Saville, J. H., communication on the new		observations. H. M. Paul. <i>Abstract</i> ..	iii 125
Japanese coinage. <i>Title only</i>	i 51	earth vibrations at Niagara Falls. J. M.	
Sawyer, C. J., communication on the Signal		Toner. <i>Abstract</i>	iv 186
Service bibliography of meteorology		seismographic record obtained in Japan.	
and terrestrial magnetism. <i>Read by</i>		E. Smith. <i>Title only</i>	vi 87
C. Abbe. <i>In full</i>	x 23	Was the earthquake of September 19th	
Schaeffer, G. C., Resolutions on the death		[1884] felt in the District of Columbia?	
of.....	i 90	T. Robinson. <i>Abstract</i>	vii 73
Schellbach, Prof. K. H., cited on Malfatti's		the Flood Rock explosion. F. W. Clarke,	
problem.....	ii 113	C. F. Marvin, and H. M. Paul. <i>Ab-</i>	
Schools of Japan.....	ii 69	<i>stract</i>	viii 28
Schott, C. A., communication on a new eye-		the Charleston earthquake. <i>Symposium.</i>	
piece for observing personal equations.		<i>Abstract. Map</i>	ix 37, 38
<i>Title only</i>	ii 200	a recent visit to the scene of the Charle-	
the secular change in the magnetic de-		ston earthquake and resulting conclu-	
clination in the United States and at		sions. C. E. Dutton. <i>Title only</i>	x 16
some foreign stations. <i>Abstract</i>	iii 45	on the depth of earthquake foci. C. E.	
remarks on calendars.....	ii 38	Dutton. <i>Title only</i>	x 17
rigidity of the earth.....	ii 77	the speed of propagation of the Charleston	
Sciences, Philosophic order of.....	v 105	earthquake. C. E. Dutton and S. New-	
Present state of.....	ii 16	comb. <i>Reference</i>	x 28
Progress of.....	ii 56	Series for determining the ratio of circum-	
Scientific administrators.....	ix xliii	ference to diameter.....	i 57
experimentation.....	ii 163, vii li	Serpent venom.....	vi 38
		Sewage in soils.....	iv 38

	Page.
Sexes, Disparity of, in mollusks.....	iii 75
Shade trees and their foes.....	x 7
Shanks, cited on computation of π	i 58
Shasta, Mount.....	x 10
Shastina, Volcanic sand from.....	vii 33
Shell heaps of the Aleutian islands.....	ii 65
Shelters for thermometers.....	vi 46
Sherman, W. T., communication on a visit to Egypt. <i>No abstract</i>	i 63
travels in Turkey and the Caucasus. <i>No abstract</i>	i 65
Sherman, Wyoming, as a site for an astron- omical observatory.....	i 70
Shields, C. W., communication on the present state of the sciences. <i>Abstract and references</i>	ii 16
the philosophical order of the sciences. <i>Reference</i>	v 105
Shoes, high-heeled.....	v 117
Shoulder girdle of fishes.....	i 64
Shrinkage cracking in basalt.....	viii 20
Siberia-Alaska boundary.....	iv 123
Sibscota, G., cited on dumbness and deaf- ness.....	vi 49
Side-coefficients, Removal of.....	viii 41
Siemens, C. W., cited on conservation of solar energy.....	v 172
Sierra Nevada, Geology of.....	i 4, 5
glaciers.....	vii 5
Sign language.....	vi 63, 84
Signal Service bibliography of meteorology,	x 23
Silver coin, Quantity of.....	ix 14
Silver-gold ratio.....	iv 141
Silver question, The.....	iii 78, 107
Similar inventions in areas widely apart,	ix 12
Sinking fund, The United States.....	iii 113
Siren.....	ii 85, (51)
Skinner, A. N., communication on the pre- cession of stars in right ascension. <i>Title only</i>	iii 21
Sling psychrometer.....	viii 25
thermometer.....	vi 46, vii 80
Smart, Dr. Chas., Researches on food adul- teration by.....	iv 39
Smith, Edwin, communication on a seismo- graphic record obtained in Japan. <i>Title only</i>	vi 87
Smithsonian bonds of State of Arkansas.....	vi 105
edition of the Bulletin.....	x 113
Smithsonian Institution under administra- tion of S. F. Baird.....	x 49
under administration of Joseph Henry,	ii 285
Snake venom.....	vi 38

	Page.
Social evolution.....	vi xlviii
progress and scientific method.....	iv 40
Social Science and Statistics, List of papers on :	
on the adjustment of census returns. E. B. Elliott. <i>Title only</i>	i 63
on the coincidence of the geographical distribution of rainfall and of illiter- acy, as shown by the statistical maps of the ninth census reports C. S. Peirce. <i>Abstract</i>	i 68
on life and annuity tables, based on the census of 1870. E. B. Elliott. <i>Title only</i>	i 74
on the use of metric weights and balances for postal purposes in the United States. E. B. Elliott. <i>Abstract</i>	ii 15
further remarks on metric weights and balances for the postal service. E. B. Elliott. <i>Abstract</i>	ii 19
on proposed reforms in spelling the Eng- lish language. A. R. Spofford. <i>Title only</i>	ii 42
the mortality among army officers. B. Alvord. <i>Reference</i>	ii 49
[proposed governmental insurance.] B. Alvord. <i>No abstract</i>	ii 49
[a statistical diagram.] E. B. Elliott. <i>No abstract</i>	ii 134
animal population of the globe. L. F. Ward. <i>Abstract</i>	iv 27
the relation of scientific method to social progress. S. Newcomb. <i>Presidential address. In full</i>	iv 40
the international convention of the teach- ers of the deaf and dumb, at Milan. E. M. Gallaudet. <i>Abstract</i>	iv 55
mortality statistics of the Tenth Census. J. S. Billings. <i>Abstract</i>	iv 163, 164
on survivorships, with tables and formulas of construction. E. B. Elliott. <i>Title only</i>	v 122
fallacies concerning the deaf, and the in- fluence of such fallacies in preventing the amelioration of their condition. A. G. Bell. <i>In full</i>	vi 48
the vital statistics of the Tenth U. S. Cen- sus, J. S. Billings. <i>Reference</i>	viii 4
a fonetic alfabet. H. Farquhar. <i>Abstract</i>	ix 17
the geographical distribution of scientific men and institutions in the United States. G. B. Goode. <i>Reference</i>	x 7
the economic phase of the English spar- row question. C. H. Merriam. <i>Refer- ence</i>	x 16

	Page.		Page.
Social Science and Statistics, List of papers on—Cont'd.		Spencer, Herbert, cited on ceremonies.....	ix 20
statistics of the Philosophical Society from its foundation. G. K. Gilbert. <i>Abstract</i>	x 29	growth of crystals.....	v 67
the progress of science as exemplified in the art of weighing and measuring. W. Harkness. <i>In full</i>	x xxxvii, 39	motion.....	vii 57
association ratios. M. H. Doolittle. <i>Abstract</i>	x 83	nerve currents.....	v 62
association ratios. M. H. Doolittle. <i>Abstract</i>	x 94	the ultimate.....	v 164, 166
Societies, American scientific.....	viii xxxiii	Spheres, Problem concerning.....	v 107
Scientific.....	i vi	Spheroid, Distances on any.....	viii 52
and Professor Baird.....	x 45	Spofford, A. R., communication on proposed reforms in spelling the English language. <i>Title only</i>	ii 42
Statistics of.....	x 29	Spontaneous generation.....	ii 109, v 64, 103
Soils and sewage.....	iv 38	Standard for micrometry.....	iii 22
Solar corona.....	i 31, iii 116, 121	Standard time.....	ii 137, 202, vi 106
eclipse, Jan. 11, 1880.....	iii 121	adopted by the society.....	vii 18
July 29, 1878.....	ii 202, iii 116	A system of.....	v 112
heat variations and climate.....	vi 10	Standards of declination.....	ix 53
parallax derived from transit of Venus, 1874.....	iv 168	length.....	ii 136
from the velocity of light.....	iii 74	value.....	iii 78, 107
methods.....	v 39	Standing rules of the General Committee, i xvii, ii vi, iii vi, 149, iv 11, v 11, vi xii, vii xii, viii xii, ix xii, x xii	
Solid, liquid, and gas defined.....	v 136	Standing rules of the Mathematical Section, vi 115, vii 85, viii 35, ix 51, x 81	
Somoff's theorem.....	ix 54	Standing rules of the Society, i xvi, ii iv, iii iv, 149, iv 7, 30, 38, v 7, vi ix, vii ix, viii ix, ix ix, x ix	
Sondhauss, cited on refraction of sound.....	ii 57	Star catalogue prepared at U. S. Naval Observatory.....	i 74
Sorghum sugar.....	iii 140	New.....	ix 14
Soul.....	v 103	Stars, Arrangement of.....	iii 76
Sound, Abnormal phenomena of.....	ii 37	Images of.....	ix 15
and fog signals.....	ii 57, 60, (45), iv 135, v 23, 39	Station errors.....	ii 82
heat.....	iv 143, 183	Statistics. (See <i>Social Science</i> .)	
light.....	iv 143	Steam as a disinfectant.....	iii 51
Determination of direction of.....	iii 69, viii 12	Steiner, Prof. J., cited on Malfatti's problem, ii 115	
from two syrens.....	ii 85	on Feuerbach's circle.....	viii 46
Joseph Henry's researches on.....	ii 344	Stellar photometry.....	i 63
Refraction of.....	ii 57, 167, (48), v 35, 39, 44	Steno, cited on crystallography.....	i 77
velocity and air temperature.....	vi 47	Sternberg, Dr. G. M., Researches on Bacillus malarie.....	iv 39
waves and earthquake waves.....	ix 42, 43	Stokes, Professor, cited on refraction of sound.....	ii 58, (47), v 40
(See also <i>Acoustics</i> .)		Stone, Ormond, communication on the determination of the errors of a provisory catalogue of fundamental stars. <i>Title only</i>	i 62
Sounds accompanying and following meteor of December 24, 1873.....	ii 157	the correction of a comet's orbit. <i>Reference</i>	ii 22
South Mountain fault.....	vi 30	a problem in probabilities. <i>Abstract</i>	x 89
Space.....	vii 56	the orbit of Hyperion. <i>Abstract and reference</i>	x 104
Resisting medium in.....	i 34, 39	Stoneham, Me., Topaz from.....	viii 5
Temperature of.....	ii 73	Stoney, cited on the radiometer.....	ii 81
Space-directed lines.....	x 105, 106	Storage of electric energy.....	v 46
Sparrows, English.....	x 16	Storm centres, Movement of.....	i 99
Specific gravity method.....	vi 26		
Spectrophone.....	iv 143, 161		
Spectrum of Encke's comet.....	i 34		
corona.....	iii 117		
Speech, Visible.....	iv 55, vi 60		
Speed of propagation of the Charleston earthquake.....	x 17, 28		

	Page.		Page.
Storm centres, Retardation of.....	v 108	Taylor, W. B., communication on the nature and origin of force. <i>Abstract and reference</i>	i 27
Storms and auroras.....	i 45	the aurora. <i>Abstract</i>	i 43
Law of.....	i 106	our present knowledge of the planet Jupiter. <i>Title only</i>	i 62
Thunder.....	ii 189	waves, molecules, and atoms. <i>Abstract</i> ,	i 66
Storr, Dr. G. C. C., cited on the classification of mammals.....	ii (3)	a calendar proposed by a Persian astronomer in 1079. <i>Abstract</i>	ii 38
Strata exposed in shaft of water-works extension.....	vii 69	the causes of the glacial climate. <i>Abstract</i>	ii 43, 46
Struve, Otto, cited on determination of planet's mass from observations on satellites.....	vi 132	acoustic refraction. <i>Abstract</i>	ii 57
satellites of Uranus.....	i (35)	the temperature of space. <i>Abstract</i>	ii 73
Saturn's rings.....	vi 42	Joseph Henry. A sketch of his scientific work. <i>In full</i>	ii 203, 230
Stryker artesian well.....	i 103	a panoramic photograph. <i>Abstract</i>	v 21
Substance.....	vi 14, vii 41	the total lunar eclipse of June 11, 1881. <i>Abstract</i>	v 90
Sugar beet culture and climate.....	iii 142	a remarkable halo. <i>Abstract</i>	v 112
from sorghum.....	iii 140	physics and occult qualities. <i>Presidential address. In full</i>	v 125, 126
Sumner, W. G., cited on bi-metallism.....	iii 84	the rings of Saturn. <i>Abstract</i>	vi 41
Sumner's method in navigation.....	ii 105	a case of discontinuity in elliptic orbits. <i>Abstract</i>	vii 122
Sun, Heat of.....	i 31	geological and physical theories. <i>Abstract</i>	viii 6
viewed by light of any desired wave length.....	x 13	the crumpling of the earth's crust. <i>Abstract and reference</i>	viii 18
Sun-glows.....	vii 17, 35	slight modification of the Newtonian formula of gravitation. <i>Abstract</i>	viii 39
Sun's apparent diameter.....	i (3)	Professor Baird as an administrator. <i>In full</i>	x 49
corona.....	i 31, iii 116, 121	remarks on calendar reform.....	ii 30
Surplus, Proposal to distribute the.....	vi 103	interior of the earth.....	ii 76, 77
Sweeping mechanism.....	iii 142	radiometer.....	ii 80
Swift, Dean, cited on the scientific crank,	viii xi	planetary motions.....	ii 188, 189
Swift's comet, Orbit of.....	iv 59	amplitude of light waves.....	iii 120, 125
Swordfish and its allies.....	iv 162	death of J. H. Lane.....	iii 124
Sylvester, J. J., communication on the theory of invariants. <i>Title only</i>	ii 95	taboo.....	iii 138
Trisection linkage of.....	x 99	Henry's acoustic researches.....	iv 140
Symbols, Archeologic.....	ii 72	radiophony.....	iv 162
Symons, Prof. G. J., Bibliographic work of,	x 21, 23	anomalies of sound.....	v 37
Symposium on the cause of the glacial climate.....	ii 43, 45	binary arithmetic.....	vi 4
the silver question.....	iii 78, 107	sling thermometer.....	vi 47
What is a glacier?.....	vii 37	satellites' orbits.....	vi 133
the Charleston earthquake.....	ix 37, 38	infinitesimals.....	vi 135
What is topography?.....	x 14	sun glows.....	vii 35
a problem in probabilities.....	x 87, 89	topophone.....	viii 13
Systems of mineralogy.....	ii 77	resolutions on the death of G. C. Schaeffer,	i 90
Taconic system of Emmons.....	x 5	Telephone, Exhibition of.....	ii 67, 103
Tainter, S., Photophonic experiments by.	iv 145, 150	Comments on.....	ii 111
Tait, Prof. P. G., cited on force.....	v 128, 152, vii 29	Telephonic study of binaural audition.....	iii 69
Talbot, H. F., cited on the history of Mal-fatti's problem.....	ii 114	Telephote.....	ii 192
Talcott's method.....	x 91	Telescope for Naval Observatory.....	i 62, 63
Target-shooting and the theory of errors.....	vi 138		
Taxonomic terms of Storr.....	ii (7)		
Taylor, F. W., Analysis by.....	vii 32		

	Page.
Temperature and pressure, Diurnal changes of.....	ii 67, 69
Conditions determining.....	v 91
distribution over the surface of the globe,.....	i 96
Measurement of atmospheric.....	vi 46
of sea water as related to winds on the coast of New Hampshire.....	ii 17
brain.....	v 75
space.....	ii 73
the air.....	vi 24
the human body.....	i 31
(See also <i>Meteorology and Thermometry</i> .)	
Temperatures at which differences between mercurial and air thermometers are greatest.....	ix 25
of the Pacific Ocean.....	ii 192
Tenth census mortality statistics.....	iv 164
Teredo navalis.....	v 98
Texas Cross Timbers, Bibliography of.....	x 23, 27
Constant <i>P</i> in observations of.....	x 102
Terquem, cited on Feuerbach's circle.....	viii 46
Texas Cross Timbers.....	x 6
Thanoffer, cited on the pulse.....	v 77
Theatres, Burning of.....	ii 95
Theology.....	v 103
of the American Indians.....	ii 176
Theory of errors.....	vi 152
practically tested by target-shooting.....	vi 138
Thermal belts of North Carolina.....	vi 11
Thermometry , List of papers on:	
on thermometers. B. F. Craig. <i>Title only</i>	i 42
a method of verifying with exactness the indications of a thermometer. B. F. Craig. <i>Title only</i>	i 43
a comparison of the thermometers used to determine the correction for atmospheric refraction at the U. S. Naval Observatory. J. R. Eastman. <i>Abstract</i>	i 68
on the air thermometer of Prof. Jolly. J. E. Hilgard. <i>Title only</i>	i 89
determining the temperature of the air. C. Abbe. <i>Abstract</i>	vi 24
hygrometric observations. H. A. Hazen. <i>Abstract</i>	vi 36
thermometer exposure. H. A. Hazen. <i>Abstract</i>	vi 46
thermometer exposure. H. A. Hazen. <i>Abstract</i>	vii 80
the measurement of temperature at distant points. T. C. Mendenhall. <i>Title only</i>	viii 18
the condensing hygrometer and sling psychrometer. H. A. Hazen. <i>Abstract</i>	viii 25

	Page.
Thermometry , List of papers on—Cont'd.	
temperatures at which differences between mercurial and air thermometers are greatest. T. Russell. <i>In full. 1 figure</i>	ix 25
the gilding of thermometer bulbs. J. H. Kidder. <i>Title only</i>	ix 33
effects of solar radiation upon thermometer bulbs having different metallic coverings. H. A. Hazen. <i>Abstract</i>	ix 33
Thompson, Gilbert, communication on the physical-geographical divisions of the southeastern portion of the United States and their corresponding topographical types. <i>Abstract</i>	ix 22
What is topography? <i>Abstract</i>	x 15
remarks on glaciers.....	vii 8
Indian paintings.....	viii 16
Thompson, Prof. S. P., cited on electricity.....	v 168
Thomson, Sir William, cited on rigidity of the earth.....	ii 78
Sumner's method.....	ii 107
Volt-meter of.....	viii 26
Thomson, William, communication on a new method for detecting and measuring the optical defects of the eye. <i>Reference</i>	i 22
Three methods of evolution.....	vi xxvii
Throwing-sticks.....	ix 13
Thunderstorms in 1834.....	viii 10
Electrical phenomena of.....	ii 139
Tidal retardation and consequent crumpling,.....	viii 19
Tides at Boston influenced by winds and barometric pressure.....	i 53
Tillo, Col., cited on levellings in Asia.....	ii 34
Time, A system of standard.....	v 112
determination with a meridian transit.....	viii 55
globe.....	iii 107
Standard.....	ii 137, 202, vi 106
Titan and Hyperion.....	iii 26, 40, x 104
Titicaca, Climate at Lake.....	ii 35
Todd, D. P., communication on solar parallax from the velocity of light. <i>Reference</i>	iii 74
a mechanical attachment for equatorial mountings to facilitate sweeping in right ascension. <i>Abstract and reference</i>	iii 142
the solar parallax as derived from the American photographs of the transit of Venus 1874, December 8-9. <i>Abstract and reference</i>	iv 168
Todd, J. E., communication on quaternary deposits of western Iowa and eastern Nebraska. <i>Abstract</i>	iv 120

	Page.		Page.
Todd, J. E., remarks on charcoal in the drift.....	iv 122	Unalashka volcanic sand.....	vii 33
Toner, J. M., communication on a method of describing and locating with ease the approximate positions of geographical regions. <i>Title only</i>	i 97	Unification of longitudes and time.....	vii 106
<i>Reference</i>	ii 95	Uniformitarianism.....	vii 6
a malformed dog. <i>No abstract</i>	ii 185	United States, Centre of population of.....	i 35
earth vibrations at Niagara Falls. <i>Abstract</i>	iv 186	Geographic centre of.....	i 22
coins and medals. <i>Abstract</i>	v 22	Urara.....	v 62
remarks on care of pamphlets.....	viii 29	Uranometria Argentina.....	iii 122
Tonto Sandstone, Age of.....	i 109	Uranus, Satellites of.....	i (30)
Topaz from Stoneham, Me.....	viii 5	Utah, Glacial epoch in.....	i 84
Topographic map defined.....	x 11	Permian formation of.....	iii 68, 105
types in the southeastern States.....	ix 22	Ute language.....	ii 28
Topography and geology of the Cross Timbers of Texas.....	x 6	Vacant offices, Filling of.....	ii 84, iii 53, v 112, vi 41, vii 36
and structure.....	x 7	Valentin, cited on mineralogy.....	i 77
defined.....	x 14	Valleys, Classification of.....	i 49
Topophone.....	viii 12	Values at different times.....	ii 87
Tornado at Rochester, Minn.....	vii 3	Relative, of gold, greenbacks, and silver.....	ii 52
Torreyia in Southern States and Japan.....	i 42	Van Sant, —, communication on a method of lighting gas-jets by electricity. <i>No abstract</i>	i 56
Townley, H., cited on transmission of sound, v.....	v 42	Variations of latitude.....	viii 10
Transit flexures.....	viii 27	Vauquelin, cited on mineralogy.....	i 78
Meridian.....	viii 55	Velocity of earth tremors.....	viii 28
of Mercury.....	ii 199	earthquake waves.....	ix 41, x 17, 28
Mercury, May, 1878.....	iii 43	Venom of serpents.....	vi 38
Venus, 1874.....	i 63, ii 31, 33, iv 168	Ventilation of the House of Representatives, v.....	v 99
Venus, 1882.....	vi 21	Venus, Transit of, 1874.....	i 63, ii 31, 33, iv 168
Trap of Orange Mt., N. J.....	viii 24	1882.....	vi 21
Treasurer's report.....	v 176, 180, vi xii, vii xxiv, viii xxviii, ix xxx, x xxxiv	Verification of weather predictions.....	viii 122, viii 8, x 83, 94
Tremors detected by astronomical observations.....	iii 120	Vertebrae, Cephalic.....	i 26
Triangle, Formulæ for the area of.....	viii 37	Virginia, Fossil plants from.....	ii (26)
Problem concerning.....	iii 55	Visible speech.....	iv 55, vi 53
Trisection of angles.....	x 96	Vision.....	vii 72
Trouvelot, L., Drawings of nebulae by.....	ii 51	Apparatus for testing.....	iii 53
Tucker, R., Solution of a geometrical problem by.....	iii 65	Vital principle.....	i 27, v 50, 102
Tupman, —, letter on solar eclipse. <i>Communicated by W. Harkness. No abstract</i>	i 56	statistics of the tenth U. S. census.....	viii 4
Twining, W. J., Death of.....	v 102	Vocabulary of an individual.....	ii 23, (16)
Tyndall, John, cited on photophonic experiments.....	iv 152	Volt-meter.....	viii 26
sound anomalies.....	v 33, 41	Volcanic dust in the Great Basin.....	vii 18
heat absorption by the air.....	v 94, 96	necks.....	vii 78
Introduction of.....	i 65	problem, The.....	vi 87
letter on fog signals. <i>Communicated by J. Henry. No abstract</i>	i 91	sands.....	vii 33
Uinta Mountains, Permian rocks of.....	iii 106	Volcano, Latest, in northern California.....	ix 46
		Volcanoes of New Mexico.....	vii 76
		Von Cronstedt, cited on mineralogy.....	i 78
		Von Jherling, Dr. H., cited on the Chitonidæ.....	ii 193
		Vortex motion.....	iii 143
		Vulcan, Search for.....	ii 85
		Wagner, cited on the sun's diameter.....	i (4)
		Waite, Chief Justice M. R., letter announcing the death of Joseph Henry.....	ii 196

	Page.
Walcott, C. D., communication on the Cambrian system in the United States and Canada. <i>Abstract. 1 figure</i>	vi 98
the geologic age of the lowest formation of Emmons' Taconic system. <i>Reference</i>	x 5
Discovery of Permian fossils by.....	iii 68, 105
Wallerius, cited on mineralogy.....	i 78
Walling, H. F., communication on topographical indications of a fault near Harper's Ferry. <i>Abstract</i>	vi 30
Ward, Lester F., communication on the natural system of plants. <i>Title only</i>	ii 186, 187
the origin of the chemical elements. <i>Title only</i>	iii 33
animal population of the globe. <i>Abstract</i> , <i>iv</i>	27
field and closet notes on the flora of Washington and vicinity. <i>Abstract</i> , <i>iv</i>	64
the organic compounds in their relations to life. <i>Title only</i>	v 91
some physical and economic features of the Upper Missouri system. <i>Reference</i>	vii 20
the flora of the Laramie group. <i>Reference</i>	viii 17
the frequency of coincidences. <i>Abstract</i> , <i>x</i>	8
the geographical distribution of fossil plants. <i>Reference</i>	x 23
remarks on vital force.....	v 105
Dismal Swamp.....	vi 30
deflection of rivers.....	vii 23
Indian observation of nature.....	viii 74
care of pamphlets.....	viii 29
Warren, G. K., cited on abnormal phenomena of sound.....	ii (48)
communication on the geological history of Lake Winnipeg. <i>Abstract</i>	ii 27
Warner, A. J., communication on the silver question. <i>Abstract</i>	iii 112
Wasatch Mountains fault.....	ii 103
Growth of.....	ii 135
Washington a scientific centre.....	i xi, viii xlv, x 47
Flora of.....	iv 64
Watershed of the Adirondack region.....	ii 67, 82
Waterspouts in North Carolina.....	ii 104
Watson, J. C., communication on the discovery of new planets having especial reference to the asteroids. <i>Title only</i>	i 53
Watson, Sereno, cited on the Great Basin flora.....	iv 99
the classification of plants.....	iv 108, 110
Wave lengths of light.....	v 142
Waves, Earthquake.....	x 17

	Page.
Waves, molecules and atoms.....	i 66
Weather forecasts.....	v 122, viii 8
Webb, Capt., cited on phenomena of sound, <i>ii</i> (49), (50)	i 78, 79
Weiss, Prof., cited on mineralogy.....	ii 203
Welling, J. C., communication on the life and character of Joseph Henry. <i>In full</i>	v 39
anomalies of sound signals. <i>In full</i>	vii xxix, 81
the atomic philosophy, physical and metaphysical. <i>Presidential address. In full</i>	vii 4
eulogy on Gen. A. A. Humphreys. <i>Abstract</i>	ii 28
remarks on vocabularies.....	vii 15
drifting buoys.....	vii 75
Indian observation of nature.....	ii 101
Wells, D. A., cited on medium of exchange, <i>ii</i>	19
Wenham, cited on microscope apertures.....	i 78, 79
Werner, cited on mineralogy.....	iv 38
Wernich, cited on contamination of air by sewage.....	vii 37
What is a glacier?.....	iv 183
Wheatstone's microphone, Modification of, <i>iv</i>	v 161
Whewell, Dr. W., cited on attraction.....	vii xxxviii
Greek philosophy.....	iv 121
White, C. A., cited on the loess of Iowa.....	ii 181
communication on the evolutionary history of the North American <i>Unionida</i> . <i>Title only</i>	ii 190
asymmetry in the form of the human cranium. <i>Title only</i>	iii 32
the fresh-water shell-heaps of the interior rivers of North America. <i>Title only</i>	iii 104
the subject of the Permian formation in North America. <i>Abstract</i>	v 161
artesian wells on the Great Plains. <i>Reference</i>	iv 119
remarks on the relations of plants to geology.....	iv 122
loess of the Mississippi valley.....	v 99
teredo.....	vi 93
theory of permanence of oceans.....	vi 97
drainage system of Iowa.....	iii 105
White, Prof. I. C., Discovery of Permian fossils by.....	iii 105
Whitfield, R. P., Observations on <i>Limnaea</i> by.....	iii 75
Whitney, Prof. J. D., cited on geology of Great Basin.....	i 56
Whitney, Prof. W. D., cited on individual vocabularies.....	ii (19)
Wiebe, H. F., cited on thermometry.....	ix 26

	Page.
Wild, Prof., cited on thermometry.....	ix 33
Williams, G. H., communication on the methods of modern petrography. <i>Abstract</i>	vii 36
Willis, Bailey, communication on the topography and structure in the Bays Mountains, Tennessee. <i>Reference</i>	x 7
development of a perspective map from a contour map. <i>Title only</i>	x 9
Mount Rainier and its glaciers. <i>Abstract</i>	x 10
remarks on geology of Cascade Mountains.....	ix 8
Winchell, Alexander, communication on the progressive dispersion of mankind over the surface of the earth. <i>Title only</i>	iii 32
Wind and hygrometry.....	vi 36
railway traction.....	iii 31
retardation of storm centres.....	v 108
as related to barometric gradient.....	i 106
velocity and pressure.....	x 10
Winds and barometric pressure in relation to tides.....	i 53
as related to ocean temperatures on the coast of New Hampshire.....	ii 17
observed in balloon ascensions.....	i 35
on mountain slopes.....	iii 38
Wind-wrought errors in barometric observation.....	v 91
Wind-vane, Theory of.....	x 9
Winlock, W. C., communication on comets II and III, 1884. <i>Title only</i>	viii 16
physical observations of Wolf's comet (1884, III). <i>Abstract</i>	viii 37
Winter of 1882-'83, Prognostication for.....	v 122
Woeikoff, Alexander, communication on the meteorology of Russia. <i>Reference</i>	i 75
the results of a recent determination of the elevation of the Caspian and Aral seas. <i>Abstract</i>	ii 34
meteorological observations in Peru, and some meteorological conditions of that country. <i>Title only</i>	ii 35
Wood, Dr. H. C., Researches on inoculation of diphtheria by.....	iv 38
Woodbury process of photo-printing.....	i 42, 57
Wooden pavements, Failure of.....	ii 26
Woodward, J. J., communication on the alleged hermaphrodite described by Drs. Acely, Blackman, and Jackson. <i>Abstract and reference</i>	i 24
he desirability of reproducing photographs of scientific objects, and especially of magnified microscopical preparations, in a permanent form by	

	Page.
Woodward, J. J., communication on—Cont'd. some photo-mechanical method. <i>Abstract</i>	i 41
the use of monochromatic sunlight as an aid to high-power definition. <i>Abstract and reference</i>	i 47
the Woodbury photo-relief process. <i>Abstract</i>	i 57
spectra and spectroscopes. <i>No abstract</i> , i 89	
micrometric writing on glass. <i>Title only</i>	i 93
the similarity between the red blood-corpuses of man and those of certain other mammals, especially the dog; considered in connection with the diagnosis of blood stains in criminal cases. <i>Abstract and reference</i>	ii 20
the markings on <i>Navicula rhomboides</i> . <i>Title only</i>	ii 69
the rulings on glass by Mr. Rogers, of Cambridge. <i>Abstract</i>	ii 130
the modern microscope, Nobert's lines, and the attempts of others to construct them. <i>Title only</i>	ii 25
diffraction phenomena in the field of the microscope. <i>Abstract and reference</i>	ii 60
the microscopical structure of wool. <i>Title only</i>	ii 62
the Papyrus Ebers. <i>Abstract</i>	ii 64
the use of photography in connection with the micrometer measurement of blood corpuscles. <i>Title only</i>	ii 79
a simple device for the illumination of balsam-mounted objects for examination with certain immersion objectives whose "balsam angle" is 90° or upwards. <i>In full</i> . 1 figure.....	ii 126
the apertometer of Prof. E. Abbe, of Jena, Germany. <i>Abstract</i>	iii 18
a standard for micrometry. <i>Abstract</i> , iii 22	
the oil-immersion objectives of Zeiss, and on convenient methods of obtaining oblique illumination for these and similar objectives. <i>Abstract</i>	iii 25
a new apertometer for microscopic objectives. <i>Title only</i>	iii 37
some apparatus recently brought into use by the Medical Department of the Army for the examination of the eye. <i>Abstract</i>	iii 53
Riddell's binocular microscope—an historical notice. <i>Abstract and reference</i>	iv 35

	Page.		Page.
Woodward, J. J., communication on—Cont'd.		Young, C. A., communication on the expedition to Pekin for observing the late transit of Venus. <i>Abstract</i>	11 33
a biographical sketch of the late Dr. Otis. <i>In full</i>	iv 171	Young, Dr. T., cited on superficial repul-	v 155
modern philosophical conceptions of life. <i>Presidential address. In full</i>	v 49	theories of heat and light.....	v 134
Death of.....	vii 72	Young-Helmholtz theory of color.....	iv 54
remarks on malformed dog.....	i 185		
diagnosis of blood-stains.....	ii 41	Ziwet, Alexander, communication on Grass-	
a new meteorological instrument.....	ii 64	mann's system of geometry. <i>Reference</i> .	
poisoned arrows.....	ii 180, 182	viii 53	
Resolutions on the death of.....	vii 75	remarks on problem in probabilities.....	x 89
Woodward, R. S., cited on infinite attraction,	viii 59	Zodiacal light.....	i (19)
communication on the special treatment		Zoological work of S. F. Baird.....	x 62
of certain forms of observation-equations. <i>Abstract</i>	vi 156	Zoology , List of papers on (See also <i>Bi-</i>	
a concrete problem in hydrostatics proposed by Mr. G. K. Gilbert. <i>Title only</i> ,	vii 101	<i>ology</i>).	
some practical features of a field time determination with a meridian transit. <i>Abstract</i>	vii 55	on the characteristics and zoological relations of man. T. Gill. <i>Abstract</i>	i 24
the changes of terrestrial level surfaces due to variations in distribution of superficial matter. <i>Reference</i>	ix 15	on the number of the cephalic vertebrae. T. Hilgard. <i>Reference</i>	i 26
the position and shape of the geoid as dependent on local masses. <i>Reference</i> ,	ix 53, 54	on additions to the fish fauna of Massachusetts, due to the researches of Prof. S. F. Baird, U. S. Fish Commissioner. T. Gill. <i>Reference</i>	i 29
the free cooling of a homogeneous sphere initially heated to a uniform temperature. <i>Reference</i>	x 90	on the tapir of the Andes and its allied forms. T. Gill. <i>Title only</i>	i 39
the conditioned cooling of a homogeneous sphere. <i>Reference</i>	x 103	on a tunny new to the American coast. T. Gill. <i>Title only</i>	i 47
remarks on deflection of plumb-line.....	vii 92	on the decrease of fish on the southern coast of New England. S. F. Baird. <i>Reference</i>	i 52
Grassmann's geometry.....	viii 53	on the homologies of the shoulder girdle of fishes. T. Gill. <i>Reference</i>	i 64
infinite attraction.....	viii 63	on the <i>Scombrococcus salmoneus</i> of Peters. T. Gill. <i>Title only</i>	i 68
problem in probabilities.....	x 89	on the homologies of the arm in fishes, and the development of the humerus in ganoids. T. Gill. <i>Title only</i>	i 73
Wolf's comet (1884 III).....	viii 37	on the habits of the fur-bearing seals of the islands of St. Paul and St. George, Behring Sea. H. W. Elliott. <i>Reference</i>	i 91
Wooara.....	v 62	on the primates and their relations to man. T. Gill. <i>Title only</i>	i 96
Words in an individual vocabulary.....	ii 28, (16)	on the structure and homologies of the limbs, especially in Aves. E. Coues. <i>Title only</i>	i 96
Written language and speech.....	iii 139	on the structure and shape of Palæotherium. T. Gill. <i>Abstract</i>	i 99
Wyandottes, Social and political organization of.....	iii 137	on the "Prodrusus methodi mammalium" of Storr. T. Gill. <i>In full</i>	ii 15, (3)
Yards, Standard.....	i 136	on the similarity between the red blood-corpuseles of man and those of certain other mammals, especially the dog; considered in connection with the diagnosis of blood-stains in criminal	
Yarnall, Mordecai, communication on the general star catalogue prepared from the observations at the Naval Observatory since 1845. <i>Reference</i>	i 74		
Death of.....	iii 28		
Yeast ferment as an insecticide.....	vii 11		
Yellowstone expedition of 1870.....	i 21		
valley.....	vii 20		
Young, C. A., cited on observations at Sherman, Wyo.....	i 71, 73		
zodiacal light.....	i (21)		

	Page.
Zoology, List of papers—Cont'd.	
cases. J. J. Woodward. <i>Abstract and reference</i>	11 20
on the geographical distribution of mammals. T. N. Gill. <i>Abstract</i>	11 26
explanatory note on the diagnosis of blood stains. J. G. Richardson. <i>Read by J. J. Woodward. Reference</i>	11 41
outlines of a natural arrangement of the Falconidæ. R. Ridgway. <i>Communicated by T. Gill. Reference</i>	11 41
the microscopical structure of wool. J. J. Woodward and John Leconte. <i>Title only</i>	11 62
the markings on <i>Navicula rhomboides</i> . J. J. Woodward. <i>Title only</i>	11 69
shower of the Rocky-Mountain grasshoppers. C. G. Boerner. <i>Communicated by J. Henry. Abstract</i>	11 87
the relations and sequences of the family Centracroides. T. N. Gill. <i>Title only</i>	11 113
the morphology of the antlers of the Cervidæ. T. Gill. <i>Abstract and reference</i> , 11 135	11 135
some phases of the evolutionary history of the North American Unionidæ. C. A. White. <i>Title only</i>	11 181
a new species of <i>Chimæra</i> found in American waters. T. Gill. <i>Abstract</i>	11 182
[exhibition of malformed dog.] J. M. Toner. <i>No abstract</i>	11 185
the results of recent investigations into the natural history of the Chitonidæ. W. H. Dall. <i>Abstract</i>	11 193
a fish found on the Florida coast. W. S. Abbey. <i>Letter, read by C. Abbe. No abstract</i>	11 202
the family of Ceratiids. T. N. Gill. <i>Title only</i>	11 202
notes on the museums and zoological gardens of northern Europe. W. H. Dall. <i>Title only</i>	11 19, 21
the artificial propagation of the cod. S. F. Baird. <i>Abstract</i>	11 29
the embryology of <i>Lingula</i> and the systematic relations of the Brachiopods. W. K. Brooks. <i>Title only</i>	11 33
the muscles of the oyster. W. H. Dall. <i>Abstract</i>	11 36

	Page.
Zoology, List of papers on—Cont'd.	
pupation of the Nymphalidæ. C. V. Riley. <i>Abstract</i>	111 41
the issuance of silkworm moths from their cocoons, and some striking departures from normal habits in insects. C. V. Riley. <i>Title only</i>	111 41
some recent observations on mollusks. W. H. Dall. <i>Abstract</i>	111 75
some remarkable instances of ingestion among fishes. T. N. Gill. <i>Abstract</i>	111 116
animal population of the globe. L. F. Ward. <i>Abstract</i>	1v 27
the swordfish and its allies. G. B. Goode. <i>Reference</i>	1v 162
on some peculiar features of mollusks found at great depths. W. H. Dall. <i>Abstract</i>	v 90
on some peculiar ravages of the <i>Teredo navalis</i> . A. B. Johnson. <i>Title only</i>	v 98
on the classification of the insectivorous mammals. T. Gill. <i>In full</i>	v 118
the prevention of malarial diseases, illustrating, <i>inter alia</i> , the conservative function of ague. A. F. A. King. <i>Abstract</i>	vi 5
recent experiments on serpent venom. R. Fletcher. <i>Reference</i>	vi 38
analogues in zoo-geography. T. N. Gill. <i>Title only</i>	vi 41
ichthyological results of the voyage of the Albatross. T. N. Gill. <i>Title only</i>	vi 48
recent advances in our knowledge of the limpets. W. H. Dall. <i>Abstract</i>	vii 4
recent advances in economic entomology. C. V. Riley. <i>Abstract</i>	vii 10
certain appendages of the mollusca. W. H. Dall. <i>Reference</i>	vii 32
two remarkable forms of mollusks. W. H. Dall. <i>Abstract and reference</i>	viii 5
the distribution of fishes in the oceanic abysses and middle strata. G. B. Goode and T. H. Bean. <i>Title only</i>	ix 22
our city shade-trees, their foes and their future. C. V. Riley. <i>Reference</i>	x 7
the economic phase of the English sparrow question. C. H. Merriam. <i>Reference</i>	x 16
Zornow, Prof. A. R., cited on Malfatti's problem.....	11 118







SMITHSONIAN INSTITUTION LIBRARIES



3 9088 01421 4241